

# Mathematica 11.3 Integration Test Results

Test results for the 855 problems in "4.3.3.1 (a+b tan)^m (c+d tan)^n (A+B tan).m"

Problem 9: Result more than twice size of optimal antiderivative.

$$\int \tan[c + dx]^2 (a + i a \tan[c + dx])^2 (A + B \tan[c + dx]) dx$$

Optimal (type 3, 141 leaves, 5 steps):

$$-2 a^2 (A - i B) x + \frac{2 a^2 (i A + B) \operatorname{Log}[\operatorname{Cos}[c + dx]]}{d} + \frac{2 a^2 (A - i B) \tan[c + dx]}{d} + \frac{a^2 (i A + B) \tan[c + dx]^2}{d} - \frac{a^2 (4 A - 5 i B) \tan[c + dx]^3}{12 d} + \frac{i B \tan[c + dx]^3 (a^2 + i a^2 \tan[c + dx])}{4 d}$$

Result (type 3, 924 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^3 \left( i A \cos [c]+B \cos [c]+A \sin [c]-i B \sin [c] \right) \right. \\
 & \quad \left. \left( -2 i \operatorname{ArcTan}[\tan [3 c+d x]] \cos [c]-2 \operatorname{ArcTan}[\tan [3 c+d x]] \sin [c] \right) \right. \\
 & \quad \left. \left( a+i a \tan [c+d x] \right)^2 (A+B \tan [c+d x]) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( \cos [c+d x]^3 \left( i A \cos [c]+B \cos [c]+A \sin [c]-i B \sin [c] \right) \right. \\
 & \quad \left. \left( \cos [c] \log [\cos [c+d x]^2]-i \log [\cos [c+d x]^2] \sin [c] \right) \left( a+i a \tan [c+d x] \right)^2 \right. \\
 & \quad \left. \left. (A+B \tan [c+d x]) \right) \right) / \left( d \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( \cos [c+d x] \sec [c] \left( 6 i A \cos [c]+9 B \cos [c]-2 A \sin [c]+4 i B \sin [c] \right) \right. \\
 & \quad \left. \left( \frac{1}{6} \cos [2 c]-\frac{1}{6} i \sin [2 c] \right) \left( a+i a \tan [c+d x] \right)^2 (A+B \tan [c+d x]) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( \sec [c+d x] \left( -\frac{1}{4} B \cos [2 c]+\frac{1}{4} i B \sin [2 c] \right) \left( a+i a \tan [c+d x] \right)^2 (A+B \tan [c+d x]) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( (A-i B) \cos [c+d x]^3 \left( -2 d x \cos [2 c]+2 i d x \sin [2 c] \right) \left( a+i a \tan [c+d x] \right)^2 \right. \\
 & \quad \left. (A+B \tan [c+d x]) \right) / \left( d \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( \sec [c] \left( \frac{1}{3} \cos [2 c]-\frac{1}{3} i \sin [2 c] \right) \left( -A \sin [d x]+2 i B \sin [d x] \right) \left( a+i a \tan [c+d x] \right)^2 \right. \\
 & \quad \left. (A+B \tan [c+d x]) \right) / \left( d \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( \cos [c+d x]^2 \sec [c] \left( \frac{1}{3} \cos [2 c]-\frac{1}{3} i \sin [2 c] \right) \left( 7 A \sin [d x]-8 i B \sin [d x] \right) \right. \\
 & \quad \left. \left( a+i a \tan [c+d x] \right)^2 (A+B \tan [c+d x]) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( x \cos [c+d x]^3 \left( -2 A \cos [c]^2+2 i B \cos [c]^2+6 i A \cos [c] \sin [c]+6 B \cos [c] \sin [c]+ \right. \right. \\
 & \quad \left. \left. 6 A \sin [c]^2-6 i B \sin [c]^2-2 i A \sin [c]^2 \tan [c]-2 B \sin [c]^2 \tan [c]- \right. \right. \\
 & \quad \left. \left. i(A-i B)\left(2 \cos [2 c]-2 i \sin [2 c]\right) \tan [c] \right) \left( a+i a \tan [c+d x] \right)^2 (A+B \tan [c+d x]) \right) / \\
 & \left( \left( \cos [d x]+i \sin [d x] \right)^2 (A \cos [c+d x]+B \sin [c+d x]) \right)
 \end{aligned}$$

**Problem 10: Result more than twice size of optimal antiderivative.**

$$\int \tan [c+d x] \left( a+i a \tan [c+d x] \right)^2 (A+B \tan [c+d x]) d x$$

Optimal (type 3, 107 leaves, 4 steps):

$$\begin{aligned}
 & -2 a^2 (i A+B) x - \frac{2 a^2 (A-i B) \log [\cos [c+d x]]}{d} + \\
 & \frac{a^2 (i A+B) \tan [c+d x]}{d} + \frac{A \left( a+i a \tan [c+d x] \right)^2}{2 d} - \frac{i B \left( a+i a \tan [c+d x] \right)^3}{3 a d}
 \end{aligned}$$

Result (type 3, 273 leaves):

$$\frac{1}{d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x])} \left( 2 (i A + B) \operatorname{ArcTan} [\operatorname{Tan} [3 c + d x]] \cos [c + d x]^3 (\cos [2 c] - i \sin [2 c]) - (A - i B) \cos [c + d x]^3 \log [\cos [c + d x]^2] (\cos [2 c] - i \sin [2 c]) + (A - i B) \cos [c + d x]^3 (-4 i d x \cos [2 c] - 4 d x \sin [2 c]) + \frac{1}{3} (6 A - 7 i B) \cos [c + d x]^2 \operatorname{Sec} [c] (i \cos [2 c] + \sin [2 c]) \sin [d x] + \frac{1}{3} B \cos [c] \sin [d x] (i + \operatorname{Tan} [c])^2 - \frac{1}{6} \cos [c + d x] (\cos [2 c] - i \sin [2 c]) (3 A - 6 i B + 2 B \operatorname{Tan} [c]) \right) (a + i a \operatorname{Tan} [c + d x])^2 (A + B \operatorname{Tan} [c + d x])$$

**Problem 11: Result more than twice size of optimal antiderivative.**

$$\int (a + i a \operatorname{Tan} [c + d x])^2 (A + B \operatorname{Tan} [c + d x]) dx$$

Optimal (type 3, 80 leaves, 3 steps):

$$2 a^2 (A - i B) x - \frac{2 a^2 (i A + B) \log [\cos [c + d x]]}{d} - \frac{a^2 (A - i B) \operatorname{Tan} [c + d x]}{d} + \frac{B (a + i a \operatorname{Tan} [c + d x])^2}{2 d}$$

Result (type 3, 263 leaves):

$$\frac{1}{4 d (\cos [d x] + i \sin [d x])^2} a^2 \operatorname{Sec} [c] \operatorname{Sec} [c + d x]^2 \left( (\cos [2 d x] + i \sin [2 d x]) (-8 (A - i B) \operatorname{ArcTan} [\operatorname{Tan} [3 c + d x]] \cos [c] \cos [c + d x]^2 - i (4 i A d x \cos [3 c + 2 d x] + 4 B d x \cos [3 c + 2 d x] + (i A + B) \cos [c + 2 d x] (4 d x - i \log [\cos [c + d x]^2]) + A \cos [3 c + 2 d x] \log [\cos [c + d x]^2] - i B \cos [3 c + 2 d x] \log [\cos [c + d x]^2] + 2 \cos [c] (-i B + 4 i A d x + 4 B d x + (A - i B) \log [\cos [c + d x]^2]) + 2 i A \sin [c] + 4 B \sin [c] - 2 i A \sin [c + 2 d x] - 4 B \sin [c + 2 d x]) \right)$$

**Problem 12: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x] (a + i a \operatorname{Tan} [c + d x])^2 (A + B \operatorname{Tan} [c + d x]) dx$$

Optimal (type 3, 75 leaves, 5 steps):

$$2 a^2 (i A + B) x + \frac{a^2 (A - 2 i B) \log [\cos [c + d x]]}{d} + \frac{a^2 A \log [\sin [c + d x]]}{d} + \frac{i B (a^2 + i a^2 \operatorname{Tan} [c + d x])}{d}$$

Result (type 3, 201 leaves):

$$\frac{1}{4 d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x])} \\ a^2 (-8 i (A - i B) \operatorname{ArcTan}[\tan [3 c + d x]] \cos [c + d x] + \\ \sec [c] (\cos [d x] (8 (i A + B) d x + (A - 2 i B) \log [\cos [c + d x]^2] + A \log [\sin [c + d x]^2]) + \\ \cos [2 c + d x] (8 (i A + B) d x + (A - 2 i B) \log [\cos [c + d x]^2] + A \log [\sin [c + d x]^2]) - \\ 4 B \sin [d x])) (\cos [2 d x] + i \sin [2 d x]) (A + B \tan [c + d x])$$

**Problem 13: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^2 (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 79 leaves, 5 steps):

$$-2 a^2 (A - i B) x + \frac{a^2 B \log [\cos [c + d x]]}{d} + \\ \frac{a^2 (2 i A + B) \log [\sin [c + d x]]}{d} - \frac{A \cot [c + d x] (a^2 + i a^2 \tan [c + d x])}{d}$$

Result (type 3, 202 leaves):

$$\frac{1}{4 d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x])} \\ a^2 (B + A \cot [c + d x]) (\cos [2 d x] + i \sin [2 d x]) \\ (\csc [c] (\cos [2 c + d x] (8 (A - i B) d x - B \log [\cos [c + d x]^2] + (-2 i A - B) \log [\sin [c + d x]^2]) + \\ \cos [d x] (-8 (A - i B) d x + B \log [\cos [c + d x]^2] + (2 i A + B) \log [\sin [c + d x]^2])) + \\ 4 A \sin [d x]) + 8 (A - i B) \operatorname{ArcTan}[\tan [3 c + d x]] \sin [c + d x])$$

**Problem 14: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^3 (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 94 leaves, 4 steps):

$$-2 a^2 (i A + B) x - \frac{a^2 (3 i A + 2 B) \cot [c + d x]}{2 d} - \\ \frac{2 a^2 (A - i B) \log [\sin [c + d x]]}{d} - \frac{A \cot [c + d x]^2 (a^2 + i a^2 \tan [c + d x])}{2 d}$$

Result (type 3, 302 leaves):

$$\frac{1}{4 d (\cos [d x] + i \sin [d x])^2}$$

$$a^2 \operatorname{Csc}[c] \operatorname{Csc}[c+d x]^2 (\cos [2 d x] + i \sin [2 d x]) (2 (2 i A+B) \cos [c] - 4 i A \cos [c+2 d x] - 2 B \cos [c+2 d x] - 2 A \sin [c] - 8 i A d x \sin [c] - 8 B d x \sin [c] - 2 A \log [\sin [c+d x]^2] \sin [c] + 2 i B \log [\sin [c+d x]^2] \sin [c] + 8 (i A+B) \operatorname{ArcTan}[\tan [3 c+d x]] \sin [c] \sin [c+d x]^2 - 4 i A d x \sin [c+2 d x] - 4 B d x \sin [c+2 d x] - A \log [\sin [c+d x]^2] \sin [c+2 d x] + i B \log [\sin [c+d x]^2] \sin [c+2 d x] + 4 i A d x \sin [3 c+2 d x] + 4 B d x \sin [3 c+2 d x] + A \log [\sin [c+d x]^2] \sin [3 c+2 d x] - i B \log [\sin [c+d x]^2] \sin [3 c+2 d x])$$

Problem 15: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^4 (a+i a \tan [c+d x])^2 (A+B \tan [c+d x]) dx$$

Optimal (type 3, 117 leaves, 5 steps):

$$2 a^2 (A-i B) x + \frac{2 a^2 (A-i B) \cot [c+d x]}{d} - \frac{a^2 (4 i A+3 B) \cot [c+d x]^2}{6 d} - \frac{2 a^2 (i A+B) \log [\sin [c+d x]]}{d} - \frac{A \cot [c+d x]^3 (a^2+i a^2 \tan [c+d x])}{3 d}$$

Result (type 3, 435 leaves):

$$\frac{1}{24 d (\cos [d x] + i \sin [d x])^2}$$

$$a^2 \operatorname{Csc}[c] \operatorname{Csc}[c+d x]^3 (\cos [2 d x] + i \sin [2 d x]) (12 i A \cos [2 c+d x] + 6 B \cos [2 c+d x] - 36 A d x \cos [2 c+d x] + 36 i B d x \cos [2 c+d x] - 12 A d x \cos [2 c+3 d x] + 12 i B d x \cos [2 c+3 d x] + 12 A d x \cos [4 c+3 d x] - 12 i B d x \cos [4 c+3 d x] + 9 i A \cos [2 c+d x] \log [\sin [c+d x]^2] + 9 B \cos [2 c+d x] \log [\sin [c+d x]^2] + 3 i A \cos [2 c+3 d x] \log [\sin [c+d x]^2] + 3 B \cos [2 c+3 d x] \log [\sin [c+d x]^2] - 3 i A \cos [4 c+3 d x] \log [\sin [c+d x]^2] - 3 B \cos [4 c+3 d x] \log [\sin [c+d x]^2] + 3 \cos [d x] (2 B (-1-6 i d x) + 4 A (-i+3 d x) + (-3 i A-3 B) \log [\sin [c+d x]^2]) - 24 A \sin [d x] + 24 i B \sin [d x] - 48 (A-i B) \operatorname{ArcTan}[\tan [3 c+d x]] \sin [c] \sin [c+d x]^3 - 18 A \sin [2 c+d x] + 12 i B \sin [2 c+d x] + 14 A \sin [2 c+3 d x] - 12 i B \sin [2 c+3 d x])$$

Problem 16: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^5 (a+i a \tan [c+d x])^2 (A+B \tan [c+d x]) dx$$

Optimal (type 3, 139 leaves, 6 steps):

$$2 a^2 (i A+B) x + \frac{2 a^2 (i A+B) \cot [c+d x]}{d} + \frac{a^2 (A-i B) \cot [c+d x]^2}{d} - \frac{a^2 (5 i A+4 B) \cot [c+d x]^3}{12 d} + \frac{2 a^2 (A-i B) \log [\sin [c+d x]]}{d} - \frac{A \cot [c+d x]^4 (a^2+i a^2 \tan [c+d x])}{4 d}$$

Result (type 3, 902 leaves):

$$\begin{aligned}
 & a^2 \left( \left( (i + \cot[c + dx])^2 (B + A \cot[c + dx]) \operatorname{Csc}[c + dx] \left( -\frac{1}{4} A \cos[2c] + \frac{1}{4} i A \sin[2c] \right) \right) / \right. \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) + \left( (i + \cot[c + dx])^2 \right. \\
 & \quad \left. (B + A \cot[c + dx]) \operatorname{Csc}[c] \left( \frac{1}{3} \cos[2c] - \frac{1}{3} i \sin[2c] \right) (2 i A \sin[dx] + B \sin[dx]) \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( (i + \cot[c + dx])^2 (B + A \cot[c + dx]) \operatorname{Csc}[c] (-4 i A \cos[c] - 2 B \cos[c] + \right. \\
 & \quad \left. 9 A \sin[c] - 6 i B \sin[c]) \left( \frac{1}{6} \cos[2c] - \frac{1}{6} i \sin[2c] \right) \sin[c + dx] \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( (i + \cot[c + dx])^2 (B + A \cot[c + dx]) \operatorname{Csc}[c] \left( \frac{1}{3} \cos[2c] - \frac{1}{3} i \sin[2c] \right) \right. \\
 & \quad \left. (-8 i A \sin[dx] - 7 B \sin[dx]) \sin[c + dx]^2 \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( (i + \cot[c + dx])^2 (B + A \cot[c + dx]) (A \cos[c] - i B \cos[c] - i A \sin[c] - B \sin[c]) \right. \\
 & \quad \left. (-2 i \operatorname{ArcTan}[\tan[3c + dx]] \cos[c] - 2 \operatorname{ArcTan}[\tan[3c + dx]] \sin[c]) \sin[c + dx]^3 \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( (i + \cot[c + dx])^2 (B + A \cot[c + dx]) (A \cos[c] - i B \cos[c] - i A \sin[c] - B \sin[c]) \right. \\
 & \quad \left. (\cos[c] \operatorname{Log}[\sin[c + dx]^2] - i \operatorname{Log}[\sin[c + dx]^2] \sin[c]) \sin[c + dx]^3 \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( x (i + \cot[c + dx])^2 (B + A \cot[c + dx]) (6 i A \cos[c]^2 + 6 B \cos[c]^2 - 2 A \cos[c]^2 \cot[c] + \right. \\
 & \quad \left. 2 i B \cos[c]^2 \cot[c] + 6 A \cos[c] \sin[c] - 6 i B \cos[c] \sin[c] - 2 i A \sin[c]^2 - \right. \\
 & \quad \left. 2 B \sin[c]^2 + (A - i B) \cot[c] (2 \cos[2c] - 2 i \sin[2c]) \right) \sin[c + dx]^3 \Big/ \\
 & \quad \left( (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( (i A + B) (i + \cot[c + dx])^2 (B + A \cot[c + dx]) (2 dx \cos[2c] - 2 i dx \sin[2c]) \right. \\
 & \quad \left. \sin[c + dx]^3 \right) / \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c + dx] + B \sin[c + dx]) \right) \Big)
 \end{aligned}$$

**Problem 17: Result more than twice size of optimal antiderivative.**

$$\int \tan[c + dx]^2 (a + i a \tan[c + dx])^3 (A + B \tan[c + dx]) dx$$

Optimal (type 3, 182 leaves, 6 steps):

$$\begin{aligned}
 & -4 a^3 (A - i B) x + \frac{4 a^3 (i A + B) \operatorname{Log}[\cos[c + dx]]}{d} + \frac{4 a^3 (A - i B) \tan[c + dx]}{d} + \\
 & \frac{2 a^3 (i A + B) \tan[c + dx]^2}{d} - \frac{a^3 (45 A - 47 i B) \tan[c + dx]^3}{60 d} + \\
 & \frac{i a B \tan[c + dx]^3 (a + i a \tan[c + dx])^2}{5 d} - \frac{(5 A - 7 i B) \tan[c + dx]^3 (a^3 + i a^3 \tan[c + dx])}{20 d}
 \end{aligned}$$

Result (type 3, 847 leaves):

$$\frac{\left( \cos [c+d x]^4 \left( i A \cos \left[ \frac{3 c}{2} \right] + B \cos \left[ \frac{3 c}{2} \right] + A \sin \left[ \frac{3 c}{2} \right] - i B \sin \left[ \frac{3 c}{2} \right] \right) \right.}{\left( 2 \cos \left[ \frac{3 c}{2} \right] \log [\cos [c+d x]^2] - 2 i \log [\cos [c+d x]^2] \sin \left[ \frac{3 c}{2} \right] \right) (a+i a \tan [c+d x])^3} + \frac{(A+B \tan [c+d x])}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c+d x] + B \sin [c+d x])} + \frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c+d x] + B \sin [c+d x])} \sec [c] \sec [c+d x] \left( \frac{1}{240} \cos [3 c] - \frac{1}{240} i \sin [3 c] \right) \left( 195 i A \cos [d x] + 225 B \cos [d x] - 300 A d x \cos [d x] + 300 i B d x \cos [d x] + 195 i A \cos [2 c+d x] + 225 B \cos [2 c+d x] - 300 A d x \cos [2 c+d x] + 300 i B d x \cos [2 c+d x] + 75 i A \cos [2 c+3 d x] + 105 B \cos [2 c+3 d x] - 150 A d x \cos [2 c+3 d x] + 150 i B d x \cos [2 c+3 d x] + 75 i A \cos [4 c+3 d x] + 105 B \cos [4 c+3 d x] - 150 A d x \cos [4 c+3 d x] + 150 i B d x \cos [4 c+3 d x] - 30 A d x \cos [4 c+5 d x] + 30 i B d x \cos [4 c+5 d x] - 30 A d x \cos [6 c+5 d x] + 30 i B d x \cos [6 c+5 d x] + 420 A \sin [d x] - 470 i B \sin [d x] - 330 A \sin [2 c+d x] + 360 i B \sin [2 c+d x] + 270 A \sin [2 c+3 d x] - 280 i B \sin [2 c+3 d x] - 105 A \sin [4 c+3 d x] + 135 i B \sin [4 c+3 d x] + 75 A \sin [4 c+5 d x] - 83 i B \sin [4 c+5 d x] \right) (a+i a \tan [c+d x])^3 (A+B \tan [c+d x]) + \frac{1}{(\cos [d x] + i \sin [d x])^3 (A \cos [c+d x] + B \sin [c+d x])} x \cos [c+d x]^4 \left( 2 A \cos [c] - 2 i B \cos [c] - 2 A \cos [c]^3 + 2 i B \cos [c]^3 - 4 i A \sin [c] - 4 B \sin [c] + 8 i A \cos [c]^2 \sin [c] + 8 B \cos [c]^2 \sin [c] + 12 A \cos [c] \sin [c]^2 - 12 i B \cos [c] \sin [c]^2 - 8 i A \sin [c]^3 - 8 B \sin [c]^3 - 2 A \sin [c] \tan [c] + 2 i B \sin [c] \tan [c] - 2 A \sin [c]^3 \tan [c] + 2 i B \sin [c]^3 \tan [c] - i (A - i B) (4 \cos [3 c] - 4 i \sin [3 c]) \tan [c] \right) (a+i a \tan [c+d x])^3 (A+B \tan [c+d x])$$

**Problem 18: Result more than twice size of optimal antiderivative.**

$$\int \tan [c+d x] (a+i a \tan [c+d x])^3 (A+B \tan [c+d x]) dx$$

Optimal (type 3, 138 leaves, 5 steps):

$$-4 a^3 (i A+B) x - \frac{4 a^3 (A-i B) \log [\cos [c+d x]]}{d} + \frac{2 a^3 (i A+B) \tan [c+d x]}{d} + \frac{a (A-i B) (a+i a \tan [c+d x])^2}{2 d} + \frac{A (a+i a \tan [c+d x])^3}{3 d} - \frac{i B (a+i a \tan [c+d x])^4}{4 a d}$$

Result (type 3, 980 leaves):

$$\begin{aligned}
 & \left( \cos [c + d x]^4 \left( A \cos \left[ \frac{3 c}{2} \right] - i B \cos \left[ \frac{3 c}{2} \right] - i A \sin \left[ \frac{3 c}{2} \right] - B \sin \left[ \frac{3 c}{2} \right] \right) \right. \\
 & \quad \left( -2 \cos \left[ \frac{3 c}{2} \right] \log [\cos [c + d x]^2] + 2 i \log [\cos [c + d x]^2] \sin \left[ \frac{3 c}{2} \right] \right) \\
 & \quad \left. (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\
 & \quad (d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])) + \\
 & \quad \left( \cos [c + d x]^2 (-9 A \cos [c] + 15 i B \cos [c] - 2 i A \sin [c] - 6 B \sin [c]) \left( \frac{1}{6} \cos [3 c] - \frac{1}{6} i \sin [3 c] \right) \right. \\
 & \quad \left. (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / (d (\cos [\frac{c}{2}] - \sin [\frac{c}{2}])) \\
 & \quad \left( \cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \Big) + \\
 & \quad \left( \left( -\frac{1}{4} i B \cos [3 c] - \frac{1}{4} B \sin [3 c] \right) (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\
 & \quad (d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])) + \\
 & \quad \left( (A - i B) \cos [c + d x]^4 (-4 i d x \cos [3 c] - 4 d x \sin [3 c]) (a + i a \tan [c + d x])^3 \right. \\
 & \quad \left. (A + B \tan [c + d x]) \right) / (d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])) + \\
 & \quad \left( \cos [c + d x] \left( \frac{1}{3} \cos [3 c] - \frac{1}{3} i \sin [3 c] \right) (-i A \sin [d x] - 3 B \sin [d x]) \right. \\
 & \quad \left. (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / (d (\cos [\frac{c}{2}] - \sin [\frac{c}{2}])) \\
 & \quad \left( \cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \Big) + \\
 & \quad \left( \cos [c + d x]^3 \left( \frac{1}{3} \cos [3 c] - \frac{1}{3} i \sin [3 c] \right) (13 i A \sin [d x] + 15 B \sin [d x]) \right. \\
 & \quad \left. (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / (d (\cos [\frac{c}{2}] - \sin [\frac{c}{2}])) \\
 & \quad \left( \cos [\frac{c}{2}] + \sin [\frac{c}{2}] \right) (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \Big) + \\
 & \quad \frac{1}{(d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]))} \\
 & \quad \times \cos [c + d x]^4 \left( 2 i A \cos [c] + 2 B \cos [c] - 2 i A \cos [c]^3 - 2 B \cos [c]^3 + 4 A \sin [c] - \right. \\
 & \quad \left. 4 i B \sin [c] - 8 A \cos [c]^2 \sin [c] + 8 i B \cos [c]^2 \sin [c] + 12 i A \cos [c] \sin [c]^2 + \right. \\
 & \quad \left. 12 B \cos [c] \sin [c]^2 + 8 A \sin [c]^3 - 8 i B \sin [c]^3 - 2 i A \sin [c] \tan [c] - 2 B \sin [c] \tan [c] - \right. \\
 & \quad \left. 2 i A \sin [c]^3 \tan [c] - 2 B \sin [c]^3 \tan [c] + (A - i B) (4 \cos [3 c] - 4 i \sin [3 c]) \tan [c] \right) \\
 & \quad \left. (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right)
 \end{aligned}$$

**Problem 19: Result more than twice size of optimal antiderivative.**

$$\int (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 110 leaves, 4 steps):



$$4 a^3 (A - i B) x - \frac{4 a^3 (i A + B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \frac{2 a^3 (A - i B) \operatorname{Tan}[c + d x]}{d} +$$

$$\frac{a (i A + B) (a + i a \operatorname{Tan}[c + d x])^2}{2 d} + \frac{B (a + i a \operatorname{Tan}[c + d x])^3}{3 d}$$

Result (type 3, 883 leaves):

$$\left( \operatorname{Cos}[c + d x]^4 \left( A \operatorname{Cos}\left[\frac{3 c}{2}\right] - i B \operatorname{Cos}\left[\frac{3 c}{2}\right] - i A \operatorname{Sin}\left[\frac{3 c}{2}\right] - B \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \right.$$

$$\left( -2 i \operatorname{Cos}\left[\frac{3 c}{2}\right] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - 2 \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}\left[\frac{3 c}{2}\right] \right)$$

$$\left. (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) +$$

$$\left( \operatorname{Cos}[c + d x]^2 (3 A \operatorname{Cos}[c] - 9 i B \operatorname{Cos}[c] + 2 B \operatorname{Sin}[c]) \left( -\frac{1}{6} i \operatorname{Cos}[3 c] - \frac{1}{6} \operatorname{Sin}[3 c] \right) \right.$$

$$\left. (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) / \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right)$$

$$\left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) +$$

$$\left( (A - i B) \operatorname{Cos}[c + d x]^4 (4 d x \operatorname{Cos}[3 c] - 4 i d x \operatorname{Sin}[3 c]) (a + i a \operatorname{Tan}[c + d x])^3 \right.$$

$$\left. (A + B \operatorname{Tan}[c + d x]) \right) / \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) -$$

$$\left( i B \operatorname{Cos}[c + d x] \left( \frac{1}{3} \operatorname{Cos}[3 c] - \frac{1}{3} i \operatorname{Sin}[3 c] \right) \operatorname{Sin}[d x] (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right.$$

$$\left. (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) +$$

$$\left( \operatorname{Cos}[c + d x]^3 \left( \frac{1}{3} \operatorname{Cos}[3 c] - \frac{1}{3} i \operatorname{Sin}[3 c] \right) (-9 A \operatorname{Sin}[d x] + 13 i B \operatorname{Sin}[d x]) \right.$$

$$\left. (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) / \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right.$$

$$\left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) +$$


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$$1$$

$$\left( \operatorname{Cos}[d x] + i \operatorname{Sin}[d x] \right)^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])$$

$$x \operatorname{Cos}[c + d x]^4 \left( -2 A \operatorname{Cos}[c] + 2 i B \operatorname{Cos}[c] + 2 A \operatorname{Cos}[c]^3 - 2 i B \operatorname{Cos}[c]^3 + 4 i A \operatorname{Sin}[c] + \right.$$

$$4 B \operatorname{Sin}[c] - 8 i A \operatorname{Cos}[c]^2 \operatorname{Sin}[c] - 8 B \operatorname{Cos}[c]^2 \operatorname{Sin}[c] - 12 A \operatorname{Cos}[c] \operatorname{Sin}[c]^2 +$$

$$12 i B \operatorname{Cos}[c] \operatorname{Sin}[c]^2 + 8 i A \operatorname{Sin}[c]^3 + 8 B \operatorname{Sin}[c]^3 + 2 A \operatorname{Sin}[c] \operatorname{Tan}[c] - 2 i B \operatorname{Sin}[c] \operatorname{Tan}[c] +$$

$$2 A \operatorname{Sin}[c]^3 \operatorname{Tan}[c] - 2 i B \operatorname{Sin}[c]^3 \operatorname{Tan}[c] + i (A - i B) (4 \operatorname{Cos}[3 c] - 4 i \operatorname{Sin}[3 c]) \operatorname{Tan}[c] \left. \right)$$

$$(a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x])$$

**Problem 20: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + d x] (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 107 leaves, 6 steps):

$$4 a^3 (i A + B) x + \frac{a^3 (3 A - 4 i B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} + \frac{a^3 A \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} + \frac{i a B (a + i a \operatorname{Tan}[c + d x])^2}{2 d} - \frac{(A - 2 i B) (a^3 + i a^3 \operatorname{Tan}[c + d x])}{d}$$

Result (type 3, 931 leaves):

$$\begin{aligned} & \left( A \operatorname{Cos}[3 c] \operatorname{Cos}[c + d x]^4 \operatorname{Log}[\operatorname{Sin}[c + d x]^2] (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) / \\ & \left( 2 d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \left( \operatorname{Cos}[c + d x]^4 \left( 3 A \operatorname{Cos}\left[\frac{3 c}{2}\right] - 4 i B \operatorname{Cos}\left[\frac{3 c}{2}\right] - 3 i A \operatorname{Sin}\left[\frac{3 c}{2}\right] - 4 B \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \right. \\ & \left. \left( \frac{1}{2} \operatorname{Cos}\left[\frac{3 c}{2}\right] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - \frac{1}{2} i \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) (a + i a \operatorname{Tan}[c + d x])^3 \right. \\ & \left. (A + B \operatorname{Tan}[c + d x]) \right) / \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) - \\ & \left( i A \operatorname{Cos}[c + d x]^4 \operatorname{Log}[\operatorname{Sin}[c + d x]^2] \operatorname{Sin}[3 c] (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) / \\ & \left( 2 d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \left( \operatorname{Cos}[c + d x]^2 \left( -\frac{1}{2} i B \operatorname{Cos}[3 c] - \frac{1}{2} B \operatorname{Sin}[3 c] \right) (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) / \\ & \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \left( (i A + B) \operatorname{Cos}[c + d x]^4 (4 d x \operatorname{Cos}[3 c] - 4 i d x \operatorname{Sin}[3 c]) (a + i a \operatorname{Tan}[c + d x])^3 \right. \\ & \left. (A + B \operatorname{Tan}[c + d x]) \right) / \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \left( \operatorname{Cos}[c + d x]^3 (\operatorname{Cos}[3 c] - i \operatorname{Sin}[3 c]) (-i A \operatorname{Sin}[d x] - 3 B \operatorname{Sin}[d x]) \right. \\ & \left. (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) / \left( d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\ & \left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \frac{1}{(\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} \\ & x \operatorname{Cos}[c + d x]^4 \left( -\frac{1}{2} i A \operatorname{Cos}[c] - 2 B \operatorname{Cos}[c] + \frac{7}{2} i A \operatorname{Cos}[c]^3 + 2 B \operatorname{Cos}[c]^3 - \frac{1}{2} A \operatorname{Cos}[c] \operatorname{Cot}[c] - \right. \\ & \left. \frac{1}{2} A \operatorname{Cos}[c]^3 \operatorname{Cot}[c] - \frac{5}{2} A \operatorname{Sin}[c] + 4 i B \operatorname{Sin}[c] + 9 A \operatorname{Cos}[c]^2 \operatorname{Sin}[c] - 8 i B \operatorname{Cos}[c]^2 \operatorname{Sin}[c] - \right. \\ & \left. 11 i A \operatorname{Cos}[c] \operatorname{Sin}[c]^2 - 12 B \operatorname{Cos}[c] \operatorname{Sin}[c]^2 - \frac{13}{2} A \operatorname{Sin}[c]^3 + 8 i B \operatorname{Sin}[c]^3 + \right. \\ & \left. (-A + 2 i B + 2 A \operatorname{Cos}[2 c] - 2 i B \operatorname{Cos}[2 c]) \operatorname{Csc}[c] \operatorname{Sec}[c] (\operatorname{Cos}[3 c] - i \operatorname{Sin}[3 c]) + \right. \\ & \left. \frac{3}{2} i A \operatorname{Sin}[c] \operatorname{Tan}[c] + 2 B \operatorname{Sin}[c] \operatorname{Tan}[c] + \frac{3}{2} i A \operatorname{Sin}[c]^3 \operatorname{Tan}[c] + 2 B \operatorname{Sin}[c]^3 \operatorname{Tan}[c] \right) \\ & (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \end{aligned}$$

**Problem 21: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + d x]^2 (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 116 leaves, 6 steps):

$$-4 a^3 (A - i B) x + \frac{a^3 (i A + 3 B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} + \frac{a^3 (3 i A + B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \frac{a A \operatorname{Cot}[c + d x] (a + i a \operatorname{Tan}[c + d x])^2}{d} + \frac{(i A - B) (a^3 + i a^3 \operatorname{Tan}[c + d x])}{d}$$

Result (type 3, 291 leaves):

$$\frac{1}{16 d} a^3 \operatorname{Csc}[c] \operatorname{Csc}[c + d x] \operatorname{Sec}[c] \operatorname{Sec}[c + d x] (14 A d x \operatorname{Cos}[4 c + 2 d x] - 10 i B d x \operatorname{Cos}[4 c + 2 d x] - i A \operatorname{Cos}[4 c + 2 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - 3 B \operatorname{Cos}[4 c + 2 d x] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - 3 i A \operatorname{Cos}[4 c + 2 d x] \operatorname{Log}[\operatorname{Sin}[c + d x]^2] - B \operatorname{Cos}[4 c + 2 d x] \operatorname{Log}[\operatorname{Sin}[c + d x]^2] + \operatorname{Cos}[2 d x] (2 (-7 A + 5 i B) d x + (i A + 3 B) \operatorname{Log}[\operatorname{Cos}[c + d x]^2] + (3 i A + B) \operatorname{Log}[\operatorname{Sin}[c + d x]^2])) - 4 A \operatorname{Sin}[2 c] - 4 i B \operatorname{Sin}[2 c] + 4 A \operatorname{Sin}[2 d x] - 4 i B \operatorname{Sin}[2 d x] + 4 A \operatorname{Sin}[2 (c + d x)] + 4 i B \operatorname{Sin}[2 (c + d x)] + 4 (3 A - i B) \operatorname{ArcTan}[\operatorname{Tan}[4 c + d x]] \operatorname{Sin}[2 c] \operatorname{Sin}[2 (c + d x)])$$

### Problem 22: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c + d x]^3 (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 123 leaves, 6 steps):

$$-4 a^3 (i A + B) x + \frac{i a^3 B \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \frac{a^3 (4 A - 3 i B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \frac{a A \operatorname{Cot}[c + d x]^2 (a + i a \operatorname{Tan}[c + d x])^2}{2 d} - \frac{(2 i A + B) \operatorname{Cot}[c + d x] (a^3 + i a^3 \operatorname{Tan}[c + d x])}{d}$$

Result (type 3, 1010 leaves):

$$\begin{aligned}
 & a^3 \left( \left( (i + \cot[c + dx])^3 (B + A \cot[c + dx]) \left( -\frac{1}{2} A \cos[3c] + \frac{1}{2} i A \sin[3c] \right) \sin[c + dx]^2 \right) / \right. \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( (i + \cot[c + dx])^3 (B + A \cot[c + dx]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \left( \frac{1}{2} \cos[3c] - \frac{1}{2} i \sin[3c] \right) (3 i A \sin[dx] + B \sin[dx]) \sin[c + dx]^3 \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( i B \cos[3c] (i + \cot[c + dx])^3 (B + A \cot[c + dx]) \operatorname{Log}[\cos[c + dx]^2] \sin[c + dx]^4 \right) / \\
 & \quad \left( 2 d (\cos[dx] + i \sin[dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right) + \left( (i + \cot[c + dx])^3 \right. \\
 & \quad \left. (B + A \cot[c + dx]) \left( 4 A \cos\left[\frac{3c}{2}\right] - 3 i B \cos\left[\frac{3c}{2}\right] - 4 i A \sin\left[\frac{3c}{2}\right] - 3 B \sin\left[\frac{3c}{2}\right] \right) \right. \\
 & \quad \left. \left( i \operatorname{ArcTan}[\tan[4c + dx]] \cos\left[\frac{3c}{2}\right] + \operatorname{ArcTan}[\tan[4c + dx]] \sin\left[\frac{3c}{2}\right] \right) \sin[c + dx]^4 \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right) + \left( (i + \cot[c + dx])^3 \right. \\
 & \quad \left. (B + A \cot[c + dx]) \left( 4 A \cos\left[\frac{3c}{2}\right] - 3 i B \cos\left[\frac{3c}{2}\right] - 4 i A \sin\left[\frac{3c}{2}\right] - 3 B \sin\left[\frac{3c}{2}\right] \right) \right. \\
 & \quad \left. \left( -\frac{1}{2} \cos\left[\frac{3c}{2}\right] \operatorname{Log}[\sin[c + dx]^2] + \frac{1}{2} i \operatorname{Log}[\sin[c + dx]^2] \sin\left[\frac{3c}{2}\right] \right) \sin[c + dx]^4 \right) / \\
 & \quad \left( d (\cos[dx] + i \sin[dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( B (i + \cot[c + dx])^3 (B + A \cot[c + dx]) \operatorname{Log}[\cos[c + dx]^2] \sin[3c] \sin[c + dx]^4 \right) / \\
 & \quad \left( 2 d (\cos[dx] + i \sin[dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \left( (A - i B) (i + \cot[c + dx])^3 (B + A \cot[c + dx]) (-4 i dx \cos[3c] - 4 dx \sin[3c]) \right. \\
 & \quad \left. \sin[c + dx]^4 \right) / \left( d (\cos[dx] + i \sin[dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right) + \\
 & \quad \frac{1}{\left( \cos[dx] + i \sin[dx] \right)^3 (A \cos[c + dx] + B \sin[c + dx])} \\
 & \quad \times (i + \cot[c + dx])^3 (B + A \cot[c + dx]) \sin[c + dx]^4 \\
 & \quad \left( \frac{1}{2} B \cos[c] - 16 i A \cos[c]^3 - \frac{25}{2} B \cos[c]^3 + 4 A \cos[c]^3 \cot[c] - 3 i B \cos[c]^3 \cot[c] - \right. \\
 & \quad i B \sin[c] - 24 A \cos[c]^2 \sin[c] + 20 i B \cos[c]^2 \sin[c] + 16 i A \cos[c] \sin[c]^2 + \\
 & \quad \left. 15 B \cos[c] \sin[c]^2 + 4 A \sin[c]^3 - 5 i B \sin[c]^3 + (2 A - i B + 2 A \cos[2c] - 2 i B \cos[2c]) \right. \\
 & \quad \left. \operatorname{Csc}[c] \operatorname{Sec}[c] (-\cos[3c] + i \sin[3c]) - \frac{1}{2} B \sin[c] \tan[c] - \frac{1}{2} B \sin[c]^3 \tan[c] \right) \Big)
 \end{aligned}$$

**Problem 23: Result more than twice size of optimal antiderivative.**

$$\int \cot[c + dx]^4 (a + i a \tan[c + dx])^3 (A + B \tan[c + dx]) dx$$

Optimal (type 3, 134 leaves, 5 steps):

$$4 a^3 (A - i B) x + \frac{a^3 (17 A - 15 i B) \operatorname{Cot}[c + d x]}{6 d} - \frac{4 a^3 (i A + B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \frac{a A \operatorname{Cot}[c + d x]^3 (a + i a \operatorname{Tan}[c + d x])^2}{3 d} - \frac{(5 i A + 3 B) \operatorname{Cot}[c + d x]^2 (a^3 + i a^3 \operatorname{Tan}[c + d x])}{6 d}$$

Result (type 3, 911 leaves):

$$\begin{aligned} & a^3 \left( \left( A (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \left(\frac{1}{6} \operatorname{Cos}[3 c] - \frac{1}{6} i \operatorname{Sin}[3 c]\right) \operatorname{Sin}[d x] \right. \right. \\ & \quad \left. \left. \operatorname{Sin}[c + d x] \right) / \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \right. \\ & \quad \left( (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (-2 A \operatorname{Cos}[c] - 9 i A \operatorname{Sin}[c] - 3 B \operatorname{Sin}[c]) \right. \\ & \quad \left. \left(\frac{1}{12} \operatorname{Cos}[3 c] - \frac{1}{12} i \operatorname{Sin}[3 c]\right) \operatorname{Sin}[c + d x]^2 \right) / \\ & \quad \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \left( (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \left(\frac{1}{6} \operatorname{Cos}[3 c] - \frac{1}{6} i \operatorname{Sin}[3 c]\right) \right. \\ & \quad \left. (-13 A \operatorname{Sin}[d x] + 9 i B \operatorname{Sin}[d x]) \operatorname{Sin}[c + d x]^3 \right) / \\ & \quad \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \left( (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \left( A \operatorname{Cos}\left[\frac{3 c}{2}\right] - i B \operatorname{Cos}\left[\frac{3 c}{2}\right] - i A \operatorname{Sin}\left[\frac{3 c}{2}\right] - B \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \right. \\ & \quad \left. \left(-4 \operatorname{ArcTan}[\operatorname{Tan}[4 c + d x]] \operatorname{Cos}\left[\frac{3 c}{2}\right] + 4 i \operatorname{ArcTan}[\operatorname{Tan}[4 c + d x]] \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \operatorname{Sin}[c + d x]^4 \right) / \\ & \quad \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \left( (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \left( A \operatorname{Cos}\left[\frac{3 c}{2}\right] - i B \operatorname{Cos}\left[\frac{3 c}{2}\right] - i A \operatorname{Sin}\left[\frac{3 c}{2}\right] - B \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \right. \\ & \quad \left. \left(-2 i \operatorname{Cos}\left[\frac{3 c}{2}\right] \operatorname{Log}[\operatorname{Sin}[c + d x]^2] - 2 \operatorname{Log}[\operatorname{Sin}[c + d x]^2] \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \operatorname{Sin}[c + d x]^4 \right) / \\ & \quad \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \frac{1}{(\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} x (i + \operatorname{Cot}[c + d x])^3 \\ & \quad (B + A \operatorname{Cot}[c + d x]) (16 A \operatorname{Cos}[c]^3 - 16 i B \operatorname{Cos}[c]^3 + 4 i A \operatorname{Cos}[c]^3 \operatorname{Cot}[c] + 4 B \operatorname{Cos}[c]^3 \operatorname{Cot}[c] - \\ & \quad 24 i A \operatorname{Cos}[c]^2 \operatorname{Sin}[c] - 24 B \operatorname{Cos}[c]^2 \operatorname{Sin}[c] - 16 A \operatorname{Cos}[c] \operatorname{Sin}[c]^2 + 16 i B \operatorname{Cos}[c] \operatorname{Sin}[c]^2 + \\ & \quad 4 i A \operatorname{Sin}[c]^3 + 4 B \operatorname{Sin}[c]^3 - i (A - i B) \operatorname{Cot}[c] (4 \operatorname{Cos}[3 c] - 4 i \operatorname{Sin}[3 c])) \operatorname{Sin}[c + d x]^4 + \\ & \quad \left. \left. (A - i B) (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) (4 d x \operatorname{Cos}[3 c] - 4 i d x \operatorname{Sin}[3 c]) \right. \right. \\ & \quad \left. \left. \operatorname{Sin}[c + d x]^4 \right) / \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) \end{aligned}$$

**Problem 24: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + d x]^5 (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 157 leaves, 6 steps):

$$\begin{aligned}
 & 4 a^3 (i A + B) x + \frac{4 a^3 (i A + B) \operatorname{Cot}[c + d x]}{d} + \\
 & \frac{a^3 (15 A - 14 i B) \operatorname{Cot}[c + d x]^2}{12 d} + \frac{4 a^3 (A - i B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \\
 & \frac{a A \operatorname{Cot}[c + d x]^4 (a + i a \operatorname{Tan}[c + d x])^2}{4 d} - \frac{(3 i A + 2 B) \operatorname{Cot}[c + d x]^3 (a^3 + i a^3 \operatorname{Tan}[c + d x])}{6 d}
 \end{aligned}$$

Result (type 3, 1007 leaves):

$$\begin{aligned}
 & a^3 \left( \left( (\dot{i} + \text{Cot}[c + d x])^3 (B + A \text{Cot}[c + d x]) \left( -\frac{1}{4} A \text{Cos}[3 c] + \frac{1}{4} \dot{i} A \text{Sin}[3 c] \right) \right) / \right. \\
 & \quad \left( d (\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\
 & \quad \left( (\dot{i} + \text{Cot}[c + d x])^3 (B + A \text{Cot}[c + d x]) \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \right. \\
 & \quad \quad \left. \left( \frac{1}{6} \text{Cos}[3 c] - \frac{1}{6} \dot{i} \text{Sin}[3 c] \right) (3 \dot{i} A \text{Sin}[d x] + B \text{Sin}[d x]) \text{Sin}[c + d x] \right) / \\
 & \quad \left( d (\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\
 & \quad \left( (\dot{i} + \text{Cot}[c + d x])^3 (B + A \text{Cot}[c + d x]) \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \right. \\
 & \quad \quad \left. (-6 \dot{i} A \text{Cos}[c] - 2 B \text{Cos}[c] + 15 A \text{Sin}[c] - 9 \dot{i} B \text{Sin}[c]) \left( \frac{1}{12} \text{Cos}[3 c] - \frac{1}{12} \dot{i} \text{Sin}[3 c] \right) \right. \\
 & \quad \quad \left. \text{Sin}[c + d x]^2 \right) / \left( d (\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\
 & \quad \left( (\dot{i} + \text{Cot}[c + d x])^3 (B + A \text{Cot}[c + d x]) \text{Csc}\left[\frac{c}{2}\right] \text{Sec}\left[\frac{c}{2}\right] \left( \frac{1}{6} \text{Cos}[3 c] - \frac{1}{6} \dot{i} \text{Sin}[3 c] \right) \right. \\
 & \quad \quad \left. (-15 \dot{i} A \text{Sin}[d x] - 13 B \text{Sin}[d x]) \text{Sin}[c + d x]^3 \right) / \\
 & \quad \left( d (\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\
 & \quad \left( (\dot{i} + \text{Cot}[c + d x])^3 (B + A \text{Cot}[c + d x]) \left( A \text{Cos}\left[\frac{3 c}{2}\right] - \dot{i} B \text{Cos}\left[\frac{3 c}{2}\right] - \dot{i} A \text{Sin}\left[\frac{3 c}{2}\right] - B \text{Sin}\left[\frac{3 c}{2}\right] \right) \right. \\
 & \quad \quad \left. \left( -4 \dot{i} \text{ArcTan}[\text{Tan}[4 c + d x]] \text{Cos}\left[\frac{3 c}{2}\right] - 4 \text{ArcTan}[\text{Tan}[4 c + d x]] \text{Sin}\left[\frac{3 c}{2}\right] \right) \text{Sin}[c + d x]^4 \right) / \\
 & \quad \left( d (\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\
 & \quad \left( (\dot{i} + \text{Cot}[c + d x])^3 (B + A \text{Cot}[c + d x]) \left( A \text{Cos}\left[\frac{3 c}{2}\right] - \dot{i} B \text{Cos}\left[\frac{3 c}{2}\right] - \dot{i} A \text{Sin}\left[\frac{3 c}{2}\right] - B \text{Sin}\left[\frac{3 c}{2}\right] \right) \right. \\
 & \quad \quad \left. \left( 2 \text{Cos}\left[\frac{3 c}{2}\right] \text{Log}[\text{Sin}[c + d x]^2] - 2 \dot{i} \text{Log}[\text{Sin}[c + d x]^2] \text{Sin}\left[\frac{3 c}{2}\right] \right) \text{Sin}[c + d x]^4 \right) / \\
 & \quad \left( d (\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\
 & \quad \frac{1}{(\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x])} x (\dot{i} + \text{Cot}[c + d x])^3 \\
 & \quad (B + A \text{Cot}[c + d x]) (16 \dot{i} A \text{Cos}[c]^3 + 16 B \text{Cos}[c]^3 - 4 A \text{Cos}[c]^3 \text{Cot}[c] + 4 \dot{i} B \text{Cos}[c]^3 \text{Cot}[c] + \\
 & \quad 24 A \text{Cos}[c]^2 \text{Sin}[c] - 24 \dot{i} B \text{Cos}[c]^2 \text{Sin}[c] - 16 \dot{i} A \text{Cos}[c] \text{Sin}[c]^2 - 16 B \text{Cos}[c] \text{Sin}[c]^2 - \\
 & \quad 4 A \text{Sin}[c]^3 + 4 \dot{i} B \text{Sin}[c]^3 + (A - \dot{i} B) \text{Cot}[c] (4 \text{Cos}[3 c] - 4 \dot{i} \text{Sin}[3 c])) \text{Sin}[c + d x]^4 + \\
 & \quad \left. \left( (\dot{i} A + B) (\dot{i} + \text{Cot}[c + d x])^3 (B + A \text{Cot}[c + d x]) (4 d x \text{Cos}[3 c] - 4 \dot{i} d x \text{Sin}[3 c]) \right. \right. \\
 & \quad \quad \left. \left. \text{Sin}[c + d x]^4 \right) / \left( d (\text{Cos}[d x] + \dot{i} \text{Sin}[d x])^3 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) \right)
 \end{aligned}$$

**Problem 25: Result more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x]^6 (a + \dot{i} a \text{Tan}[c + d x])^3 (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 180 leaves, 7 steps):

$$\begin{aligned}
 & -4 a^3 (A - i B) x - \frac{4 a^3 (A - i B) \operatorname{Cot}[c + d x]}{d} + \frac{2 a^3 (i A + B) \operatorname{Cot}[c + d x]^2}{d} + \\
 & \frac{a^3 (47 A - 45 i B) \operatorname{Cot}[c + d x]^3}{60 d} + \frac{4 a^3 (i A + B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \\
 & \frac{a A \operatorname{Cot}[c + d x]^5 (a + i a \operatorname{Tan}[c + d x])^2}{5 d} - \frac{(7 i A + 5 B) \operatorname{Cot}[c + d x]^4 (a^3 + i a^3 \operatorname{Tan}[c + d x])}{20 d}
 \end{aligned}$$

Result (type 3, 943 leaves):

$$\begin{aligned}
 & a^3 \left( \left( (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \left( i A \operatorname{Cos}\left[\frac{3 c}{2}\right] + B \operatorname{Cos}\left[\frac{3 c}{2}\right] + A \operatorname{Sin}\left[\frac{3 c}{2}\right] - i B \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \right. \right. \\
 & \quad \left. \left. \left( -4 i \operatorname{ArcTan}[\operatorname{Tan}[4 c + d x]] \operatorname{Cos}\left[\frac{3 c}{2}\right] - 4 \operatorname{ArcTan}[\operatorname{Tan}[4 c + d x]] \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \operatorname{Sin}[c + d x]^4 \right) / \right. \\
 & \quad \left. \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \right. \\
 & \quad \left. \left( (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \left( i A \operatorname{Cos}\left[\frac{3 c}{2}\right] + B \operatorname{Cos}\left[\frac{3 c}{2}\right] + A \operatorname{Sin}\left[\frac{3 c}{2}\right] - i B \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \right. \right. \\
 & \quad \left. \left. \left( 2 \operatorname{Cos}\left[\frac{3 c}{2}\right] \operatorname{Log}[\operatorname{Sin}[c + d x]^2] - 2 i \operatorname{Log}[\operatorname{Sin}[c + d x]^2] \operatorname{Sin}\left[\frac{3 c}{2}\right] \right) \operatorname{Sin}[c + d x]^4 \right) / \right. \\
 & \quad \left. \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \right. \\
 & \quad \left. \frac{1}{(\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} \right. \\
 & \quad \left. x (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \right. \\
 & \quad \left. (-16 A \operatorname{Cos}[c]^3 + 16 i B \operatorname{Cos}[c]^3 - 4 i A \operatorname{Cos}[c]^3 \operatorname{Cot}[c] - 4 B \operatorname{Cos}[c]^3 \operatorname{Cot}[c] + \right. \\
 & \quad \left. 24 i A \operatorname{Cos}[c]^2 \operatorname{Sin}[c] + 24 B \operatorname{Cos}[c]^2 \operatorname{Sin}[c] + 16 A \operatorname{Cos}[c] \operatorname{Sin}[c]^2 - 16 i B \operatorname{Cos}[c] \operatorname{Sin}[c]^2 - \right. \\
 & \quad \left. 4 i A \operatorname{Sin}[c]^3 - 4 B \operatorname{Sin}[c]^3 + (i A + B) \operatorname{Cot}[c] (4 \operatorname{Cos}[3 c] - 4 i \operatorname{Sin}[3 c])) \operatorname{Sin}[c + d x]^4 + \right. \\
 & \quad \left. \frac{1}{d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} \right. \\
 & \quad \left. (i + \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c] \operatorname{Csc}[c + d x] \left( \frac{1}{240} \operatorname{Cos}[3 c] - \frac{1}{240} i \operatorname{Sin}[3 c] \right) \right. \\
 & \quad \left. (225 i A \operatorname{Cos}[d x] + 195 B \operatorname{Cos}[d x] - 300 A d x \operatorname{Cos}[d x] + 300 i B d x \operatorname{Cos}[d x] - \right. \\
 & \quad \left. 225 i A \operatorname{Cos}[2 c + d x] - 195 B \operatorname{Cos}[2 c + d x] + 300 A d x \operatorname{Cos}[2 c + d x] - \right. \\
 & \quad \left. 300 i B d x \operatorname{Cos}[2 c + d x] - 105 i A \operatorname{Cos}[2 c + 3 d x] - 75 B \operatorname{Cos}[2 c + 3 d x] + \right. \\
 & \quad \left. 150 A d x \operatorname{Cos}[2 c + 3 d x] - 150 i B d x \operatorname{Cos}[2 c + 3 d x] + 105 i A \operatorname{Cos}[4 c + 3 d x] + \right. \\
 & \quad \left. 75 B \operatorname{Cos}[4 c + 3 d x] - 150 A d x \operatorname{Cos}[4 c + 3 d x] + 150 i B d x \operatorname{Cos}[4 c + 3 d x] - \right. \\
 & \quad \left. 30 A d x \operatorname{Cos}[4 c + 5 d x] + 30 i B d x \operatorname{Cos}[4 c + 5 d x] + 30 A d x \operatorname{Cos}[6 c + 5 d x] - \right. \\
 & \quad \left. 30 i B d x \operatorname{Cos}[6 c + 5 d x] + 470 A \operatorname{Sin}[d x] - 420 i B \operatorname{Sin}[d x] + 360 A \operatorname{Sin}[2 c + d x] - \right. \\
 & \quad \left. 330 i B \operatorname{Sin}[2 c + d x] - 280 A \operatorname{Sin}[2 c + 3 d x] + 270 i B \operatorname{Sin}[2 c + 3 d x] - 135 A \operatorname{Sin}[4 c + 3 d x] + \right. \\
 & \quad \left. 105 i B \operatorname{Sin}[4 c + 3 d x] + 83 A \operatorname{Sin}[4 c + 5 d x] - 75 i B \operatorname{Sin}[4 c + 5 d x] \right) \left. \right)
 \end{aligned}$$

**Problem 26: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Tan}[c + d x]^2 (a + i a \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 225 leaves, 7 steps):



$$\begin{aligned}
 & -8 a^4 (A - i B) x + \frac{8 a^4 (i A + B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} + \frac{8 a^4 (A - i B) \operatorname{Tan}[c + d x]}{d} + \\
 & \frac{4 a^4 (i A + B) \operatorname{Tan}[c + d x]^2}{d} - \frac{a^4 (92 A - 93 i B) \operatorname{Tan}[c + d x]^3}{60 d} + \\
 & \frac{i a B \operatorname{Tan}[c + d x]^3 (a + i a \operatorname{Tan}[c + d x])^3}{6 d} - \frac{(2 A - 3 i B) \operatorname{Tan}[c + d x]^3 (a^2 + i a^2 \operatorname{Tan}[c + d x])^2}{10 d} - \\
 & \frac{(12 A - 13 i B) \operatorname{Tan}[c + d x]^3 (a^4 + i a^4 \operatorname{Tan}[c + d x])}{20 d}
 \end{aligned}$$

Result (type 3, 951 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c + d x]^5 (i A \operatorname{Cos}[2 c] + B \operatorname{Cos}[2 c] + A \operatorname{Sin}[2 c] - i B \operatorname{Sin}[2 c]) \right. \\
 & \quad \left. (4 \operatorname{Cos}[2 c] \operatorname{Log}[\operatorname{Cos}[c + d x]^2] - 4 i \operatorname{Log}[\operatorname{Cos}[c + d x]^2] \operatorname{Sin}[2 c]) (a + i a \operatorname{Tan}[c + d x])^4 \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + d x]) \right) / \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \frac{1}{d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} \\
 & \operatorname{Sec}[c] \operatorname{Sec}[c + d x] \left( \frac{1}{240} \operatorname{Cos}[4 c] - \frac{1}{240} i \operatorname{Sin}[4 c] \right) \\
 & (420 i A \operatorname{Cos}[c] + 490 B \operatorname{Cos}[c] - 600 A d x \operatorname{Cos}[c] + 600 i B d x \operatorname{Cos}[c] + 300 i A \operatorname{Cos}[c + 2 d x] + \\
 & \quad 345 B \operatorname{Cos}[c + 2 d x] - 450 A d x \operatorname{Cos}[c + 2 d x] + 450 i B d x \operatorname{Cos}[c + 2 d x] + \\
 & \quad 300 i A \operatorname{Cos}[3 c + 2 d x] + 345 B \operatorname{Cos}[3 c + 2 d x] - 450 A d x \operatorname{Cos}[3 c + 2 d x] + \\
 & \quad 450 i B d x \operatorname{Cos}[3 c + 2 d x] + 90 i A \operatorname{Cos}[3 c + 4 d x] + 120 B \operatorname{Cos}[3 c + 4 d x] - \\
 & \quad 180 A d x \operatorname{Cos}[3 c + 4 d x] + 180 i B d x \operatorname{Cos}[3 c + 4 d x] + 90 i A \operatorname{Cos}[5 c + 4 d x] + \\
 & \quad 120 B \operatorname{Cos}[5 c + 4 d x] - 180 A d x \operatorname{Cos}[5 c + 4 d x] + 180 i B d x \operatorname{Cos}[5 c + 4 d x] - \\
 & \quad 30 A d x \operatorname{Cos}[5 c + 6 d x] + 30 i B d x \operatorname{Cos}[5 c + 6 d x] - 30 A d x \operatorname{Cos}[7 c + 6 d x] + \\
 & \quad 30 i B d x \operatorname{Cos}[7 c + 6 d x] - 790 A \operatorname{Sin}[c] + 860 i B \operatorname{Sin}[c] + 720 A \operatorname{Sin}[c + 2 d x] - \\
 & \quad 780 i B \operatorname{Sin}[c + 2 d x] - 465 A \operatorname{Sin}[3 c + 2 d x] + 510 i B \operatorname{Sin}[3 c + 2 d x] + 354 A \operatorname{Sin}[3 c + 4 d x] - \\
 & \quad 366 i B \operatorname{Sin}[3 c + 4 d x] - 120 A \operatorname{Sin}[5 c + 4 d x] + 150 i B \operatorname{Sin}[5 c + 4 d x] + \\
 & \quad 79 A \operatorname{Sin}[5 c + 6 d x] - 86 i B \operatorname{Sin}[5 c + 6 d x]) (a + i a \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) + \\
 & \frac{1}{(\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} \\
 & x \operatorname{Cos}[c + d x]^5 (4 A \operatorname{Cos}[c]^2 - 4 i B \operatorname{Cos}[c]^2 - 4 A \operatorname{Cos}[c]^4 + 4 i B \operatorname{Cos}[c]^4 - 12 i A \operatorname{Cos}[c] \operatorname{Sin}[c] - \\
 & \quad 12 B \operatorname{Cos}[c] \operatorname{Sin}[c] + 20 i A \operatorname{Cos}[c]^3 \operatorname{Sin}[c] + 20 B \operatorname{Cos}[c]^3 \operatorname{Sin}[c] - 12 A \operatorname{Sin}[c]^2 + \\
 & \quad 12 i B \operatorname{Sin}[c]^2 + 40 A \operatorname{Cos}[c]^2 \operatorname{Sin}[c]^2 - 40 i B \operatorname{Cos}[c]^2 \operatorname{Sin}[c]^2 - 40 i A \operatorname{Cos}[c] \operatorname{Sin}[c]^3 - \\
 & \quad 40 B \operatorname{Cos}[c] \operatorname{Sin}[c]^3 - 20 A \operatorname{Sin}[c]^4 + 20 i B \operatorname{Sin}[c]^4 + 4 i A \operatorname{Sin}[c]^2 \operatorname{Tan}[c] + 4 B \operatorname{Sin}[c]^2 \operatorname{Tan}[c] + \\
 & \quad 4 i A \operatorname{Sin}[c]^4 \operatorname{Tan}[c] + 4 B \operatorname{Sin}[c]^4 \operatorname{Tan}[c] - i (A - i B) (8 \operatorname{Cos}[4 c] - 8 i \operatorname{Sin}[4 c]) \operatorname{Tan}[c]) \\
 & (a + i a \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x])
 \end{aligned}$$

**Problem 27: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Tan}[c + d x] (a + i a \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 168 leaves, 6 steps):

$$\begin{aligned}
 & -8 a^4 (\text{i A} + \text{B}) x - \frac{8 a^4 (A - \text{i B}) \text{Log}[\text{Cos}[c + d x]]}{d} + \\
 & \frac{4 a^4 (\text{i A} + \text{B}) \text{Tan}[c + d x]}{d} + \frac{a (A - \text{i B}) (a + \text{i a Tan}[c + d x])^3}{3 d} + \\
 & \frac{A (a + \text{i a Tan}[c + d x])^4}{4 d} - \frac{\text{i B} (a + \text{i a Tan}[c + d x])^5}{5 a d} + \frac{(A - \text{i B}) (a^2 + \text{i a}^2 \text{Tan}[c + d x])^2}{d}
 \end{aligned}$$

Result (type 3, 879 leaves):

$$\begin{aligned}
 & (\text{Cos}[c + d x]^5 (A \text{Cos}[2 c] - \text{i B Cos}[2 c] - \text{i A Sin}[2 c] - B \text{Sin}[2 c]) \\
 & (-4 \text{Cos}[2 c] \text{Log}[\text{Cos}[c + d x]^2] + 4 \text{i Log}[\text{Cos}[c + d x]^2] \text{Sin}[2 c]) (a + \text{i a Tan}[c + d x])^4 \\
 & (A + B \text{Tan}[c + d x])) / (d (\text{Cos}[d x] + \text{i Sin}[d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x])) + \\
 & \frac{1}{d (\text{Cos}[d x] + \text{i Sin}[d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x])} \\
 & \text{Sec}[c] \left( \frac{1}{120} \text{Cos}[4 c] - \frac{1}{120} \text{i Sin}[4 c] \right) (-165 A \text{Cos}[d x] + 210 \text{i B Cos}[d x] - \\
 & 300 \text{i A d x Cos}[d x] - 300 B d x \text{Cos}[d x] - 165 A \text{Cos}[2 c + d x] + 210 \text{i B Cos}[2 c + d x] - \\
 & 300 \text{i A d x Cos}[2 c + d x] - 300 B d x \text{Cos}[2 c + d x] - 60 A \text{Cos}[2 c + 3 d x] + \\
 & 90 \text{i B Cos}[2 c + 3 d x] - 150 \text{i A d x Cos}[2 c + 3 d x] - 150 B d x \text{Cos}[2 c + 3 d x] - \\
 & 60 A \text{Cos}[4 c + 3 d x] + 90 \text{i B Cos}[4 c + 3 d x] - 150 \text{i A d x Cos}[4 c + 3 d x] - \\
 & 150 B d x \text{Cos}[4 c + 3 d x] - 30 \text{i A d x Cos}[4 c + 5 d x] - 30 B d x \text{Cos}[4 c + 5 d x] - \\
 & 30 \text{i A d x Cos}[6 c + 5 d x] - 30 B d x \text{Cos}[6 c + 5 d x] + 400 \text{i A Sin}[d x] + 445 B \text{Sin}[d x] - \\
 & 300 \text{i A Sin}[2 c + d x] - 345 B \text{Sin}[2 c + d x] + 260 \text{i A Sin}[2 c + 3 d x] + 275 B \text{Sin}[2 c + 3 d x] - \\
 & 90 \text{i A Sin}[4 c + 3 d x] - 120 B \text{Sin}[4 c + 3 d x] + 70 \text{i A Sin}[4 c + 5 d x] + 79 B \text{Sin}[4 c + 5 d x]) \\
 & (a + \text{i a Tan}[c + d x])^4 (A + B \text{Tan}[c + d x]) + \\
 & \frac{1}{(\text{Cos}[d x] + \text{i Sin}[d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x])} \\
 & x \text{Cos}[c + d x]^5 (4 \text{i A Cos}[c]^2 + 4 B \text{Cos}[c]^2 - 4 \text{i A Cos}[c]^4 - 4 B \text{Cos}[c]^4 + \\
 & 12 A \text{Cos}[c] \text{Sin}[c] - 12 \text{i B Cos}[c] \text{Sin}[c] - 20 A \text{Cos}[c]^3 \text{Sin}[c] + 20 \text{i B Cos}[c]^3 \text{Sin}[c] - \\
 & 12 \text{i A Sin}[c]^2 - 12 B \text{Sin}[c]^2 + 40 \text{i A Cos}[c]^2 \text{Sin}[c]^2 + 40 B \text{Cos}[c]^2 \text{Sin}[c]^2 + \\
 & 40 A \text{Cos}[c] \text{Sin}[c]^3 - 40 \text{i B Cos}[c] \text{Sin}[c]^3 - 20 \text{i A Sin}[c]^4 - 20 B \text{Sin}[c]^4 - \\
 & 4 A \text{Sin}[c]^2 \text{Tan}[c] + 4 \text{i B Sin}[c]^2 \text{Tan}[c] - 4 A \text{Sin}[c]^4 \text{Tan}[c] + 4 \text{i B Sin}[c]^4 \text{Tan}[c] + \\
 & (A - \text{i B}) (8 \text{Cos}[4 c] - 8 \text{i Sin}[4 c]) \text{Tan}[c]) (a + \text{i a Tan}[c + d x])^4 (A + B \text{Tan}[c + d x])
 \end{aligned}$$

### Problem 28: Result more than twice size of optimal antiderivative.

$$\int (a + \text{i a Tan}[c + d x])^4 (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 140 leaves, 5 steps):

$$\begin{aligned}
 & 8 a^4 (A - \text{i B}) x - \frac{8 a^4 (\text{i A} + \text{B}) \text{Log}[\text{Cos}[c + d x]]}{d} - \frac{4 a^4 (A - \text{i B}) \text{Tan}[c + d x]}{d} + \\
 & \frac{a (\text{i A} + \text{B}) (a + \text{i a Tan}[c + d x])^3}{3 d} + \frac{B (a + \text{i a Tan}[c + d x])^4}{4 d} + \frac{(\text{i A} + \text{B}) (a^2 + \text{i a}^2 \text{Tan}[c + d x])^2}{d}
 \end{aligned}$$

Result (type 3, 937 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^5 \left( A \cos [2 c]-i B \cos [2 c]-i A \sin [2 c]-B \sin [2 c] \right) \right. \\
 & \quad \left. \left( -4 i \cos [2 c] \log [\cos [c+d x]^2]-4 \log [\cos [c+d x]^2] \sin [2 c] \right) \left( a+i a \tan [c+d x] \right)^4 \right. \\
 & \quad \left. \left( A+B \tan [c+d x] \right) \right) / \left( d \left( \cos [d x]+i \sin [d x] \right)^4 \left( A \cos [c+d x]+B \sin [c+d x] \right) \right) + \\
 & \left( \cos [c+d x]^3 \sec [c] \left( 6 A \cos [c]-12 i B \cos [c]+i A \sin [c]+4 B \sin [c] \right) \right. \\
 & \quad \left. \left( -\frac{1}{3} i \cos [4 c]-\frac{1}{3} \sin [4 c] \right) \left( a+i a \tan [c+d x] \right)^4 \left( A+B \tan [c+d x] \right) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^4 \left( A \cos [c+d x]+B \sin [c+d x] \right) \right) + \\
 & \left( \cos [c+d x] \left( \frac{1}{4} B \cos [4 c]-\frac{1}{4} i B \sin [4 c] \right) \left( a+i a \tan [c+d x] \right)^4 \left( A+B \tan [c+d x] \right) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^4 \left( A \cos [c+d x]+B \sin [c+d x] \right) \right) + \\
 & \left( (A-i B) \cos [c+d x]^5 \left( 8 d x \cos [4 c]-8 i d x \sin [4 c] \right) \left( a+i a \tan [c+d x] \right)^4 \right. \\
 & \quad \left. \left( A+B \tan [c+d x] \right) \right) / \left( d \left( \cos [d x]+i \sin [d x] \right)^4 \left( A \cos [c+d x]+B \sin [c+d x] \right) \right) + \\
 & \left( \cos [c+d x]^2 \sec [c] \left( \frac{1}{3} \cos [4 c]-\frac{1}{3} i \sin [4 c] \right) \left( A \sin [d x]-4 i B \sin [d x] \right) \right. \\
 & \quad \left. \left( a+i a \tan [c+d x] \right)^4 \left( A+B \tan [c+d x] \right) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^4 \left( A \cos [c+d x]+B \sin [c+d x] \right) \right) + \\
 & \left( \cos [c+d x]^4 \sec [c] \left( -\frac{2}{3} \cos [4 c]+\frac{2}{3} i \sin [4 c] \right) \right. \\
 & \quad \left. \left( 11 A \sin [d x]-14 i B \sin [d x] \right) \left( a+i a \tan [c+d x] \right)^4 \left( A+B \tan [c+d x] \right) \right) / \\
 & \left( d \left( \cos [d x]+i \sin [d x] \right)^4 \left( A \cos [c+d x]+B \sin [c+d x] \right) \right) + \\
 & \frac{1}{\left( \cos [d x]+i \sin [d x] \right)^4 \left( A \cos [c+d x]+B \sin [c+d x] \right)} \\
 & x \cos [c+d x]^5 \left( -4 A \cos [c]^2+4 i B \cos [c]^2+4 A \cos [c]^4-4 i B \cos [c]^4+12 i A \cos [c] \sin [c]+ \right. \\
 & \quad 12 B \cos [c] \sin [c]-20 i A \cos [c]^3 \sin [c]-20 B \cos [c]^3 \sin [c]+12 A \sin [c]^2- \\
 & \quad 12 i B \sin [c]^2-40 A \cos [c]^2 \sin [c]^2+40 i B \cos [c]^2 \sin [c]^2+40 i A \cos [c] \sin [c]^3+ \\
 & \quad 40 B \cos [c] \sin [c]^3+20 A \sin [c]^4-20 i B \sin [c]^4-4 i A \sin [c]^2 \tan [c]-4 B \sin [c]^2 \tan [c]- \\
 & \quad \left. 4 i A \sin [c]^4 \tan [c]-4 B \sin [c]^4 \tan [c]+(i A+B) \left( 8 \cos [4 c]-8 i \sin [4 c] \right) \tan [c] \right) \\
 & \quad \left. \left( a+i a \tan [c+d x] \right)^4 \left( A+B \tan [c+d x] \right) \right)
 \end{aligned}$$

**Problem 29: Result more than twice size of optimal antiderivative.**

$$\int \cot [c+d x] \left( a+i a \tan [c+d x] \right)^4 \left( A+B \tan [c+d x] \right) dx$$

Optimal (type 3, 142 leaves, 7 steps):

$$\begin{aligned}
 & 8 a^4 (i A+B) x + \frac{a^4 (7 A-8 i B) \log [\cos [c+d x]]}{d} + \\
 & \frac{a^4 A \log [\sin [c+d x]]}{d} + \frac{i a B \left( a+i a \tan [c+d x] \right)^3}{3 d} - \\
 & \frac{(A-2 i B) \left( a^2+i a^2 \tan [c+d x] \right)^2}{2 d} - \frac{(3 A-4 i B) \left( a^4+i a^4 \tan [c+d x] \right)}{d}
 \end{aligned}$$

Result (type 3, 1060 leaves):

$$\begin{aligned}
 & \left( A \cos[4c] \cos[c+dx]^5 \log[\sin[c+dx]^2] (a+ia \tan[c+dx])^4 (A+B \tan[c+dx]) \right) / \\
 & \left( 2d (\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( \cos[c+dx]^5 (7A \cos[2c] - 8iB \cos[2c] - 7iA \sin[2c] - 8B \sin[2c]) \right. \\
 & \left. \left( \frac{1}{2} \cos[2c] \log[\cos[c+dx]^2] - \frac{1}{2} i \log[\cos[c+dx]^2] \sin[2c] \right) (a+ia \tan[c+dx])^4 \right. \\
 & \left. (A+B \tan[c+dx]) \right) / \left( d (\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( \cos[c+dx]^3 \sec[c] (3A \cos[c] - 12iB \cos[c] + 2B \sin[c]) \right. \\
 & \left. \left( \frac{1}{6} \cos[4c] - \frac{1}{6} i \sin[4c] \right) (a+ia \tan[c+dx])^4 (A+B \tan[c+dx]) \right) / \\
 & \left( d (\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx]) \right) - \\
 & \left( iA \cos[c+dx]^5 \log[\sin[c+dx]^2] \sin[4c] (a+ia \tan[c+dx])^4 (A+B \tan[c+dx]) \right) / \\
 & \left( 2d (\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( (iA+B) \cos[c+dx]^5 (8dx \cos[4c] - 8i dx \sin[4c]) (a+ia \tan[c+dx])^4 \right. \\
 & \left. (A+B \tan[c+dx]) \right) / \left( d (\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( B \cos[c+dx]^2 \sec[c] \left( \frac{1}{3} \cos[4c] - \frac{1}{3} i \sin[4c] \right) \sin[dx] (a+ia \tan[c+dx])^4 \right. \\
 & \left. (A+B \tan[c+dx]) \right) / \left( d (\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( \cos[c+dx]^4 \sec[c] \left( \frac{2}{3} \cos[4c] - \frac{2}{3} i \sin[4c] \right) (-6iA \sin[dx] - 11B \sin[dx]) \right. \\
 & \left. (a+ia \tan[c+dx])^4 (A+B \tan[c+dx]) \right) / \\
 & \left( d (\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \frac{1}{(\cos[dx] + i \sin[dx])^4 (A \cos[c+dx] + B \sin[c+dx])} \\
 & x \cos[c+dx]^5 \left( -2iA \cos[c]^2 - 4B \cos[c]^2 + 6iA \cos[c]^4 + 4B \cos[c]^4 - \frac{1}{2} A \cos[c]^2 \cot[c] - \right. \\
 & \frac{1}{2} A \cos[c]^4 \cot[c] - 9A \cos[c] \sin[c] + 12iB \cos[c] \sin[c] + \frac{45}{2} A \cos[c]^3 \sin[c] - \\
 & 20iB \cos[c]^3 \sin[c] + 10iA \sin[c]^2 + 12B \sin[c]^2 - 40iA \cos[c]^2 \sin[c]^2 - 40B \cos[c]^2 \\
 & \sin[c]^2 - \frac{75}{2} A \cos[c] \sin[c]^3 + 40iB \cos[c] \sin[c]^3 + 18iA \sin[c]^4 + 20B \sin[c]^4 + \\
 & \left. (-3A + 4iB + 4A \cos[2c] - 4iB \cos[2c]) \csc[c] \sec[c] (\cos[4c] - i \sin[4c]) + \right. \\
 & \left. \frac{7}{2} A \sin[c]^2 \tan[c] - 4iB \sin[c]^2 \tan[c] + \frac{7}{2} A \sin[c]^4 \tan[c] - 4iB \sin[c]^4 \tan[c] \right) \\
 & (a+ia \tan[c+dx])^4 (A+B \tan[c+dx])
 \end{aligned}$$

### Problem 30: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x]^2 (a + i a \tan [c + d x])^4 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 144 leaves, 7 steps):

$$\begin{aligned}
 & -8 a^4 (A - i B) x + \frac{a^4 (4 i A + 7 B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} + \\
 & \frac{a^4 (4 i A + B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \frac{a A \cot [c + d x] (a + i a \tan [c + d x])^3}{d} + \\
 & \frac{(2 i A - B) (a^2 + i a^2 \tan [c + d x])^2}{2 d} - \frac{3 B (a^4 + i a^4 \tan [c + d x])}{d}
 \end{aligned}$$

Result (type 3, 1122 leaves):

a<sup>4</sup>

$$\begin{aligned}
 & \left( \left( A (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 (B + A \operatorname{Cot}[c + dx]) \operatorname{Csc}[c] (\operatorname{Cos}[4c] - \operatorname{Im} \operatorname{Sin}[4c]) \operatorname{Sin}[dx] \operatorname{Sin}[c + dx]^4 \right) / \right. \\
 & \quad \left( d (\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx])^4 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) + \\
 & \quad \left( (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 (B + A \operatorname{Cot}[c + dx]) (4 \operatorname{Im} A \operatorname{Cos}[2c] + B \operatorname{Cos}[2c] + 4 A \operatorname{Sin}[2c] - \operatorname{Im} B \operatorname{Sin}[2c]) \right. \\
 & \quad \left. (-\operatorname{Im} \operatorname{ArcTan}[\operatorname{Tan}[5c + dx]] \operatorname{Cos}[2c] - \operatorname{ArcTan}[\operatorname{Tan}[5c + dx]] \operatorname{Sin}[2c]) \operatorname{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx])^4 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) + \left( (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 \right. \\
 & \quad \left. (B + A \operatorname{Cot}[c + dx]) (4 \operatorname{Im} A \operatorname{Cos}[2c] + 7 B \operatorname{Cos}[2c] + 4 A \operatorname{Sin}[2c] - 7 \operatorname{Im} B \operatorname{Sin}[2c]) \right. \\
 & \quad \left. \left( \frac{1}{2} \operatorname{Cos}[2c] \operatorname{Log}[\operatorname{Cos}[c + dx]^2] - \frac{1}{2} \operatorname{Im} \operatorname{Log}[\operatorname{Cos}[c + dx]^2] \operatorname{Sin}[2c] \right) \operatorname{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx])^4 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) + \\
 & \quad \left( (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 (B + A \operatorname{Cot}[c + dx]) (4 \operatorname{Im} A \operatorname{Cos}[2c] + B \operatorname{Cos}[2c] + 4 A \operatorname{Sin}[2c] - \operatorname{Im} B \operatorname{Sin}[2c]) \right. \\
 & \quad \left. \left( \frac{1}{2} \operatorname{Cos}[2c] \operatorname{Log}[\operatorname{Sin}[c + dx]^2] - \frac{1}{2} \operatorname{Im} \operatorname{Log}[\operatorname{Sin}[c + dx]^2] \operatorname{Sin}[2c] \right) \operatorname{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx])^4 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) + \\
 & \quad \left( (A - \operatorname{Im} B) (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 (B + A \operatorname{Cot}[c + dx]) (-8 dx \operatorname{Cos}[4c] + 8 \operatorname{Im} dx \operatorname{Sin}[4c]) \right. \\
 & \quad \left. \operatorname{Sin}[c + dx]^5 \right) / \left( d (\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx])^4 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) + \\
 & \quad \frac{1}{\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx]} \left( A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx] \right) \\
 & \quad \times (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 (B + A \operatorname{Cot}[c + dx]) \operatorname{Sin}[c + dx]^5 \\
 & \quad \left( 2 A \operatorname{Cos}[c]^2 - \frac{7}{2} \operatorname{Im} B \operatorname{Cos}[c]^2 - 22 A \operatorname{Cos}[c]^4 + \frac{17}{2} \operatorname{Im} B \operatorname{Cos}[c]^4 - 4 \operatorname{Im} A \operatorname{Cos}[c]^4 \operatorname{Cot}[c] - \right. \\
 & \quad B \operatorname{Cos}[c]^4 \operatorname{Cot}[c] - 6 \operatorname{Im} A \operatorname{Cos}[c] \operatorname{Sin}[c] - \frac{21}{2} B \operatorname{Cos}[c] \operatorname{Sin}[c] + 50 \operatorname{Im} A \operatorname{Cos}[c]^3 \operatorname{Sin}[c] + \\
 & \quad \frac{55}{2} B \operatorname{Cos}[c]^3 \operatorname{Sin}[c] - 6 A \operatorname{Sin}[c]^2 + \frac{21}{2} \operatorname{Im} B \operatorname{Sin}[c]^2 + 60 A \operatorname{Cos}[c]^2 \operatorname{Sin}[c]^2 - 45 \operatorname{Im} B \operatorname{Cos}[c]^2 \\
 & \quad \operatorname{Sin}[c]^2 - 40 \operatorname{Im} A \operatorname{Cos}[c] \operatorname{Sin}[c]^3 - 40 B \operatorname{Cos}[c] \operatorname{Sin}[c]^3 - 14 A \operatorname{Sin}[c]^4 + \frac{37}{2} \operatorname{Im} B \operatorname{Sin}[c]^4 + \\
 & \quad \left. (-3 B + 4 \operatorname{Im} A \operatorname{Cos}[2c] + 4 B \operatorname{Cos}[2c]) \operatorname{Csc}[c] \operatorname{Sec}[c] (\operatorname{Cos}[4c] - \operatorname{Im} \operatorname{Sin}[4c]) + \right. \\
 & \quad \left. 2 \operatorname{Im} A \operatorname{Sin}[c]^2 \operatorname{Tan}[c] + \frac{7}{2} B \operatorname{Sin}[c]^2 \operatorname{Tan}[c] + 2 \operatorname{Im} A \operatorname{Sin}[c]^4 \operatorname{Tan}[c] + \frac{7}{2} B \operatorname{Sin}[c]^4 \operatorname{Tan}[c] \right) + \\
 & \quad \left( (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 (B + A \operatorname{Cot}[c + dx]) \operatorname{Sec}[c] (\operatorname{Cos}[4c] - \operatorname{Im} \operatorname{Sin}[4c]) \right. \\
 & \quad \left. (A \operatorname{Sin}[dx] - 4 \operatorname{Im} B \operatorname{Sin}[dx]) \operatorname{Sin}[c + dx]^4 \operatorname{Tan}[c + dx] \right) / \\
 & \quad \left( d (\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx])^4 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) + \\
 & \quad \left( (\operatorname{Im} + \operatorname{Cot}[c + dx])^4 (B + A \operatorname{Cot}[c + dx]) \left( \frac{1}{2} B \operatorname{Cos}[4c] - \frac{1}{2} \operatorname{Im} B \operatorname{Sin}[4c] \right) \operatorname{Sin}[c + dx]^3 \right. \\
 & \quad \left. \operatorname{Tan}[c + dx]^2 \right) / \left( d (\operatorname{Cos}[dx] + \operatorname{Im} \operatorname{Sin}[dx])^4 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) \Big)
 \end{aligned}$$

**Problem 31: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^3 (a + i a \tan [c + d x])^4 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 156 leaves, 7 steps):

$$-8 a^4 (i A + B) x - \frac{a^4 (A - 4 i B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \frac{a^4 (7 A - 4 i B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \frac{a A \cot [c + d x]^2 (a + i a \tan [c + d x])^3}{2 d} - \frac{(5 i A + 2 B) \cot [c + d x] (a^2 + i a^2 \tan [c + d x])^2}{2 d} - \frac{3 A (a^4 + i a^4 \tan [c + d x])}{d}$$

Result (type 3, 1116 leaves):

$$\begin{aligned}
 & a^4 \left( \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \left( -\frac{1}{2} A \text{Cos}[4c] + \frac{1}{2} \mathfrak{i} A \text{Sin}[4c] \right) \text{Sin}[c + dx]^3 \right) / \right. \\
 & \quad \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Csc}[c] (\text{Cos}[4c] - \mathfrak{i} \text{Sin}[4c]) \right. \\
 & \quad \left. (4 \mathfrak{i} A \text{Sin}[dx] + B \text{Sin}[dx]) \text{Sin}[c + dx]^4 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 \right. \\
 & \quad \left. (B + A \text{Cot}[c + dx]) (7 A \text{Cos}[2c] - 4 \mathfrak{i} B \text{Cos}[2c] - 7 \mathfrak{i} A \text{Sin}[2c] - 4 B \text{Sin}[2c]) \right. \\
 & \quad \left. (\mathfrak{i} \text{ArcTan}[\text{Tan}[5c + dx]] \text{Cos}[2c] + \text{ArcTan}[\text{Tan}[5c + dx]] \text{Sin}[2c]) \text{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) (A \text{Cos}[2c] - 4 \mathfrak{i} B \text{Cos}[2c] - \mathfrak{i} A \text{Sin}[2c] - 4 B \text{Sin}[2c]) \right. \\
 & \quad \left. \left( -\frac{1}{2} \text{Cos}[2c] \text{Log}[\text{Cos}[c + dx]^2] + \frac{1}{2} \mathfrak{i} \text{Log}[\text{Cos}[c + dx]^2] \text{Sin}[2c] \right) \text{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 \right. \\
 & \quad \left. (B + A \text{Cot}[c + dx]) (7 A \text{Cos}[2c] - 4 \mathfrak{i} B \text{Cos}[2c] - 7 \mathfrak{i} A \text{Sin}[2c] - 4 B \text{Sin}[2c]) \right. \\
 & \quad \left. \left( -\frac{1}{2} \text{Cos}[2c] \text{Log}[\text{Sin}[c + dx]^2] + \frac{1}{2} \mathfrak{i} \text{Log}[\text{Sin}[c + dx]^2] \text{Sin}[2c] \right) \text{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (A - \mathfrak{i} B) (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) (-8 \mathfrak{i} dx \text{Cos}[4c] - 8 dx \text{Sin}[4c]) \right. \\
 & \quad \left. \text{Sin}[c + dx]^5 \right) / \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \frac{1}{\left( \text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx] \right)^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx])} \\
 & \quad \times (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Sin}[c + dx]^5 \\
 & \quad \left( \frac{1}{2} \mathfrak{i} A \text{Cos}[c]^2 + 2 B \text{Cos}[c]^2 - \frac{71}{2} \mathfrak{i} A \text{Cos}[c]^4 - 22 B \text{Cos}[c]^4 + 7 A \text{Cos}[c]^4 \text{Cot}[c] - \right. \\
 & \quad \left. 4 \mathfrak{i} B \text{Cos}[c]^4 \text{Cot}[c] + \frac{3}{2} A \text{Cos}[c] \text{Sin}[c] - 6 \mathfrak{i} B \text{Cos}[c] \text{Sin}[c] - \frac{145}{2} A \text{Cos}[c]^3 \text{Sin}[c] + \right. \\
 & \quad \left. 50 \mathfrak{i} B \text{Cos}[c]^3 \text{Sin}[c] - \frac{3}{2} \mathfrak{i} A \text{Sin}[c]^2 - 6 B \text{Sin}[c]^2 + 75 \mathfrak{i} A \text{Cos}[c]^2 \text{Sin}[c]^2 + \right. \\
 & \quad \left. 60 B \text{Cos}[c]^2 \text{Sin}[c]^2 + 40 A \text{Cos}[c] \text{Sin}[c]^3 - 40 \mathfrak{i} B \text{Cos}[c] \text{Sin}[c]^3 - \frac{19}{2} \mathfrak{i} A \text{Sin}[c]^4 - \right. \\
 & \quad \left. 14 B \text{Sin}[c]^4 + (3 A + 4 A \text{Cos}[2c] - 4 \mathfrak{i} B \text{Cos}[2c]) \text{Csc}[c] \text{Sec}[c] (-\text{Cos}[4c] + \mathfrak{i} \text{Sin}[4c]) - \right. \\
 & \quad \left. \frac{1}{2} A \text{Sin}[c]^2 \text{Tan}[c] + 2 \mathfrak{i} B \text{Sin}[c]^2 \text{Tan}[c] - \frac{1}{2} A \text{Sin}[c]^4 \text{Tan}[c] + 2 \mathfrak{i} B \text{Sin}[c]^4 \text{Tan}[c] \right) + \\
 & \quad \left( B (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Sec}[c] (\text{Cos}[4c] - \mathfrak{i} \text{Sin}[4c]) \text{Sin}[dx] \right. \\
 & \quad \left. \text{Sin}[c + dx]^4 \text{Tan}[c + dx] \right) / \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) \Big)
 \end{aligned}$$



### Problem 32: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c + d x]^4 (a + i a \text{Tan}[c + d x])^4 (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 163 leaves, 7 steps):

$$8 a^4 (A - i B) x - \frac{a^4 B \text{Log}[\text{Cos}[c + d x]]}{d} - \frac{a^4 (8 i A + 7 B) \text{Log}[\text{Sin}[c + d x]]}{d} - \frac{a A \text{Cot}[c + d x]^3 (a + i a \text{Tan}[c + d x])^3}{3 d} - \frac{(2 i A + B) \text{Cot}[c + d x]^2 (a^2 + i a^2 \text{Tan}[c + d x])^2}{2 d} + \frac{(4 A - 3 i B) \text{Cot}[c + d x] (a^4 + i a^4 \text{Tan}[c + d x])}{d}$$

Result (type 3, 1138 leaves):

$$\begin{aligned}
 & a^4 \left( \left( A (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Csc}[c] \left( \frac{1}{3} \text{Cos}[4c] - \frac{1}{3} \mathfrak{i} \text{Sin}[4c] \right) \text{Sin}[dx] \right. \right. \\
 & \quad \left. \left. \text{Sin}[c + dx]^2 \right) / \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \right. \\
 & \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Csc}[c] (-2A \text{Cos}[c] - 12 \mathfrak{i} A \text{Sin}[c] - 3B \text{Sin}[c]) \right. \\
 & \quad \left. \left( \frac{1}{6} \text{Cos}[4c] - \frac{1}{6} \mathfrak{i} \text{Sin}[4c] \right) \text{Sin}[c + dx]^3 \right) / \\
 & \left. \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \right. \\
 & \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Csc}[c] \left( -\frac{2}{3} \text{Cos}[4c] + \frac{2}{3} \mathfrak{i} \text{Sin}[4c] \right) \right. \\
 & \quad \left. (11A \text{Sin}[dx] - 6 \mathfrak{i} B \text{Sin}[dx]) \text{Sin}[c + dx]^4 \right) / \\
 & \left. \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) - \right. \\
 & \left( B \text{Cos}[4c] (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Log}[\text{Cos}[c + dx]^2 \text{Sin}[c + dx]^5] / \right. \\
 & \quad \left( 2d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 \right. \\
 & \quad \left. (B + A \text{Cot}[c + dx]) (8A \text{Cos}[2c] - 7 \mathfrak{i} B \text{Cos}[2c] - 8 \mathfrak{i} A \text{Sin}[2c] - 7B \text{Sin}[2c]) \right. \\
 & \quad \left. (-\text{ArcTan}[\text{Tan}[5c + dx]] \text{Cos}[2c] + \mathfrak{i} \text{ArcTan}[\text{Tan}[5c + dx]] \text{Sin}[2c]) \text{Sin}[c + dx]^5 \right) / \\
 & \left. \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \left( (\mathfrak{i} + \text{Cot}[c + dx])^4 \right. \right. \\
 & \quad \left. \left. (B + A \text{Cot}[c + dx]) (8A \text{Cos}[2c] - 7 \mathfrak{i} B \text{Cos}[2c] - 8 \mathfrak{i} A \text{Sin}[2c] - 7B \text{Sin}[2c]) \right. \right. \\
 & \quad \left. \left. \left( -\frac{1}{2} \mathfrak{i} \text{Cos}[2c] \text{Log}[\text{Sin}[c + dx]^2] - \frac{1}{2} \text{Log}[\text{Sin}[c + dx]^2] \text{Sin}[2c] \right) \text{Sin}[c + dx]^5 \right) / \right. \\
 & \left. \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \right. \\
 & \left. (\mathfrak{i} B (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Log}[\text{Cos}[c + dx]^2 \text{Sin}[4c] \text{Sin}[c + dx]^5] / \right. \\
 & \quad \left. \left( 2d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \right. \\
 & \left. \left( (A - \mathfrak{i} B) (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) (8dx \text{Cos}[4c] - 8 \mathfrak{i} dx \text{Sin}[4c]) \right. \right. \\
 & \quad \left. \left. \text{Sin}[c + dx]^5 \right) / \left( d (\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \right. \\
 & \quad \left. \frac{1}{(\text{Cos}[dx] + \mathfrak{i} \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx])} \right. \\
 & \quad \times (\mathfrak{i} + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Sin}[c + dx]^5 \\
 & \quad \left. \left( \frac{1}{2} \mathfrak{i} B \text{Cos}[c]^2 + 40A \text{Cos}[c]^4 - \frac{71}{2} \mathfrak{i} B \text{Cos}[c]^4 + 8 \mathfrak{i} A \text{Cos}[c]^4 \text{Cot}[c] + 7B \text{Cos}[c]^4 \text{Cot}[c] + \right. \right. \\
 & \quad \frac{3}{2} B \text{Cos}[c] \text{Sin}[c] - 80 \mathfrak{i} A \text{Cos}[c]^3 \text{Sin}[c] - \frac{145}{2} B \text{Cos}[c]^3 \text{Sin}[c] - \frac{3}{2} \mathfrak{i} B \text{Sin}[c]^2 - \\
 & \quad 80A \text{Cos}[c]^2 \text{Sin}[c]^2 + 75 \mathfrak{i} B \text{Cos}[c]^2 \text{Sin}[c]^2 + 40 \mathfrak{i} A \text{Cos}[c] \text{Sin}[c]^3 + 40B \text{Cos}[c] \text{Sin}[c]^3 + \\
 & \quad \left. \left. 8A \text{Sin}[c]^4 - \frac{19}{2} \mathfrak{i} B \text{Sin}[c]^4 - \mathfrak{i} (4A - 3 \mathfrak{i} B + 4A \text{Cos}[2c] - 4 \mathfrak{i} B \text{Cos}[2c]) \text{Csc}[c] \right. \right. \\
 & \quad \left. \left. \text{Sec}[c] (\text{Cos}[4c] - \mathfrak{i} \text{Sin}[4c]) - \frac{1}{2} B \text{Sin}[c]^2 \text{Tan}[c] - \frac{1}{2} B \text{Sin}[c]^4 \text{Tan}[c] \right) \right) \Bigg)
 \end{aligned}$$

**Problem 33: Result more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x]^5 (a + i a \text{Tan}[c + d x])^4 (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 177 leaves, 6 steps):

$$8 a^4 (i A + B) x + \frac{a^4 (67 i A + 64 B) \text{Cot}[c + d x]}{12 d} + \frac{8 a^4 (A - i B) \text{Log}[\text{Sin}[c + d x]]}{d} - \frac{a A \text{Cot}[c + d x]^4 (a + i a \text{Tan}[c + d x])^3}{4 d} - \frac{(7 i A + 4 B) \text{Cot}[c + d x]^3 (a^2 + i a^2 \text{Tan}[c + d x])^2}{12 d} + \frac{(19 A - 16 i B) \text{Cot}[c + d x]^2 (a^4 + i a^4 \text{Tan}[c + d x])}{12 d}$$

Result (type 3, 985 leaves):

$$\begin{aligned}
 & a^4 \left( \left( (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \left( -\frac{1}{4} A \text{Cos}[4c] + \frac{1}{4} \i A \text{Sin}[4c] \right) \text{Sin}[c + dx] \right) / \right. \\
 & \quad \left( d (\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Csc}[c] \left( \frac{1}{3} \text{Cos}[4c] - \frac{1}{3} \i \text{Sin}[4c] \right) \right. \\
 & \quad \left. (4 \i A \text{Sin}[dx] + B \text{Sin}[dx]) \text{Sin}[c + dx]^2 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Csc}[c] (-4 \i A \text{Cos}[c] - B \text{Cos}[c] + \right. \\
 & \quad \left. 12 A \text{Sin}[c] - 6 \i B \text{Sin}[c]) \left( \frac{1}{3} \text{Cos}[4c] - \frac{1}{3} \i \text{Sin}[4c] \right) \text{Sin}[c + dx]^3 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) \text{Csc}[c] \left( \frac{2}{3} \text{Cos}[4c] - \frac{2}{3} \i \text{Sin}[4c] \right) \right. \\
 & \quad \left. (-14 \i A \text{Sin}[dx] - 11 B \text{Sin}[dx]) \text{Sin}[c + dx]^4 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) (A \text{Cos}[2c] - \i B \text{Cos}[2c] - \i A \text{Sin}[2c] - B \text{Sin}[2c]) \right. \\
 & \quad \left. (-8 \i \text{ArcTan}[\text{Tan}[5c + dx]] \text{Cos}[2c] - 8 \text{ArcTan}[\text{Tan}[5c + dx]] \text{Sin}[2c]) \text{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \left( (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) (A \text{Cos}[2c] - \i B \text{Cos}[2c] - \i A \text{Sin}[2c] - B \text{Sin}[2c]) \right. \\
 & \quad \left. (4 \text{Cos}[2c] \text{Log}[\text{Sin}[c + dx]^2] - 4 \i \text{Log}[\text{Sin}[c + dx]^2] \text{Sin}[2c]) \text{Sin}[c + dx]^5 \right) / \\
 & \quad \left( d (\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) + \\
 & \quad \frac{1}{(\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx])} \\
 & \quad \times (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) (40 \i A \text{Cos}[c]^4 + 40 B \text{Cos}[c]^4 - 8 A \text{Cos}[c]^4 \text{Cot}[c] + \\
 & \quad 8 \i B \text{Cos}[c]^4 \text{Cot}[c] + 80 A \text{Cos}[c]^3 \text{Sin}[c] - 80 \i B \text{Cos}[c]^3 \text{Sin}[c] - 80 \i A \text{Cos}[c]^2 \text{Sin}[c]^2 - \\
 & \quad 80 B \text{Cos}[c]^2 \text{Sin}[c]^2 - 40 A \text{Cos}[c] \text{Sin}[c]^3 + 40 \i B \text{Cos}[c] \text{Sin}[c]^3 + 8 \i A \text{Sin}[c]^4 + \\
 & \quad 8 B \text{Sin}[c]^4 + (A - \i B) \text{Cot}[c] (8 \text{Cos}[4c] - 8 \i \text{Sin}[4c])) \text{Sin}[c + dx]^5 + \\
 & \quad \left. \left( (\i A + B) (\i + \text{Cot}[c + dx])^4 (B + A \text{Cot}[c + dx]) (8 dx \text{Cos}[4c] - 8 \i dx \text{Sin}[4c]) \right. \right. \\
 & \quad \left. \left. \text{Sin}[c + dx]^5 \right) / \left( d (\text{Cos}[dx] + \i \text{Sin}[dx])^4 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) \right)
 \end{aligned}$$

**Problem 34: Result more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + dx]^6 (a + \i a \text{Tan}[c + dx])^4 (A + B \text{Tan}[c + dx]) dx$$

Optimal (type 3, 200 leaves, 7 steps):

$$\begin{aligned}
 & -8 a^4 (A - i B) x - \frac{8 a^4 (A - i B) \operatorname{Cot}[c + d x]}{d} + \\
 & \frac{a^4 (148 i A + 145 B) \operatorname{Cot}[c + d x]^2}{60 d} + \frac{8 a^4 (i A + B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \\
 & \frac{a A \operatorname{Cot}[c + d x]^5 (a + i a \operatorname{Tan}[c + d x])^3}{5 d} - \frac{(8 i A + 5 B) \operatorname{Cot}[c + d x]^4 (a^2 + i a^2 \operatorname{Tan}[c + d x])^2}{20 d} + \\
 & \frac{(28 A - 25 i B) \operatorname{Cot}[c + d x]^3 (a^4 + i a^4 \operatorname{Tan}[c + d x])}{30 d}
 \end{aligned}$$

Result (type 3, 937 leaves):

$$\begin{aligned}
 & a^4 \left( \left( (i + \operatorname{Cot}[c + d x])^4 (B + A \operatorname{Cot}[c + d x]) (i A \operatorname{Cos}[2 c] + B \operatorname{Cos}[2 c] + A \operatorname{Sin}[2 c] - i B \operatorname{Sin}[2 c]) \right. \right. \\
 & \quad \left. \left. (-8 i \operatorname{ArcTan}[\operatorname{Tan}[5 c + d x]] \operatorname{Cos}[2 c] - 8 \operatorname{ArcTan}[\operatorname{Tan}[5 c + d x]] \operatorname{Sin}[2 c]) \operatorname{Sin}[c + d x]^5 \right) / \right. \\
 & \quad \left. \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) + \\
 & \quad \left( (i + \operatorname{Cot}[c + d x])^4 (B + A \operatorname{Cot}[c + d x]) (i A \operatorname{Cos}[2 c] + B \operatorname{Cos}[2 c] + A \operatorname{Sin}[2 c] - i B \operatorname{Sin}[2 c]) \right. \\
 & \quad \left. (4 \operatorname{Cos}[2 c] \operatorname{Log}[\operatorname{Sin}[c + d x]^2] - 4 i \operatorname{Log}[\operatorname{Sin}[c + d x]^2] \operatorname{Sin}[2 c]) \operatorname{Sin}[c + d x]^5 \right) / \\
 & \quad \left. \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) + \\
 & \quad \frac{1}{\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]} \left( A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x] \right) \\
 & \quad \times (i + \operatorname{Cot}[c + d x])^4 (B + A \operatorname{Cot}[c + d x]) \left( -40 A \operatorname{Cos}[c]^4 + 40 i B \operatorname{Cos}[c]^4 - 8 i A \operatorname{Cos}[c]^4 \operatorname{Cot}[c] - \right. \\
 & \quad \left. 8 B \operatorname{Cos}[c]^4 \operatorname{Cot}[c] + 80 i A \operatorname{Cos}[c]^3 \operatorname{Sin}[c] + 80 B \operatorname{Cos}[c]^3 \operatorname{Sin}[c] + 80 A \operatorname{Cos}[c]^2 \operatorname{Sin}[c]^2 - \right. \\
 & \quad \left. 80 i B \operatorname{Cos}[c]^2 \operatorname{Sin}[c]^2 - 40 i A \operatorname{Cos}[c] \operatorname{Sin}[c]^3 - 40 B \operatorname{Cos}[c] \operatorname{Sin}[c]^3 - 8 A \operatorname{Sin}[c]^4 + \right. \\
 & \quad \left. 8 i B \operatorname{Sin}[c]^4 + (i A + B) \operatorname{Cot}[c] (8 \operatorname{Cos}[4 c] - 8 i \operatorname{Sin}[4 c]) \right) \operatorname{Sin}[c + d x]^5 + \\
 & \quad \frac{1}{d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} \\
 & \quad \left. (i + \operatorname{Cot}[c + d x])^4 (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c] \left( \frac{1}{120} \operatorname{Cos}[4 c] - \frac{1}{120} i \operatorname{Sin}[4 c] \right) \right. \\
 & \quad \left. (210 i A \operatorname{Cos}[d x] + 165 B \operatorname{Cos}[d x] - 300 A d x \operatorname{Cos}[d x] + 300 i B d x \operatorname{Cos}[d x] - \right. \\
 & \quad \left. 210 i A \operatorname{Cos}[2 c + d x] - 165 B \operatorname{Cos}[2 c + d x] + 300 A d x \operatorname{Cos}[2 c + d x] - \right. \\
 & \quad \left. 300 i B d x \operatorname{Cos}[2 c + d x] - 90 i A \operatorname{Cos}[2 c + 3 d x] - 60 B \operatorname{Cos}[2 c + 3 d x] + \right. \\
 & \quad \left. 150 A d x \operatorname{Cos}[2 c + 3 d x] - 150 i B d x \operatorname{Cos}[2 c + 3 d x] + 90 i A \operatorname{Cos}[4 c + 3 d x] + \right. \\
 & \quad \left. 60 B \operatorname{Cos}[4 c + 3 d x] - 150 A d x \operatorname{Cos}[4 c + 3 d x] + 150 i B d x \operatorname{Cos}[4 c + 3 d x] - \right. \\
 & \quad \left. 30 A d x \operatorname{Cos}[4 c + 5 d x] + 30 i B d x \operatorname{Cos}[4 c + 5 d x] + 30 A d x \operatorname{Cos}[6 c + 5 d x] - \right. \\
 & \quad \left. 30 i B d x \operatorname{Cos}[6 c + 5 d x] + 445 A \operatorname{Sin}[d x] - 400 i B \operatorname{Sin}[d x] + 345 A \operatorname{Sin}[2 c + d x] - \right. \\
 & \quad \left. 300 i B \operatorname{Sin}[2 c + d x] - 275 A \operatorname{Sin}[2 c + 3 d x] + 260 i B \operatorname{Sin}[2 c + 3 d x] - \right. \\
 & \quad \left. 120 A \operatorname{Sin}[4 c + 3 d x] + 90 i B \operatorname{Sin}[4 c + 3 d x] + 79 A \operatorname{Sin}[4 c + 5 d x] - 70 i B \operatorname{Sin}[4 c + 5 d x] \right) \left. \right)
 \end{aligned}$$

**Problem 35: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + d x]^7 (a + i a \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 223 leaves, 8 steps):

$$\begin{aligned}
 & -8 a^4 (\text{i} A + B) x - \frac{8 a^4 (\text{i} A + B) \text{Cot}[c + d x]}{d} - \frac{4 a^4 (A - \text{i} B) \text{Cot}[c + d x]^2}{d} + \\
 & \frac{a^4 (93 \text{i} A + 92 B) \text{Cot}[c + d x]^3}{60 d} - \frac{8 a^4 (A - \text{i} B) \text{Log}[\text{Sin}[c + d x]]}{d} - \\
 & \frac{a A \text{Cot}[c + d x]^6 (a + \text{i} a \text{Tan}[c + d x])^3}{6 d} - \frac{(3 \text{i} A + 2 B) \text{Cot}[c + d x]^5 (a^2 + \text{i} a^2 \text{Tan}[c + d x])^2}{10 d} + \\
 & \frac{(13 A - 12 \text{i} B) \text{Cot}[c + d x]^4 (a^4 + \text{i} a^4 \text{Tan}[c + d x])}{20 d}
 \end{aligned}$$

Result (type 3, 1009 leaves):

$$\begin{aligned}
 & a^4 \left( \left( (\text{i} + \text{Cot}[c + d x])^4 (B + A \text{Cot}[c + d x]) (A \text{Cos}[2 c] - \text{i} B \text{Cos}[2 c] - \text{i} A \text{Sin}[2 c] - B \text{Sin}[2 c]) \right. \right. \\
 & \quad \left. \left. (8 \text{i} \text{ArcTan}[\text{Tan}[5 c + d x]] \text{Cos}[2 c] + 8 \text{ArcTan}[\text{Tan}[5 c + d x]] \text{Sin}[2 c]) \text{Sin}[c + d x]^5 \right) / \right. \\
 & \quad \left. \left( d (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) \right) + \\
 & \left( (\text{i} + \text{Cot}[c + d x])^4 (B + A \text{Cot}[c + d x]) (A \text{Cos}[2 c] - \text{i} B \text{Cos}[2 c] - \text{i} A \text{Sin}[2 c] - B \text{Sin}[2 c]) \right. \\
 & \quad \left. (-4 \text{Cos}[2 c] \text{Log}[\text{Sin}[c + d x]^2] + 4 \text{i} \text{Log}[\text{Sin}[c + d x]^2] \text{Sin}[2 c]) \text{Sin}[c + d x]^5 \right) / \\
 & \quad \left( d (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\
 & \quad \frac{1}{(\text{Cos}[d x] + \text{i} \text{Sin}[d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x])} \\
 & \quad x (\text{i} + \text{Cot}[c + d x])^4 (B + A \text{Cot}[c + d x]) \left( -40 \text{i} A \text{Cos}[c]^4 - 40 B \text{Cos}[c]^4 + 8 A \text{Cos}[c]^4 \text{Cot}[c] - \right. \\
 & \quad \left. 8 \text{i} B \text{Cos}[c]^4 \text{Cot}[c] - 80 A \text{Cos}[c]^3 \text{Sin}[c] + 80 \text{i} B \text{Cos}[c]^3 \text{Sin}[c] + 80 \text{i} A \text{Cos}[c]^2 \text{Sin}[c]^2 + \right. \\
 & \quad \left. 80 B \text{Cos}[c]^2 \text{Sin}[c]^2 + 40 A \text{Cos}[c] \text{Sin}[c]^3 - 40 \text{i} B \text{Cos}[c] \text{Sin}[c]^3 - 8 \text{i} A \text{Sin}[c]^4 - \right. \\
 & \quad \left. 8 B \text{Sin}[c]^4 + (A - \text{i} B) \text{Cot}[c] (-8 \text{Cos}[4 c] + 8 \text{i} \text{Sin}[4 c]) \right) \text{Sin}[c + d x]^5 + \\
 & \quad \frac{1}{d (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x])} \\
 & \quad (\text{i} + \text{Cot}[c + d x])^4 (B + A \text{Cot}[c + d x]) \text{Csc}[c] \text{Csc}[c + d x] \left( \frac{1}{240} \text{Cos}[4 c] - \frac{1}{240} \text{i} \text{Sin}[4 c] \right) \\
 & \quad \left( 860 \text{i} A \text{Cos}[c] + 790 B \text{Cos}[c] - 780 \text{i} A \text{Cos}[c + 2 d x] - 720 B \text{Cos}[c + 2 d x] - \right. \\
 & \quad 510 \text{i} A \text{Cos}[3 c + 2 d x] - 465 B \text{Cos}[3 c + 2 d x] + 366 \text{i} A \text{Cos}[3 c + 4 d x] + \\
 & \quad 354 B \text{Cos}[3 c + 4 d x] + 150 \text{i} A \text{Cos}[5 c + 4 d x] + 120 B \text{Cos}[5 c + 4 d x] - \\
 & \quad 86 \text{i} A \text{Cos}[5 c + 6 d x] - 79 B \text{Cos}[5 c + 6 d x] - 490 A \text{Sin}[c] + 420 \text{i} B \text{Sin}[c] - \\
 & \quad 600 \text{i} A d x \text{Sin}[c] - 600 B d x \text{Sin}[c] - 345 A \text{Sin}[c + 2 d x] + 300 \text{i} B \text{Sin}[c + 2 d x] - \\
 & \quad 450 \text{i} A d x \text{Sin}[c + 2 d x] - 450 B d x \text{Sin}[c + 2 d x] + 345 A \text{Sin}[3 c + 2 d x] - \\
 & \quad 300 \text{i} B \text{Sin}[3 c + 2 d x] + 450 \text{i} A d x \text{Sin}[3 c + 2 d x] + 450 B d x \text{Sin}[3 c + 2 d x] + \\
 & \quad 120 A \text{Sin}[3 c + 4 d x] - 90 \text{i} B \text{Sin}[3 c + 4 d x] + 180 \text{i} A d x \text{Sin}[3 c + 4 d x] + \\
 & \quad 180 B d x \text{Sin}[3 c + 4 d x] - 120 A \text{Sin}[5 c + 4 d x] + 90 \text{i} B \text{Sin}[5 c + 4 d x] - \\
 & \quad \left. 180 \text{i} A d x \text{Sin}[5 c + 4 d x] - 180 B d x \text{Sin}[5 c + 4 d x] - 30 \text{i} A d x \text{Sin}[5 c + 6 d x] - \right. \\
 & \quad \left. 30 B d x \text{Sin}[5 c + 6 d x] + 30 \text{i} A d x \text{Sin}[7 c + 6 d x] + 30 B d x \text{Sin}[7 c + 6 d x] \right)
 \end{aligned}$$

### Problem 36: Result more than twice size of optimal antiderivative.

$$\int \frac{\tan [c+d x]^3 (A+B \tan [c+d x])}{a+i a \tan [c+d x]} dx$$

Optimal (type 3, 129 leaves, 4 steps):

$$\frac{3 (i A - B) x}{2 a} - \frac{(A + 2 i B) \operatorname{Log}[\operatorname{Cos}[c+d x]]}{a d} - \frac{3 (i A - B) \tan [c+d x]}{2 a d} - \frac{(A + 2 i B) \tan [c+d x]^2}{2 a d} + \frac{(i A - B) \tan [c+d x]^3}{2 d (a + i a \tan [c+d x])}$$

Result (type 3, 898 leaves):

$$\begin{aligned} & \left( \left( A \operatorname{Cos}\left[\frac{c}{2}\right] + 2 i B \operatorname{Cos}\left[\frac{c}{2}\right] + i A \operatorname{Sin}\left[\frac{c}{2}\right] - 2 B \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\ & \quad \left. \left( i \operatorname{ArcTan}[\tan [d x]] \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{ArcTan}[\tan [d x]] \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \right. \\ & \quad \left. (A + B \tan [c+d x]) \right) / \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) + \\ & \left( \left( A \operatorname{Cos}\left[\frac{c}{2}\right] + 2 i B \operatorname{Cos}\left[\frac{c}{2}\right] + i A \operatorname{Sin}\left[\frac{c}{2}\right] - 2 B \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\ & \quad \left( -\frac{1}{2} \operatorname{Cos}\left[\frac{c}{2}\right] \operatorname{Log}[\operatorname{Cos}[c+d x]^2] - \frac{1}{2} i \operatorname{Log}[\operatorname{Cos}[c+d x]^2] \operatorname{Sin}\left[\frac{c}{2}\right] \right) \\ & \quad \left. (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A + B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) + \\ & \left( (A + i B) \operatorname{Cos}[2 d x] \left( \frac{\operatorname{Cos}[c]}{4} - \frac{1}{4} i \operatorname{Sin}[c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A + B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) + \\ & \left( \operatorname{Sec}[c+d x]^2 \left( -\frac{1}{2} i B \operatorname{Cos}[c] + \frac{1}{2} B \operatorname{Sin}[c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A + B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) + \\ & \left( (A + i B) \left( \frac{3}{2} i d x \operatorname{Cos}[c] - \frac{3}{2} d x \operatorname{Sin}[c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A + B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) + \\ & \left( (-i A + B) \left( \frac{\operatorname{Cos}[c]}{4} - \frac{1}{4} i \operatorname{Sin}[c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \operatorname{Sin}[2 d x] (A + B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) + \\ & \left( \operatorname{Sec}[c+d x] (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A \operatorname{Cos}[c-d x] + i B \operatorname{Cos}[c-d x] - A \operatorname{Cos}[c+d x] - \right. \\ & \quad \left. i B \operatorname{Cos}[c+d x] + i A \operatorname{Sin}[c-d x] - B \operatorname{Sin}[c-d x] - i A \operatorname{Sin}[c+d x] + B \operatorname{Sin}[c+d x]) \right. \\ & \quad \left. (A + B \tan [c+d x]) \right) / \left( 2 d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\ & \quad \left. (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) + \\ & \left( x (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (-i A \operatorname{Sec}[c] + 2 B \operatorname{Sec}[c] + (A + 2 i B) (\operatorname{Cos}[c] + i \operatorname{Sin}[c]) \operatorname{Tan}[c]) \right. \\ & \quad \left. (A + B \tan [c+d x]) \right) / \left( (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \tan [c+d x]) \right) \end{aligned}$$

### Problem 37: Result more than twice size of optimal antiderivative.

$$\int \frac{\tan [c+d x]^2 (A+B \tan [c+d x])}{a+i a \tan [c+d x]} dx$$

Optimal (type 3, 101 leaves, 3 steps):

$$\frac{(A+3 i B) x}{2 a} + \frac{(i A-B) \operatorname{Log}[\operatorname{Cos}[c+d x]]}{a d} - \frac{(A+3 i B) \tan [c+d x]}{2 a d} + \frac{(i A-B) \tan [c+d x]^2}{2 d (a+i a \tan [c+d x])}$$

Result (type 3, 773 leaves):

$$\begin{aligned} & \left( \left( A \operatorname{Cos}\left[\frac{c}{2}\right] + i B \operatorname{Cos}\left[\frac{c}{2}\right] + i A \operatorname{Sin}\left[\frac{c}{2}\right] - B \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\ & \quad \left( \operatorname{ArcTan}[\tan [d x]] \operatorname{Cos}\left[\frac{c}{2}\right] + i \operatorname{ArcTan}[\tan [d x]] \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \\ & \quad \left. (A+B \tan [c+d x]) \right) / \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \tan [c+d x]) \right) + \\ & \left( \left( A \operatorname{Cos}\left[\frac{c}{2}\right] + i B \operatorname{Cos}\left[\frac{c}{2}\right] + i A \operatorname{Sin}\left[\frac{c}{2}\right] - B \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\ & \quad \left( \frac{1}{2} i \operatorname{Cos}\left[\frac{c}{2}\right] \operatorname{Log}[\operatorname{Cos}[c+d x]^2] - \frac{1}{2} \operatorname{Log}[\operatorname{Cos}[c+d x]^2] \operatorname{Sin}\left[\frac{c}{2}\right] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \\ & \quad \left. (A+B \tan [c+d x]) \right) / \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \tan [c+d x]) \right) + \\ & \left( (-i A+B) \operatorname{Cos}[2 d x] \left( \frac{\operatorname{Cos}[c]}{4} - \frac{1}{4} i \operatorname{Sin}[c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A+B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \tan [c+d x]) \right) + \\ & \left( (A+3 i B) \left( \frac{1}{2} d x \operatorname{Cos}[c] + \frac{1}{2} i d x \operatorname{Sin}[c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A+B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \tan [c+d x]) \right) + \\ & \left( (A+i B) \left( -\frac{\operatorname{Cos}[c]}{4} + \frac{1}{4} i \operatorname{Sin}[c] \right) (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \operatorname{Sin}[2 d x] (A+B \tan [c+d x]) \right) / \\ & \quad \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \tan [c+d x]) \right) + (\operatorname{Sec}[c+d x] (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) \\ & \quad (B \operatorname{Cos}[c-d x] - B \operatorname{Cos}[c+d x] + i B \operatorname{Sin}[c-d x] - i B \operatorname{Sin}[c+d x]) (A+B \tan [c+d x])) / \\ & \left( 2 d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) \right. \\ & \quad \left. (a+i a \tan [c+d x]) \right) + \\ & \left( x (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (-A \operatorname{Sec}[c] - i B \operatorname{Sec}[c] - i (A+i B) (\operatorname{Cos}[c] + i \operatorname{Sin}[c]) \tan [c]) \right. \\ & \quad \left. (A+B \tan [c+d x]) \right) / \left( (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \tan [c+d x]) \right) \end{aligned}$$

### Problem 38: Result more than twice size of optimal antiderivative.

$$\int \frac{\tan [c+d x] (A+B \tan [c+d x])}{a+i a \tan [c+d x]} dx$$

Optimal (type 3, 67 leaves, 5 steps):



$$-\frac{(i A - B) x}{2 a} + \frac{i B \operatorname{Log}[\operatorname{Cos}[c + d x]]}{a d} - \frac{A + i B}{2 a d (1 + i \operatorname{Tan}[c + d x])}$$

Result (type 3, 148 leaves):

$$\begin{aligned} & (\operatorname{Cos}[c + d x] (A + B \operatorname{Tan}[c + d x]) (i A - B - 2 A d x + 2 i B d x + 2 B \operatorname{Log}[\operatorname{Cos}[c + d x]^2] + \\ & (A + i B - 2 i A d x - 2 B d x + 2 i B \operatorname{Log}[\operatorname{Cos}[c + d x]^2]) \operatorname{Tan}[c + d x] + \\ & 4 B \operatorname{ArcTan}[\operatorname{Tan}[d x]] (-i + \operatorname{Tan}[c + d x])) / \\ & (4 a d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (-i + \operatorname{Tan}[c + d x])) \end{aligned}$$

**Problem 39: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan}[c + d x]}{a + i a \operatorname{Tan}[c + d x]} dx$$

Optimal (type 3, 47 leaves, 2 steps):

$$\frac{(A - i B) x}{2 a} + \frac{i A - B}{2 d (a + i a \operatorname{Tan}[c + d x])}$$

Result (type 3, 102 leaves):

$$\begin{aligned} & (\operatorname{Cos}[c + d x] (A + B \operatorname{Tan}[c + d x]) \\ & (A - 2 i A d x + B (i - 2 d x) + (B - 2 i B d x + A (-i + 2 d x)) \operatorname{Tan}[c + d x])) / \\ & (4 a d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (-i + \operatorname{Tan}[c + d x])) \end{aligned}$$

**Problem 40: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x] (A + B \operatorname{Tan}[c + d x])}{a + i a \operatorname{Tan}[c + d x]} dx$$

Optimal (type 3, 62 leaves, 3 steps):

$$-\frac{(i A - B) x}{2 a} + \frac{A \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a d} + \frac{A + i B}{2 d (a + i a \operatorname{Tan}[c + d x])}$$

Result (type 3, 150 leaves):

$$\begin{aligned} & (\operatorname{Cos}[c + d x] (A + B \operatorname{Tan}[c + d x]) (-i A + B + 2 A d x - 2 i B d x - 2 i A \operatorname{Log}[\operatorname{Sin}[c + d x]^2] + \\ & (-A - i B + 2 i A d x + 2 B d x + 2 A \operatorname{Log}[\operatorname{Sin}[c + d x]^2]) \operatorname{Tan}[c + d x] - \\ & 4 i A \operatorname{ArcTan}[\operatorname{Tan}[d x]] (-i + \operatorname{Tan}[c + d x])) / \\ & (4 a d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (-i + \operatorname{Tan}[c + d x])) \end{aligned}$$

**Problem 41: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{a + i a \operatorname{Tan}[c + d x]} dx$$

Optimal (type 3, 102 leaves, 4 steps):

$$-\frac{(3A + iB)x}{2a} - \frac{(3A + iB) \operatorname{Cot}[c + dx]}{2ad} - \frac{(iA - B) \operatorname{Log}[\operatorname{Sin}[c + dx]]}{ad} + \frac{(A + iB) \operatorname{Cot}[c + dx]}{2d(a + ia \operatorname{Tan}[c + dx])}$$

Result (type 3, 225 leaves):

$$\frac{1}{2d(A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])$$

$$\left( \frac{1}{2} (-iA + B) \operatorname{Cos}[2dx] (\operatorname{Cos}[c] - i \operatorname{Sin}[c]) + 2(A + iB) dx (\operatorname{Cos}[c] + i \operatorname{Sin}[c]) - \right.$$

$$\left. (3A + iB) dx (\operatorname{Cos}[c] + i \operatorname{Sin}[c]) - 2(A + iB) \operatorname{ArcTan}[\operatorname{Tan}[dx]] (\operatorname{Cos}[c] + i \operatorname{Sin}[c]) + \right.$$

$$\left. (-iA + B) \operatorname{Log}[\operatorname{Sin}[c + dx]^2] (\operatorname{Cos}[c] + i \operatorname{Sin}[c]) + 2A (i + \operatorname{Cot}[c]) \operatorname{Csc}[c + dx] \operatorname{Sin}[dx] - \right.$$

$$\left. \frac{1}{2} (A + iB) (\operatorname{Cos}[c] - i \operatorname{Sin}[c]) \operatorname{Sin}[2dx] \right) (A + B \operatorname{Tan}[c + dx])$$

### Problem 42: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + dx]^3 (A + B \operatorname{Tan}[c + dx])}{a + ia \operatorname{Tan}[c + dx]} dx$$

Optimal (type 3, 131 leaves, 5 steps):

$$\frac{3(iA - B)x}{2a} + \frac{3(iA - B) \operatorname{Cot}[c + dx]}{2ad} - \frac{(2A + iB) \operatorname{Cot}[c + dx]^2}{2ad} -$$

$$\frac{(2A + iB) \operatorname{Log}[\operatorname{Sin}[c + dx]]}{ad} + \frac{(A + iB) \operatorname{Cot}[c + dx]^2}{2d(a + ia \operatorname{Tan}[c + dx])}$$

Result (type 3, 902 leaves):

$$\begin{aligned}
 & \left( \left( 2 A \cos\left[\frac{c}{2}\right] + i B \cos\left[\frac{c}{2}\right] + 2 i A \sin\left[\frac{c}{2}\right] - B \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left( i \operatorname{ArcTan}[\tan[dx]] \cos\left[\frac{c}{2}\right] - \operatorname{ArcTan}[\tan[dx]] \sin\left[\frac{c}{2}\right] \right) (\cos[dx] + i \sin[dx]) \\
 & \quad \left. (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( \left( 2 A \cos\left[\frac{c}{2}\right] + i B \cos\left[\frac{c}{2}\right] + 2 i A \sin\left[\frac{c}{2}\right] - B \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left( -\frac{1}{2} \cos\left[\frac{c}{2}\right] \log[\sin[c + dx]^2] - \frac{1}{2} i \log[\sin[c + dx]^2] \sin\left[\frac{c}{2}\right] \right) \\
 & \quad \left. (\cos[dx] + i \sin[dx]) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( x (2 A \csc[c] + i B \csc[c] + (2 A + i B) \cot[c] (-\cos[c] - i \sin[c])) (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left. (A + B \tan[c + dx]) \right) / \left( (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( (A + i B) \cos[2 dx] \left( -\frac{\cos[c]}{4} + \frac{1}{4} i \sin[c] \right) (\cos[dx] + i \sin[dx]) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( \csc[c + dx]^2 \left( -\frac{1}{2} A \cos[c] - \frac{1}{2} i A \sin[c] \right) (\cos[dx] + i \sin[dx]) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( (A + i B) \left( \frac{3}{2} i dx \cos[c] - \frac{3}{2} dx \sin[c] \right) (\cos[dx] + i \sin[dx]) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( (A + i B) \left( \frac{1}{4} i \cos[c] + \frac{\sin[c]}{4} \right) (\cos[dx] + i \sin[dx]) \sin[2 dx] (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( \csc\left[\frac{c}{2}\right] \csc[c + dx] \sec\left[\frac{c}{2}\right] (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left( \frac{1}{2} A \cos[c - dx] + \frac{1}{2} i B \cos[c - dx] - \frac{1}{2} A \cos[c + dx] - \frac{1}{2} i B \cos[c + dx] + \frac{1}{2} i A \sin[c - dx] - \right. \\
 & \quad \left. \frac{1}{2} B \sin[c - dx] - \frac{1}{2} i A \sin[c + dx] + \frac{1}{2} B \sin[c + dx] \right) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( 2 d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right)
 \end{aligned}$$

**Problem 43: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cot[c + dx]^4 (A + B \tan[c + dx])}{a + i a \tan[c + dx]} dx$$

Optimal (type 3, 155 leaves, 6 steps):

$$\begin{aligned}
 & \frac{(5 A + 3 i B) x}{2 a} + \frac{(5 A + 3 i B) \cot[c + dx]}{2 a d} + \frac{(i A - B) \cot[c + dx]^2}{a d} - \\
 & \frac{(5 A + 3 i B) \cot[c + dx]^3}{6 a d} + \frac{2 (i A - B) \log[\sin[c + dx]]}{a d} + \frac{(A + i B) \cot[c + dx]^3}{2 d (a + i a \tan[c + dx])}
 \end{aligned}$$

Result (type 3, 1062 leaves):

$$\begin{aligned}
 & \left( \left( A \cos\left[\frac{c}{2}\right] + i B \cos\left[\frac{c}{2}\right] + i A \sin\left[\frac{c}{2}\right] - B \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( 2 \operatorname{ArcTan}[\tan[dx]] \cos\left[\frac{c}{2}\right] + 2 i \operatorname{ArcTan}[\tan[dx]] \sin\left[\frac{c}{2}\right] \right) (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left. (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( \left( A \cos\left[\frac{c}{2}\right] + i B \cos\left[\frac{c}{2}\right] + i A \sin\left[\frac{c}{2}\right] - B \sin\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( i \cos\left[\frac{c}{2}\right] \log[\sin[c + dx]^2] - \log[\sin[c + dx]^2] \sin\left[\frac{c}{2}\right] \right) (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left. (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( x (-2 i A \csc[c] + 2 B \csc[c] + i (A + i B) \cot[c] (2 \cos[c] + 2 i \sin[c])) (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left. (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( (A + i B) \cos[2 dx] \left( \frac{1}{4} i \cos[c] + \frac{\sin[c]}{4} \right) (\cos[dx] + i \sin[dx]) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( \csc\left[\frac{c}{2}\right] \csc[c + dx]^2 \sec\left[\frac{c}{2}\right] \left( -\frac{\cos[c]}{12} - \frac{1}{12} i \sin[c] \right) \right. \\
 & \quad \left. (2 A \cos[c] - 3 i A \sin[c] + 3 B \sin[c]) (\cos[dx] + i \sin[dx]) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( (5 A + 3 i B) \left( \frac{1}{2} dx \cos[c] + \frac{1}{2} i dx \sin[c] \right) (\cos[dx] + i \sin[dx]) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( (A + i B) \left( \frac{\cos[c]}{4} - \frac{1}{4} i \sin[c] \right) (\cos[dx] + i \sin[dx]) \sin[2 dx] (A + B \tan[c + dx]) \right) / \\
 & \quad \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( \csc\left[\frac{c}{2}\right] \csc[c + dx]^3 \sec\left[\frac{c}{2}\right] (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left. \left( \frac{1}{2} i A \cos[c - dx] - \frac{1}{2} i A \cos[c + dx] - \frac{1}{2} A \sin[c - dx] + \frac{1}{2} A \sin[c + dx] \right) \right. \\
 & \quad \left. (A + B \tan[c + dx]) \right) / \left( 6 d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right) + \\
 & \left( \csc\left[\frac{c}{2}\right] \csc[c + dx] \sec\left[\frac{c}{2}\right] (\cos[dx] + i \sin[dx]) \right. \\
 & \quad \left. \left( -\frac{7}{2} i A \cos[c - dx] + \frac{3}{2} B \cos[c - dx] + \frac{7}{2} i A \cos[c + dx] - \frac{3}{2} B \cos[c + dx] + \frac{7}{2} A \sin[c - dx] + \right. \right. \\
 & \quad \left. \left. \frac{3}{2} i B \sin[c - dx] - \frac{7}{2} A \sin[c + dx] - \frac{3}{2} i B \sin[c + dx] \right) (A + B \tan[c + dx]) \right) / \\
 & \quad \left( 6 d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx]) \right)
 \end{aligned}$$

**Problem 44: Result more than twice size of optimal antiderivative.**

$$\int \frac{\tan[c + dx]^3 (A + B \tan[c + dx])}{(a + i a \tan[c + dx])^2} dx$$

Optimal (type 3, 142 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{3 (\text{i} A - 3 B) x}{4 a^2} + \frac{(A + 2 \text{i} B) \text{Log}[\text{Cos}[c + d x]]}{a^2 d} + \\
 & \frac{3 (\text{i} A - 3 B) \text{Tan}[c + d x]}{4 a^2 d} + \frac{(A + 2 \text{i} B) \text{Tan}[c + d x]^2}{2 a^2 d (1 + \text{i} \text{Tan}[c + d x])} + \frac{(\text{i} A - B) \text{Tan}[c + d x]^3}{4 d (a + \text{i} a \text{Tan}[c + d x])^2}
 \end{aligned}$$

Result (type 3, 956 leaves):

$$\begin{aligned}
 & - \left( \left( (2 A + 3 \text{i} B) \text{Cos}[2 d x] \text{Sec}[c + d x] (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 (A + B \text{Tan}[c + d x]) \right) / \right. \\
 & \quad \left. (4 d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) \right) + \\
 & \left( \text{Sec}[c + d x] (A \text{Cos}[c] + 2 \text{i} B \text{Cos}[c] + \text{i} A \text{Sin}[c] - 2 B \text{Sin}[c]) \right. \\
 & \quad \left. (-\text{i} \text{ArcTan}[\text{Tan}[d x]] \text{Cos}[c] + \text{ArcTan}[\text{Tan}[d x]] \text{Sin}[c]) (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 \right. \\
 & \quad \left. (A + B \text{Tan}[c + d x]) \right) / (d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) + \\
 & \left( \text{Sec}[c + d x] (A \text{Cos}[c] + 2 \text{i} B \text{Cos}[c] + \text{i} A \text{Sin}[c] - 2 B \text{Sin}[c]) \right. \\
 & \quad \left. \left( \frac{1}{2} \text{Cos}[c] \text{Log}[\text{Cos}[c + d x]^2] + \frac{1}{2} \text{i} \text{Log}[\text{Cos}[c + d x]^2] \text{Sin}[c] \right) (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 \right. \\
 & \quad \left. (A + B \text{Tan}[c + d x]) \right) / (d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) + \\
 & \left( (A + \text{i} B) \text{Cos}[4 d x] \text{Sec}[c + d x] \left( \frac{1}{16} \text{Cos}[2 c] - \frac{1}{16} \text{i} \text{Sin}[2 c] \right) (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 \right. \\
 & \quad \left. (A + B \text{Tan}[c + d x]) \right) / (d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) + \\
 & \left( (-\text{i} A + 3 B) \text{Sec}[c + d x] \left( \frac{3}{4} d x \text{Cos}[2 c] + \frac{3}{4} \text{i} d x \text{Sin}[2 c] \right) (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 \right. \\
 & \quad \left. (A + B \text{Tan}[c + d x]) \right) / (d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) + \\
 & \left( \text{i} (2 A + 3 \text{i} B) \text{Sec}[c + d x] (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 \text{Sin}[2 d x] (A + B \text{Tan}[c + d x]) \right) / \\
 & \quad (4 d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) + \\
 & \left( (-\text{i} A + B) \text{Sec}[c + d x] \left( \frac{1}{16} \text{Cos}[2 c] - \frac{1}{16} \text{i} \text{Sin}[2 c] \right) (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 \text{Sin}[4 d x] \right. \\
 & \quad \left. (A + B \text{Tan}[c + d x]) \right) / (d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) + \\
 & \left( \text{i} \text{Sec}[c] \text{Sec}[c + d x]^2 (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 (-B \text{Cos}[2 c - d x] + B \text{Cos}[2 c + d x] - \right. \\
 & \quad \left. \text{i} B \text{Sin}[2 c - d x] + \text{i} B \text{Sin}[2 c + d x]) (A + B \text{Tan}[c + d x]) \right) / \\
 & \quad (2 d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2) + \\
 & \left( x \text{Sec}[c + d x] (\text{Cos}[d x] + \text{i} \text{Sin}[d x])^2 \right. \\
 & \quad \left. (\text{i} A - 2 B - A \text{Tan}[c] - 2 \text{i} B \text{Tan}[c] + (A + 2 \text{i} B) (-\text{Cos}[2 c] - \text{i} \text{Sin}[2 c]) \text{Tan}[c]) \right. \\
 & \quad \left. (A + B \text{Tan}[c + d x]) \right) / ((A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + \text{i} a \text{Tan}[c + d x])^2)
 \end{aligned}$$

**Problem 49: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cot}[c + d x]^2 (A + B \text{Tan}[c + d x])}{(a + \text{i} a \text{Tan}[c + d x])^2} dx$$

Optimal (type 3, 141 leaves, 5 steps):

$$\frac{\frac{3(3A + iB)x}{4a^2} - \frac{3(3A + iB)\text{Cot}[c + dx]}{4a^2d}}{\frac{(2ia - B)\text{Log}[\text{Sin}[c + dx]]}{a^2d} + \frac{(2A + iB)\text{Cot}[c + dx]}{2a^2d(1 + i\tan[c + dx])} + \frac{(A + iB)\text{Cot}[c + dx]}{4d(a + ia\tan[c + dx])^2}}$$

Result (type 3, 960 leaves):

$$\begin{aligned} & \left( (-3ia + 2B)\text{Cos}[2dx]\text{Sec}[c + dx](\text{Cos}[dx] + i\text{Sin}[dx])^2(A + B\tan[c + dx]) \right) / \\ & \left( 4d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) + \\ & \left( \text{Sec}[c + dx](-2ia\text{Cos}[c] + B\text{Cos}[c] + 2A\text{Sin}[c] + iB\text{Sin}[c]) \right. \\ & \quad \left. (-i\text{ArcTan}[\tan[dx]]\text{Cos}[c] + \text{ArcTan}[\tan[dx]]\text{Sin}[c])(\text{Cos}[dx] + i\text{Sin}[dx])^2 \right. \\ & \quad \left. (A + B\tan[c + dx]) \right) / \left( d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) + \\ & \left( \text{Sec}[c + dx](-2ia\text{Cos}[c] + B\text{Cos}[c] + 2A\text{Sin}[c] + iB\text{Sin}[c]) \right. \\ & \quad \left. \left( \frac{1}{2}\text{Cos}[c]\text{Log}[\text{Sin}[c + dx]^2] + \frac{1}{2}i\text{Log}[\text{Sin}[c + dx]^2]\text{Sin}[c] \right) (\text{Cos}[dx] + i\text{Sin}[dx])^2 \right. \\ & \quad \left. (A + B\tan[c + dx]) \right) / \left( d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) + \\ & \left( x\text{Sec}[c + dx](-2A - iB + 2ia\text{Cot}[c] - B\text{Cot}[c] + (-2ia + B)\text{Cot}[c](\text{Cos}[2c] + i\text{Sin}[2c])) \right. \\ & \quad \left. (\text{Cos}[dx] + i\text{Sin}[dx])^2(A + B\tan[c + dx]) \right) / \\ & \left( (A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) + \\ & \left( (-ia + B)\text{Cos}[4dx]\text{Sec}[c + dx] \left( \frac{1}{16}\text{Cos}[2c] - \frac{1}{16}i\text{Sin}[2c] \right) (\text{Cos}[dx] + i\text{Sin}[dx])^2 \right. \\ & \quad \left. (A + B\tan[c + dx]) \right) / \left( d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) + \\ & \left( (3A + iB)\text{Sec}[c + dx] \left( -\frac{3}{4}dx\text{Cos}[2c] - \frac{3}{4}i dx\text{Sin}[2c] \right) (\text{Cos}[dx] + i\text{Sin}[dx])^2 \right. \\ & \quad \left. (A + B\tan[c + dx]) \right) / \left( d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) - \\ & \left( (3A + 2iB)\text{Sec}[c + dx](\text{Cos}[dx] + i\text{Sin}[dx])^2\text{Sin}[2dx](A + B\tan[c + dx]) \right) / \\ & \left( 4d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) + \\ & \left( (A + iB)\text{Sec}[c + dx] \left( -\frac{1}{16}\text{Cos}[2c] + \frac{1}{16}i\text{Sin}[2c] \right) (\text{Cos}[dx] + i\text{Sin}[dx])^2\text{Sin}[4dx] \right. \\ & \quad \left. (A + B\tan[c + dx]) \right) / \left( d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) + \\ & \left( \text{Csc}[c]\text{Csc}[c + dx]\text{Sec}[c + dx](\text{Cos}[dx] + i\text{Sin}[dx])^2 \right. \\ & \quad \left. \left( \frac{1}{2}ia\text{Cos}[2c - dx] - \frac{1}{2}ia\text{Cos}[2c + dx] - \frac{1}{2}A\text{Sin}[2c - dx] + \frac{1}{2}A\text{Sin}[2c + dx] \right) \right. \\ & \quad \left. (A + B\tan[c + dx]) \right) / \left( d(A\text{Cos}[c + dx] + B\text{Sin}[c + dx])(a + ia\tan[c + dx])^2 \right) \end{aligned}$$

Problem 50: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^3 (A + B \text{Tan}[c + d x])}{(a + i a \text{Tan}[c + d x])^2} dx$$

Optimal (type 3, 170 leaves, 6 steps):

$$\frac{3 (5 i A - 3 B) x}{4 a^2} + \frac{3 (5 i A - 3 B) \text{Cot}[c + d x]}{4 a^2 d} - \frac{(2 A + i B) \text{Cot}[c + d x]^2}{a^2 d} - \frac{2 (2 A + i B) \text{Log}[\text{Sin}[c + d x]]}{a^2 d} + \frac{(5 A + 3 i B) \text{Cot}[c + d x]^2}{4 a^2 d (1 + i \text{Tan}[c + d x])} + \frac{(A + i B) \text{Cot}[c + d x]^2}{4 d (a + i a \text{Tan}[c + d x])^2}$$

Result (type 3, 1112 leaves):

$$\begin{aligned}
& - \left( \left( (4A + 3iB) \cos[2dx] \sec[c+dx] (\cos[dx] + i \sin[dx])^2 (A + B \tan[c+dx]) \right) / \right. \\
& \quad \left. (4d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2) \right) + \\
& \left( \sec[c+dx] (2A \cos[c] + iB \cos[c] + 2iA \sin[c] - B \sin[c]) \right. \\
& \quad \left. (2i \operatorname{ArcTan}[\tan[dx]] \cos[c] - 2 \operatorname{ArcTan}[\tan[dx]] \sin[c]) (\cos[dx] + i \sin[dx])^2 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / (d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2) + \\
& \left( \sec[c+dx] (2A \cos[c] + iB \cos[c] + 2iA \sin[c] - B \sin[c]) \right. \\
& \quad \left. (-\cos[c] \log[\sin[c+dx]^2] - i \log[\sin[c+dx]^2] \sin[c]) \right. \\
& \quad \left. (\cos[dx] + i \sin[dx])^2 (A + B \tan[c+dx]) \right) / \\
& \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2 \right) + (x \sec[c+dx] \\
& \quad (4iA - 2B + 4A \cot[c] + 2iB \cot[c] + (2A + iB) \cot[c] (-2 \cos[2c] - 2i \sin[2c])) \\
& \quad (\cos[dx] + i \sin[dx])^2 (A + B \tan[c+dx]) / \\
& \left( (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2 \right) + \\
& \left( (A + iB) \cos[4dx] \sec[c+dx] \left( -\frac{1}{16} \cos[2c] + \frac{1}{16} i \sin[2c] \right) (\cos[dx] + i \sin[dx])^2 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / (d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2) + \\
& \left( \csc[c+dx]^2 \sec[c+dx] \left( -\frac{1}{2} A \cos[2c] - \frac{1}{2} i A \sin[2c] \right) (\cos[dx] + i \sin[dx])^2 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / (d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2) + \\
& \left( (5A + 3iB) \sec[c+dx] \left( \frac{3}{4} i dx \cos[2c] - \frac{3}{4} dx \sin[2c] \right) (\cos[dx] + i \sin[dx])^2 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / (d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2) + \\
& \left( i (4A + 3iB) \sec[c+dx] (\cos[dx] + i \sin[dx])^2 \sin[2dx] (A + B \tan[c+dx]) \right) / \\
& \quad (4d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2) + \\
& \left( (A + iB) \sec[c+dx] \left( \frac{1}{16} i \cos[2c] + \frac{1}{16} \sin[2c] \right) (\cos[dx] + i \sin[dx])^2 \sin[4dx] \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / (d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2) + \\
& \left( \csc[c] \csc[c+dx] \sec[c+dx] (\cos[dx] + i \sin[dx])^2 \right. \\
& \quad \left( A \cos[2c-dx] + \frac{1}{2} i B \cos[2c-dx] - A \cos[2c+dx] - \frac{1}{2} i B \cos[2c+dx] + \right. \\
& \quad \left. i A \sin[2c-dx] - \frac{1}{2} B \sin[2c-dx] - i A \sin[2c+dx] + \frac{1}{2} B \sin[2c+dx] \right) \\
& \quad \left. (A + B \tan[c+dx]) \right) / (d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^2)
\end{aligned}$$

**Problem 51: Result more than twice size of optimal antiderivative.**

$$\int \frac{\tan[c+dx]^4 (A + B \tan[c+dx])}{(a + ia \tan[c+dx])^3} dx$$



Optimal (type 3, 191 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{(7A + 25iB)x}{8a^3} - \frac{(iA - 3B) \operatorname{Log}[\operatorname{Cos}[c + dx]]}{a^3 d} + \frac{(7A + 25iB) \operatorname{Tan}[c + dx]}{8a^3 d} + \\
 & \frac{(iA - B) \operatorname{Tan}[c + dx]^4}{6d(a + ia \operatorname{Tan}[c + dx])^3} + \frac{(5A + 11iB) \operatorname{Tan}[c + dx]^3}{24ad(a + ia \operatorname{Tan}[c + dx])^2} - \frac{(iA - 3B) \operatorname{Tan}[c + dx]^2}{2d(a^3 + ia^3 \operatorname{Tan}[c + dx])}
 \end{aligned}$$

Result (type 3, 1251 leaves):

$$\begin{aligned}
 & \left( (11A + 23iB) \operatorname{Cos}[2dx] \operatorname{Sec}[c + dx]^2 \left( \frac{1}{16} i \operatorname{Cos}[c] - \frac{\operatorname{Sin}[c]}{16} \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( (-5iA + 7B) \operatorname{Cos}[4dx] \operatorname{Sec}[c + dx]^2 \left( \frac{\operatorname{Cos}[c]}{32} - \frac{1}{32} i \operatorname{Sin}[c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( \operatorname{Sec}[c + dx]^2 \left( -iA \operatorname{Cos}\left[\frac{3c}{2}\right] + 3B \operatorname{Cos}\left[\frac{3c}{2}\right] + A \operatorname{Sin}\left[\frac{3c}{2}\right] + 3iB \operatorname{Sin}\left[\frac{3c}{2}\right] \right) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{3c}{2}\right] \operatorname{Log}[\operatorname{Cos}[c + dx]] + i \operatorname{Log}[\operatorname{Cos}[c + dx]] \operatorname{Sin}\left[\frac{3c}{2}\right] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( (A + iB) \operatorname{Cos}[6dx] \operatorname{Sec}[c + dx]^2 \left( \frac{1}{48} i \operatorname{Cos}[3c] + \frac{1}{48} \operatorname{Sin}[3c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( (7A + 25iB) \operatorname{Sec}[c + dx]^2 \left( -\frac{1}{8} dx \operatorname{Cos}[3c] - \frac{1}{8} i dx \operatorname{Sin}[3c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( (11A + 23iB) \operatorname{Sec}[c + dx]^2 \left( \frac{\operatorname{Cos}[c]}{16} + \frac{1}{16} i \operatorname{Sin}[c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \operatorname{Sin}[2dx] \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( (5A + 7iB) \operatorname{Sec}[c + dx]^2 \left( -\frac{\operatorname{Cos}[c]}{32} + \frac{1}{32} i \operatorname{Sin}[c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \operatorname{Sin}[4dx] \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( (A + iB) \operatorname{Sec}[c + dx]^2 \left( \frac{1}{48} \operatorname{Cos}[3c] - \frac{1}{48} i \operatorname{Sin}[3c] \right) (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \operatorname{Sin}[6dx] \right. \\
 & \quad \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) + \\
 & \left( \operatorname{Sec}[c + dx]^3 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 (-B \operatorname{Cos}[3c - dx] + B \operatorname{Cos}[3c + dx] - \right. \\
 & \quad \left. iB \operatorname{Sin}[3c - dx] + iB \operatorname{Sin}[3c + dx]) (A + B \operatorname{Tan}[c + dx]) \right) / \left( 2d \left( \operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \right. \\
 & \quad \left. \left( \operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right] \right) (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + ia \operatorname{Tan}[c + dx])^3 \right) +
 \end{aligned}$$

$$\frac{1}{(A \cos [c+d x]+B \sin [c+d x])(a+i a \tan [c+d x])^3} \times \sec [c+d x]^2(\cos [d x]+i \sin [d x])^3$$

$$\left(\frac{1}{2} A \cos [c]+\frac{3}{2} i B \cos [c]-\frac{1}{2} A \cos [c]^3-\frac{3}{2} i B \cos [c]^3+i A \sin [c]-3 B \sin [c]-\right.$$

$$2 i A \cos [c]^2 \sin [c]+6 B \cos [c]^2 \sin [c]+3 A \cos [c] \sin [c]^2+9 i B \cos [c] \sin [c]^2+$$

$$2 i A \sin [c]^3-6 B \sin [c]^3-\frac{1}{2} A \sin [c] \tan [c]-\frac{3}{2} i B \sin [c] \tan [c]-\frac{1}{2} A \sin [c]^3 \tan [c]-$$

$$\left.\frac{3}{2} i B \sin [c]^3 \tan [c]+i(A+3 i B)(\cos [3 c]+i \sin [3 c]) \tan [c]\right)(A+B \tan [c+d x])$$

**Problem 57: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cot [c+d x]^2(A+B \tan [c+d x])}{(a+i a \tan [c+d x])^3} d x$$

Optimal (type 3, 183 leaves, 6 steps):

$$-\frac{(25 A+7 i B) x}{8 a^3}-\frac{(25 A+7 i B) \cot [c+d x]}{8 a^3 d}-\frac{(3 i A-B) \operatorname{Log}[\sin [c+d x]]}{a^3 d}+$$

$$\frac{(A+i B) \cot [c+d x]}{6 d(a+i a \tan [c+d x])^3}+\frac{(11 A+5 i B) \cot [c+d x]}{24 a d(a+i a \tan [c+d x])^2}+\frac{(3 A+i B) \cot [c+d x]}{2 d\left(a^3+i a^3 \tan [c+d x]\right)}$$

Result (type 3, 1282 leaves):

$$\left(\left(-7 i A+5 B\right) \cos [4 d x] \sec [c+d x]^2\left(\frac{\cos [c]}{32}-\frac{1}{32} i \sin [c]\right)(\cos [d x]+i \sin [d x])^3\right.$$

$$\left.\left(A+B \tan [c+d x]\right)\right) / \left(d(A \cos [c+d x]+B \sin [c+d x])(a+i a \tan [c+d x])^3\right)+$$

$$\left(\left(-23 i A+11 B\right) \cos [2 d x] \sec [c+d x]^2\left(\frac{\cos [c]}{16}+\frac{1}{16} i \sin [c]\right)(\cos [d x]+i \sin [d x])^3\right.$$

$$\left.\left(A+B \tan [c+d x]\right)\right) / \left(d(A \cos [c+d x]+B \sin [c+d x])(a+i a \tan [c+d x])^3\right)+$$

$$\left(\sec [c+d x]^2\left(-3 i A \cos \left[\frac{3 c}{2}\right]+B \cos \left[\frac{3 c}{2}\right]+3 A \sin \left[\frac{3 c}{2}\right]+i B \sin \left[\frac{3 c}{2}\right]\right)\right.$$

$$\left.\left(-i \operatorname{ArcTan}[\tan [d x]] \cos \left[\frac{3 c}{2}\right]+\operatorname{ArcTan}[\tan [d x]] \sin \left[\frac{3 c}{2}\right]\right)(\cos [d x]+i \sin [d x])^3\right.$$

$$\left.\left(A+B \tan [c+d x]\right)\right) / \left(d(A \cos [c+d x]+B \sin [c+d x])(a+i a \tan [c+d x])^3\right)+$$

$$\left(\sec [c+d x]^2\left(-3 i A \cos \left[\frac{3 c}{2}\right]+B \cos \left[\frac{3 c}{2}\right]+3 A \sin \left[\frac{3 c}{2}\right]+i B \sin \left[\frac{3 c}{2}\right]\right)\right.$$

$$\left.\left(\frac{1}{2} \cos \left[\frac{3 c}{2}\right] \operatorname{Log}[\sin [c+d x]^2]+\frac{1}{2} i \operatorname{Log}[\sin [c+d x]^2] \sin \left[\frac{3 c}{2}\right]\right)(\cos [d x]+i \sin [d x])^3\right.$$

$$\left.\left(A+B \tan [c+d x]\right)\right) / \left(d(A \cos [c+d x]+B \sin [c+d x])(a+i a \tan [c+d x])^3\right)+$$

$$\left(x \sec [c+d x]^2(-6 A \cos [c]-2 i B \cos [c]+3 i A \cos [c] \cot [c]-B \cos [c] \cot [c]-3 i A \sin [c]+B \sin [c]+(-3 i A+B) \cot [c](\cos [3 c]+i \sin [3 c]))(\cos [d x]+i \sin [d x])^3\right.$$

$$\left.\left(A+B \tan [c+d x]\right)\right) / \left((A \cos [c+d x]+B \sin [c+d x])(a+i a \tan [c+d x])^3\right)+$$

$$\begin{aligned}
 & \left( (-i A + B) \cos[6 d x] \sec[c + d x]^2 \left( \frac{1}{48} \cos[3 c] - \frac{1}{48} i \sin[3 c] \right) (\cos[d x] + i \sin[d x])^3 \right. \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^3 \right) + \\
 & \left( (25 A + 7 i B) \sec[c + d x]^2 \left( -\frac{1}{8} d x \cos[3 c] - \frac{1}{8} i d x \sin[3 c] \right) (\cos[d x] + i \sin[d x])^3 \right. \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^3 \right) + \\
 & \left( (23 A + 11 i B) \sec[c + d x]^2 \left( -\frac{\cos[c]}{16} - \frac{1}{16} i \sin[c] \right) (\cos[d x] + i \sin[d x])^3 \sin[2 d x] \right. \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^3 \right) + \\
 & \left( (7 A + 5 i B) \sec[c + d x]^2 \left( -\frac{\cos[c]}{32} + \frac{1}{32} i \sin[c] \right) (\cos[d x] + i \sin[d x])^3 \sin[4 d x] \right. \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^3 \right) + \\
 & \left( (A + i B) \sec[c + d x]^2 \left( -\frac{1}{48} \cos[3 c] + \frac{1}{48} i \sin[3 c] \right) (\cos[d x] + i \sin[d x])^3 \sin[6 d x] \right. \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^3 \right) + \\
 & \left( \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Csc}[c + d x] \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 (\cos[d x] + i \sin[d x])^3 \right. \\
 & \quad \left( \frac{1}{2} i A \cos[3 c - d x] - \frac{1}{2} i A \cos[3 c + d x] - \frac{1}{2} A \sin[3 c - d x] + \frac{1}{2} A \sin[3 c + d x] \right) \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( 2 d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^3 \right)
 \end{aligned}$$

**Problem 58: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cot[c + d x]^3 (A + B \tan[c + d x])}{(a + i a \tan[c + d x])^3} dx$$

Optimal (type 3, 216 leaves, 7 steps):

$$\begin{aligned}
 & \frac{5 (11 i A - 5 B) x}{8 a^3} + \frac{5 (11 i A - 5 B) \cot[c + d x]}{8 a^3 d} - \frac{(7 A + 3 i B) \cot[c + d x]^2}{2 a^3 d} - \\
 & \frac{(7 A + 3 i B) \operatorname{Log}[\sin[c + d x]]}{a^3 d} + \frac{(A + i B) \cot[c + d x]^2}{6 d (a + i a \tan[c + d x])^3} + \\
 & \frac{(13 A + 7 i B) \cot[c + d x]^2}{24 a d (a + i a \tan[c + d x])^2} + \frac{5 (11 A + 5 i B) \cot[c + d x]^2}{24 d (a^3 + i a^3 \tan[c + d x])}
 \end{aligned}$$

Result (type 3, 1448 leaves):

$$\begin{aligned}
 & \left( (9 A + 7 i B) \cos[4 d x] \sec[c + d x]^2 \left( -\frac{\cos[c]}{32} + \frac{1}{32} i \sin[c] \right) (\cos[d x] + i \sin[d x])^3 \right. \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^3 \right) +
 \end{aligned}$$

$$\begin{aligned}
& \left( (39A + 23iB) \cos[2dx] \sec[c+dx]^2 \left( -\frac{\cos[c]}{16} - \frac{1}{16}i \sin[c] \right) (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( \sec[c+dx]^2 \left( 7A \cos\left[\frac{3c}{2}\right] + 3iB \cos\left[\frac{3c}{2}\right] + 7iA \sin\left[\frac{3c}{2}\right] - 3B \sin\left[\frac{3c}{2}\right] \right) \right. \\
& \quad \left. \left( i \operatorname{ArcTan}[\tan[dx]] \cos\left[\frac{3c}{2}\right] - \operatorname{ArcTan}[\tan[dx]] \sin\left[\frac{3c}{2}\right] \right) (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( \sec[c+dx]^2 \left( 7A \cos\left[\frac{3c}{2}\right] + 3iB \cos\left[\frac{3c}{2}\right] + 7iA \sin\left[\frac{3c}{2}\right] - 3B \sin\left[\frac{3c}{2}\right] \right) \right. \\
& \quad \left. \left( -\frac{1}{2} \cos\left[\frac{3c}{2}\right] \log[\sin[c+dx]^2] - \frac{1}{2}i \log[\sin[c+dx]^2] \sin\left[\frac{3c}{2}\right] \right) (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( x \sec[c+dx]^2 (14iA \cos[c] - 6B \cos[c] + 7A \cos[c] \cot[c] + 3iB \cos[c] \cot[c] - 7A \sin[c] - \right. \\
& \quad \left. 3iB \sin[c] + (7A + 3iB) \cot[c] (-\cos[3c] - i \sin[3c])) (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( (A + iB) \cos[6dx] \sec[c+dx]^2 \left( -\frac{1}{48} \cos[3c] + \frac{1}{48}i \sin[3c] \right) (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( \csc[c+dx]^2 \sec[c+dx]^2 \left( -\frac{1}{2} A \cos[3c] - \frac{1}{2}i A \sin[3c] \right) (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( (11A + 5iB) \sec[c+dx]^2 \left( \frac{5}{8}i dx \cos[3c] - \frac{5}{8} dx \sin[3c] \right) (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( (39A + 23iB) \sec[c+dx]^2 \left( \frac{1}{16}i \cos[c] - \frac{\sin[c]}{16} \right) (\cos[dx] + i \sin[dx])^3 \sin[2dx] \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( (9A + 7iB) \sec[c+dx]^2 \left( \frac{1}{32}i \cos[c] + \frac{\sin[c]}{32} \right) (\cos[dx] + i \sin[dx])^3 \sin[4dx] \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( (A + iB) \sec[c+dx]^2 \left( \frac{1}{48}i \cos[3c] + \frac{1}{48} \sin[3c] \right) (\cos[dx] + i \sin[dx])^3 \sin[6dx] \right. \\
& \quad \left. (A + B \tan[c+dx]) \right) / \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + ia \tan[c+dx])^3 \right) + \\
& \left( \csc\left[\frac{c}{2}\right] \csc[c+dx] \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (\cos[dx] + i \sin[dx])^3 \right. \\
& \quad \left. \left( \frac{3}{2} A \cos[3c-dx] + \frac{1}{2}i B \cos[3c-dx] - \frac{3}{2} A \cos[3c+dx] - \frac{1}{2}i B \cos[3c+dx] + \right. \right.
\end{aligned}$$

$$\frac{\frac{3}{2} \operatorname{Im} A \sin[3c-dx] - \frac{1}{2} B \sin[3c-dx] - \frac{3}{2} \operatorname{Im} A \sin[3c+dx] + \frac{1}{2} B \sin[3c+dx]}{(A+B \tan[c+dx])} \Big/ \left( 2d (A \cos[c+dx] + B \sin[c+dx]) (a + \operatorname{Im} a \tan[c+dx])^3 \right)$$

**Problem 65: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cot[c+dx]^2 (A+B \tan[c+dx])}{(a + \operatorname{Im} a \tan[c+dx])^4} dx$$

Optimal (type 3, 220 leaves, 7 steps):

$$\frac{5 (13A + 3 \operatorname{Im} B) x}{16 a^4} - \frac{5 (13A + 3 \operatorname{Im} B) \cot[c+dx]}{16 a^4 d} - \frac{(4 \operatorname{Im} A - B) \operatorname{Log}[\sin[c+dx]]}{a^4 d} + \frac{(31A + 9 \operatorname{Im} B) \cot[c+dx]}{48 a^4 d (1 + \operatorname{Im} \tan[c+dx])^2} + \frac{(4A + \operatorname{Im} B) \cot[c+dx]}{2 a^4 d (1 + \operatorname{Im} \tan[c+dx])} + \frac{(A + \operatorname{Im} B) \cot[c+dx]}{8 d (a + \operatorname{Im} a \tan[c+dx])^4} + \frac{(7A + 3 \operatorname{Im} B) \cot[c+dx]}{24 a d (a + \operatorname{Im} a \tan[c+dx])^3}$$

Result (type 3, 1466 leaves):

$$\begin{aligned} & \left( (-15 \operatorname{Im} A + 8B) \cos[4dx] \sec[c+dx]^3 (\cos[dx] + \operatorname{Im} \sin[dx])^4 (A+B \tan[c+dx]) \right) \Big/ \\ & \left( 32d (A \cos[c+dx] + B \sin[c+dx]) (a + \operatorname{Im} a \tan[c+dx])^4 \right) + \\ & \left( (-4 \operatorname{Im} A + 3B) \cos[6dx] \sec[c+dx]^3 \left( \frac{1}{48} \cos[2c] - \frac{1}{48} \operatorname{Im} \sin[2c] \right) (\cos[dx] + \operatorname{Im} \sin[dx])^4 \right. \\ & \left. (A+B \tan[c+dx]) \right) \Big/ \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + \operatorname{Im} a \tan[c+dx])^4 \right) + \\ & \left( (-36 \operatorname{Im} A + 13B) \cos[2dx] \sec[c+dx]^3 \left( \frac{1}{16} \cos[2c] + \frac{1}{16} \operatorname{Im} \sin[2c] \right) (\cos[dx] + \operatorname{Im} \sin[dx])^4 \right. \\ & \left. (A+B \tan[c+dx]) \right) \Big/ \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + \operatorname{Im} a \tan[c+dx])^4 \right) + \\ & \left( \sec[c+dx]^3 (-4 \operatorname{Im} A \cos[2c] + B \cos[2c] + 4A \sin[2c] + \operatorname{Im} B \sin[2c]) \right. \\ & \left. (-\operatorname{Im} \operatorname{ArcTan}[\tan[dx]] \cos[2c] + \operatorname{ArcTan}[\tan[dx]] \sin[2c]) (\cos[dx] + \operatorname{Im} \sin[dx])^4 \right. \\ & \left. (A+B \tan[c+dx]) \right) \Big/ \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + \operatorname{Im} a \tan[c+dx])^4 \right) + \\ & \left( \sec[c+dx]^3 (-4 \operatorname{Im} A \cos[2c] + B \cos[2c] + 4A \sin[2c] + \operatorname{Im} B \sin[2c]) \right. \\ & \left. \left( \frac{1}{2} \cos[2c] \operatorname{Log}[\sin[c+dx]^2] + \frac{1}{2} \operatorname{Im} \operatorname{Log}[\sin[c+dx]^2] \sin[2c] \right) (\cos[dx] + \operatorname{Im} \sin[dx])^4 \right. \\ & \left. (A+B \tan[c+dx]) \right) \Big/ \left( d (A \cos[c+dx] + B \sin[c+dx]) (a + \operatorname{Im} a \tan[c+dx])^4 \right) + \\ & \left( x \sec[c+dx]^3 (-12A \cos[c]^2 - 3 \operatorname{Im} B \cos[c]^2 + 4 \operatorname{Im} A \cos[c]^2 \cot[c] - B \cos[c]^2 \cot[c] - \right. \\ & \left. 12 \operatorname{Im} A \cos[c] \sin[c] + 3B \cos[c] \sin[c] + 4A \sin[c]^2 + \operatorname{Im} B \sin[c]^2 + \right. \\ & \left. (-4 \operatorname{Im} A + B) \cot[c] (\cos[4c] + \operatorname{Im} \sin[4c]) \right) (\cos[dx] + \operatorname{Im} \sin[dx])^4 (A+B \tan[c+dx]) \Big/ \\ & \left( (A \cos[c+dx] + B \sin[c+dx]) (a + \operatorname{Im} a \tan[c+dx])^4 \right) + \\ & \left( (-\operatorname{Im} A + B) \cos[8dx] \sec[c+dx]^3 \left( \frac{1}{128} \cos[4c] - \frac{1}{128} \operatorname{Im} \sin[4c] \right) (\cos[dx] + \operatorname{Im} \sin[dx])^4 \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \left( (A + B \tan[c + dx]) \right) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right) + \\
 & \left( (13 A + 3 i B) \sec[c + dx]^3 \left( -\frac{5}{16} dx \cos[4c] - \frac{5}{16} i dx \sin[4c] \right) (\cos[dx] + i \sin[dx])^4 \right. \\
 & \left. \left( (A + B \tan[c + dx]) \right) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right) + \\
 & \left( (36 A + 13 i B) \sec[c + dx]^3 \left( -\frac{1}{16} \cos[2c] - \frac{1}{16} i \sin[2c] \right) (\cos[dx] + i \sin[dx])^4 \right. \\
 & \left. \sin[2dx] (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right) - \\
 & \left( (15 A + 8 i B) \sec[c + dx]^3 (\cos[dx] + i \sin[dx])^4 \sin[4dx] (A + B \tan[c + dx]) \right) / \\
 & \left( 32 d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right) + \\
 & \left( (4 A + 3 i B) \sec[c + dx]^3 \left( -\frac{1}{48} \cos[2c] + \frac{1}{48} i \sin[2c] \right) (\cos[dx] + i \sin[dx])^4 \sin[6dx] \right. \\
 & \left. (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right) + \\
 & \left( (A + i B) \sec[c + dx]^3 \left( -\frac{1}{128} \cos[4c] + \frac{1}{128} i \sin[4c] \right) (\cos[dx] + i \sin[dx])^4 \sin[8dx] \right. \\
 & \left. (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right) + \\
 & \left( \csc[c] \csc[c + dx] \sec[c + dx]^3 (\cos[dx] + i \sin[dx])^4 \right. \\
 & \left. \left( \frac{1}{2} i A \cos[4c - dx] - \frac{1}{2} i A \cos[4c + dx] - \frac{1}{2} A \sin[4c - dx] + \frac{1}{2} A \sin[4c + dx] \right) \right. \\
 & \left. (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right)
 \end{aligned}$$

**Problem 66: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cot[c + dx]^3 (A + B \tan[c + dx])}{(a + i a \tan[c + dx])^4} dx$$

Optimal (type 3, 255 leaves, 8 steps):

$$\begin{aligned}
 & \frac{5 (35 i A - 13 B) x}{16 a^4} + \frac{5 (35 i A - 13 B) \cot[c + dx]}{16 a^4 d} - \frac{(11 A + 4 i B) \cot[c + dx]^2}{2 a^4 d} - \\
 & \frac{(11 A + 4 i B) \log[\sin[c + dx]]}{a^4 d} + \frac{(43 A + 17 i B) \cot[c + dx]^2}{48 a^4 d (1 + i \tan[c + dx])^2} + \\
 & \frac{5 (35 A + 13 i B) \cot[c + dx]^2}{48 a^4 d (1 + i \tan[c + dx])} + \frac{(A + i B) \cot[c + dx]^2}{8 d (a + i a \tan[c + dx])^4} + \frac{(2 A + i B) \cot[c + dx]^2}{6 a d (a + i a \tan[c + dx])^3}
 \end{aligned}$$

Result (type 3, 1625 leaves):

$$\begin{aligned}
 & - \left( \left( (3 (8 A + 5 i B) \cos[4dx] \sec[c + dx]^3 (\cos[dx] + i \sin[dx])^4 (A + B \tan[c + dx])) \right) / \right. \\
 & \left. (32 d (A \cos[c + dx] + B \sin[c + dx]) (a + i a \tan[c + dx])^4 \right) + \\
 & \left( (5 A + 4 i B) \cos[6dx] \sec[c + dx]^3 \left( -\frac{1}{48} \cos[2c] + \frac{1}{48} i \sin[2c] \right) (\cos[dx] + i \sin[dx])^4 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( (25 A + 12 i B) \cos[2 d x] \sec[c + d x]^3 \left( -\frac{3}{16} \cos[2 c] - \frac{3}{16} i \sin[2 c] \right) (\cos[d x] + i \sin[d x])^4 \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( \sec[c + d x]^3 (11 A \cos[2 c] + 4 i B \cos[2 c] + 11 i A \sin[2 c] - 4 B \sin[2 c]) \right. \\
 & \left. (i \operatorname{ArcTan}[\tan[d x]] \cos[2 c] - \operatorname{ArcTan}[\tan[d x]] \sin[2 c]) (\cos[d x] + i \sin[d x])^4 \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( \sec[c + d x]^3 (11 A \cos[2 c] + 4 i B \cos[2 c] + 11 i A \sin[2 c] - 4 B \sin[2 c]) \right. \\
 & \left. \left( -\frac{1}{2} \cos[2 c] \log[\sin[c + d x]^2] - \frac{1}{2} i \log[\sin[c + d x]^2] \sin[2 c] \right) (\cos[d x] + i \sin[d x])^4 \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( x \sec[c + d x]^3 (33 i A \cos[c]^2 - 12 B \cos[c]^2 + 11 A \cos[c]^2 \cot[c] + 4 i B \cos[c]^2 \cot[c] - \right. \\
 & \quad 33 A \cos[c] \sin[c] - 12 i B \cos[c] \sin[c] - 11 i A \sin[c]^2 + 4 B \sin[c]^2 + \\
 & \quad \left. (11 A + 4 i B) \cot[c] (-\cos[4 c] - i \sin[4 c]) \right) (\cos[d x] + i \sin[d x])^4 \\
 & \left. (A + B \tan[c + d x]) \right) / \left( (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( (A + i B) \cos[8 d x] \sec[c + d x]^3 \left( -\frac{1}{128} \cos[4 c] + \frac{1}{128} i \sin[4 c] \right) (\cos[d x] + i \sin[d x])^4 \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( \csc[c + d x]^2 \sec[c + d x]^3 \left( -\frac{1}{2} A \cos[4 c] - \frac{1}{2} i A \sin[4 c] \right) (\cos[d x] + i \sin[d x])^4 \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( (35 A + 13 i B) \sec[c + d x]^3 \left( \frac{5}{16} i d x \cos[4 c] - \frac{5}{16} d x \sin[4 c] \right) (\cos[d x] + i \sin[d x])^4 \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( (25 A + 12 i B) \sec[c + d x]^3 \left( \frac{3}{16} i \cos[2 c] - \frac{3}{16} \sin[2 c] \right) (\cos[d x] + i \sin[d x])^4 \right. \\
 & \left. \sin[2 d x] (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( 3 i (8 A + 5 i B) \sec[c + d x]^3 (\cos[d x] + i \sin[d x])^4 \sin[4 d x] (A + B \tan[c + d x]) \right) / \\
 & \left( 32 d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( (5 A + 4 i B) \sec[c + d x]^3 \left( \frac{1}{48} i \cos[2 c] + \frac{1}{48} \sin[2 c] \right) (\cos[d x] + i \sin[d x])^4 \sin[6 d x] \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) + \\
 & \left( (A + i B) \sec[c + d x]^3 \left( \frac{1}{128} i \cos[4 c] + \frac{1}{128} \sin[4 c] \right) (\cos[d x] + i \sin[d x])^4 \sin[8 d x] \right. \\
 & \left. (A + B \tan[c + d x]) \right) / \left( d (A \cos[c + d x] + B \sin[c + d x]) (a + i a \tan[c + d x])^4 \right) +
 \end{aligned}$$

$$\left( \text{Csc}[c] \text{Csc}[c+dx] \text{Sec}[c+dx]^3 (\text{Cos}[dx] + i \text{Sin}[dx])^4 \right. \\ \left. \left( 2A \text{Cos}[4c-dx] + \frac{1}{2} i B \text{Cos}[4c-dx] - 2A \text{Cos}[4c+dx] - \frac{1}{2} i B \text{Cos}[4c+dx] + \right. \right. \\ \left. \left. 2i A \text{Sin}[4c-dx] - \frac{1}{2} B \text{Sin}[4c-dx] - 2i A \text{Sin}[4c+dx] + \frac{1}{2} B \text{Sin}[4c+dx] \right) \right. \\ \left. (A+B \text{Tan}[c+dx]) \right) / \left( d (A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a+i a \text{Tan}[c+dx])^4 \right)$$

**Problem 71: Result more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c+dx] \sqrt{a+i a \text{Tan}[c+dx]} (A+B \text{Tan}[c+dx]) dx$$

Optimal (type 3, 86 leaves, 6 steps):

$$-\frac{2\sqrt{a} A \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+dx]}}{\sqrt{a}}\right]}{d} + \frac{\sqrt{2}\sqrt{a} (A-i B) \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{d}$$

Result (type 3, 192 leaves):

$$\frac{1}{2d} e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \left( 2(A-i B) \text{ArcSinh}\left[e^{i(c+dx)}\right] + \right. \\ \left. \sqrt{2} A \left( \text{Log}\left[1-e^{i(c+dx)}\right] - \text{Log}\left[1+e^{i(c+dx)}\right] + \text{Log}\left[1-e^{i(c+dx)} + \sqrt{2}\sqrt{1+e^{2i(c+dx)}}\right] - \right. \right. \\ \left. \left. \text{Log}\left[1+e^{i(c+dx)} + \sqrt{2}\sqrt{1+e^{2i(c+dx)}}\right] \right) \right) \sqrt{a+i a \text{Tan}[c+dx]}$$

**Problem 72: Result more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c+dx]^2 \sqrt{a+i a \text{Tan}[c+dx]} (A+B \text{Tan}[c+dx]) dx$$

Optimal (type 3, 123 leaves, 7 steps):

$$-\frac{\sqrt{a} (i A + 2 B) \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+dx]}}{\sqrt{a}}\right]}{d} + \\ \frac{\sqrt{2}\sqrt{a} (i A + B) \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{d} - \frac{A \text{Cot}[c+dx] \sqrt{a+i a \text{Tan}[c+dx]}}{d}$$

Result (type 3, 293 leaves):



$$\frac{1}{8d} \left( -8A \operatorname{Cot}[c+dx] + e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \right. \\ \left. \left( 8(iA+B) \operatorname{ArcSinh}[e^{i(c+dx)}] + \sqrt{2}(iA+2B) \left( \operatorname{Log}[(-1+e^{i(c+dx)})^2] - \operatorname{Log}[(1+e^{i(c+dx)})^2] + \right. \right. \right. \\ \left. \left. \operatorname{Log}[3+3e^{2i(c+dx)}+2\sqrt{2}\sqrt{1+e^{2i(c+dx)}}] - 2e^{i(c+dx)} \left( 1+\sqrt{2}\sqrt{1+e^{2i(c+dx)}} \right) \right) - \right. \\ \left. \left. \operatorname{Log}[3+3e^{2i(c+dx)}+2\sqrt{2}\sqrt{1+e^{2i(c+dx)}}] + \right. \right. \\ \left. \left. 2e^{i(c+dx)} \left( 1+\sqrt{2}\sqrt{1+e^{2i(c+dx)}} \right) \right) \right) \sqrt{a+ia \operatorname{Tan}[c+dx]}$$

**Problem 73: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c+dx]^3 \sqrt{a+ia \operatorname{Tan}[c+dx]} (A+B \operatorname{Tan}[c+dx]) dx$$

Optimal (type 3, 169 leaves, 8 steps):

$$\frac{\sqrt{a}(7A-4iB) \operatorname{ArcTanh}\left[\frac{\sqrt{a+ia \operatorname{Tan}[c+dx]}}{\sqrt{a}}\right]}{4d} - \frac{\sqrt{2}\sqrt{a}(A-iB) \operatorname{ArcTanh}\left[\frac{\sqrt{a+ia \operatorname{Tan}[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{d} - \\ \frac{(iA+4B) \operatorname{Cot}[c+dx] \sqrt{a+ia \operatorname{Tan}[c+dx]}}{4d} - \frac{A \operatorname{Cot}[c+dx]^2 \sqrt{a+ia \operatorname{Tan}[c+dx]}}{2d}$$

Result (type 3, 388 leaves):

$$\left( \left( - \left( 2 \left( 16\sqrt{2}(A-iB) \operatorname{ArcSinh}[e^{i(c+dx)}] + (7A-4iB) \left( \operatorname{Log}[(-1+e^{i(c+dx)})^2] - \operatorname{Log}[(1+e^{i(c+dx)})^2] + \right. \right. \right. \right. \right. \\ \left. \left. \operatorname{Log}[3+3e^{2i(c+dx)}+2\sqrt{2}\sqrt{1+e^{2i(c+dx)}}] - 2e^{i(c+dx)} \left( 1+\sqrt{2}\sqrt{1+e^{2i(c+dx)}} \right) \right) - \right. \\ \left. \left. \operatorname{Log}[3+3e^{2i(c+dx)}+2\sqrt{2}\sqrt{1+e^{2i(c+dx)}}] + \right. \right. \\ \left. \left. 2e^{i(c+dx)} \left( 1+\sqrt{2}\sqrt{1+e^{2i(c+dx)}} \right) \right) \right) \left/ \left( \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \sqrt{1+e^{2i(c+dx)}} \right) \right) - \\ \frac{8 \operatorname{Csc}[c+dx] (2A \operatorname{Csc}[c+dx] + (iA+4B) \operatorname{Sec}[c+dx])}{\operatorname{Sec}[c+dx]^{3/2}} \left. \right) \\ \left( \sqrt{a+ia \operatorname{Tan}[c+dx]} (A + B \operatorname{Tan}[c+dx]) \right) \left/ \right. \\ (32d \operatorname{Sec}[c+dx]^{3/2} (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]))$$

### Problem 78: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x] (a + i a \tan [c + d x])^{3/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 113 leaves, 7 steps):

$$-\frac{2 a^{3/2} A \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \tan [c+d x]}}{\sqrt{a}}\right]}{d} + \frac{2 \sqrt{2} a^{3/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \tan [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} + \frac{2 i a B \sqrt{a+i a \tan [c+d x]}}{d}$$

Result (type 3, 287 leaves):

$$\frac{1}{\sqrt{2} d} a e^{-i (c+d x)} \left( 2 i \sqrt{2} B e^{i (c+d x)} + 2 \sqrt{2} (A - i B) \sqrt{1 + e^{2 i (c+d x)}} \operatorname{ArcSinh}\left[e^{i (c+d x)}\right] + A \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Log}\left[1 - e^{i (c+d x)}\right] - A \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Log}\left[1 + e^{i (c+d x)}\right] + A \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Log}\left[1 - e^{i (c+d x)} + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}}\right] - A \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Log}\left[1 + e^{i (c+d x)} + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}}\right] \right) \sqrt{a + i a \tan [c + d x]}$$

### Problem 79: Result more than twice size of optimal antiderivative.

$$\int \cot [c + d x]^2 (a + i a \tan [c + d x])^{3/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 125 leaves, 7 steps):

$$-\frac{a^{3/2} (3 i A + 2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \tan [c+d x]}}{\sqrt{a}}\right]}{d} + \frac{2 \sqrt{2} a^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \tan [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} - \frac{a A \cot [c + d x] \sqrt{a + i a \tan [c + d x]}}{d}$$

Result (type 3, 496 leaves):

$$\begin{aligned}
 & \left( e^{-i c} \sqrt{e^{i d x}} \left( 16 (i A + B) \operatorname{ArcSinh}\left[e^{i (c+d x)}\right] + \right. \right. \\
 & \quad \left. \sqrt{2} (3 i A + 2 B) \left( \operatorname{Log}\left[-1 + e^{i (c+d x)}\right]^2\right) - \operatorname{Log}\left[1 + e^{i (c+d x)}\right]^2\right) + \right. \\
 & \quad \left. \operatorname{Log}\left[3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left(1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}}\right)\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left(1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}}\right)\right] \right) \Bigg) \\
 & \left( a + i a \operatorname{Tan}[c + d x] \right)^{3/2} (A + B \operatorname{Tan}[c + d x]) \Bigg) / \left( 4 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Sec}[c + d x]^{5/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{3/2} \right. \\
 & \quad \left. (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + (\operatorname{Cos}[c + d x])^2 \\
 & \quad (\operatorname{Cot}[c] (-A \operatorname{Cos}[c] + i A \operatorname{Sin}[c]) + A \operatorname{Csc}[c] \operatorname{Csc}[c + d x] (\operatorname{Cos}[c] - i \operatorname{Sin}[c]) \operatorname{Sin}[d x]) \\
 & \quad (a + i a \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x]) \Bigg) / \\
 & \quad (d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]) (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]))
 \end{aligned}$$

**Problem 80: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + d x]^3 (a + i a \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 171 leaves, 8 steps):

$$\frac{a^{3/2} (11 A - 12 i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a}}\right]}{4 d} - \frac{2 \sqrt{2} a^{3/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} - \frac{a (5 i A + 4 B) \operatorname{Cot}[c + d x] \sqrt{a + i a \operatorname{Tan}[c + d x]}}{4 d} - \frac{a A \operatorname{Cot}[c + d x]^2 \sqrt{a + i a \operatorname{Tan}[c + d x]}}{2 d}$$

Result (type 3, 565 leaves):

$$\begin{aligned}
 & - \left( \left( e^{-i c} \sqrt{e^{i d x}} \left( 64 (A - i B) \operatorname{ArcSinh} \left[ e^{i (c+d x)} \right] + \right. \right. \right. \\
 & \quad \sqrt{2} (11 A - 12 i B) \left( \operatorname{Log} \left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log} \left[ (1 + e^{i (c+d x)})^2 \right] + \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] \right) \right) \\
 & \quad \left( a + i a \operatorname{Tan} [c + d x] \right)^{3/2} (A + B \operatorname{Tan} [c + d x]) \Bigg) / \left( 16 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Sec} [c + d x]^{5/2} (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^{3/2} \right. \\
 & \quad \left. (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right) \Bigg) + \\
 & \quad \left( \operatorname{Cos} [c + d x] \right)^2 \left( \operatorname{Csc} [c + d x] \right)^2 \left( -\frac{1}{2} A \operatorname{Cos} [c] + \frac{1}{2} i A \operatorname{Sin} [c] \right) - \\
 & \quad i \operatorname{Csc} [c] \left( \frac{\operatorname{Cos} [c]}{4} - \frac{1}{4} i \operatorname{Sin} [c] \right) (5 A \operatorname{Cos} [c] - 4 i B \operatorname{Cos} [c] + 2 i A \operatorname{Sin} [c]) + \\
 & \quad \operatorname{Csc} [c] \operatorname{Csc} [c + d x] \left( \frac{\operatorname{Cos} [c]}{4} - \frac{1}{4} i \operatorname{Sin} [c] \right) (5 i A \operatorname{Sin} [d x] + 4 B \operatorname{Sin} [d x]) \Bigg) \\
 & \quad \left( a + i a \operatorname{Tan} [c + d x] \right)^{3/2} (A + B \operatorname{Tan} [c + d x]) \Bigg) / \\
 & \quad (d (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x]) (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]))
 \end{aligned}$$

**Problem 81: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot} [c + d x]^4 (a + i a \operatorname{Tan} [c + d x])^{3/2} (A + B \operatorname{Tan} [c + d x]) dx$$

Optimal (type 3, 213 leaves, 9 steps):

$$\begin{aligned}
 & \frac{a^{3/2} (23 i A + 22 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + i a \operatorname{Tan} [c + d x]}}{\sqrt{a}} \right]}{8 d} - \\
 & \frac{2 \sqrt{2} a^{3/2} (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + i a \operatorname{Tan} [c + d x]}}{\sqrt{2} \sqrt{a}} \right]}{d} + \frac{a (9 A - 10 i B) \operatorname{Cot} [c + d x] \sqrt{a + i a \operatorname{Tan} [c + d x]}}{8 d} - \\
 & \frac{a (7 i A + 6 B) \operatorname{Cot} [c + d x]^2 \sqrt{a + i a \operatorname{Tan} [c + d x]}}{12 d} - \frac{a A \operatorname{Cot} [c + d x]^3 \sqrt{a + i a \operatorname{Tan} [c + d x]}}{3 d}
 \end{aligned}$$

Result (type 3, 613 leaves):

$$\begin{aligned}
 & - \left( \left( i e^{-i c} \sqrt{e^{i d x}} \left( 128 (A - i B) \operatorname{ArcSinh} \left[ e^{i (c+d x)} \right] + \right. \right. \right. \\
 & \quad \sqrt{2} (23 A - 22 i B) \left( \operatorname{Log} \left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log} \left[ (1 + e^{i (c+d x)})^2 \right] + \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] \right) \right) \\
 & \quad \left( (a + i a \operatorname{Tan} [c + d x])^{3/2} (A + B \operatorname{Tan} [c + d x]) \right) / \left( 32 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Sec} [c + d x]^{5/2} (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^{3/2} \right. \\
 & \quad \left. (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right) \Bigg) + \\
 & \quad \frac{1}{d (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x]) (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x])} \\
 & \quad \operatorname{Cos} [c + d x]^2 \\
 & \quad \left( (7 A - 6 i B) \operatorname{Csc} [c] \left( \frac{\operatorname{Cos} [c]}{24} - \frac{1}{24} i \operatorname{Sin} [c] \right) (5 \operatorname{Cos} [c] + 2 i \operatorname{Sin} [c]) + \right. \\
 & \quad \operatorname{Csc} [c] \operatorname{Csc} [c + d x]^2 \left( \frac{\operatorname{Cos} [c]}{12} - \frac{1}{12} i \operatorname{Sin} [c] \right) (-4 A \operatorname{Cos} [c] - 7 i A \operatorname{Sin} [c] - 6 B \operatorname{Sin} [c]) + \\
 & \quad A \operatorname{Csc} [c] \operatorname{Csc} [c + d x]^3 \left( \frac{\operatorname{Cos} [c]}{3} - \frac{1}{3} i \operatorname{Sin} [c] \right) \operatorname{Sin} [d x] + \\
 & \quad \left. \operatorname{Csc} [c] \operatorname{Csc} [c + d x] \left( -\frac{5 \operatorname{Cos} [c]}{24} + \frac{5}{24} i \operatorname{Sin} [c] \right) (7 A \operatorname{Sin} [d x] - 6 i B \operatorname{Sin} [d x]) \right) \\
 & \quad (a + i a \operatorname{Tan} [c + d x])^{3/2} (A + B \operatorname{Tan} [c + d x])
 \end{aligned}$$

**Problem 85: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot} [c + d x] (a + i a \operatorname{Tan} [c + d x])^{5/2} (A + B \operatorname{Tan} [c + d x]) dx$$

Optimal (type 3, 147 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{2 a^{5/2} A \operatorname{ArcTanh} \left[ \frac{\sqrt{a + i a \operatorname{Tan} [c + d x]}}{\sqrt{a}} \right]}{d} + \frac{4 \sqrt{2} a^{5/2} (A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + i a \operatorname{Tan} [c + d x]}}{\sqrt{2} \sqrt{a}} \right]}{d} - \\
 & \frac{2 a^2 (A - 2 i B) \sqrt{a + i a \operatorname{Tan} [c + d x]}}{d} + \frac{2 i a B (a + i a \operatorname{Tan} [c + d x])^{3/2}}{3 d}
 \end{aligned}$$

Result (type 3, 429 leaves):

$$\left( e^{-2i c} \sqrt{e^{i d x}} \left( 8 (A - i B) \operatorname{ArcSinh}\left[e^{i(c+d x)}\right] + \sqrt{2} A \left( \operatorname{Log}\left[1 - e^{i(c+d x)}\right] - \operatorname{Log}\left[1 + e^{i(c+d x)}\right] + \operatorname{Log}\left[1 - e^{i(c+d x)} + \sqrt{2} \sqrt{1 + e^{2i(c+d x)}}\right] - \operatorname{Log}\left[1 + e^{i(c+d x)} + \sqrt{2} \sqrt{1 + e^{2i(c+d x)}}\right] \right) \right) \right) \\ \left( a + i a \operatorname{Tan}[c + d x] \right)^{5/2} (A + B \operatorname{Tan}[c + d x]) \Big/ \left( \sqrt{2} d \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2i(c+d x)}}} \sqrt{1 + e^{2i(c+d x)}} \right) \\ \operatorname{Sec}[c + d x]^{7/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{5/2} (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \Big) + \\ \left( \operatorname{Cos}[c + d x] \right)^3 \left( (3 A - 8 i B) \left( -\frac{2}{3} \operatorname{Cos}[2 c] + \frac{2}{3} i \operatorname{Sin}[2 c] \right) + \operatorname{Sec}[c + d x] \right. \\ \left. \left( -\frac{2}{3} i B \operatorname{Cos}[3 c + d x] - \frac{2}{3} B \operatorname{Sin}[3 c + d x] \right) \right) (a + i a \operatorname{Tan}[c + d x])^{5/2} (A + B \operatorname{Tan}[c + d x]) \Big/ \\ \left( d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right)$$

**Problem 86: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + d x]^2 (a + i a \operatorname{Tan}[c + d x])^{5/2} (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 158 leaves, 8 steps):

$$-\frac{a^{5/2} (5 i A + 2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a}}\right]}{d} + \frac{4 \sqrt{2} a^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} + \\ \frac{a^2 (i A - 2 B) \sqrt{a+i a \operatorname{Tan}[c+d x]}}{d} - \frac{a A \operatorname{Cot}[c+d x] (a+i a \operatorname{Tan}[c+d x])^{3/2}}{d}$$

Result (type 3, 512 leaves):

$$\begin{aligned}
 & \left( e^{-2i c} \sqrt{e^{i d x}} \left( 32 (i A + B) \operatorname{ArcSinh} \left[ e^{i (c+d x)} \right] + \right. \right. \\
 & \quad \sqrt{2} (5 i A + 2 B) \left( \operatorname{Log} \left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log} \left[ (1 + e^{i (c+d x)})^2 \right] + \right. \\
 & \quad \quad \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] - \\
 & \quad \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] \right) \right) \\
 & \left( a + i a \operatorname{Tan} [c + d x] \right)^{5/2} (A + B \operatorname{Tan} [c + d x]) \Bigg/ \left( 4 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Sec} [c + d x]^{7/2} (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^{5/2} \right. \\
 & \quad \left. (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right) + \\
 & \left( \operatorname{Cos} [c + d x]^3 (\operatorname{Csc} [c] (A \operatorname{Cos} [c] + 2 B \operatorname{Sin} [c]) (-\operatorname{Cos} [2 c] + i \operatorname{Sin} [2 c]) + \right. \\
 & \quad \left. A \operatorname{Csc} [c] \operatorname{Csc} [c + d x] (\operatorname{Cos} [2 c] - i \operatorname{Sin} [2 c]) \operatorname{Sin} [d x] \right) \\
 & \quad \left( a + i a \operatorname{Tan} [c + d x] \right)^{5/2} (A + B \operatorname{Tan} [c + d x]) \Bigg/ \\
 & \quad \left( d (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^2 (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right)
 \end{aligned}$$

**Problem 87: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot} [c + d x]^3 (a + i a \operatorname{Tan} [c + d x])^{5/2} (A + B \operatorname{Tan} [c + d x]) dx$$

Optimal (type 3, 173 leaves, 8 steps):

$$\frac{a^{5/2} (23 A - 20 i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a}} \right]}{4 d} - \frac{4 \sqrt{2} a^{5/2} (A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{2} \sqrt{a}} \right]}{d} - \frac{a^2 (7 i A + 4 B) \operatorname{Cot} [c + d x] \sqrt{a + i a \operatorname{Tan} [c + d x]}}{4 d} - \frac{a A \operatorname{Cot} [c + d x]^2 (a + i a \operatorname{Tan} [c + d x])^{3/2}}{2 d}$$

Result (type 3, 577 leaves):

$$\begin{aligned}
 & - \left( \left( e^{-2i c} \sqrt{e^{i d x}} \left( 128 (A - i B) \operatorname{ArcSinh} \left[ e^{i (c+d x)} \right] + \right. \right. \right. \\
 & \quad \sqrt{2} (23 A - 20 i B) \left( \operatorname{Log} \left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log} \left[ (1 + e^{i (c+d x)})^2 \right] + \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] \right) \right) \right) \\
 & \left( a + i a \operatorname{Tan} [c + d x] \right)^{5/2} (A + B \operatorname{Tan} [c + d x]) \Bigg/ \left( 16 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Sec} [c + d x]^{7/2} (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^{5/2} \right. \\
 & \quad \left. (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right) \Bigg) + \\
 & \left( \operatorname{Cos} [c + d x] \right)^3 \left( -i \operatorname{Csc} [c] (9 A \operatorname{Cos} [c] - 4 i B \operatorname{Cos} [c] + 2 i A \operatorname{Sin} [c]) \left( \frac{1}{4} \operatorname{Cos} [2 c] - \frac{1}{4} i \operatorname{Sin} [2 c] \right) + \right. \\
 & \quad \operatorname{Csc} [c + d x]^2 \left( -\frac{1}{2} A \operatorname{Cos} [2 c] + \frac{1}{2} i A \operatorname{Sin} [2 c] \right) + \\
 & \quad \left. \operatorname{Csc} [c] \operatorname{Csc} [c + d x] \left( \frac{1}{4} \operatorname{Cos} [2 c] - \frac{1}{4} i \operatorname{Sin} [2 c] \right) (9 i A \operatorname{Sin} [d x] + 4 B \operatorname{Sin} [d x]) \right) \Bigg) \\
 & \left( a + i a \operatorname{Tan} [c + d x] \right)^{5/2} (A + B \operatorname{Tan} [c + d x]) \Bigg/ \\
 & \left( d (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^2 (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right)
 \end{aligned}$$

**Problem 88: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot} [c + d x]^4 (a + i a \operatorname{Tan} [c + d x])^{5/2} (A + B \operatorname{Tan} [c + d x]) dx$$

Optimal (type 3, 217 leaves, 9 steps):

$$\begin{aligned}
 & \frac{a^{5/2} (45 i A + 46 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+i a \operatorname{Tan} [c+d x]}}{\sqrt{a}} \right]}{8 d} - \frac{4 \sqrt{2} a^{5/2} (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+i a \operatorname{Tan} [c+d x]}}{\sqrt{2} \sqrt{a}} \right]}{d} + \\
 & \frac{a^2 (19 A - 18 i B) \operatorname{Cot} [c + d x] \sqrt{a + i a \operatorname{Tan} [c + d x]}}{8 d} - \\
 & \frac{a^2 (3 i A + 2 B) \operatorname{Cot} [c + d x]^2 \sqrt{a + i a \operatorname{Tan} [c + d x]}}{4 d} - \frac{a A \operatorname{Cot} [c + d x]^3 (a + i a \operatorname{Tan} [c + d x])^{3/2}}{3 d}
 \end{aligned}$$

Result (type 3, 634 leaves):



$$\begin{aligned}
 & - \left( \left( i e^{-2 i c} \sqrt{e^{i d x}} \left( 256 (A - i B) \operatorname{ArcSinh} \left[ e^{i (c+d x)} \right] + \right. \right. \right. \\
 & \quad \sqrt{2} (45 A - 46 i B) \left( \operatorname{Log} \left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log} \left[ (1 + e^{i (c+d x)})^2 \right] + \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] \right) \right) \\
 & \quad \left( a + i a \operatorname{Tan} [c + d x] \right)^{5/2} (A + B \operatorname{Tan} [c + d x]) \Bigg/ \left( 32 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \right. \\
 & \quad \left. \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Sec} [c + d x]^{7/2} (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^{5/2} \right. \\
 & \quad \left. (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right) \Bigg) + \\
 & \quad \frac{1}{d (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^2 (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x])} \\
 & \quad \operatorname{Cos} [c + d x]^3 \\
 & \quad \left( \operatorname{Csc} [c] (65 A \operatorname{Cos} [c] - 54 i B \operatorname{Cos} [c] + 26 i A \operatorname{Sin} [c] + 12 B \operatorname{Sin} [c]) \right. \\
 & \quad \left. \left( \frac{1}{24} \operatorname{Cos} [2 c] - \frac{1}{24} i \operatorname{Sin} [2 c] \right) + \right. \\
 & \quad \operatorname{Csc} [c] \operatorname{Csc} [c + d x]^2 (-4 A \operatorname{Cos} [c] - 13 i A \operatorname{Sin} [c] - 6 B \operatorname{Sin} [c]) \left( \frac{1}{12} \operatorname{Cos} [2 c] - \frac{1}{12} i \operatorname{Sin} [2 c] \right) + \\
 & \quad A \operatorname{Csc} [c] \operatorname{Csc} [c + d x]^3 \left( \frac{1}{3} \operatorname{Cos} [2 c] - \frac{1}{3} i \operatorname{Sin} [2 c] \right) \operatorname{Sin} [d x] + \\
 & \quad \left. \operatorname{Csc} [c] \operatorname{Csc} [c + d x] \left( \frac{1}{24} \operatorname{Cos} [2 c] - \frac{1}{24} i \operatorname{Sin} [2 c] \right) (-65 A \operatorname{Sin} [d x] + 54 i B \operatorname{Sin} [d x]) \right) \\
 & \quad \left. (a + i a \operatorname{Tan} [c + d x])^{5/2} (A + B \operatorname{Tan} [c + d x]) \right)
 \end{aligned}$$

**Problem 89: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot} [c + d x]^5 (a + i a \operatorname{Tan} [c + d x])^{5/2} (A + B \operatorname{Tan} [c + d x]) dx$$

Optimal (type 3, 261 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{3 a^{5/2} (121 A - 120 i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a}}\right]}{64 d} + \frac{4 \sqrt{2} a^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} + \\
 & \frac{a^2 (149 i A + 152 B) \operatorname{Cot}[c+d x] \sqrt{a+i a \operatorname{Tan}[c+d x]}}{64 d} + \\
 & \frac{a^2 (107 A - 104 i B) \operatorname{Cot}[c+d x]^2 \sqrt{a+i a \operatorname{Tan}[c+d x]}}{96 d} - \\
 & \frac{a^2 (11 i A + 8 B) \operatorname{Cot}[c+d x]^3 \sqrt{a+i a \operatorname{Tan}[c+d x]}}{24 d} - \frac{a A \operatorname{Cot}[c+d x]^4 (a+i a \operatorname{Tan}[c+d x])^{3/2}}{4 d}
 \end{aligned}$$

Result (type 3, 698 leaves):

$$\begin{aligned}
 & \left( e^{-2 i c} \sqrt{e^{i d x}} \left( 2048 (A - i B) \operatorname{ArcSinh}\left[ e^{i (c+d x)} \right] + \right. \right. \\
 & \quad 3 \sqrt{2} (121 A - 120 i B) \left( \operatorname{Log}\left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log}\left[ (1 + e^{i (c+d x)})^2 \right] + \right. \\
 & \quad \left. \left. \operatorname{Log}\left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] \right) \right) \\
 & \left. \left( (a + i a \operatorname{Tan}[c+d x])^{5/2} (A + B \operatorname{Tan}[c+d x]) \right) \right) / \left( 256 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \right. \\
 & \left. \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Sec}[c+d x]^{7/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{5/2} \right. \\
 & \left. (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) \right) + \\
 & \frac{1}{d (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^2 (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) \operatorname{Cos}[c+d x]^3} \\
 & \left( \operatorname{Csc}[c] (583 i A \operatorname{Cos}[c] + 520 B \operatorname{Cos}[c] - 262 A \operatorname{Sin}[c] + 208 i B \operatorname{Sin}[c]) \right. \\
 & \quad \left( \frac{1}{192} \operatorname{Cos}[2 c] - \frac{1}{192} i \operatorname{Sin}[2 c] \right) + \operatorname{Csc}[c+d x]^4 \left( -\frac{1}{4} A \operatorname{Cos}[2 c] + \frac{1}{4} i A \operatorname{Sin}[2 c] \right) + \\
 & \quad \operatorname{Csc}[c] \operatorname{Csc}[c+d x]^2 (87 i A + 72 B - 223 i A \operatorname{Cos}[2 c] - 136 B \operatorname{Cos}[2 c] + \\
 & \quad 223 A \operatorname{Sin}[2 c] - 136 i B \operatorname{Sin}[2 c]) \left( \frac{1}{192} \operatorname{Cos}[3 c] - \frac{1}{192} i \operatorname{Sin}[3 c] \right) + \\
 & \quad \operatorname{Csc}[c] \operatorname{Csc}[c+d x] \left( \frac{1}{192} \operatorname{Cos}[2 c] - \frac{1}{192} i \operatorname{Sin}[2 c] \right) (-583 i A \operatorname{Sin}[d x] - 520 B \operatorname{Sin}[d x]) + \\
 & \quad \left. \operatorname{Csc}[c] \operatorname{Csc}[c+d x]^3 \left( \frac{1}{24} \operatorname{Cos}[2 c] - \frac{1}{24} i \operatorname{Sin}[2 c] \right) (17 i A \operatorname{Sin}[d x] + 8 B \operatorname{Sin}[d x]) \right) \\
 & (a + i a \operatorname{Tan}[c+d x])^{5/2} (A + B \operatorname{Tan}[c+d x])
 \end{aligned}$$

**Problem 94: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cot}[c + d x] (A + B \text{Tan}[c + d x])}{\sqrt{a + i a \text{Tan}[c + d x]}} dx$$

Optimal (type 3, 114 leaves, 7 steps):

$$-\frac{2 A \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{\sqrt{a} d} + \frac{(A - i B) \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{\sqrt{2} \sqrt{a} d} + \frac{A + i B}{d \sqrt{a + i a \text{Tan}[c + d x]}}$$

Result (type 3, 350 leaves):

$$\left( \left( A \sqrt{1 + e^{2 i (c+d x)}} + i B \sqrt{1 + e^{2 i (c+d x)}} + \right. \right. \\ \left. \left. (A - i B) e^{i (c+d x)} \text{ArcSinh}\left[e^{i (c+d x)}\right] + \sqrt{2} A e^{i (c+d x)} \text{Log}\left[1 - e^{i (c+d x)}\right] - \right. \right. \\ \left. \left. \sqrt{2} A e^{i (c+d x)} \text{Log}\left[1 + e^{i (c+d x)}\right] + \sqrt{2} A e^{i (c+d x)} \text{Log}\left[1 - e^{i (c+d x)} + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}}\right] - \right. \right. \\ \left. \left. \sqrt{2} A e^{i (c+d x)} \text{Log}\left[1 + e^{i (c+d x)} + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}}\right]\right) \sqrt{\text{Sec}[c + d x]} \right) / \\ \left( 2 d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \sqrt{\frac{a e^{2 i (c+d x)}}{1 + e^{2 i (c+d x)}}} \sqrt{1 + e^{2 i (c+d x)}} \right)$$

**Problem 95: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cot}[c + d x]^2 (A + B \text{Tan}[c + d x])}{\sqrt{a + i a \text{Tan}[c + d x]}} dx$$

Optimal (type 3, 167 leaves, 8 steps):

$$\frac{(i A - 2 B) \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{\sqrt{a} d} + \frac{(i A + B) \text{ArcTanh}\left[\frac{\sqrt{a+i a \text{Tan}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{\sqrt{2} \sqrt{a} d} + \\ \frac{(A + i B) \text{Cot}[c + d x]}{d \sqrt{a + i a \text{Tan}[c + d x]}} - \frac{(2 A + i B) \text{Cot}[c + d x] \sqrt{a + i a \text{Tan}[c + d x]}}{a d}$$

Result (type 3, 387 leaves):

$$\left( (B + A \operatorname{Cot}[c + d x]) \right. \\ \left. \left( \left( (-1 + e^{2i(c+dx)}) \left( 4(A - iB) \operatorname{ArcSinh}[e^{i(c+dx)}] - \sqrt{2}(A + 2iB) \left( \operatorname{Log}[(-1 + e^{i(c+dx)})^2] - \right. \right. \right. \right. \right. \right. \\ \left. \left. \left. \operatorname{Log}[(1 + e^{i(c+dx)})^2] + \operatorname{Log}[3 + 3e^{2i(c+dx)} + 2\sqrt{2}\sqrt{1 + e^{2i(c+dx)}} - 2 \right. \right. \right. \right. \\ \left. \left. \left. e^{i(c+dx)} \left( 1 + \sqrt{2}\sqrt{1 + e^{2i(c+dx)}} \right) \right] - \operatorname{Log}[3 + 3e^{2i(c+dx)} + 2\sqrt{2}\sqrt{1 + e^{2i(c+dx)}} + 2e^{i(c+dx)} \left( 1 + \sqrt{2}\sqrt{1 + e^{2i(c+dx)}} \right) \right] \right) \sqrt{\operatorname{Sec}[c + d x]} \right) / \\ \left. \left( \sqrt{2} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \sqrt{1 + e^{2i(c+dx)}} - 8(A \operatorname{Cos}[c + d x] + (2iA - B) \operatorname{Sin}[c + d x]) \right) \right) / \\ (8d(A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \\ \sqrt{a + ia \operatorname{Tan}[c + d x]})$$

**Problem 103: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^3 (A + B \operatorname{Tan}[c + d x])}{(a + ia \operatorname{Tan}[c + d x])^{3/2}} dx$$

Optimal (type 3, 268 leaves, 10 steps):

$$\frac{(23A + 12iB) \operatorname{ArcTanh}\left[\frac{\sqrt{a+ia \operatorname{Tan}[c+dx]}}{\sqrt{a}}\right] - (A - iB) \operatorname{ArcTanh}\left[\frac{\sqrt{a+ia \operatorname{Tan}[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{4a^{3/2}d} + \\ \frac{(A + iB) \operatorname{Cot}[c + d x]^2}{3d(a + ia \operatorname{Tan}[c + d x])^{3/2}} + \frac{(17A + 11iB) \operatorname{Cot}[c + d x]^2}{6ad\sqrt{a + ia \operatorname{Tan}[c + d x]}} + \\ \frac{7(3iA - 2B) \operatorname{Cot}[c + d x] \sqrt{a + ia \operatorname{Tan}[c + d x]}}{4a^2d} - \frac{(22A + 13iB) \operatorname{Cot}[c + d x]^2 \sqrt{a + ia \operatorname{Tan}[c + d x]}}{6a^2d}$$

Result (type 3, 755 leaves):

$$\begin{aligned}
 & - \left( e^{2 i c} \sqrt{e^{i d x}} \left( 8 (A - i B) \operatorname{ArcSinh} \left[ e^{i (c+d x)} \right] + \right. \right. \\
 & \quad \left. \sqrt{2} (23 A + 12 i B) \left( \operatorname{Log} \left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log} \left[ (1 + e^{i (c+d x)})^2 \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2 i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2 i (c+d x)}} \right) \right] \right) \right) \\
 & \quad \left. \left. \sqrt{\operatorname{Sec}[c+d x]} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{3/2} (A + B \operatorname{Tan}[c+d x]) \right) / \right. \\
 & \quad \left. \left( 16 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} \sqrt{1 + e^{2 i (c+d x)}} (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) \right. \right. \\
 & \quad \left. \left. (a + i a \operatorname{Tan}[c+d x])^{3/2} \right) \right) + \\
 & \quad \frac{1}{d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a + i a \operatorname{Tan}[c+d x])^{3/2}} \\
 & \quad \frac{\operatorname{Sec}[c+d x]}{(\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^2} \\
 & \quad \left( -\frac{1}{12} (23 A + 17 i B) \operatorname{Cos}[2 d x] + (A + i B) \operatorname{Cos}[4 d x] \left( -\frac{1}{12} \operatorname{Cos}[2 c] + \frac{1}{12} i \operatorname{Sin}[2 c] \right) + \right. \\
 & \quad \operatorname{Csc}[c] (21 i A \operatorname{Cos}[c] - 12 B \operatorname{Cos}[c] - 16 A \operatorname{Sin}[c] - 16 i B \operatorname{Sin}[c]) \\
 & \quad \left. \left( \frac{1}{12} \operatorname{Cos}[2 c] + \frac{1}{12} i \operatorname{Sin}[2 c] \right) + \operatorname{Csc}[c+d x]^2 \left( -\frac{1}{2} A \operatorname{Cos}[2 c] - \frac{1}{2} i A \operatorname{Sin}[2 c] \right) + \right. \\
 & \quad \frac{1}{12} i (23 A + 17 i B) \operatorname{Sin}[2 d x] + (A + i B) \left( \frac{1}{12} i \operatorname{Cos}[2 c] + \frac{1}{12} \operatorname{Sin}[2 c] \right) \operatorname{Sin}[4 d x] + \\
 & \quad \frac{1}{4} \operatorname{Csc}[c] \operatorname{Csc}[c+d x] \left( \frac{7}{2} A \operatorname{Cos}[2 c - d x] + 2 i B \operatorname{Cos}[2 c - d x] - \right. \\
 & \quad \left. \frac{7}{2} A \operatorname{Cos}[2 c + d x] - 2 i B \operatorname{Cos}[2 c + d x] + \frac{7}{2} i A \operatorname{Sin}[2 c - d x] - \right. \\
 & \quad \left. \left. 2 B \operatorname{Sin}[2 c - d x] - \frac{7}{2} i A \operatorname{Sin}[2 c + d x] + 2 B \operatorname{Sin}[2 c + d x] \right) \right) (A + B \operatorname{Tan}[c+d x])
 \end{aligned}$$

**Problem 109: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c+d x] (A + B \operatorname{Tan}[c+d x])}{(a + i a \operatorname{Tan}[c+d x])^{5/2}} dx$$

Optimal (type 3, 192 leaves, 9 steps):

$$-\frac{2 A \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{a}}\right]}{a^{5/2} d} + \frac{(A-i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+i a \operatorname{Tan}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{4 \sqrt{2} a^{5/2} d} + \frac{A+i B}{5 d (a+i a \operatorname{Tan}[c+d x])^{5/2}} + \frac{3 A+i B}{6 a d (a+i a \operatorname{Tan}[c+d x])^{3/2}} + \frac{7 A+i B}{4 a^2 d \sqrt{a+i a \operatorname{Tan}[c+d x]}}$$

Result (type 3, 580 leaves):

$$\left( e^{3 i c} \sqrt{e^{i d x}} \left( (A-i B) \operatorname{ArcSinh}\left[e^{i(c+d x)}\right] + 4 \sqrt{2} A \left( \operatorname{Log}\left[1-e^{i(c+d x)}\right] - \operatorname{Log}\left[1+e^{i(c+d x)}\right] + \operatorname{Log}\left[1-e^{i(c+d x)} + \sqrt{2} \sqrt{1+e^{2 i(c+d x)}}\right] - \operatorname{Log}\left[1+e^{i(c+d x)} + \sqrt{2} \sqrt{1+e^{2 i(c+d x)}}\right] \right) \right) \operatorname{Sec}[c+d x]^{3/2} (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{5/2} (A+B \operatorname{Tan}[c+d x]) \right) / \left( 4 \sqrt{2} d \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \sqrt{1+e^{2 i(c+d x)}} (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \operatorname{Tan}[c+d x])^{5/2} \right) + \frac{1}{d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+i a \operatorname{Tan}[c+d x])^{5/2} \operatorname{Sec}[c+d x]^2 (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3} \left( (12 A+7 i B) \operatorname{Cos}[4 d x] \left( \frac{\operatorname{Cos}[c]}{60} - \frac{1}{60} i \operatorname{Sin}[c] \right) + (72 A+17 i B) \operatorname{Cos}[2 d x] \left( \frac{\operatorname{Cos}[c]}{60} + \frac{1}{60} i \operatorname{Sin}[c] \right) + (123 A+23 i B) \left( \frac{1}{120} \operatorname{Cos}[3 c] + \frac{1}{120} i \operatorname{Sin}[3 c] \right) + (A+i B) \operatorname{Cos}[6 d x] \left( \frac{1}{40} \operatorname{Cos}[3 c] - \frac{1}{40} i \operatorname{Sin}[3 c] \right) + (-72 i A+17 B) \left( \frac{\operatorname{Cos}[c]}{60} + \frac{1}{60} i \operatorname{Sin}[c] \right) \operatorname{Sin}[2 d x] + (-12 i A+7 B) \left( \frac{\operatorname{Cos}[c]}{60} - \frac{1}{60} i \operatorname{Sin}[c] \right) \operatorname{Sin}[4 d x] + (-i A+B) \left( \frac{1}{40} \operatorname{Cos}[3 c] - \frac{1}{40} i \operatorname{Sin}[3 c] \right) \operatorname{Sin}[6 d x] \right) (A+B \operatorname{Tan}[c+d x])$$

**Problem 110: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c+d x]^2 (A+B \operatorname{Tan}[c+d x])}{(a+i a \operatorname{Tan}[c+d x])^{5/2}} dx$$

Optimal (type 3, 259 leaves, 10 steps):

$$\frac{(5iA - 2B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+ia \tan[c+dx]}}{\sqrt{a}}\right]}{a^{5/2} d} + \frac{(iA + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+ia \tan[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{4\sqrt{2} a^{5/2} d} +$$

$$\frac{(A + iB) \operatorname{Cot}[c + dx]}{5d (a + ia \tan[c + dx])^{5/2}} + \frac{(19A + 9iB) \operatorname{Cot}[c + dx]}{30ad (a + ia \tan[c + dx])^{3/2}} +$$

$$\frac{(41A + 15iB) \operatorname{Cot}[c + dx]}{12a^2 d \sqrt{a + ia \tan[c + dx]}} - \frac{7(3A + iB) \operatorname{Cot}[c + dx] \sqrt{a + ia \tan[c + dx]}}{4a^3 d}$$

Result (type 3, 748 leaves):

$$\left( e^{3ic} \sqrt{e^{id x}} \right. \\
 \left. \left( (iA + B) \operatorname{ArcSinh}\left[e^{i(c+dx)}\right] + \sqrt{2}(-5iA + 2B) \left( \operatorname{Log}\left[(-1 + e^{i(c+dx)})^2\right] - \operatorname{Log}\left[(1 + e^{i(c+dx)})^2\right] + \right. \right. \right. \\
 \left. \left. \operatorname{Log}\left[3 + 3e^{2i(c+dx)} + 2\sqrt{2}\sqrt{1 + e^{2i(c+dx)}} - 2e^{i(c+dx)}\left(1 + \sqrt{2}\sqrt{1 + e^{2i(c+dx)}}\right)\right] - \right. \right. \\
 \left. \left. \operatorname{Log}\left[3 + 3e^{2i(c+dx)} + 2\sqrt{2}\sqrt{1 + e^{2i(c+dx)}} + 2e^{i(c+dx)}\left(1 + \sqrt{2}\sqrt{1 + e^{2i(c+dx)}}\right)\right] \right) \right) \\
 \left. \operatorname{Sec}[c + dx]^{3/2} (\cos[dx] + i \sin[dx])^{5/2} (A + B \tan[c + dx]) \right) / \\
 \left( 4\sqrt{2} d \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \sqrt{1 + e^{2i(c+dx)}} (A \cos[c + dx] + B \sin[c + dx]) \right. \\
 \left. (a + ia \tan[c + dx])^{5/2} \right) + \\
 \frac{1}{d (A \cos[c + dx] + B \sin[c + dx]) (a + ia \tan[c + dx])^{5/2} \operatorname{Sec}[c + dx]^2 (\cos[dx] + i \sin[dx])^3} \\
 \left( (-17iA + 12B) \cos[4dx] \left( \frac{\cos[c]}{60} - \frac{1}{60} i \sin[c] \right) + \right. \\
 (-157iA + 72B) \cos[2dx] \left( \frac{\cos[c]}{60} + \frac{1}{60} i \sin[c] \right) + \\
 \operatorname{Csc}[c] (120A \cos[c] + 283iA \sin[c] - 123B \sin[c]) \left( -\frac{1}{120} \cos[3c] - \frac{1}{120} i \sin[3c] \right) + \\
 (-iA + B) \cos[6dx] \left( \frac{1}{40} \cos[3c] - \frac{1}{40} i \sin[3c] \right) + \\
 (157A + 72iB) \left( -\frac{\cos[c]}{60} - \frac{1}{60} i \sin[c] \right) \sin[2dx] + \\
 (17A + 12iB) \left( -\frac{\cos[c]}{60} + \frac{1}{60} i \sin[c] \right) \sin[4dx] + (A + iB) \\
 \left( -\frac{1}{40} \cos[3c] + \frac{1}{40} i \sin[3c] \right) \sin[6dx] + \operatorname{Csc}[c] \operatorname{Csc}[c + dx] \left( \frac{1}{2} i A \cos[3c - dx] - \right. \\
 \left. \frac{1}{2} i A \cos[3c + dx] - \frac{1}{2} A \sin[3c - dx] + \frac{1}{2} A \sin[3c + dx] \right) \left. \right) (A + B \tan[c + dx])$$

### Problem 111: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^3 (A + B \text{Tan}[c + d x])}{(a + i a \text{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 312 leaves, 11 steps):

$$\begin{aligned} & \frac{(43 A + 20 i B) \text{ArcTanh}\left[\frac{\sqrt{a + i a \text{Tan}[c + d x]}}{\sqrt{a}}\right]}{4 a^{5/2} d} - \frac{(A - i B) \text{ArcTanh}\left[\frac{\sqrt{a + i a \text{Tan}[c + d x]}}{\sqrt{2} \sqrt{a}}\right]}{4 \sqrt{2} a^{5/2} d} + \\ & \frac{(A + i B) \text{Cot}[c + d x]^2}{5 d (a + i a \text{Tan}[c + d x])^{5/2}} + \frac{(23 A + 13 i B) \text{Cot}[c + d x]^2}{30 a d (a + i a \text{Tan}[c + d x])^{3/2}} + \frac{(337 A + 167 i B) \text{Cot}[c + d x]^2}{60 a^2 d \sqrt{a + i a \text{Tan}[c + d x]}} + \\ & \frac{21 (2 i A - B) \text{Cot}[c + d x] \sqrt{a + i a \text{Tan}[c + d x]}}{4 a^3 d} - \frac{(85 A + 41 i B) \text{Cot}[c + d x]^2 \sqrt{a + i a \text{Tan}[c + d x]}}{12 a^3 d} \end{aligned}$$

Result (type 3, 839 leaves):



$$\begin{aligned}
 & - \left( e^{3i c} \sqrt{e^{i d x}} \left( 4 (A - i B) \operatorname{ArcSinh} \left[ e^{i (c+d x)} \right] + \right. \right. \\
 & \quad \sqrt{2} (43 A + 20 i B) \left( \operatorname{Log} \left[ (-1 + e^{i (c+d x)})^2 \right] - \operatorname{Log} \left[ (1 + e^{i (c+d x)})^2 \right] + \right. \\
 & \quad \left. \operatorname{Log} \left[ 3 + 3 e^{2i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2i (c+d x)}} - 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2i (c+d x)}} \right) \right] - \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ 3 + 3 e^{2i (c+d x)} + 2 \sqrt{2} \sqrt{1 + e^{2i (c+d x)}} + 2 e^{i (c+d x)} \left( 1 + \sqrt{2} \sqrt{1 + e^{2i (c+d x)}} \right) \right] \right) \right) \\
 & \quad \operatorname{Sec} [c + d x]^{3/2} (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^{5/2} (A + B \operatorname{Tan} [c + d x]) \Big/ \\
 & \quad \left( 16 \sqrt{2} d \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2i (c+d x)}}} \sqrt{1 + e^{2i (c+d x)}} (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right. \\
 & \quad \left. (a + i a \operatorname{Tan} [c + d x])^{5/2} \right) \Bigg) + \\
 & \quad \frac{1}{d (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) (a + i a \operatorname{Tan} [c + d x])^{5/2}} \\
 & \quad \operatorname{Sec} [c + d x]^2 \\
 & \quad (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^3 \\
 & \quad \left( (272 A + 157 i B) \operatorname{Cos} [2 d x] \left( -\frac{\operatorname{Cos} [c]}{60} - \frac{1}{60} i \operatorname{Sin} [c] \right) + \right. \\
 & \quad (22 A + 17 i B) \operatorname{Cos} [4 d x] \left( -\frac{\operatorname{Cos} [c]}{60} + \frac{1}{60} i \operatorname{Sin} [c] \right) + \\
 & \quad \operatorname{Csc} [c] (330 i A \operatorname{Cos} [c] - 120 B \operatorname{Cos} [c] - 443 A \operatorname{Sin} [c] - 283 i B \operatorname{Sin} [c]) \\
 & \quad \left( \frac{1}{120} \operatorname{Cos} [3 c] + \frac{1}{120} i \operatorname{Sin} [3 c] \right) + (A + i B) \operatorname{Cos} [6 d x] \left( -\frac{1}{40} \operatorname{Cos} [3 c] + \frac{1}{40} i \operatorname{Sin} [3 c] \right) + \\
 & \quad \operatorname{Csc} [c + d x]^2 \left( -\frac{1}{2} A \operatorname{Cos} [3 c] - \frac{1}{2} i A \operatorname{Sin} [3 c] \right) + \\
 & \quad (272 A + 157 i B) \left( \frac{1}{60} i \operatorname{Cos} [c] - \frac{\operatorname{Sin} [c]}{60} \right) \operatorname{Sin} [2 d x] + \\
 & \quad (22 A + 17 i B) \left( \frac{1}{60} i \operatorname{Cos} [c] + \frac{\operatorname{Sin} [c]}{60} \right) \operatorname{Sin} [4 d x] + \\
 & \quad (A + i B) \left( \frac{1}{40} i \operatorname{Cos} [3 c] + \frac{1}{40} \operatorname{Sin} [3 c] \right) \operatorname{Sin} [6 d x] + \\
 & \quad \frac{1}{4} \operatorname{Csc} [c] \operatorname{Csc} [c + d x] \left( \frac{11}{2} A \operatorname{Cos} [3 c - d x] + 2 i B \operatorname{Cos} [3 c - d x] - \right. \\
 & \quad \frac{11}{2} A \operatorname{Cos} [3 c + d x] - 2 i B \operatorname{Cos} [3 c + d x] + \frac{11}{2} i A \operatorname{Sin} [3 c - d x] - \\
 & \quad \left. \left. 2 B \operatorname{Sin} [3 c - d x] - \frac{11}{2} i A \operatorname{Sin} [3 c + d x] + 2 B \operatorname{Sin} [3 c + d x] \right) \right) (A + B \operatorname{Tan} [c + d x])
 \end{aligned}$$

### Problem 112: Result more than twice size of optimal antiderivative.

$$\int \tan[c + dx]^{5/2} (a + i a \tan[c + dx]) (A + B \tan[c + dx]) dx$$

Optimal (type 3, 130 leaves, 6 steps):

$$\frac{2 (-1)^{1/4} a (i A + B) \operatorname{ArcTan}\left[(-1)^{3/4} \sqrt{\tan[c + dx]}\right]}{d} - \frac{2 a (i A + B) \sqrt{\tan[c + dx]}}{d} + \frac{2 a (A - i B) \tan[c + dx]^{3/2}}{3 d} + \frac{2 a (i A + B) \tan[c + dx]^{5/2}}{5 d} + \frac{2 i a B \tan[c + dx]^{7/2}}{7 d}$$

Result (type 3, 366 leaves):

$$\frac{1}{d (\cos[dx] + i \sin[dx]) (A \cos[c + dx] + B \sin[c + dx])} \cos[c + dx]^2 \left( \sec[c] \sec[c + dx]^2 \left( \frac{2 \cos[c]}{35} - \frac{2}{35} i \sin[c] \right) (7 i A \cos[c] + 7 B \cos[c] + 5 i B \sin[c]) + \sec[c] \left( -\frac{2}{105} i \cos[c] - \frac{2 \sin[c]}{105} \right) (126 A \cos[c] - 126 i B \cos[c] + 35 i A \sin[c] + 50 B \sin[c]) + i B \sec[c] \sec[c + dx]^3 \left( \frac{2 \cos[c]}{7} - \frac{2}{7} i \sin[c] \right) \sin[dx] + \sec[c] \sec[c + dx] \left( \frac{2 \cos[c]}{21} - \frac{2}{21} i \sin[c] \right) (7 A \sin[dx] - 10 i B \sin[dx]) \right) \sqrt{\tan[c + dx]} (a + i a \tan[c + dx]) (A + B \tan[c + dx]) + \left( (A - i B) \operatorname{ArcCosh}\left[e^{2 i (c + dx)}\right] \cos[c + dx]^2 (i \cos[c] + \sin[c]) \sqrt{\tan[c + dx]} (a + i a \tan[c + dx]) (A + B \tan[c + dx]) \right) / \left( d (\cos[dx] + i \sin[dx]) (A \cos[c + dx] + B \sin[c + dx]) \sqrt{i \tan[c + dx]} \right)$$

### Problem 118: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan[c + dx]) (A + B \tan[c + dx])}{\tan[c + dx]^{7/2}} dx$$

Optimal (type 3, 103 leaves, 5 steps):

$$\frac{2 (-1)^{1/4} a (i A + B) \operatorname{ArcTan}\left[(-1)^{3/4} \sqrt{\tan[c + dx]}\right]}{d} - \frac{2 a A}{5 d \tan[c + dx]^{5/2}} - \frac{2 a (i A + B)}{3 d \tan[c + dx]^{3/2}} + \frac{2 a (A - i B)}{d \sqrt{\tan[c + dx]}}$$

Result (type 3, 363 leaves):

$$\begin{aligned}
 & \frac{1}{d (\cos [d x] + i \sin [d x]) (A \cos [c + d x] + B \sin [c + d x])} \cos [c + d x]^2 \\
 & \left( \csc [c] \csc [c + d x]^2 \left( -\frac{2 \cos [c]}{15} + \frac{2}{15} i \sin [c] \right) (3 A \cos [c] + 5 i A \sin [c] + 5 B \sin [c]) + \right. \\
 & \quad \csc [c] \left( \frac{2 \cos [c]}{15} - \frac{2}{15} i \sin [c] \right) (18 A \cos [c] - 15 i B \cos [c] + 5 i A \sin [c] + 5 B \sin [c]) + \\
 & \quad A \csc [c] \csc [c + d x]^3 \left( \frac{2 \cos [c]}{5} - \frac{2}{5} i \sin [c] \right) \sin [d x] + \\
 & \quad \left. \csc [c] \csc [c + d x] \left( -\frac{2 \cos [c]}{5} + \frac{2}{5} i \sin [c] \right) (6 A \sin [d x] - 5 i B \sin [d x]) \right) \\
 & \sqrt{\tan [c + d x]} (a + i a \tan [c + d x]) (A + B \tan [c + d x]) + \\
 & \left( (A - i B) \operatorname{ArcCosh} \left[ e^{2 i (c + d x)} \right] \cos [c + d x]^2 (-i \cos [c] - \sin [c]) \right. \\
 & \quad \left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x]) (A + B \tan [c + d x]) \right) / \\
 & \left( d (\cos [d x] + i \sin [d x]) (A \cos [c + d x] + B \sin [c + d x]) \sqrt{i \tan [c + d x]} \right)
 \end{aligned}$$

**Problem 119: Result more than twice size of optimal antiderivative.**

$$\int \tan [c + d x]^{5/2} (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 183 leaves, 7 steps):

$$\begin{aligned}
 & \frac{4 (-1)^{1/4} a^2 (i A + B) \operatorname{ArcTan} \left[ (-1)^{3/4} \sqrt{\tan [c + d x]} \right]}{d} \\
 & \frac{4 a^2 (i A + B) \sqrt{\tan [c + d x]}}{d} + \frac{4 a^2 (A - i B) \tan [c + d x]^{3/2}}{3 d} + \frac{4 a^2 (i A + B) \tan [c + d x]^{5/2}}{5 d} \\
 & \frac{2 a^2 (9 A - 11 i B) \tan [c + d x]^{7/2}}{63 d} + \frac{2 i B \tan [c + d x]^{7/2} (a^2 + i a^2 \tan [c + d x])}{9 d}
 \end{aligned}$$

Result (type 3, 434 leaves):

$$\frac{1}{d \left( \cos [d x] + i \sin [d x] \right)^2 \left( A \cos [c + d x] + B \sin [c + d x] \right)}$$

$$\cos [c + d x]^3 \left( \sec [c] \left( 756 A \cos [c] - 791 i B \cos [c] + 255 i A \sin [c] + 300 B \sin [c] \right) \right.$$

$$\left. \left( -\frac{2}{315} i \cos [2 c] - \frac{2}{315} \sin [2 c] \right) + \right.$$

$$\sec [c] \sec [c + d x]^2 \left( 126 i A \cos [c] + 196 B \cos [c] - 45 A \sin [c] + 90 i B \sin [c] \right)$$

$$\left. \left( \frac{2}{315} \cos [2 c] - \frac{2}{315} i \sin [2 c] \right) + \sec [c + d x]^4 \left( -\frac{2}{9} B \cos [2 c] + \frac{2}{9} i B \sin [2 c] \right) + \right.$$

$$\sec [c] \sec [c + d x]^3 \left( -\frac{2}{7} \cos [2 c] + \frac{2}{7} i \sin [2 c] \right) \left( A \sin [d x] - 2 i B \sin [d x] \right) +$$

$$\left. \sec [c] \sec [c + d x] \left( \frac{2}{21} \cos [2 c] - \frac{2}{21} i \sin [2 c] \right) \left( 17 A \sin [d x] - 20 i B \sin [d x] \right) \right)$$

$$\sqrt{\tan [c + d x]} \left( a + i a \tan [c + d x] \right)^2 \left( A + B \tan [c + d x] \right) +$$

$$\left( 2 \left( A - i B \right) \operatorname{ArcCosh} \left[ e^{2 i (c+d x)} \right] \cos [c + d x]^3 \left( i \cos [2 c] + \sin [2 c] \right) \right.$$

$$\left. \sqrt{\tan [c + d x]} \left( a + i a \tan [c + d x] \right)^2 \left( A + B \tan [c + d x] \right) \right) /$$

$$\left( d \left( \cos [d x] + i \sin [d x] \right)^2 \left( A \cos [c + d x] + B \sin [c + d x] \right) \sqrt{i \tan [c + d x]} \right)$$

**Problem 120: Result more than twice size of optimal antiderivative.**

$$\int \tan [c + d x]^{3/2} \left( a + i a \tan [c + d x] \right)^2 \left( A + B \tan [c + d x] \right) dx$$

Optimal (type 3, 156 leaves, 6 steps):

$$\frac{4 (-1)^{1/4} a^2 (A - i B) \operatorname{ArcTan} \left[ (-1)^{3/4} \sqrt{\tan [c + d x]} \right]}{d} +$$

$$\frac{4 a^2 (A - i B) \sqrt{\tan [c + d x]}}{d} + \frac{4 a^2 (i A + B) \tan [c + d x]^{3/2}}{3 d} -$$

$$\frac{2 a^2 (7 A - 9 i B) \tan [c + d x]^{5/2}}{35 d} + \frac{2 i B \tan [c + d x]^{5/2} \left( a^2 + i a^2 \tan [c + d x] \right)}{7 d}$$

Result (type 3, 386 leaves):

$$\begin{aligned}
 & \left( 2 (A - i B) \operatorname{ArcCosh} \left[ e^{2 i (c+d x)} \right] \operatorname{Cos} [c+d x]^3 \right. \\
 & \quad \left. (i \operatorname{Cos} [2 c] + \operatorname{Sin} [2 c]) \sqrt{i \operatorname{Tan} [c+d x]} (a + i a \operatorname{Tan} [c+d x])^2 (A + B \operatorname{Tan} [c+d x]) \right) / \\
 & \quad \left( d (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^2 (A \operatorname{Cos} [c+d x] + B \operatorname{Sin} [c+d x]) \sqrt{\operatorname{Tan} [c+d x]} \right) + \\
 & \quad \frac{1}{d (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^2 (A \operatorname{Cos} [c+d x] + B \operatorname{Sin} [c+d x])} \\
 & \quad \operatorname{Cos} [c+d x]^3 \left( \operatorname{Sec} [c] (231 A \operatorname{Cos} [c] - 252 i B \operatorname{Cos} [c] + 70 i A \operatorname{Sin} [c] + 85 B \operatorname{Sin} [c]) \right. \\
 & \quad \left. \left( \frac{2}{105} \operatorname{Cos} [2 c] - \frac{2}{105} i \operatorname{Sin} [2 c] \right) + \right. \\
 & \quad \operatorname{Sec} [c] \operatorname{Sec} [c+d x]^2 (7 A \operatorname{Cos} [c] - 14 i B \operatorname{Cos} [c] + 5 B \operatorname{Sin} [c]) \left( -\frac{2}{35} \operatorname{Cos} [2 c] + \frac{2}{35} i \operatorname{Sin} [2 c] \right) + \\
 & \quad B \operatorname{Sec} [c] \operatorname{Sec} [c+d x]^3 \left( -\frac{2}{7} \operatorname{Cos} [2 c] + \frac{2}{7} i \operatorname{Sin} [2 c] \right) \operatorname{Sin} [d x] + \\
 & \quad \left. \operatorname{Sec} [c] \operatorname{Sec} [c+d x] \left( \frac{2}{21} \operatorname{Cos} [2 c] - \frac{2}{21} i \operatorname{Sin} [2 c] \right) (14 i A \operatorname{Sin} [d x] + 17 B \operatorname{Sin} [d x]) \right) \\
 & \quad \sqrt{\operatorname{Tan} [c+d x]} (a + i a \operatorname{Tan} [c+d x])^2 (A + B \operatorname{Tan} [c+d x])
 \end{aligned}$$

**Problem 125: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \operatorname{Tan} [c+d x])^2 (A + B \operatorname{Tan} [c+d x])}{\operatorname{Tan} [c+d x]^{7/2}} dx$$

Optimal (type 3, 127 leaves, 5 steps):

$$\frac{4 (-1)^{1/4} a^2 (i A + B) \operatorname{ArcTan} \left[ (-1)^{3/4} \sqrt{\operatorname{Tan} [c+d x]} \right]}{d} - \frac{2 a^2 (7 i A + 5 B)}{15 d \operatorname{Tan} [c+d x]^{3/2}} + \frac{4 a^2 (A - i B)}{d \sqrt{\operatorname{Tan} [c+d x]}} - \frac{2 A (a^2 + i a^2 \operatorname{Tan} [c+d x])}{5 d \operatorname{Tan} [c+d x]^{5/2}}$$

Result (type 3, 386 leaves):

$$\begin{aligned}
& \frac{1}{d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x])} \\
& \cos [c + d x]^3 \left( \csc [c] (33 A \cos [c] - 30 i B \cos [c] + 10 i A \sin [c] + 5 B \sin [c]) \right. \\
& \quad \left. \left( \frac{2}{15} \cos [2 c] - \frac{2}{15} i \sin [2 c] \right) + \right. \\
& \quad \csc [c] \csc [c + d x]^2 (3 A \cos [c] + 10 i A \sin [c] + 5 B \sin [c]) \left( -\frac{2}{15} \cos [2 c] + \frac{2}{15} i \sin [2 c] \right) + \\
& \quad A \csc [c] \csc [c + d x]^3 \left( \frac{2}{5} \cos [2 c] - \frac{2}{5} i \sin [2 c] \right) \sin [d x] + \\
& \quad \left. \csc [c] \csc [c + d x] \left( -\frac{2}{5} \cos [2 c] + \frac{2}{5} i \sin [2 c] \right) (11 A \sin [d x] - 10 i B \sin [d x]) \right) \\
& \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) + \\
& \left( 2 (A - i B) \operatorname{ArcCosh} [e^{2 i (c+d x)}] \cos [c + d x]^3 (\cos [2 c] - i \sin [2 c]) \right. \\
& \quad \left. \tan [c + d x]^{3/2} (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) \right) / \\
& \left( d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x]) (i \tan [c + d x])^{3/2} \right)
\end{aligned}$$

**Problem 126: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [c + d x])^2 (A + B \tan [c + d x])}{\tan [c + d x]^{9/2}} dx$$

Optimal (type 3, 154 leaves, 6 steps):

$$\begin{aligned}
& -\frac{4 (-1)^{1/4} a^2 (A - i B) \operatorname{ArcTan} [(-1)^{3/4} \sqrt{\tan [c + d x]}]}{d} - \frac{2 a^2 (9 i A + 7 B)}{35 d \tan [c + d x]^{5/2}} + \\
& \frac{4 a^2 (A - i B)}{3 d \tan [c + d x]^{3/2}} + \frac{4 a^2 (i A + B)}{d \sqrt{\tan [c + d x]}} - \frac{2 A (a^2 + i a^2 \tan [c + d x])}{7 d \tan [c + d x]^{7/2}}
\end{aligned}$$

Result (type 3, 434 leaves):

$$\begin{aligned}
 & \frac{1}{d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x])} \\
 & \cos [c + d x]^3 \left( \csc [c] \csc [c + d x]^2 (-42 i A \cos [c] - 21 B \cos [c] + 100 A \sin [c] - 70 i B \sin [c]) \right. \\
 & \quad \left. \left( \frac{2}{105} \cos [2 c] - \frac{2}{105} i \sin [2 c] \right) + \right. \\
 & \quad \csc [c] (252 i A \cos [c] + 231 B \cos [c] - 85 A \sin [c] + 70 i B \sin [c]) \\
 & \quad \left. \left( \frac{2}{105} \cos [2 c] - \frac{2}{105} i \sin [2 c] \right) + \csc [c + d x]^4 \left( -\frac{2}{7} A \cos [2 c] + \frac{2}{7} i A \sin [2 c] \right) + \right. \\
 & \quad \csc [c] \csc [c + d x] \left( \frac{2}{5} \cos [2 c] - \frac{2}{5} i \sin [2 c] \right) (-12 i A \sin [d x] - 11 B \sin [d x]) + \\
 & \quad \left. \csc [c] \csc [c + d x]^3 \left( \frac{2}{5} \cos [2 c] - \frac{2}{5} i \sin [2 c] \right) (2 i A \sin [d x] + B \sin [d x]) \right) \\
 & \quad \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) + \\
 & \quad \left( 2 (A - i B) \operatorname{ArcCosh} [e^{2 i (c+d x)}] \cos [c + d x]^3 (\cos [2 c] - i \sin [2 c]) \right. \\
 & \quad \left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) \right) / \\
 & \quad \left( d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \sqrt{i \tan [c + d x]} \right)
 \end{aligned}$$

### Problem 127: Result more than twice size of optimal antiderivative.

$$\int \tan [c + d x]^{3/2} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 198 leaves, 7 steps):

$$\begin{aligned}
 & \frac{8 (-1)^{1/4} a^3 (A - i B) \operatorname{ArcTan} [(-1)^{3/4} \sqrt{\tan [c + d x]}]}{d} + \frac{8 a^3 (A - i B) \sqrt{\tan [c + d x]}}{d} + \\
 & \frac{8 a^3 (i A + B) \tan [c + d x]^{3/2}}{3 d} - \frac{16 a^3 (18 A - 19 i B) \tan [c + d x]^{5/2}}{315 d} + \\
 & \frac{2 i a B \tan [c + d x]^{5/2} (a + i a \tan [c + d x])^2}{9 d} - \frac{2 (9 A - 13 i B) \tan [c + d x]^{5/2} (a^3 + i a^3 \tan [c + d x])}{63 d}
 \end{aligned}$$

Result (type 3, 435 leaves):

$$\begin{aligned}
& \frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])} \\
& \cos [c + d x]^4 \left( \sec [c] (1449 A \cos [c] - 1547 i B \cos [c] + 465 i A \sin [c] + 555 B \sin [c]) \right. \\
& \quad \left. \left( \frac{2}{315} \cos [3 c] - \frac{2}{315} i \sin [3 c] \right) + \right. \\
& \quad \sec [c] \sec [c + d x]^2 (189 A \cos [c] - 322 i B \cos [c] + 45 i A \sin [c] + 135 B \sin [c]) \\
& \quad \left. \left( -\frac{2}{315} \cos [3 c] + \frac{2}{315} i \sin [3 c] \right) + \sec [c + d x]^4 \left( -\frac{2}{9} i B \cos [3 c] - \frac{2}{9} B \sin [3 c] \right) + \right. \\
& \quad \sec [c] \sec [c + d x]^3 \left( \frac{2}{7} \cos [3 c] - \frac{2}{7} i \sin [3 c] \right) (-i A \sin [d x] - 3 B \sin [d x]) + \\
& \quad \left. \sec [c] \sec [c + d x] \left( \frac{2}{21} \cos [3 c] - \frac{2}{21} i \sin [3 c] \right) (31 i A \sin [d x] + 37 B \sin [d x]) \right) \\
& \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) - \\
& \left( 4 (A - i B) \operatorname{ArcCosh} \left[ e^{2 i (c + d x)} \right] \cos [c + d x]^4 (\cos [3 c] - i \sin [3 c]) \right. \\
& \quad \left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\
& \left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \sqrt{i \tan [c + d x]} \right)
\end{aligned}$$

### Problem 128: Result more than twice size of optimal antiderivative.

$$\int \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 171 leaves, 6 steps):

$$\begin{aligned}
& \frac{8 (-1)^{1/4} a^3 (i A + B) \operatorname{ArcTan} \left[ (-1)^{3/4} \sqrt{\tan [c + d x]} \right]}{d} + \\
& \frac{8 a^3 (i A + B) \sqrt{\tan [c + d x]}}{d} - \frac{8 a^3 (21 A - 23 i B) \tan [c + d x]^{3/2}}{105 d} + \\
& \frac{2 i a B \tan [c + d x]^{3/2} (a + i a \tan [c + d x])^2}{7 d} - \frac{2 (7 A - 11 i B) \tan [c + d x]^{3/2} (a^3 + i a^3 \tan [c + d x])}{35 d}
\end{aligned}$$

Result (type 3, 389 leaves):



$$\frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])} \cos [c + d x]^4$$

$$\left( \sec [c] \sec [c + d x]^2 (7 A \cos [c] - 21 i B \cos [c] + 5 B \sin [c]) \left( -\frac{2}{35} i \cos [3 c] - \frac{2}{35} \sin [3 c] \right) + \right.$$

$$\sec [c] (441 i A \cos [c] + 483 B \cos [c] - 105 A \sin [c] + 155 i B \sin [c])$$

$$\left. \left( \frac{2}{105} \cos [3 c] - \frac{2}{105} i \sin [3 c] \right) - \right.$$

$$i B \sec [c] \sec [c + d x]^3 \left( \frac{2}{7} \cos [3 c] - \frac{2}{7} i \sin [3 c] \right) \sin [d x] +$$

$$\left. \sec [c] \sec [c + d x] \left( -\frac{2}{21} \cos [3 c] + \frac{2}{21} i \sin [3 c] \right) (21 A \sin [d x] - 31 i B \sin [d x]) \right)$$

$$\sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) +$$

$$\left( 4 (A - i B) \operatorname{ArcCosh} [e^{2 i (c+d x)}] \cos [c + d x]^4 (\cos [3 c] - i \sin [3 c]) \right.$$

$$\left. \tan [c + d x]^{3/2} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) /$$

$$\left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) (i \tan [c + d x])^{3/2} \right)$$

**Problem 129: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [c + d x])^3 (A + B \tan [c + d x])}{\sqrt{\tan [c + d x]}} dx$$

Optimal (type 3, 146 leaves, 5 steps):

$$\frac{8 (-1)^{1/4} a^3 (A - i B) \operatorname{ArcTan} [(-1)^{3/4} \sqrt{\tan [c + d x]}]}{d} - \frac{16 a^3 (5 A - 6 i B) \sqrt{\tan [c + d x]}}{15 d} +$$

$$\frac{2 i a B \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^2}{5 d} - \frac{2 (5 A - 9 i B) \sqrt{\tan [c + d x]} (a^3 + i a^3 \tan [c + d x])}{15 d}$$

Result (type 3, 333 leaves):

$$\frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])}$$

$$\cos [c + d x]^4 \left( \sec [c] (45 A \cos [c] - 63 i B \cos [c] + 5 i A \sin [c] + 15 B \sin [c]) \right.$$

$$\left( -\frac{2}{15} \cos [3 c] + \frac{2}{15} i \sin [3 c] \right) + \sec [c + d x]^2 \left( -\frac{2}{5} i B \cos [3 c] - \frac{2}{5} B \sin [3 c] \right) +$$

$$\left. \sec [c] \sec [c + d x] \left( \frac{2}{3} \cos [3 c] - \frac{2}{3} i \sin [3 c] \right) (-i A \sin [d x] - 3 B \sin [d x]) \right)$$

$$\sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) +$$

$$\left( 4 (A - i B) \operatorname{ArcCosh} [e^{2 i (c+d x)}] \cos [c + d x]^4 (\cos [3 c] - i \sin [3 c]) \right.$$

$$\left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) /$$

$$\left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \sqrt{i \tan [c + d x]} \right)$$

### Problem 130: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan [c + d x])^3 (A + B \tan [c + d x])}{\tan [c + d x]^{3/2}} dx$$

Optimal (type 3, 134 leaves, 5 steps):

$$\frac{8 (-1)^{1/4} a^3 (i A + B) \operatorname{ArcTan} [(-1)^{3/4} \sqrt{\tan [c + d x]}]}{d} - \frac{16 a^3 B \sqrt{\tan [c + d x]}}{3 d} - \frac{2 a A (a + i a \tan [c + d x])^2}{d \sqrt{\tan [c + d x]}} + \frac{2 (3 i A - B) \sqrt{\tan [c + d x]} (a^3 + i a^3 \tan [c + d x])}{3 d}$$

Result (type 3, 341 leaves):

$$\frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])} \left( \cos [c + d x]^4 \left( \operatorname{Csc} [c] \operatorname{Sec} [c] (3 A + i B + 3 A \cos [2 c] - i B \cos [2 c] + 3 i A \sin [2 c] + 9 B \sin [2 c]) \right. \right. \\ \left. \left. \left( -\frac{1}{3} \cos [3 c] + \frac{1}{3} i \sin [3 c] \right) - i B \operatorname{Sec} [c] \operatorname{Sec} [c + d x] \left( \frac{2}{3} \cos [3 c] - \frac{2}{3} i \sin [3 c] \right) \sin [d x] + \right. \right. \\ \left. \left. A \operatorname{Csc} [c] \operatorname{Csc} [c + d x] (2 \cos [3 c] - 2 i \sin [3 c]) \sin [d x] \right) \right. \\ \left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) + \right. \\ \left. (4 (A - i B) \operatorname{ArcCosh} [e^{2 i (c + d x)}] \cos [c + d x]^4 (i \cos [3 c] + \sin [3 c]) \right. \\ \left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\ \left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \sqrt{i \tan [c + d x]} \right)$$

### Problem 131: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan [c + d x])^3 (A + B \tan [c + d x])}{\tan [c + d x]^{5/2}} dx$$

Optimal (type 3, 136 leaves, 5 steps):

$$\frac{8 (-1)^{1/4} a^3 (A - i B) \operatorname{ArcTan} [(-1)^{3/4} \sqrt{\tan [c + d x]}]}{d} - \frac{16 a^3 A \sqrt{\tan [c + d x]}}{3 d} - \frac{2 a A (a + i a \tan [c + d x])^2}{3 d \tan [c + d x]^{3/2}} - \frac{2 (7 i A + 3 B) (a^3 + i a^3 \tan [c + d x])}{3 d \sqrt{\tan [c + d x]}}$$

Result (type 3, 331 leaves):

$$\frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])} \\
 \cos [c + d x]^4 \left( -i \operatorname{Csc}[c] (9 A \cos [c] - 3 i B \cos [c] + i A \sin [c] + 3 B \sin [c]) \right. \\
 \left. \left( \frac{2}{3} \cos [3 c] - \frac{2}{3} i \sin [3 c] \right) + \operatorname{Csc}[c + d x]^2 \left( -\frac{2}{3} A \cos [3 c] + \frac{2}{3} i A \sin [3 c] \right) + \right. \\
 \left. \operatorname{Csc}[c] \operatorname{Csc}[c + d x] (2 \cos [3 c] - 2 i \sin [3 c]) (3 i A \sin [d x] + B \sin [d x]) \right) \\
 \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) - \\
 \left( 4 (A - i B) \operatorname{ArcCosh}\left[e^{2 i (c + d x)}\right] \cos [c + d x]^4 (\cos [3 c] - i \sin [3 c]) \right. \\
 \left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\
 \left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \sqrt{i \tan [c + d x]} \right)$$

**Problem 132: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [c + d x])^3 (A + B \tan [c + d x])}{\tan [c + d x]^{7/2}} dx$$

Optimal (type 3, 144 leaves, 5 steps):

$$\frac{8 (-1)^{1/4} a^3 (i A + B) \operatorname{ArcTan}\left[(-1)^{3/4} \sqrt{\tan [c + d x]}\right]}{d} + \frac{16 a^3 (6 A - 5 i B)}{15 d \sqrt{\tan [c + d x]}} - \\
 \frac{2 a A (a + i a \tan [c + d x])^2}{5 d \tan [c + d x]^{5/2}} - \frac{2 (9 i A + 5 B) (a^3 + i a^3 \tan [c + d x])}{15 d \tan [c + d x]^{3/2}}$$

Result (type 3, 386 leaves):

$$\frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])} \\
 \cos [c + d x]^4 \left( \operatorname{Csc}[c] (63 A \cos [c] - 45 i B \cos [c] + 15 i A \sin [c] + 5 B \sin [c]) \right. \\
 \left. \left( \frac{2}{15} \cos [3 c] - \frac{2}{15} i \sin [3 c] \right) + \right. \\
 \left. \operatorname{Csc}[c] \operatorname{Csc}[c + d x]^2 (3 A \cos [c] + 15 i A \sin [c] + 5 B \sin [c]) \left( -\frac{2}{15} \cos [3 c] + \frac{2}{15} i \sin [3 c] \right) + \right. \\
 \left. A \operatorname{Csc}[c] \operatorname{Csc}[c + d x]^3 \left( \frac{2}{5} \cos [3 c] - \frac{2}{5} i \sin [3 c] \right) \sin [d x] + \right. \\
 \left. \operatorname{Csc}[c] \operatorname{Csc}[c + d x] \left( -\frac{6}{5} \cos [3 c] + \frac{6}{5} i \sin [3 c] \right) (7 A \sin [d x] - 5 i B \sin [d x]) \right) \\
 \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) + \\
 \left( 4 (A - i B) \operatorname{ArcCosh}\left[e^{2 i (c + d x)}\right] \cos [c + d x]^4 (\cos [3 c] - i \sin [3 c]) \right. \\
 \left. \tan [c + d x]^{3/2} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\
 \left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) (i \tan [c + d x])^{3/2} \right)$$

### Problem 133: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan [c + d x])^3 (A + B \tan [c + d x])}{\tan [c + d x]^{9/2}} dx$$

Optimal (type 3, 169 leaves, 6 steps):

$$\begin{aligned} & -\frac{8(-1)^{1/4} a^3 (A - i B) \operatorname{ArcTan}\left[(-1)^{3/4} \sqrt{\tan [c + d x]}\right]}{d} + \frac{8 a^3 (23 A - 21 i B)}{105 d \tan [c + d x]^{3/2}} + \\ & \frac{8 a^3 (i A + B)}{d \sqrt{\tan [c + d x]}} - \frac{2 a A (a + i a \tan [c + d x])^2}{7 d \tan [c + d x]^{7/2}} - \frac{2 (11 i A + 7 B) (a^3 + i a^3 \tan [c + d x])}{35 d \tan [c + d x]^{5/2}} \end{aligned}$$

Result (type 3, 434 leaves):

$$\begin{aligned} & \frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])} \\ & \cos [c + d x]^4 \left( \operatorname{Csc}[c] \operatorname{Csc}[c + d x]^2 (-63 i A \cos [c] - 21 B \cos [c] + 170 A \sin [c] - 105 i B \sin [c]) \right. \\ & \quad \left. \left( \frac{2}{105} \cos [3 c] - \frac{2}{105} i \sin [3 c] \right) + \right. \\ & \quad \operatorname{Csc}[c] (483 i A \cos [c] + 441 B \cos [c] - 155 A \sin [c] + 105 i B \sin [c]) \\ & \quad \left. \left( \frac{2}{105} \cos [3 c] - \frac{2}{105} i \sin [3 c] \right) + \operatorname{Csc}[c + d x]^4 \left( -\frac{2}{7} A \cos [3 c] + \frac{2}{7} i A \sin [3 c] \right) + \right. \\ & \quad \operatorname{Csc}[c] \operatorname{Csc}[c + d x] \left( \frac{2}{5} \cos [3 c] - \frac{2}{5} i \sin [3 c] \right) (-23 i A \sin [d x] - 21 B \sin [d x]) + \\ & \quad \left. \operatorname{Csc}[c] \operatorname{Csc}[c + d x]^3 \left( \frac{2}{5} \cos [3 c] - \frac{2}{5} i \sin [3 c] \right) (3 i A \sin [d x] + B \sin [d x]) \right) \\ & \quad \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) + \\ & \quad \left( 4 (A - i B) \operatorname{ArcCosh}\left[e^{2 i (c + d x)}\right] \cos [c + d x]^4 (\cos [3 c] - i \sin [3 c]) \right. \\ & \quad \left. \sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\ & \quad \left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \sqrt{i \tan [c + d x]} \right) \end{aligned}$$

### Problem 154: Unable to integrate problem.

$$\int \tan [c + d x]^{3/2} \sqrt{a + i a \tan [c + d x]} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 200 leaves, 9 steps):

$$\frac{(-1)^{3/4} \sqrt{a} (4 i A + 7 B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{4 d} +$$

$$\frac{(1+i) \sqrt{a} (i A + B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{d} +$$

$$\frac{(4 A - i B) \sqrt{\tan[c+dx]} \sqrt{a+i a \tan[c+dx]}}{4 d} + \frac{B \tan[c+dx]^{3/2} \sqrt{a+i a \tan[c+dx]}}{2 d}$$

Result (type 8, 40 leaves):

$$\int \tan[c+dx]^{3/2} \sqrt{a+i a \tan[c+dx]} (A+B \tan[c+dx]) dx$$

**Problem 155: Result more than twice size of optimal antiderivative.**

$$\int \sqrt{\tan[c+dx]} \sqrt{a+i a \tan[c+dx]} (A+B \tan[c+dx]) dx$$

Optimal (type 3, 152 leaves, 8 steps):

$$-\frac{(-1)^{3/4} \sqrt{a} (2 A - i B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{d} -$$

$$\frac{(1+i) \sqrt{a} (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{d} + \frac{B \sqrt{\tan[c+dx]} \sqrt{a+i a \tan[c+dx]}}{d}$$

Result (type 3, 560 leaves):

$$-\frac{1}{4 \sqrt{2} d \sqrt{-1+e^{2 i(c+dx)}} \sqrt{\sec[c+dx]}} e^{-i(c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2 i(c+dx)}}} \sqrt{-\frac{i(-1+e^{2 i(c+dx)})}{1+e^{2 i(c+dx)}}} -$$

$$\left(-8 B e^{i(c+dx)} \sqrt{-1+e^{2 i(c+dx)}} + 8(i A+B)(1+e^{2 i(c+dx)}) \operatorname{Log}\left[e^{i(c+dx)} + \sqrt{-1+e^{2 i(c+dx)}}\right] -\right.$$

$$i \sqrt{2}(2 A-i B)(1+e^{2 i(c+dx)}) \operatorname{Log}\left[1-3 e^{2 i(c+dx)} - 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2 i(c+dx)}}\right] +$$

$$2 i \sqrt{2} A \operatorname{Log}\left[1-3 e^{2 i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2 i(c+dx)}}\right] +$$

$$\sqrt{2} B \operatorname{Log}\left[1-3 e^{2 i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2 i(c+dx)}}\right] +$$

$$2 i \sqrt{2} A e^{2 i(c+dx)} \operatorname{Log}\left[1-3 e^{2 i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2 i(c+dx)}}\right] +$$

$$\left.\sqrt{2} B e^{2 i(c+dx)} \operatorname{Log}\left[1-3 e^{2 i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2 i(c+dx)}}\right]\right) \sqrt{a+i a \tan[c+dx]}$$

**Problem 156: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a+i a \tan[c+dx]} (A+B \tan[c+dx])}{\sqrt{\tan[c+dx]}} dx$$

Optimal (type 3, 112 leaves, 7 steps):

$$\frac{2 (-1)^{3/4} \sqrt{a} B \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{d} - \frac{(1+i) \sqrt{a} (i A+B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{d}$$

Result (type 3, 241 leaves):

$$\left( e^{-i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \left( (-4iA-4B) \operatorname{Log}\left[ e^{i(c+dx)} + \sqrt{-1+e^{2i(c+dx)}} \right] + \sqrt{2} B \left( \operatorname{Log}\left[ 1-3e^{2i(c+dx)} - 2\sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] - \operatorname{Log}\left[ 1-3e^{2i(c+dx)} + 2\sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] \right) \right) \sqrt{a+i a \tan[c+dx]} \Big/ \left( 4d \sqrt{-\frac{i(-1+e^{2i(c+dx)})}{1+e^{2i(c+dx)}}} \right)$$

**Problem 161: Result more than twice size of optimal antiderivative.**

$$\int \tan[c+dx]^{3/2} (a+i a \tan[c+dx])^{3/2} (A+B \tan[c+dx]) dx$$

Optimal (type 3, 248 leaves, 10 steps):

$$\frac{(-1)^{3/4} a^{3/2} (22iA+23B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{8d} + \frac{(2+2i) a^{3/2} (iA+B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{d} + \frac{a(10A-9iB) \sqrt{\tan[c+dx]} \sqrt{a+i a \tan[c+dx]}}{8d} + \frac{a(6iA+7B) \tan[c+dx]^{3/2} \sqrt{a+i a \tan[c+dx]}}{12d} + \frac{iaB \tan[c+dx]^{5/2} \sqrt{a+i a \tan[c+dx]}}{3d}$$

Result (type 3, 527 leaves):

$$\begin{aligned}
 & \left( e^{-i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1+e^{2i(c+dx)})}{1+e^{2i(c+dx)}}} \left( -128 (A-i B) \operatorname{Log}\left[ e^{i(c+dx)} + \sqrt{-1+e^{2i(c+dx)}} \right] + \right. \right. \\
 & \quad \left. \sqrt{2} (22 A-23 i B) \left( \operatorname{Log}\left[ 1-3 e^{2i(c+dx)} - 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[ 1-3 e^{2i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] \right) \right) (a+i a \operatorname{Tan}[c+d x])^{3/2} \\
 & (A+B \operatorname{Tan}[c+d x]) \left. \right) / \left( 32 \sqrt{2} d \sqrt{-1+e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Sec}[c+d x]^{5/2} \right. \\
 & \left. (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^{3/2} (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right) + \\
 & \left( \operatorname{Cos}[c+d x]^2 \left( (6 A-7 i B) \left( \frac{7 \operatorname{Cos}[c]}{24} - \frac{7}{24} i \operatorname{Sin}[c] \right) + \operatorname{Sec}[c+d x]^2 \left( \frac{1}{3} i B \operatorname{Cos}[c] + \frac{1}{3} B \operatorname{Sin}[c] \right) \right) \right. \\
 & \quad \left. (6 A-7 i B) \operatorname{Sec}[c+d x] \left( -\frac{1}{12} \operatorname{Cos}[2 c+d x] + \frac{1}{12} i \operatorname{Sin}[2 c+d x] \right) \right) \\
 & \quad \left. \sqrt{\operatorname{Tan}[c+d x]} (a+i a \operatorname{Tan}[c+d x])^{3/2} (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & (d (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x]) (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]))
 \end{aligned}$$

**Problem 162: Result more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Tan}[c+d x]} (a+i a \operatorname{Tan}[c+d x])^{3/2} (A+B \operatorname{Tan}[c+d x]) dx$$

Optimal (type 3, 204 leaves, 9 steps):

$$\begin{aligned}
 & \frac{(-1)^{3/4} a^{3/2} (12 A-11 i B) \operatorname{ArcTan}\left[ \frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}} \right]}{4 d} - \\
 & \frac{(2+2 i) a^{3/2} (A-i B) \operatorname{ArcTanh}\left[ \frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}} \right]}{d} + \\
 & \frac{a (4 i A+5 B) \sqrt{\operatorname{Tan}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{4 d} + \frac{i a B \operatorname{Tan}[c+d x]^{3/2} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{2 d}
 \end{aligned}$$

Result (type 3, 496 leaves):

$$\left( e^{-i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1+e^{2 i(c+d x)})}{1+e^{2 i(c+d x)}}} \left( -64 i(A-i B) \operatorname{Log}\left[ e^{i(c+d x)} + \sqrt{-1+e^{2 i(c+d x)}} \right] + \right. \right. \\ \left. \sqrt{2}(12 i A+11 B) \left( \operatorname{Log}\left[ 1-3 e^{2 i(c+d x)}-2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}} \right] - \right. \right. \\ \left. \left. \operatorname{Log}\left[ 1-3 e^{2 i(c+d x)}+2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}} \right] \right) \right) (a+i a \operatorname{Tan}[c+d x])^{3/2} \\ (A+B \operatorname{Tan}[c+d x]) \left. \right) / \left( 16 \sqrt{2} d \sqrt{-1+e^{2 i(c+d x)}} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \operatorname{Sec}[c+d x]^{5/2} \right. \\ \left. (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^{3/2} (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right) + \\ \left( \operatorname{Cos}[c+d x]^2 \left( (4 i A+7 B) \left( \frac{\operatorname{Cos}[c]}{4}-\frac{1}{4} i \operatorname{Sin}[c] \right) + \right. \right. \\ \left. \left. \operatorname{Sec}[c+d x] \left( -\frac{1}{2} B \operatorname{Cos}[2 c+d x]+\frac{1}{2} i B \operatorname{Sin}[2 c+d x] \right) \right) \right) \\ \left. \sqrt{\operatorname{Tan}[c+d x]} (a+i a \operatorname{Tan}[c+d x])^{3/2} (A+B \operatorname{Tan}[c+d x]) \right) / \\ (d(\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])(A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]))$$

**Problem 163: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \operatorname{Tan}[c+d x])^{3/2} (A+B \operatorname{Tan}[c+d x])}{\sqrt{\operatorname{Tan}[c+d x]}} dx$$

Optimal (type 3, 156 leaves, 8 steps):

$$\frac{(-1)^{3/4} a^{3/2} (2 i A+3 B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}}\right]}{d} - \\ \frac{(2+2 i) a^{3/2} (i A+B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}}\right]}{d} + \frac{i a B \sqrt{\operatorname{Tan}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]}}{d}$$

Result (type 3, 481 leaves):



$$\frac{1}{4 \sqrt{2} d \sqrt{-1 + e^{2i(c+dx)}}} a e^{-i(c+dx)} \left( 4 i \sqrt{2} B e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} + \right. \\ \left. 8 \sqrt{2} (A - i B) (1 + e^{2i(c+dx)}) \operatorname{Log} \left[ e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}} \right] - \right. \\ \left. (2A - 3 i B) (1 + e^{2i(c+dx)}) \operatorname{Log} \left[ 1 - 3 e^{2i(c+dx)} - 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} \right] + \right. \\ \left. 2A \operatorname{Log} \left[ 1 - 3 e^{2i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} \right] - \right. \\ \left. 3 i B \operatorname{Log} \left[ 1 - 3 e^{2i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} \right] + \right. \\ \left. 2A e^{2i(c+dx)} \operatorname{Log} \left[ 1 - 3 e^{2i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} \right] - \right. \\ \left. 3 i B e^{2i(c+dx)} \operatorname{Log} \left[ 1 - 3 e^{2i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} \right] \right) \\ \sqrt{\operatorname{Tan}[c+dx]} \sqrt{a + i a \operatorname{Tan}[c+dx]}$$

**Problem 164: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x])}{\operatorname{Tan}[c + d x]^{3/2}} dx$$

Optimal (type 3, 146 leaves, 8 steps):

$$\frac{2 (-1)^{1/4} a^{3/2} B \operatorname{ArcTan} \left[ \frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}} \right]}{d} + \\ \frac{(2 + 2 i) a^{3/2} (A - i B) \operatorname{ArcTanh} \left[ \frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}} \right]}{d} - \frac{2 a A \sqrt{a + i a \operatorname{Tan}[c + d x]}}{d \sqrt{\operatorname{Tan}[c + d x]}}$$

Result (type 3, 307 leaves):

$$- \frac{1}{4 \sqrt{2} d \sqrt{-1 + e^{2i(c+dx)}}} a e^{-\frac{1}{2}i(4c+5dx)} \sqrt{\frac{a e^{2i(c+dx)}}{1 + e^{2i(c+dx)}}} (1 + e^{2i(c+dx)})^2 \\ \left( 4A \sqrt{-1 + e^{2i(c+dx)}} \operatorname{Csc}[c + d x] + (-8 i A - 8 B) \operatorname{Log} \left[ e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}} \right] + \right. \\ \left. \sqrt{2} B \left( \operatorname{Log} \left[ 1 - 3 e^{2i(c+dx)} - 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} \right] - \right. \right. \\ \left. \left. \operatorname{Log} \left[ 1 - 3 e^{2i(c+dx)} + 2 \sqrt{2} e^{i(c+dx)} \sqrt{-1 + e^{2i(c+dx)}} \right] \right) \right) \\ \operatorname{Sec}[c + d x] \left( \operatorname{Cos} \left[ \frac{dx}{2} \right] + i \operatorname{Sin} \left[ \frac{dx}{2} \right] \right) \sqrt{\operatorname{Tan}[c + d x]}$$

**Problem 170: Result more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Tan}[c + d x]} (a + i a \operatorname{Tan}[c + d x])^{5/2} (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 252 leaves, 10 steps):

$$\begin{aligned}
 & \frac{(-1)^{3/4} a^{5/2} (46 A - 45 i B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right]}{8 d} \\
 & \frac{(4 + 4 i) a^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right]}{d} + \\
 & \frac{a^2 (18 i A + 19 B) \sqrt{\operatorname{Tan}[c+dx]} \sqrt{a+i a \operatorname{Tan}[c+dx]}}{8 d} \\
 & \frac{a^2 (2 A - 3 i B) \operatorname{Tan}[c+dx]^{3/2} \sqrt{a+i a \operatorname{Tan}[c+dx]}}{4 d} + \frac{i a B \operatorname{Tan}[c+dx]^{3/2} (a+i a \operatorname{Tan}[c+dx])^{3/2}}{3 d}
 \end{aligned}$$

Result (type 3, 537 leaves):

$$\begin{aligned}
 & \left( e^{-2 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1+e^{2 i(c+d x)})}{1+e^{2 i(c+d x)}}} \left( -256 i(A-i B) \operatorname{Log}\left[ e^{i(c+d x)} + \sqrt{-1+e^{2 i(c+d x)}} \right] + \right. \right. \\
 & \quad \left. \sqrt{2}(46 i A+45 B) \left( \operatorname{Log}\left[ 1-3 e^{2 i(c+d x)}-2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[ 1-3 e^{2 i(c+d x)}+2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}} \right] \right) \right) (a+i a \operatorname{Tan}[c+d x])^{5/2} \\
 & \left. (A+B \operatorname{Tan}[c+d x]) \right) / \left( 32 \sqrt{2} d \sqrt{-1+e^{2 i(c+d x)}} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \operatorname{Sec}[c+d x]^{7/2} \right. \\
 & \left. (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^{5/2} (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right) + \\
 & \left( \operatorname{Cos}[c+d x] \right)^3 \left( (66 i A+91 B) \left( \frac{1}{24} \operatorname{Cos}[2 c]-\frac{1}{24} i \operatorname{Sin}[2 c] \right) + \right. \\
 & \quad \operatorname{Sec}[c+d x]^2 \left( -\frac{1}{3} B \operatorname{Cos}[2 c]+\frac{1}{3} i B \operatorname{Sin}[2 c] \right) + \\
 & \quad \left. (6 A-13 i B) \operatorname{Sec}[c+d x] \left( -\frac{1}{12} i \operatorname{Cos}[3 c+d x]-\frac{1}{12} \operatorname{Sin}[3 c+d x] \right) \right) \\
 & \left. \sqrt{\operatorname{Tan}[c+d x]} (a+i a \operatorname{Tan}[c+d x])^{5/2} (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & \left( d (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^2 (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right)
 \end{aligned}$$

**Problem 171: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \operatorname{Tan}[c+d x])^{5/2} (A+B \operatorname{Tan}[c+d x])}{\sqrt{\operatorname{Tan}[c+d x]}} dx$$

Optimal (type 3, 206 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{(-1)^{3/4} a^{5/2} (20 i A + 23 B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{4 d} + \\
 & \frac{(4 - 4 i) a^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{d} - \\
 & \frac{a^2 (4 A - 7 i B) \sqrt{\tan[c+dx]} \sqrt{a+i a \tan[c+dx]}}{4 d} + \frac{i a B \sqrt{\tan[c+dx]} (a+i a \tan[c+dx])^{3/2}}{2 d}
 \end{aligned}$$

Result (type 3, 499 leaves):

$$\begin{aligned}
 & \left( e^{-2 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1+e^{2 i(c+d x)})}{1+e^{2 i(c+d x)}}} \left( 128 (A - i B) \operatorname{Log}\left[e^{i(c+d x)} + \sqrt{-1+e^{2 i(c+d x)}}\right] - \right. \right. \\
 & \quad \left. \sqrt{2} (20 A - 23 i B) \left( \operatorname{Log}\left[1 - 3 e^{2 i(c+d x)} - 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}}\right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[1 - 3 e^{2 i(c+d x)} + 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}}\right]\right) \right) (a+i a \tan[c+dx])^{5/2} \\
 & (A+B \tan[c+dx]) \left. \right) / \left( 16 \sqrt{2} d \sqrt{-1+e^{2 i(c+d x)}} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \operatorname{Sec}[c+dx]^{7/2} \right. \\
 & \left. (\cos[dx] + i \sin[dx])^{5/2} (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( \cos[c+dx]^3 \left( (4 A - 11 i B) \left( -\frac{1}{4} \cos[2c] + \frac{1}{4} i \sin[2c] \right) + \right. \right. \\
 & \quad \left. \operatorname{Sec}[c+dx] \left( -\frac{1}{2} i B \cos[3c+dx] - \frac{1}{2} B \sin[3c+dx] \right) \right) \right) \\
 & \left. \sqrt{\tan[c+dx]} (a+i a \tan[c+dx])^{5/2} (A+B \tan[c+dx]) \right) / \\
 & \left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c+dx] + B \sin[c+dx]) \right)
 \end{aligned}$$

**Problem 172: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \tan[c+dx])^{5/2} (A+B \tan[c+dx])}{\tan[c+dx]^{3/2}} dx$$

Optimal (type 3, 196 leaves, 9 steps):

$$\frac{(-1)^{3/4} a^{5/2} (2A - 5iB) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right]}{d} +$$

$$\frac{(4+4i) a^{5/2} (A-iB) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right]}{d} +$$

$$\frac{a^2 (2iA-B) \sqrt{\tan[c+dx]} \sqrt{a+ia \tan[c+dx]}}{d} - \frac{2aA (a+ia \tan[c+dx])^{3/2}}{d \sqrt{\tan[c+dx]}}$$

Result (type 3, 493 leaves):

$$\left( e^{-2ic} \sqrt{e^{id}} \sqrt{-\frac{i(-1+e^{2i(c+dx)})}{1+e^{2i(c+dx)}}} \left( 32 (iA+B) \operatorname{Log}\left[ e^{i(c+dx)} + \sqrt{-1+e^{2i(c+dx)}} \right] - \right. \right.$$

$$i\sqrt{2} (2A-5iB) \left( \operatorname{Log}\left[ 1-3e^{2i(c+dx)} - 2\sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] - \right.$$

$$\left. \left. \operatorname{Log}\left[ 1-3e^{2i(c+dx)} + 2\sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] \right) \right) (a+ia \tan[c+dx])^{5/2}$$

$$(A+B \tan[c+dx]) \left/ \left( 4\sqrt{2} d \sqrt{-1+e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \operatorname{Sec}[c+dx]^{7/2} \right. \right.$$

$$\left. \left. (\cos[dx] + i \sin[dx])^{5/2} (A \cos[c+dx] + B \sin[c+dx]) \right) \right. +$$

$$\left( \cos[c+dx]^3 (\operatorname{Csc}[c] (2A \cos[c] + B \sin[c]) (-\cos[2c] + i \sin[2c]) + \right.$$

$$A \operatorname{Csc}[c] \operatorname{Csc}[c+dx] (2 \cos[2c] - 2i \sin[2c]) \sin[dx])$$

$$\left. \sqrt{\tan[c+dx]} (a+ia \tan[c+dx])^{5/2} (A+B \tan[c+dx]) \right) \left/ \right.$$

$$\left( d (\cos[dx] + i \sin[dx])^2 (A \cos[c+dx] + B \sin[c+dx]) \right)$$

**Problem 173: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+ia \tan[c+dx])^{5/2} (A+B \tan[c+dx])}{\tan[c+dx]^{5/2}} dx$$

Optimal (type 3, 190 leaves, 9 steps):

$$\frac{2(-1)^{3/4} a^{5/2} B \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right]}{d} + \frac{(4+4i) a^{5/2} (iA+B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right]}{d} -$$

$$\frac{2a^2 (2iA+B) \sqrt{a+ia \tan[c+dx]}}{d \sqrt{\tan[c+dx]}} - \frac{2aA (a+ia \tan[c+dx])^{3/2}}{3d \tan[c+dx]^{3/2}}$$

Result (type 3, 618 leaves):

$$\begin{aligned}
 & \left( e^{-i(3c+dx)} \sqrt{e^{i dx}} \sqrt{-1+e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \\
 & \left( \sqrt{2} B \operatorname{Log} \left[ \frac{2 e^{\frac{7ic}{2}} \left( \sqrt{2} - i \sqrt{2} e^{i(c+dx)} + 2 i \sqrt{-1+e^{2i(c+dx)}} \right)}{B(-i+e^{i(c+dx)})} \right] + \right. \\
 & \left. 8(iA+B) \operatorname{Log} \left[ e^{-ic} \left( e^{i(c+dx)} + \sqrt{-1+e^{2i(c+dx)}} \right) \right] - \right. \\
 & \left. \left. \sqrt{2} B \operatorname{Log} \left[ -\frac{2 i e^{\frac{7ic}{2}} \left( -i \sqrt{2} + \sqrt{2} e^{i(c+dx)} + 2 \sqrt{-1+e^{2i(c+dx)}} \right)}{B(i+e^{i(c+dx)})} \right] \right] \right) \\
 & \left( (a+i a \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) \right) / \left( \sqrt{2} d \sqrt{-\frac{i(-1+e^{2i(c+dx)})}{1+e^{2i(c+dx)}}} \right) \\
 & \left. \operatorname{Sec}[c+dx]^{7/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{5/2} (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right) + \\
 & \frac{1}{d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^2 (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx])} \\
 & \operatorname{Cos}[c+dx]^3 \left( -i \operatorname{Csc}[c] (7A \operatorname{Cos}[c] - 3iB \operatorname{Cos}[c] + iA \operatorname{Sin}[c]) \left( \frac{2}{3} \operatorname{Cos}[2c] - \frac{2}{3} i \operatorname{Sin}[2c] \right) + \right. \\
 & \left. \operatorname{Csc}[c+dx]^2 \left( -\frac{2}{3} A \operatorname{Cos}[2c] + \frac{2}{3} i A \operatorname{Sin}[2c] \right) + \right. \\
 & \left. \operatorname{Csc}[c] \operatorname{Csc}[c+dx] \left( \frac{2}{3} \operatorname{Cos}[2c] - \frac{2}{3} i \operatorname{Sin}[2c] \right) (7iA \operatorname{Sin}[dx] + 3B \operatorname{Sin}[dx]) \right) \\
 & \sqrt{\operatorname{Tan}[c+dx]} (a+i a \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx])
 \end{aligned}$$

**Problem 177: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx])}{\operatorname{Tan}[c+dx]^{13/2}} dx$$

Optimal (type 3, 323 leaves, 9 steps):

$$\frac{(4 + 4 i) a^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan [c+d x]}}{\sqrt{a+i a \tan [c+d x]}}\right]}{d} -$$

$$\frac{2 a^2 (14 i A + 11 B) \sqrt{a+i a \tan [c+d x]}}{99 d \tan [c+d x]^{9/2}} + \frac{2 a^2 (212 A - 209 i B) \sqrt{a+i a \tan [c+d x]}}{693 d \tan [c+d x]^{7/2}} +$$

$$\frac{4 a^2 (250 i A + 253 B) \sqrt{a+i a \tan [c+d x]}}{1155 d \tan [c+d x]^{5/2}} - \frac{8 a^2 (655 A - 649 i B) \sqrt{a+i a \tan [c+d x]}}{3465 d \tan [c+d x]^{3/2}} -$$

$$\frac{8 a^2 (2155 i A + 2167 B) \sqrt{a+i a \tan [c+d x]}}{3465 d \sqrt{\tan [c+d x]}} - \frac{2 a A (a+i a \tan [c+d x])^{3/2}}{11 d \tan [c+d x]^{11/2}}$$

Result (type 3, 656 leaves):

$$\left( 4 \sqrt{2} (i A + B) e^{-i (3 c+d x)} \sqrt{e^{i d x}} \sqrt{-1 + e^{2 i (c+d x)}} \right.$$

$$\left. \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}} \operatorname{Log}\left[e^{i (c+d x)} + \sqrt{-1 + e^{2 i (c+d x)}}\right]} (a + i a \tan [c + d x])^{5/2}} \right) /$$

$$\left( d \sqrt{-\frac{i (-1 + e^{2 i (c+d x)})}{1 + e^{2 i (c+d x)}}} \operatorname{Sec}[c + d x]^{5/2} (\cos [d x] + i \sin [d x])^{5/2}} \right) +$$

$$\frac{1}{(\cos [d x] + i \sin [d x])^2} \cos [c + d x]^2$$

$$\left( -i \operatorname{Csc}[c] (10925 A \cos [c] - 10571 i B \cos [c] + 3995 i A \sin [c] + 3641 B \sin [c]) \left( \frac{2 \cos [2 c]}{3465 d} - \right. \right.$$

$$\left. \frac{2 i \sin [2 c]}{3465 d} \right) + \operatorname{Csc}[c + d x]^6 \left( -\frac{2 A \cos [2 c]}{11 d} + \frac{2 i A \sin [2 c]}{11 d} \right) + \operatorname{Csc}[c] \operatorname{Csc}[c + d x]^2$$

$$\left( -2575 i A - 2398 B + 8795 i A \cos [2 c] + 6974 B \cos [2 c] - 8795 A \sin [2 c] + 6974 i B \sin [2 c] \right)$$

$$\left( \frac{\cos [3 c]}{3465 d} - \frac{i \sin [3 c]}{3465 d} \right) + \operatorname{Csc}[c] \operatorname{Csc}[c + d x]^4 (120 i A + 66 B - 281 i A \cos [2 c] -$$

$$143 B \cos [2 c] + 281 A \sin [2 c] - 143 i B \sin [2 c]) \left( \frac{2 \cos [3 c]}{693 d} - \frac{2 i \sin [3 c]}{693 d} \right) +$$

$$\operatorname{Csc}[c] \operatorname{Csc}[c + d x]^3 \left( \frac{4 \cos [2 c]}{3465 d} - \frac{4 i \sin [2 c]}{3465 d} \right) (-1555 i A \sin [d x] - 1144 B \sin [d x]) +$$

$$\operatorname{Csc}[c] \operatorname{Csc}[c + d x]^5 \left( \frac{2 \cos [2 c]}{99 d} - \frac{2 i \sin [2 c]}{99 d} \right) (23 i A \sin [d x] + 11 B \sin [d x]) +$$

$$\operatorname{Csc}[c] \operatorname{Csc}[c + d x] \left( \frac{2 \cos [2 c]}{3465 d} - \frac{2 i \sin [2 c]}{3465 d} \right) (10925 i A \sin [d x] + 10571 B \sin [d x]) \right)$$

$$\sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^{5/2}$$

**Problem 178: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [c + d x])^{5/2} \left( \frac{3 b B}{2 a} + B \tan [c + d x] \right)}{\tan [c + d x]^{5/2}} dx$$

Optimal (type 3, 190 leaves, 9 steps):

$$\frac{2 (-1)^{3/4} a^{5/2} B \operatorname{ArcTan} \left[ \frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan [c + d x]}}{\sqrt{a + i a \tan [c + d x]}} \right]}{d} +$$

$$\frac{(2 + 2 i) a^{3/2} (2 a + 3 i b) B \operatorname{ArcTanh} \left[ \frac{(1 + i) \sqrt{a} \sqrt{\tan [c + d x]}}{\sqrt{a + i a \tan [c + d x]}} \right]}{d} -$$

$$\frac{2 a (a + 3 i b) B \sqrt{a + i a \tan [c + d x]}}{d \sqrt{\tan [c + d x]}} - \frac{b B (a + i a \tan [c + d x])^{3/2}}{d \tan [c + d x]^{3/2}}$$

Result (type 3, 555 leaves):

$$\left( i e^{-2 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i (-1 + e^{2 i (c + d x)})}{1 + e^{2 i (c + d x)}}} \left( 8 (2 a + 3 i b) \operatorname{Log} \left[ e^{i (c + d x)} + \sqrt{-1 + e^{2 i (c + d x)}} \right] + \right. \right.$$

$$\left. \sqrt{2} a \left( -\operatorname{Log} \left[ 1 - 3 e^{2 i (c + d x)} - 2 \sqrt{2} e^{i (c + d x)} \sqrt{-1 + e^{2 i (c + d x)}} \right] + \right. \right.$$

$$\left. \left. \operatorname{Log} \left[ 1 - 3 e^{2 i (c + d x)} + 2 \sqrt{2} e^{i (c + d x)} \sqrt{-1 + e^{2 i (c + d x)}} \right] \right) \right) (a + i a \tan [c + d x])^{5/2}$$

$$\left( \frac{3 b B}{2 a} + B \tan [c + d x] \right) \left/ \left( \sqrt{2} d \sqrt{-1 + e^{2 i (c + d x)}} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \operatorname{Sec} [c + d x]^{7/2} \right. \right.$$

$$\left. \left. (\cos [d x] + i \sin [d x])^{5/2} (3 b \cos [c + d x] + 2 a \sin [c + d x]) \right) \right) +$$

$$\left( \cos [c + d x]^3 (-i \operatorname{Csc} [c] (-2 i a \cos [c] + 7 b \cos [c] + i b \sin [c]) (2 \cos [2 c] - 2 i \sin [2 c]) + \right.$$

$$\operatorname{Csc} [c + d x]^2 (-2 b \cos [2 c] + 2 i b \sin [2 c]) +$$

$$\operatorname{Csc} [c] \operatorname{Csc} [c + d x] (2 \cos [2 c] - 2 i \sin [2 c]) (2 a \sin [d x] + 7 i b \sin [d x]) \left. \right)$$

$$\sqrt{\tan [c + d x]} (a + i a \tan [c + d x])^{5/2} \left( \frac{3 b B}{2 a} + B \tan [c + d x] \right) \left/ \right.$$

$$\left( d (\cos [d x] + i \sin [d x])^2 (3 b \cos [c + d x] + 2 a \sin [c + d x]) \right)$$

**Problem 185: Result more than twice size of optimal antiderivative.**

$$\int \frac{\tan [c + d x]^{3/2} (A + B \tan [c + d x])}{(a + i a \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 203 leaves, 9 steps):

$$\frac{2 (-1)^{3/4} B \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right]}{a^{3/2} d} - \frac{\left(\frac{1}{4} - \frac{i}{4}\right) (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right]}{a^{3/2} d} + \frac{(i A - B) \operatorname{Tan}[c+dx]^{3/2}}{3 d (a+i a \operatorname{Tan}[c+dx])^{3/2}} + \frac{(A+3 i B) \sqrt{\operatorname{Tan}[c+dx]}}{2 a d \sqrt{a+i a \operatorname{Tan}[c+dx]}}$$

Result (type 3, 552 leaves):

$$\begin{aligned} & - \left( \left( e^{2 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1+e^{2 i(c+d x)})}{1+e^{2 i(c+d x)}}} \left( (A-i B) \operatorname{Log}\left[e^{i(c+d x)} + \sqrt{-1+e^{2 i(c+d x)}}\right] + \right. \right. \right. \\ & \quad \left. \left. \left. i \sqrt{2} B \left( \operatorname{Log}\left[1-3 e^{2 i(c+d x)} - 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}}\right] - \right. \right. \right. \\ & \quad \left. \left. \left. \operatorname{Log}\left[1-3 e^{2 i(c+d x)} + 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}}\right] \right) \right) \right) \\ & \quad \left. \left. \left. \sqrt{\operatorname{Sec}[c+dx]} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{3/2} (A+B \operatorname{Tan}[c+dx]) \right) \right) / \right. \\ & \quad \left. \left( 2 \sqrt{2} d \sqrt{-1+e^{2 i(c+d x)}} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right. \right. \\ & \quad \left. \left. (a+i a \operatorname{Tan}[c+dx])^{3/2} \right) \right) + \\ & \quad \left( \operatorname{Sec}[c+dx] (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^2 \left( \frac{1}{4} (A+3 i B) \operatorname{Cos}[2 dx] + \right. \right. \\ & \quad \left. \left. (A+i B) \operatorname{Cos}[4 dx] \left( -\frac{1}{12} \operatorname{Cos}[2 c] + \frac{1}{12} i \operatorname{Sin}[2 c] \right) + \right. \right. \\ & \quad \left. \left. (2 A+5 i B) \left( \frac{1}{6} \operatorname{Cos}[2 c] + \frac{1}{6} i \operatorname{Sin}[2 c] \right) + \frac{1}{4} (-i A+3 B) \operatorname{Sin}[2 dx] + \right. \right. \\ & \quad \left. \left. (A+i B) \left( \frac{1}{12} i \operatorname{Cos}[2 c] + \frac{1}{12} \operatorname{Sin}[2 c] \right) \operatorname{Sin}[4 dx] \right) \sqrt{\operatorname{Tan}[c+dx]} (A+B \operatorname{Tan}[c+dx]) \right) / \right. \\ & \quad \left. (d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+i a \operatorname{Tan}[c+dx])^{3/2}) \right) \end{aligned}$$

**Problem 189: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Tan}[c+dx]}{\operatorname{Tan}[c+dx]^{5/2} (a+i a \operatorname{Tan}[c+dx])^{3/2}} dx$$

Optimal (type 3, 240 leaves, 7 steps):



$$\frac{\left(\frac{1}{4} + \frac{i}{4}\right) (i A + B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right]}{a^{3/2} d} + \frac{A + i B}{3 d \tan[c+dx]^{3/2} (a + i a \tan[c+dx])^{3/2}} + \frac{5 A + 3 i B}{2 a d \tan[c+dx]^{3/2} \sqrt{a + i a \tan[c+dx]}} - \frac{(21 A + 11 i B) \sqrt{a + i a \tan[c+dx]}}{6 a^2 d \tan[c+dx]^{3/2}} + \frac{(39 i A - 25 B) \sqrt{a + i a \tan[c+dx]}}{6 a^2 d \sqrt{\tan[c+dx]}}$$

Result (type 3, 624 leaves):

$$\left( (i A + B) e^{i(c-dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Log}\left[e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}}\right] \right. \\ \left. \sqrt{\operatorname{Sec}[c+dx]} (\cos[dx] + i \sin[dx])^{3/2} (A + B \tan[c+dx]) \right) / \\ \left( 2 \sqrt{2} d \sqrt{-\frac{i(-1 + e^{2i(c+dx)})}{1 + e^{2i(c+dx)}}} (A \cos[c+dx] + B \sin[c+dx]) (a + i a \tan[c+dx])^{3/2} \right) + \\ \frac{1}{d (A \cos[c+dx] + B \sin[c+dx]) (a + i a \tan[c+dx])^{3/2}} \operatorname{Sec}[c+dx] (\cos[dx] + i \sin[dx])^2 \\ \left( -\frac{1}{4} (7A + 5iB) \cos[2dx] + (A + iB) \cos[4dx] \left( -\frac{1}{12} \cos[2c] + \frac{1}{12} i \sin[2c] \right) + \right. \\ \left. i \operatorname{Csc}[c] (20A \cos[c] + 12iB \cos[c] + 6iA \sin[c] - 7B \sin[c]) \left( \frac{1}{6} \cos[2c] + \frac{1}{6} i \sin[2c] \right) + \right. \\ \left. \operatorname{Csc}[c+dx]^2 \left( -\frac{2}{3} A \cos[2c] - \frac{2}{3} i A \sin[2c] \right) + \frac{1}{4} i (7A + 5iB) \sin[2dx] + \right. \\ \left. (A + iB) \left( \frac{1}{12} i \cos[2c] + \frac{1}{12} \sin[2c] \right) \sin[4dx] + \right. \\ \left. \frac{2}{3} \operatorname{Csc}[c] \operatorname{Csc}[c+dx] \left( \frac{5}{2} A \cos[2c-dx] + \frac{3}{2} i B \cos[2c-dx] - \right. \right. \\ \left. \left. \frac{5}{2} A \cos[2c+dx] - \frac{3}{2} i B \cos[2c+dx] + \frac{5}{2} A \sin[2c-dx] - \frac{3}{2} B \sin[2c-dx] - \right. \right. \\ \left. \left. \frac{5}{2} i A \sin[2c+dx] + \frac{3}{2} B \sin[2c+dx] \right) \right) \sqrt{\tan[c+dx]} (A + B \tan[c+dx])$$

**Problem 190: Result more than twice size of optimal antiderivative.**

$$\int \frac{\tan[c+dx]^{5/2} (A + B \tan[c+dx])}{(a + i a \tan[c+dx])^{5/2}} dx$$

Optimal (type 3, 249 leaves, 10 steps):

$$\frac{2 (-1)^{1/4} B \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right]}{a^{5/2} d} + \frac{\left(\frac{1}{8} + \frac{i}{8}\right) (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right]}{a^{5/2} d} +$$

$$\frac{(i A - B) \operatorname{Tan}[c+dx]^{5/2}}{5 d (a+i a \operatorname{Tan}[c+dx])^{5/2}} + \frac{(A+3 i B) \operatorname{Tan}[c+dx]^{3/2}}{6 a d (a+i a \operatorname{Tan}[c+dx])^{3/2}} - \frac{(i A - 7 B) \sqrt{\operatorname{Tan}[c+dx]}}{4 a^2 d \sqrt{a+i a \operatorname{Tan}[c+dx]}}$$

Result (type 3, 638 leaves):

$$\left( e^{3 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1+e^{2 i(c+d x)})}{1+e^{2 i(c+d x)}}} \left( (i A+B) \operatorname{Log}\left[ e^{i(c+d x)} + \sqrt{-1+e^{2 i(c+d x)}} \right] + \right. \right.$$

$$2 \sqrt{2} B \left( -\operatorname{Log}\left[ 1-3 e^{2 i(c+d x)} - 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}} \right] + \right.$$

$$\left. \left. \operatorname{Log}\left[ 1-3 e^{2 i(c+d x)} + 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}} \right] \right) \right) \operatorname{Sec}[c+dx]^{3/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) \Big/$$

$$\left( 4 \sqrt{2} d \sqrt{-1+e^{2 i(c+d x)}} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right.$$

$$\left. (a+i a \operatorname{Tan}[c+dx])^{5/2} \right) +$$


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$$d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+i a \operatorname{Tan}[c+dx])^{5/2}$$

$$\operatorname{Sec}[c+dx]^2 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3$$

$$\left( (-2 i A+17 B) \operatorname{Cos}[2 d x] \left( \frac{\operatorname{Cos}[c]}{20} + \frac{1}{20} i \operatorname{Sin}[c] \right) + (4 A+9 i B) \operatorname{Cos}[4 d x] \right.$$

$$\left( \frac{1}{60} i \operatorname{Cos}[c] + \frac{\operatorname{Sin}[c]}{60} \right) + (-23 i A+123 B) \left( \frac{1}{120} \operatorname{Cos}[3 c] + \frac{1}{120} i \operatorname{Sin}[3 c] \right) +$$

$$(-i A+B) \operatorname{Cos}[6 d x] \left( \frac{1}{40} \operatorname{Cos}[3 c] - \frac{1}{40} i \operatorname{Sin}[3 c] \right) + (2 A+17 i B)$$

$$\left( -\frac{\operatorname{Cos}[c]}{20} - \frac{1}{20} i \operatorname{Sin}[c] \right) \operatorname{Sin}[2 d x] + (4 A+9 i B) \left( \frac{\operatorname{Cos}[c]}{60} - \frac{1}{60} i \operatorname{Sin}[c] \right) \operatorname{Sin}[4 d x] +$$

$$(A+i B) \left( -\frac{1}{40} \operatorname{Cos}[3 c] + \frac{1}{40} i \operatorname{Sin}[3 c] \right) \operatorname{Sin}[6 d x] \Big) \sqrt{\operatorname{Tan}[c+dx]} (A+B \operatorname{Tan}[c+dx])$$

**Problem 191: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c+dx]^{3/2} (A+B \operatorname{Tan}[c+dx])}{(a+i a \operatorname{Tan}[c+dx])^{5/2}} dx$$

Optimal (type 3, 194 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{\left(\frac{1}{8} - \frac{i}{8}\right) (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{a^{5/2} d} + \frac{(i A - B) \tan[c+dx]^{3/2}}{5 d (a+i a \tan[c+dx])^{5/2}} + \\
 & \frac{(A+11 i B) \sqrt{\tan[c+dx]}}{30 a d (a+i a \tan[c+dx])^{3/2}} + \frac{(13 A - 37 i B) \sqrt{\tan[c+dx]}}{60 a^2 d \sqrt{a+i a \tan[c+dx]}}
 \end{aligned}$$

Result (type 3, 527 leaves):

$$\begin{aligned}
 & \left( (i A + B) e^{-i(-2c+dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Log}\left[e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}}\right] \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^{3/2} (\cos[dx] + i \sin[dx])^{5/2} (A + B \tan[c+dx]) \right) / \\
 & \left( 4 \sqrt{2} d \sqrt{-\frac{i(-1 + e^{2i(c+dx)})}{1 + e^{2i(c+dx)}}} (A \cos[c+dx] + B \sin[c+dx]) (a+i a \tan[c+dx])^{5/2} \right) + \\
 & \frac{1}{d (A \cos[c+dx] + B \sin[c+dx]) (a+i a \tan[c+dx])^{5/2}} \operatorname{Sec}[c+dx]^2 (\cos[dx] + i \sin[dx])^3 \\
 & \left( (A - 4 i B) \cos[4 dx] \left(-\frac{\cos[c]}{60} + \frac{1}{60} i \sin[c]\right) + (3 A - 2 i B) \cos[2 dx] \right. \\
 & \quad \left( \frac{\cos[c]}{20} + \frac{1}{20} i \sin[c] \right) + (17 A - 23 i B) \left( \frac{1}{120} \cos[3 c] + \frac{1}{120} i \sin[3 c] \right) + \\
 & \quad (A + i B) \cos[6 dx] \left(-\frac{1}{40} \cos[3 c] + \frac{1}{40} i \sin[3 c]\right) + (3 A - 2 i B) \\
 & \quad \left(-\frac{1}{20} i \cos[c] + \frac{\sin[c]}{20}\right) \sin[2 dx] + (i A + 4 B) \left(\frac{\cos[c]}{60} - \frac{1}{60} i \sin[c]\right) \sin[4 dx] + \\
 & \quad \left. (A + i B) \left(\frac{1}{40} i \cos[3 c] + \frac{1}{40} \sin[3 c]\right) \sin[6 dx] \right) \sqrt{\tan[c+dx]} (A + B \tan[c+dx])
 \end{aligned}$$

**Problem 192: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\tan[c+dx]} (A + B \tan[c+dx])}{(a+i a \tan[c+dx])^{5/2}} dx$$

Optimal (type 3, 196 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{\left(\frac{1}{8} + \frac{i}{8}\right) (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}}\right]}{a^{5/2} d} + \frac{(i A - B) \sqrt{\tan[c+dx]}}{5 d (a+i a \tan[c+dx])^{5/2}} + \\
 & \frac{(3 i A + 7 B) \sqrt{\tan[c+dx]}}{30 a d (a+i a \tan[c+dx])^{3/2}} - \frac{(3 i A - 13 B) \sqrt{\tan[c+dx]}}{60 a^2 d \sqrt{a+i a \tan[c+dx]}}
 \end{aligned}$$

Result (type 3, 525 leaves):

$$\begin{aligned}
 & - \left( \left( i (A - i B) e^{3 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i (-1 + e^{2 i (c+d x)})}{1 + e^{2 i (c+d x)}}} \operatorname{Log} \left[ e^{i (c+d x)} + \sqrt{-1 + e^{2 i (c+d x)}} \right] \operatorname{Sec} [c + d x] \right)^{3/2} \right. \\
 & \quad \left. \left( \operatorname{Cos} [d x] + i \operatorname{Sin} [d x] \right)^{5/2} (A + B \operatorname{Tan} [c + d x]) \right) / \left( 4 \sqrt{2} d \sqrt{-1 + e^{2 i (c+d x)}} \right. \\
 & \quad \left. \sqrt{\frac{e^{i (c+d x)}}{1 + e^{2 i (c+d x)}}} (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) (a + i a \operatorname{Tan} [c + d x])^{5/2} \right) + \\
 & \quad \frac{1}{d (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) (a + i a \operatorname{Tan} [c + d x])^{5/2}} \\
 & \quad \operatorname{Sec} [c + d x]^2 (\operatorname{Cos} [d x] + i \operatorname{Sin} [d x])^3 \\
 & \quad \left( (2 i A + 3 B) \operatorname{Cos} [2 d x] \left( \frac{\operatorname{Cos} [c]}{20} + \frac{1}{20} i \operatorname{Sin} [c] \right) + (6 A + i B) \operatorname{Cos} [4 d x] \right. \\
 & \quad \left( \frac{1}{60} i \operatorname{Cos} [c] + \frac{\operatorname{Sin} [c]}{60} \right) + (3 i A + 17 B) \left( \frac{1}{120} \operatorname{Cos} [3 c] + \frac{1}{120} i \operatorname{Sin} [3 c] \right) + \\
 & \quad (A + i B) \operatorname{Cos} [6 d x] \left( \frac{1}{40} i \operatorname{Cos} [3 c] + \frac{1}{40} \operatorname{Sin} [3 c] \right) + (2 A - 3 i B) \\
 & \quad \left( \frac{\operatorname{Cos} [c]}{20} + \frac{1}{20} i \operatorname{Sin} [c] \right) \operatorname{Sin} [2 d x] + (6 A + i B) \left( \frac{\operatorname{Cos} [c]}{60} - \frac{1}{60} i \operatorname{Sin} [c] \right) \operatorname{Sin} [4 d x] + \\
 & \quad \left. (A + i B) \left( \frac{1}{40} \operatorname{Cos} [3 c] - \frac{1}{40} i \operatorname{Sin} [3 c] \right) \operatorname{Sin} [6 d x] \right) \sqrt{\operatorname{Tan} [c + d x]} (A + B \operatorname{Tan} [c + d x])
 \end{aligned}$$

**Problem 193: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan} [c + d x]}{\sqrt{\operatorname{Tan} [c + d x]} (a + i a \operatorname{Tan} [c + d x])^{5/2}} dx$$

Optimal (type 3, 194 leaves, 6 steps):

$$\begin{aligned}
 & \frac{\left( \frac{1}{8} - \frac{i}{8} \right) (A - i B) \operatorname{ArcTanh} \left[ \frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan} [c+d x]}}{\sqrt{a+i a \operatorname{Tan} [c+d x]}} \right]}{a^{5/2} d} + \frac{(A + i B) \sqrt{\operatorname{Tan} [c + d x]}}{5 d (a + i a \operatorname{Tan} [c + d x])^{5/2}} + \\
 & \frac{(13 A + 3 i B) \sqrt{\operatorname{Tan} [c + d x]}}{30 a d (a + i a \operatorname{Tan} [c + d x])^{3/2}} + \frac{(67 A - 3 i B) \sqrt{\operatorname{Tan} [c + d x]}}{60 a^2 d \sqrt{a + i a \operatorname{Tan} [c + d x]}}
 \end{aligned}$$

Result (type 3, 523 leaves):

$$\begin{aligned}
 & \left( (A - i B) e^{3 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1 + e^{2 i(c+d x)})}{1 + e^{2 i(c+d x)}}} \operatorname{Log}\left[e^{i(c+d x)} + \sqrt{-1 + e^{2 i(c+d x)}}\right] \operatorname{Sec}[c + d x]^{3/2} \right. \\
 & \quad \left. (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^{5/2} (A + B \operatorname{Tan}[c + d x]) \right) / \left( 4 \sqrt{2} d \sqrt{-1 + e^{2 i(c+d x)}} \right. \\
 & \quad \left. \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2 i(c+d x)}}} (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + i a \operatorname{Tan}[c + d x])^{5/2} \right) + \\
 & \frac{1}{d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + i a \operatorname{Tan}[c + d x])^{5/2}} \operatorname{Sec}[c + d x]^2 (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 \\
 & \left( (11 A + 6 i B) \operatorname{Cos}[4 d x] \left( \frac{\operatorname{Cos}[c]}{60} - \frac{1}{60} i \operatorname{Sin}[c] \right) + (17 A + 2 i B) \operatorname{Cos}[2 d x] \right. \\
 & \quad \left( \frac{\operatorname{Cos}[c]}{20} + \frac{1}{20} i \operatorname{Sin}[c] \right) + (83 A + 3 i B) \left( \frac{1}{120} \operatorname{Cos}[3 c] + \frac{1}{120} i \operatorname{Sin}[3 c] \right) + \\
 & \quad (A + i B) \operatorname{Cos}[6 d x] \left( \frac{1}{40} \operatorname{Cos}[3 c] - \frac{1}{40} i \operatorname{Sin}[3 c] \right) + (-17 i A + 2 B) \\
 & \quad \left( \frac{\operatorname{Cos}[c]}{20} + \frac{1}{20} i \operatorname{Sin}[c] \right) \operatorname{Sin}[2 d x] + (-11 i A + 6 B) \left( \frac{\operatorname{Cos}[c]}{60} - \frac{1}{60} i \operatorname{Sin}[c] \right) \operatorname{Sin}[4 d x] + \\
 & \quad \left. (-i A + B) \left( \frac{1}{40} \operatorname{Cos}[3 c] - \frac{1}{40} i \operatorname{Sin}[3 c] \right) \operatorname{Sin}[6 d x] \right) \sqrt{\operatorname{Tan}[c + d x]} (A + B \operatorname{Tan}[c + d x])
 \end{aligned}$$

**Problem 194: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan}[c + d x]}{\operatorname{Tan}[c + d x]^{3/2} (a + i a \operatorname{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 240 leaves, 7 steps):

$$\begin{aligned}
 & \frac{\left(\frac{1}{8} + \frac{i}{8}\right) (A - i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}}\right]}{a^{5/2} d} + \\
 & \frac{A + i B}{5 d \sqrt{\operatorname{Tan}[c + d x]} (a + i a \operatorname{Tan}[c + d x])^{5/2}} + \frac{17 A + 7 i B}{30 a d \sqrt{\operatorname{Tan}[c + d x]} (a + i a \operatorname{Tan}[c + d x])^{3/2}} + \\
 & \frac{151 A + 41 i B}{60 a^2 d \sqrt{\operatorname{Tan}[c + d x]} \sqrt{a + i a \operatorname{Tan}[c + d x]}} - \frac{(317 A + 67 i B) \sqrt{a + i a \operatorname{Tan}[c + d x]}}{60 a^3 d \sqrt{\operatorname{Tan}[c + d x]}}
 \end{aligned}$$

Result (type 3, 603 leaves):

$$\left( \frac{(i A + B) e^{3 i c} \sqrt{e^{i d x}} \sqrt{-\frac{i(-1 + e^{2 i(c+d x)})}{1 + e^{2 i(c+d x)}}} \operatorname{Log}\left[e^{i(c+d x)} + \sqrt{-1 + e^{2 i(c+d x)}}\right] \operatorname{Sec}[c + d x]^{3/2}}{\left(\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]\right)^{5/2} (A + B \operatorname{Tan}[c + d x])} \right) / \left( 4 \sqrt{2} d \sqrt{-1 + e^{2 i(c+d x)}} \right. \\ \left. \sqrt{\frac{e^{i(c+d x)}}{1 + e^{2 i(c+d x)}}} (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + i a \operatorname{Tan}[c + d x])^{5/2}} \right) + \\ \frac{1}{d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + i a \operatorname{Tan}[c + d x])^{5/2}} \\ \operatorname{Sec}[c + d x]^2 (\operatorname{Cos}[d x] + i \operatorname{Sin}[d x])^3 \left( (-16 i A + 11 B) \operatorname{Cos}[4 d x] \left( \frac{\operatorname{Cos}[c]}{60} - \frac{1}{60} i \operatorname{Sin}[c] \right) + \right. \\ \left. (-42 i A + 17 B) \operatorname{Cos}[2 d x] \left( \frac{\operatorname{Cos}[c]}{20} + \frac{1}{20} i \operatorname{Sin}[c] \right) + \right. \\ \left. \operatorname{Csc}[c] (240 A \operatorname{Cos}[c] + 223 i A \operatorname{Sin}[c] - 83 B \operatorname{Sin}[c]) \left( -\frac{1}{120} \operatorname{Cos}[3 c] - \frac{1}{120} i \operatorname{Sin}[3 c] \right) + \right. \\ \left. (-i A + B) \operatorname{Cos}[6 d x] \left( \frac{1}{40} \operatorname{Cos}[3 c] - \frac{1}{40} i \operatorname{Sin}[3 c] \right) + (42 A + 17 i B) \right. \\ \left. \left( -\frac{\operatorname{Cos}[c]}{20} - \frac{1}{20} i \operatorname{Sin}[c] \right) \operatorname{Sin}[2 d x] + (16 A + 11 i B) \left( -\frac{\operatorname{Cos}[c]}{60} + \frac{1}{60} i \operatorname{Sin}[c] \right) \operatorname{Sin}[4 d x] + \right. \\ \left. (A + i B) \left( -\frac{1}{40} \operatorname{Cos}[3 c] + \frac{1}{40} i \operatorname{Sin}[3 c] \right) \operatorname{Sin}[6 d x] + 2 \operatorname{Csc}[c] \operatorname{Csc}[c + d x] \right. \\ \left. \left( \frac{1}{2} i A \operatorname{Cos}[3 c - d x] - \frac{1}{2} i A \operatorname{Cos}[3 c + d x] - \frac{1}{2} A \operatorname{Sin}[3 c - d x] + \frac{1}{2} A \operatorname{Sin}[3 c + d x] \right) \right) \\ \sqrt{\operatorname{Tan}[c + d x]} (A + B \operatorname{Tan}[c + d x])$$

**Problem 195: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan}[c + d x]}{\operatorname{Tan}[c + d x]^{5/2} (a + i a \operatorname{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 286 leaves, 8 steps):

$$\frac{\left(\frac{1}{8} + \frac{i}{8}\right) (i A + B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}}\right]}{a^{5/2} d} + \frac{A + i B}{5 d \operatorname{Tan}[c + d x]^{3/2} (a + i a \operatorname{Tan}[c + d x])^{5/2}} + \\ \frac{21 A + 11 i B}{30 a d \operatorname{Tan}[c + d x]^{3/2} (a + i a \operatorname{Tan}[c + d x])^{3/2}} + \frac{89 A + 39 i B}{20 a^2 d \operatorname{Tan}[c + d x]^{3/2} \sqrt{a + i a \operatorname{Tan}[c + d x]}} - \\ \frac{(361 A + 151 i B) \sqrt{a + i a \operatorname{Tan}[c + d x]}}{60 a^3 d \operatorname{Tan}[c + d x]^{3/2}} + \frac{(707 i A - 317 B) \sqrt{a + i a \operatorname{Tan}[c + d x]}}{60 a^3 d \sqrt{\operatorname{Tan}[c + d x]}}$$

Result (type 3, 701 leaves):

$$\left( (i A + B) e^{-i(-2c+dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \operatorname{Log}\left[e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}}\right] \right. \\
 \left. \operatorname{Sec}[c + dx]^{3/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{5/2} (A + B \operatorname{Tan}[c + dx]) \right) / \\
 \left( 4 \sqrt{2} d \sqrt{-\frac{i(-1 + e^{2i(c+dx)})}{1 + e^{2i(c+dx)}}} (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + i a \operatorname{Tan}[c + dx])^{5/2} \right) + \\
 \frac{1}{d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + i a \operatorname{Tan}[c + dx])^{5/2}} \\
 \operatorname{Sec}[c + dx]^2 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \left( (21 A + 16 i B) \operatorname{Cos}[4 dx] \left( -\frac{\operatorname{Cos}[c]}{60} + \frac{1}{60} i \operatorname{Sin}[c] \right) + \right. \\
 (11 A + 6 i B) \operatorname{Cos}[2 dx] \left( -\frac{7 \operatorname{Cos}[c]}{20} - \frac{7}{20} i \operatorname{Sin}[c] \right) + \\
 i \operatorname{Csc}[c] (640 A \operatorname{Cos}[c] + 240 i B \operatorname{Cos}[c] + 343 i A \operatorname{Sin}[c] - 223 B \operatorname{Sin}[c]) \\
 \left. \left( \frac{1}{120} \operatorname{Cos}[3 c] + \frac{1}{120} i \operatorname{Sin}[3 c] \right) + (A + i B) \operatorname{Cos}[6 dx] \left( -\frac{1}{40} \operatorname{Cos}[3 c] + \frac{1}{40} i \operatorname{Sin}[3 c] \right) + \right. \\
 \operatorname{Csc}[c + dx]^2 \left( -\frac{2}{3} A \operatorname{Cos}[3 c] - \frac{2}{3} i A \operatorname{Sin}[3 c] \right) + (11 A + 6 i B) \left( \frac{7}{20} i \operatorname{Cos}[c] - \frac{7 \operatorname{Sin}[c]}{20} \right) \\
 \operatorname{Sin}[2 dx] + (21 A + 16 i B) \left( \frac{1}{60} i \operatorname{Cos}[c] + \frac{\operatorname{Sin}[c]}{60} \right) \operatorname{Sin}[4 dx] + \\
 (A + i B) \left( \frac{1}{40} i \operatorname{Cos}[3 c] + \frac{1}{40} \operatorname{Sin}[3 c] \right) \operatorname{Sin}[6 dx] + \\
 \frac{2}{3} \operatorname{Csc}[c] \operatorname{Csc}[c + dx] \left( 4 A \operatorname{Cos}[3 c - dx] + \frac{3}{2} i B \operatorname{Cos}[3 c - dx] - \right. \\
 4 A \operatorname{Cos}[3 c + dx] - \frac{3}{2} i B \operatorname{Cos}[3 c + dx] + 4 i A \operatorname{Sin}[3 c - dx] - \frac{3}{2} B \operatorname{Sin}[3 c - dx] - \\
 \left. \left. 4 i A \operatorname{Sin}[3 c + dx] + \frac{3}{2} B \operatorname{Sin}[3 c + dx] \right) \right) \sqrt{\operatorname{Tan}[c + dx]} (A + B \operatorname{Tan}[c + dx])$$

Problem 196: Attempted integration timed out after 120 seconds.

$$\int (a + i a \operatorname{Tan}[c + dx])^{1/3} (A + B \operatorname{Tan}[c + dx]) dx$$

Optimal (type 3, 201 leaves, 6 steps):

$$-\frac{a^{1/3} (A - i B) x}{2 \times 2^{2/3}} - \frac{\sqrt{3} a^{1/3} (i A + B) \operatorname{ArcTan}\left[\frac{a^{1/3+2/3} (a + i a \operatorname{Tan}[c + dx])^{1/3}}{\sqrt{3} a^{1/3}}\right]}{2^{2/3} d} + \\
 \frac{a^{1/3} (i A + B) \operatorname{Log}[\operatorname{Cos}[c + dx]]}{2 \times 2^{2/3} d} + \\
 \frac{3 a^{1/3} (i A + B) \operatorname{Log}\left[2^{1/3} a^{1/3} - (a + i a \operatorname{Tan}[c + dx])^{1/3}\right]}{2 \times 2^{2/3} d} + \frac{3 B (a + i a \operatorname{Tan}[c + dx])^{1/3}}{d}$$

Result (type 1, 1 leaves):

???

**Problem 197: Result unnecessarily involves higher level functions.**

$$\int \tan [c+d x]^2 (a+i a \tan [c+d x])^{2 / 3}(A+B \tan [c+d x]) d x$$

Optimal (type 3, 270 leaves, 8 steps):

$$\frac{a^{2 / 3}(A-i B) x}{2 \times 2^{1 / 3}}-\frac{\sqrt{3} a^{2 / 3}(i A+B) \operatorname{ArcTan}\left[\frac{a^{1 / 3}+2^{2 / 3}(a+i a \tan [c+d x])^{1 / 3}}{\sqrt{3} a^{1 / 3}}\right]}{2^{1 / 3} d}-\frac{a^{2 / 3}(i A+B) \operatorname{Log}[\operatorname{Cos}[c+d x]]}{2 \times 2^{1 / 3} d}-\frac{3 a^{2 / 3}(i A+B) \operatorname{Log}\left[2^{1 / 3} a^{1 / 3}-\left(a+i a \tan [c+d x]\right)^{1 / 3}\right]}{2 \times 2^{1 / 3} d}-\frac{9 B(a+i a \tan [c+d x])^{2 / 3}}{8 d}+\frac{3 B \tan [c+d x]^2(a+i a \tan [c+d x])^{2 / 3}}{8 d}-\frac{3(4 i A+B)\left(a+i a \tan [c+d x]\right)^{5 / 3}}{20 a d}$$

Result (type 5, 109 leaves):

$$\frac{1}{40 d} 3(a+i a \tan [c+d x])^{2 / 3}\left(-8 i A-22 B+10(i A+B)\left(1+e^{2 i(c+d x)}\right)^{2 / 3} \operatorname{Hypergeometric2F1}\left[\frac{2}{3}, \frac{2}{3}, \frac{5}{3},-e^{2 i(c+d x)}\right]+5 B \operatorname{Sec}[c+d x]^2+(8 A-2 i B) \tan [c+d x]\right)$$

**Problem 198: Result unnecessarily involves higher level functions.**

$$\int \tan [c+d x](a+i a \tan [c+d x])^{2 / 3}(A+B \tan [c+d x]) d x$$

Optimal (type 3, 232 leaves, 7 steps):

$$\frac{a^{2 / 3}(i A+B) x}{2 \times 2^{1 / 3}}+\frac{\sqrt{3} a^{2 / 3}(A-i B) \operatorname{ArcTan}\left[\frac{a^{1 / 3}+2^{2 / 3}(a+i a \tan [c+d x])^{1 / 3}}{\sqrt{3} a^{1 / 3}}\right]}{2^{1 / 3} d}+\frac{a^{2 / 3}(A-i B) \operatorname{Log}[\operatorname{Cos}[c+d x]]}{2 \times 2^{1 / 3} d}+\frac{3 a^{2 / 3}(A-i B) \operatorname{Log}\left[2^{1 / 3} a^{1 / 3}-\left(a+i a \tan [c+d x]\right)^{1 / 3}\right]}{2 \times 2^{1 / 3} d}+\frac{3 A(a+i a \tan [c+d x])^{2 / 3}}{2 d}-\frac{3 i B(a+i a \tan [c+d x])^{5 / 3}}{5 a d}$$

Result (type 5, 120 leaves):



$$\left( 3 \left( e^{i d x} \right)^{2/3} \left( a + i a \tan [c + d x] \right)^{2/3} \right. \\ \left. \left( 10 A - 4 i B - 5 (A - i B) \left( 1 + e^{2 i (c+d x)} \right)^{2/3} \text{Hypergeometric2F1} \left[ \frac{2}{3}, \frac{2}{3}, \frac{5}{3}, -e^{2 i (c+d x)} \right] + \right. \right. \\ \left. \left. 4 B \tan [c + d x] \right) \right) / \left( 20 d \left( \cos [d x] + i \sin [d x] \right)^{2/3} \right)$$

**Problem 199: Result unnecessarily involves higher level functions.**

$$\int \left( a + i a \tan [c + d x] \right)^{2/3} \left( A + B \tan [c + d x] \right) dx$$

Optimal (type 3, 202 leaves, 6 steps):

$$-\frac{a^{2/3} (A - i B) x}{2 \times 2^{1/3}} + \frac{\sqrt{3} a^{2/3} (i A + B) \text{ArcTan} \left[ \frac{a^{1/3} + 2^{2/3} (a + i a \tan [c + d x])^{1/3}}{\sqrt{3} a^{1/3}} \right]}{2^{1/3} d} + \\ \frac{a^{2/3} (i A + B) \text{Log} [\cos [c + d x]]}{2 \times 2^{1/3} d} + \\ \frac{3 a^{2/3} (i A + B) \text{Log} [2^{1/3} a^{1/3} - (a + i a \tan [c + d x])^{1/3}]}{2 \times 2^{1/3} d} + \frac{3 B (a + i a \tan [c + d x])^{2/3}}{2 d}$$

Result (type 5, 96 leaves):

$$-\frac{1}{2 \times 2^{1/3} d} \\ 3 \left( \frac{a e^{2 i (c+d x)}}{1 + e^{2 i (c+d x)}} \right)^{2/3} \left( -2 B + (i A + B) \left( 1 + e^{2 i (c+d x)} \right)^{2/3} \text{Hypergeometric2F1} \left[ \frac{2}{3}, \frac{2}{3}, \frac{5}{3}, -e^{2 i (c+d x)} \right] \right)$$

**Problem 200: Unable to integrate problem.**

$$\int \cot [c + d x] \left( a + i a \tan [c + d x] \right)^{2/3} \left( A + B \tan [c + d x] \right) dx$$

Optimal (type 3, 289 leaves, 11 steps):

$$-\frac{a^{2/3} (i A + B) x}{2 \times 2^{1/3}} + \frac{\sqrt{3} a^{2/3} A \text{ArcTan} \left[ \frac{a^{1/3} + 2 (a + i a \tan [c + d x])^{1/3}}{\sqrt{3} a^{1/3}} \right]}{d} - \\ \frac{\sqrt{3} a^{2/3} (A - i B) \text{ArcTan} \left[ \frac{a^{1/3} + 2^{2/3} (a + i a \tan [c + d x])^{1/3}}{\sqrt{3} a^{1/3}} \right]}{2^{1/3} d} - \frac{a^{2/3} (A - i B) \text{Log} [\cos [c + d x]]}{2 \times 2^{1/3} d} - \\ \frac{a^{2/3} A \text{Log} [\tan [c + d x]]}{2 d} + \frac{3 a^{2/3} A \text{Log} [a^{1/3} - (a + i a \tan [c + d x])^{1/3}]}{2 d} - \\ \frac{3 a^{2/3} (A - i B) \text{Log} [2^{1/3} a^{1/3} - (a + i a \tan [c + d x])^{1/3}]}{2 \times 2^{1/3} d}$$

Result (type 8, 36 leaves):

$$\int \cot [c + d x] \left( a + i a \tan [c + d x] \right)^{2/3} \left( A + B \tan [c + d x] \right) dx$$

**Problem 201: Unable to integrate problem.**

$$\int \text{Cot}[c + d x]^2 (a + i a \text{Tan}[c + d x])^{2/3} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 342 leaves, 12 steps):

$$\frac{a^{2/3} (A - i B) x}{2 \times 2^{1/3}} + \frac{a^{2/3} (2 i A + 3 B) \text{ArcTan}\left[\frac{a^{1/3} + 2 (a + i a \text{Tan}[c + d x])^{1/3}}{\sqrt{3} a^{1/3}}\right]}{\sqrt{3} d} - \frac{\sqrt{3} a^{2/3} (i A + B) \text{ArcTan}\left[\frac{a^{1/3} + 2^{2/3} (a + i a \text{Tan}[c + d x])^{1/3}}{\sqrt{3} a^{1/3}}\right]}{2^{1/3} d} - \frac{a^{2/3} (i A + B) \text{Log}[\text{Cos}[c + d x]]}{2 \times 2^{1/3} d} - \frac{a^{2/3} (2 i A + 3 B) \text{Log}[\text{Tan}[c + d x]]}{6 d} + \frac{a^{2/3} (2 i A + 3 B) \text{Log}\left[a^{1/3} - (a + i a \text{Tan}[c + d x])^{1/3}\right]}{2 d} - \frac{3 a^{2/3} (i A + B) \text{Log}\left[2^{1/3} a^{1/3} - (a + i a \text{Tan}[c + d x])^{1/3}\right]}{2 \times 2^{1/3} d} - \frac{A \text{Cot}[c + d x] (a + i a \text{Tan}[c + d x])^{2/3}}{d}$$

Result (type 8, 38 leaves):

$$\int \text{Cot}[c + d x]^2 (a + i a \text{Tan}[c + d x])^{2/3} (A + B \text{Tan}[c + d x]) dx$$

**Problem 202: Result unnecessarily involves higher level functions.**

$$\int \frac{A + B \text{Tan}[c + d x]}{(a + i a \text{Tan}[c + d x])^{1/3}} dx$$

Optimal (type 3, 213 leaves, 6 steps):

$$-\frac{(A - i B) x}{4 \times 2^{1/3} a^{1/3}} + \frac{\sqrt{3} (i A + B) \text{ArcTan}\left[\frac{a^{1/3} + 2^{2/3} (a + i a \text{Tan}[c + d x])^{1/3}}{\sqrt{3} a^{1/3}}\right]}{2 \times 2^{1/3} a^{1/3} d} + \frac{(i A + B) \text{Log}[\text{Cos}[c + d x]]}{4 \times 2^{1/3} a^{1/3} d} + \frac{3 (i A + B) \text{Log}\left[2^{1/3} a^{1/3} - (a + i a \text{Tan}[c + d x])^{1/3}\right]}{4 \times 2^{1/3} a^{1/3} d} + \frac{3 (i A - B)}{2 d (a + i a \text{Tan}[c + d x])^{1/3}}$$

Result (type 5, 142 leaves):

$$-\frac{1}{4 \times 2^{1/3} a d} 3 i e^{-2 i (c + d x)} \left(\frac{a e^{2 i (c + d x)}}{1 + e^{2 i (c + d x)}}\right)^{2/3} \left(-2 (A + i B) (1 + e^{2 i (c + d x)}) + (A - i B) e^{2 i (c + d x)} (1 + e^{2 i (c + d x)})^{2/3} \text{Hypergeometric2F1}\left[\frac{2}{3}, \frac{2}{3}, \frac{5}{3}, -e^{2 i (c + d x)}\right]\right)$$

**Problem 203: Unable to integrate problem.**

$$\int \frac{A + B \text{Tan}[c + d x]}{(a + i a \text{Tan}[c + d x])^{2/3}} dx$$

Optimal (type 3, 213 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{(A - i B) x}{4 \times 2^{2/3} a^{2/3}} - \frac{\sqrt{3} (i A + B) \operatorname{ArcTan}\left[\frac{a^{1/3} + 2^{2/3} (a + i a \operatorname{Tan}[c + d x])^{1/3}}{\sqrt{3} a^{1/3}}\right]}{2 \times 2^{2/3} a^{2/3} d} + \frac{(i A + B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{4 \times 2^{2/3} a^{2/3} d} + \\
 & \frac{3 (i A + B) \operatorname{Log}\left[2^{1/3} a^{1/3} - (a + i a \operatorname{Tan}[c + d x])^{1/3}\right]}{4 \times 2^{2/3} a^{2/3} d} + \frac{3 (i A - B)}{4 d (a + i a \operatorname{Tan}[c + d x])^{2/3}}
 \end{aligned}$$

Result (type 8, 30 leaves):

$$\int \frac{A + B \operatorname{Tan}[c + d x]}{(a + i a \operatorname{Tan}[c + d x])^{2/3}} dx$$

Problem 204: Unable to integrate problem.

$$\int \operatorname{Tan}[c + d x]^m (a + i a \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 5, 290 leaves, 7 steps):

$$\begin{aligned}
 & - \left( (2 a^4 (A (64 + 60 m + 19 m^2 + 2 m^3) - i B (67 + 60 m + 19 m^2 + 2 m^3)) \operatorname{Tan}[c + d x]^{1+m}) / \right. \\
 & \quad \left. (d (1 + m) (2 + m) (3 + m) (4 + m)) \right) + \frac{1}{d (1 + m)} \\
 & 8 a^4 (A - i B) \operatorname{Hypergeometric2F1}[1, 1 + m, 2 + m, i \operatorname{Tan}[c + d x]] \operatorname{Tan}[c + d x]^{1+m} + \\
 & \frac{i a B \operatorname{Tan}[c + d x]^{1+m} (a + i a \operatorname{Tan}[c + d x])^3}{d (4 + m)} - \\
 & \frac{(A (4 + m) - i B (7 + m)) \operatorname{Tan}[c + d x]^{1+m} (a^2 + i a^2 \operatorname{Tan}[c + d x])^2}{d (3 + m) (4 + m)} - \\
 & \frac{(2 (A (4 + m)^2 - i B (19 + 8 m + m^2)) \operatorname{Tan}[c + d x]^{1+m} (a^4 + i a^4 \operatorname{Tan}[c + d x]))}{(d (2 + m) (3 + m) (4 + m))} /
 \end{aligned}$$

Result (type 8, 36 leaves):

$$\int \operatorname{Tan}[c + d x]^m (a + i a \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) dx$$

Problem 205: Unable to integrate problem.

$$\int \operatorname{Tan}[c + d x]^m (a + i a \operatorname{Tan}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 5, 205 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{a^3 (A (15 + 11 m + 2 m^2) - i B (17 + 11 m + 2 m^2)) \operatorname{Tan}[c + d x]^{1+m}}{d (1 + m) (2 + m) (3 + m)} + \frac{1}{d (1 + m)} \\
 & 4 a^3 (A - i B) \operatorname{Hypergeometric2F1}[1, 1 + m, 2 + m, i \operatorname{Tan}[c + d x]] \operatorname{Tan}[c + d x]^{1+m} + \\
 & \frac{i a B \operatorname{Tan}[c + d x]^{1+m} (a + i a \operatorname{Tan}[c + d x])^2}{d (3 + m)} - \\
 & \frac{(A (3 + m) - i B (5 + m)) \operatorname{Tan}[c + d x]^{1+m} (a^3 + i a^3 \operatorname{Tan}[c + d x])}{d (2 + m) (3 + m)}
 \end{aligned}$$

Result (type 8, 36 leaves):

$$\int \tan [c + d x]^m (a + i a \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

Problem 206: Unable to integrate problem.

$$\int \tan [c + d x]^m (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) dx$$

Optimal (type 5, 132 leaves, 5 steps):

$$\frac{i a^2 (B + (i A + B) (2 + m)) \tan [c + d x]^{1+m}}{d (1 + m) (2 + m)} + \frac{1}{d (1 + m)}$$

$$2 a^2 (A - i B) \text{Hypergeometric2F1}[1, 1 + m, 2 + m, i \tan [c + d x]] \tan [c + d x]^{1+m} +$$

$$\frac{i B \tan [c + d x]^{1+m} (a^2 + i a^2 \tan [c + d x])}{d (2 + m)}$$

Result (type 8, 36 leaves):

$$\int \tan [c + d x]^m (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) dx$$

Problem 207: Unable to integrate problem.

$$\int \tan [c + d x]^m (a + i a \tan [c + d x]) (A + B \tan [c + d x]) dx$$

Optimal (type 5, 70 leaves, 3 steps):

$$\frac{i a B \tan [c + d x]^{1+m}}{d (1 + m)} + \frac{1}{d (1 + m)}$$

$$a (A - i B) \text{Hypergeometric2F1}[1, 1 + m, 2 + m, i \tan [c + d x]] \tan [c + d x]^{1+m}$$

Result (type 8, 34 leaves):

$$\int \tan [c + d x]^m (a + i a \tan [c + d x]) (A + B \tan [c + d x]) dx$$

Problem 208: Unable to integrate problem.

$$\int \frac{\tan [c + d x]^m (A + B \tan [c + d x])}{a + i a \tan [c + d x]} dx$$

Optimal (type 5, 168 leaves, 6 steps):

$$\frac{1}{2 a d (1+m)} \left( A (1-m) - i B (1+m) \right) \text{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{1+m} +$$

$$\frac{1}{2 a d (2+m)} \left( i A - B \right) m \text{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{2+m} +$$

$$\frac{(A+i B) \text{Tan}[c+d x]^{1+m}}{2 d (a+i a \text{Tan}[c+d x])}$$

Result (type 8, 36 leaves):

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{a+i a \text{Tan}[c+d x]} dx$$

Problem 209: Unable to integrate problem.

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{(a+i a \text{Tan}[c+d x])^2} dx$$

Optimal (type 5, 226 leaves, 7 steps):

$$\frac{1}{4 a^2 d (1+m)} (1-m) \left( A (1-m) - i B (1+m) \right) \text{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{1+m} +$$

$$\frac{(A(2-m) - i B m) \text{Tan}[c+d x]^{1+m}}{4 a^2 d (1+i \text{Tan}[c+d x])} + \frac{1}{4 a^2 d (2+m)}$$

$$m (i A (2-m) + B m) \text{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{2+m} +$$

$$\frac{(A+i B) \text{Tan}[c+d x]^{1+m}}{4 d (a+i a \text{Tan}[c+d x])^2}$$

Result (type 8, 36 leaves):

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{(a+i a \text{Tan}[c+d x])^2} dx$$

Problem 210: Attempted integration timed out after 120 seconds.

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{(a+i a \text{Tan}[c+d x])^3} dx$$

Optimal (type 5, 308 leaves, 8 steps):

$$\begin{aligned}
 & -\frac{1}{24 a^3 d (1+m)} (1-m) (i B (3+m-2 m^2) - A (3-7 m+2 m^2)) \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{1+m} + \frac{1}{24 a^3 d (2+m)} \\
 & (2-m) m (B+i A (5-2 m)+2 B m) \text{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, -\text{Tan}[c+d x]^2\right] \\
 & \quad \text{Tan}[c+d x]^{2+m} + \frac{(A+i B) \text{Tan}[c+d x]^{1+m}}{6 d (a+i a \text{Tan}[c+d x])^3} + \\
 & \quad \frac{(i B (1-2 m)+A (7-2 m)) \text{Tan}[c+d x]^{1+m}}{24 a d (a+i a \text{Tan}[c+d x])^2} + \frac{(2-m) (A (5-2 m)-i (B+2 B m)) \text{Tan}[c+d x]^{1+m}}{24 d (a^3+i a^3 \text{Tan}[c+d x])}
 \end{aligned}$$

Result(type 1, 1 leaves):

???

### Problem 211: Attempted integration timed out after 120 seconds.

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{(a+i a \text{Tan}[c+d x])^4} dx$$

Optimal (type 5, 386 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{48 a^4 d (1+m)} (3-4 m+m^2) (i B (1-m^2) - A (1-4 m+m^2)) \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{1+m} - \\
 & \quad \frac{(i B (1+3 m-m^2) - A (13-7 m+m^2)) \text{Tan}[c+d x]^{1+m}}{48 a^4 d (1+i \text{Tan}[c+d x])^2} - \\
 & \quad \frac{(2-m) (i B (2+2 m-m^2) - A (8-6 m+m^2)) \text{Tan}[c+d x]^{1+m}}{48 a^4 d (1+i \text{Tan}[c+d x])} + \\
 & \quad \frac{1}{48 a^4 d (2+m)} (2-m) m (B (2+2 m-m^2) +i A (8-6 m+m^2)) \\
 & \quad \text{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{2+m} + \\
 & \quad \frac{(A+i B) \text{Tan}[c+d x]^{1+m}}{8 d (a+i a \text{Tan}[c+d x])^4} + \frac{(i B (1-m)+A (5-m)) \text{Tan}[c+d x]^{1+m}}{24 a d (a+i a \text{Tan}[c+d x])^3}
 \end{aligned}$$

Result(type 1, 1 leaves):

???

### Problem 212: Unable to integrate problem.

$$\int \text{Tan}[c+d x]^m (a+i a \text{Tan}[c+d x])^{5/2} (A+B \text{Tan}[c+d x]) dx$$

Optimal (type 6, 316 leaves, 9 steps):

$$\begin{aligned} & \left( 4 a^3 (A - i B) \operatorname{AppellF1}\left[1 + m, \frac{1}{2}, 1, 2 + m, -i \operatorname{Tan}[c + d x], i \operatorname{Tan}[c + d x]\right] \right. \\ & \quad \left. \sqrt{1 + i \operatorname{Tan}[c + d x]} \operatorname{Tan}[c + d x]^{1+m} \right) / \left( d (1 + m) \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) + \\ & \left( 2 a^2 (2 B (19 + 17 m + 4 m^2) + i A (35 + 34 m + 8 m^2)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, -m, \frac{3}{2}, \right. \right. \\ & \quad \left. \left. 1 + i \operatorname{Tan}[c + d x]\right] (-i \operatorname{Tan}[c + d x])^{-m} \operatorname{Tan}[c + d x]^m \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) / \\ & \left( d (3 + 2 m) (5 + 2 m) \right) + \frac{2 a^2 (2 i B (4 + m) - A (5 + 2 m)) \operatorname{Tan}[c + d x]^{1+m} \sqrt{a + i a \operatorname{Tan}[c + d x]}}{d (3 + 2 m) (5 + 2 m)} + \\ & \frac{2 i a B \operatorname{Tan}[c + d x]^{1+m} (a + i a \operatorname{Tan}[c + d x])^{3/2}}{d (5 + 2 m)} \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \operatorname{Tan}[c + d x]^m (a + i a \operatorname{Tan}[c + d x])^{5/2} (A + B \operatorname{Tan}[c + d x]) dx$$

**Problem 213: Unable to integrate problem.**

$$\int \operatorname{Tan}[c + d x]^m (a + i a \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 6, 227 leaves, 8 steps):

$$\begin{aligned} & \left( 2 a^2 (A - i B) \operatorname{AppellF1}\left[1 + m, \frac{1}{2}, 1, 2 + m, -i \operatorname{Tan}[c + d x], i \operatorname{Tan}[c + d x]\right] \right. \\ & \quad \left. \sqrt{1 + i \operatorname{Tan}[c + d x]} \operatorname{Tan}[c + d x]^{1+m} \right) / \left( d (1 + m) \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) + \frac{1}{d (3 + 2 m)} \\ & 2 a (B + (i A + B) (3 + 2 m)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, -m, \frac{3}{2}, 1 + i \operatorname{Tan}[c + d x]\right] (-i \operatorname{Tan}[c + d x])^{-m} \\ & \operatorname{Tan}[c + d x]^m \sqrt{a + i a \operatorname{Tan}[c + d x]} + \frac{2 i a B \operatorname{Tan}[c + d x]^{1+m} \sqrt{a + i a \operatorname{Tan}[c + d x]}}{d (3 + 2 m)} \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \operatorname{Tan}[c + d x]^m (a + i a \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x]) dx$$

**Problem 214: Unable to integrate problem.**

$$\int \operatorname{Tan}[c + d x]^m \sqrt{a + i a \operatorname{Tan}[c + d x]} (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 6, 159 leaves, 7 steps):

$$\left( a (A - i B) \operatorname{AppellF1}\left[1 + m, \frac{1}{2}, 1, 2 + m, -i \operatorname{Tan}[c + d x], i \operatorname{Tan}[c + d x]\right] \sqrt{1 + i \operatorname{Tan}[c + d x]} \operatorname{Tan}[c + d x]^{1+m} \right) / \left( d (1 + m) \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) + \frac{1}{d} 2 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, -m, \frac{3}{2}, 1 + i \operatorname{Tan}[c + d x]\right] (-i \operatorname{Tan}[c + d x])^{-m} \operatorname{Tan}[c + d x]^m \sqrt{a + i a \operatorname{Tan}[c + d x]}$$

Result (type 8, 38 leaves):

$$\int \operatorname{Tan}[c + d x]^m \sqrt{a + i a \operatorname{Tan}[c + d x]} (A + B \operatorname{Tan}[c + d x]) dx$$

Problem 215: Attempted integration timed out after 120 seconds.

$$\int \frac{\operatorname{Tan}[c + d x]^m (A + B \operatorname{Tan}[c + d x])}{\sqrt{a + i a \operatorname{Tan}[c + d x]}} dx$$

Optimal (type 6, 214 leaves, 8 steps):

$$\frac{(A + i B) \operatorname{Tan}[c + d x]^{1+m}}{d \sqrt{a + i a \operatorname{Tan}[c + d x]}} + \left( (A - i B) \operatorname{AppellF1}\left[1 + m, \frac{1}{2}, 1, 2 + m, -i \operatorname{Tan}[c + d x], i \operatorname{Tan}[c + d x]\right] \sqrt{1 + i \operatorname{Tan}[c + d x]} \operatorname{Tan}[c + d x]^{1+m} \right) / \left( 2 d (1 + m) \sqrt{a + i a \operatorname{Tan}[c + d x]} \right) + \frac{1}{a d} (i A - B) (1 + 2 m) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, -m, \frac{3}{2}, 1 + i \operatorname{Tan}[c + d x]\right] (-i \operatorname{Tan}[c + d x])^{-m} \operatorname{Tan}[c + d x]^m \sqrt{a + i a \operatorname{Tan}[c + d x]}$$

Result (type 1, 1 leaves):

???

Problem 216: Unable to integrate problem.

$$\int \frac{\operatorname{Tan}[c + d x]^m (A + B \operatorname{Tan}[c + d x])}{(a + i a \operatorname{Tan}[c + d x])^{3/2}} dx$$

Optimal (type 6, 285 leaves, 9 steps):



$$\frac{(A + i B) \tan [c + d x]^{1+m}}{3 d (a + i a \tan [c + d x])^{3/2}} + \frac{(A (5 - 4 m) - i (B + 4 B m)) \tan [c + d x]^{1+m}}{6 a d \sqrt{a + i a \tan [c + d x]}} +$$

$$\left( (A - i B) \operatorname{AppellF1} \left[ 1 + m, \frac{1}{2}, 1, 2 + m, -i \tan [c + d x], i \tan [c + d x] \right] \right.$$

$$\left. \sqrt{1 + i \tan [c + d x]} \tan [c + d x]^{1+m} \right) / \left( 4 a d (1 + m) \sqrt{a + i a \tan [c + d x]} \right) + \frac{1}{6 a^2 d}$$

$$(1 + 2 m) (B + i A (5 - 4 m) + 4 B m) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, -m, \frac{3}{2}, 1 + i \tan [c + d x] \right]$$

$$(-i \tan [c + d x])^{-m} \tan [c + d x]^m \sqrt{a + i a \tan [c + d x]}$$

Result (type 8, 38 leaves):

$$\int \frac{\tan [c + d x]^m (A + B \tan [c + d x])}{(a + i a \tan [c + d x])^{3/2}} dx$$

Problem 217: Unable to integrate problem.

$$\int \frac{\tan [c + d x]^m (A + B \tan [c + d x])}{(a + i a \tan [c + d x])^{5/2}} dx$$

Optimal (type 6, 363 leaves, 10 steps):

$$\frac{(A + i B) \tan [c + d x]^{1+m}}{5 d (a + i a \tan [c + d x])^{5/2}} + \frac{(i B (1 - 4 m) + A (11 - 4 m)) \tan [c + d x]^{1+m}}{30 a d (a + i a \tan [c + d x])^{3/2}} -$$

$$\frac{(i B (13 + 12 m - 16 m^2) - A (37 - 52 m + 16 m^2)) \tan [c + d x]^{1+m}}{60 a^2 d \sqrt{a + i a \tan [c + d x]}} +$$

$$\left( (A - i B) \operatorname{AppellF1} \left[ 1 + m, \frac{1}{2}, 1, 2 + m, -i \tan [c + d x], i \tan [c + d x] \right] \right.$$

$$\left. \sqrt{1 + i \tan [c + d x]} \tan [c + d x]^{1+m} \right) / \left( 8 a^2 d (1 + m) \sqrt{a + i a \tan [c + d x]} \right) +$$

$$\frac{1}{60 a^3 d} (1 + 2 m) (B (13 + 12 m - 16 m^2) + i A (37 - 52 m + 16 m^2)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \right.$$

$$\left. -m, \frac{3}{2}, 1 + i \tan [c + d x] \right] (-i \tan [c + d x])^{-m} \tan [c + d x]^m \sqrt{a + i a \tan [c + d x]}$$

Result (type 8, 38 leaves):

$$\int \frac{\tan [c + d x]^m (A + B \tan [c + d x])}{(a + i a \tan [c + d x])^{5/2}} dx$$

Problem 218: Unable to integrate problem.

$$\int \tan [c + d x]^m (a + i a \tan [c + d x])^n (A + B \tan [c + d x]) dx$$

Optimal (type 6, 167 leaves, 7 steps):

$$\frac{1}{d(1+m)} (A - i B) \text{AppellF1}[1+m, 1-n, 1, 2+m, -i \tan[c+dx], i \tan[c+dx]]$$

$$(1+i \tan[c+dx])^{-n} \tan[c+dx]^{1+m} (a+i a \tan[c+dx])^n +$$

$$\frac{1}{d(1+m)} i B \text{Hypergeometric2F1}[1+m, 1-n, 2+m, -i \tan[c+dx]]$$

$$(1+i \tan[c+dx])^{-n} \tan[c+dx]^{1+m} (a+i a \tan[c+dx])^n$$

Result (type 8, 36 leaves):

$$\int \tan[c+dx]^m (a+i a \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

### Problem 219: Unable to integrate problem.

$$\int \tan[c+dx]^3 (a+i a \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

Optimal (type 5, 245 leaves, 6 steps):

$$\frac{2(i B n - A(3+n))(a+i a \tan[c+dx])^n}{d n(2+n)(3+n)} + \frac{1}{2 d n}$$

$$(A - i B) \text{Hypergeometric2F1}\left[1, n, 1+n, \frac{1}{2}(1+i \tan[c+dx])\right] (a+i a \tan[c+dx])^n -$$

$$\frac{(i B n - A(3+n)) \tan[c+dx]^2 (a+i a \tan[c+dx])^n}{d(2+n)(3+n)} +$$

$$\frac{B \tan[c+dx]^3 (a+i a \tan[c+dx])^n}{d(3+n)} - \frac{(A n(3+n) - i B(6+3n+n^2))(a+i a \tan[c+dx])^{1+n}}{a d(1+n)(2+n)(3+n)}$$

Result (type 8, 36 leaves):

$$\int \tan[c+dx]^3 (a+i a \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

### Problem 220: Unable to integrate problem.

$$\int \tan[c+dx]^2 (a+i a \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

Optimal (type 5, 164 leaves, 5 steps):

$$-\frac{2 B (a+i a \tan[c+dx])^n}{d n(2+n)} + \frac{1}{2 d n}$$

$$(i A + B) \text{Hypergeometric2F1}\left[1, n, 1+n, \frac{1}{2}(1+i \tan[c+dx])\right] (a+i a \tan[c+dx])^n +$$

$$\frac{B \tan[c+dx]^2 (a+i a \tan[c+dx])^n}{d(2+n)} - \frac{(B n + i A(2+n))(a+i a \tan[c+dx])^{1+n}}{a d(1+n)(2+n)}$$

Result (type 8, 36 leaves):

$$\int \tan [c+d x]^2 (a+i a \tan [c+d x])^n (A+B \tan [c+d x]) d x$$

**Problem 221: Result more than twice size of optimal antiderivative.**

$$\int \tan [c+d x] (a+i a \tan [c+d x])^n (A+B \tan [c+d x]) d x$$

Optimal (type 5, 111 leaves, 4 steps):

$$\frac{A (a+i a \tan [c+d x])^n}{d n} - \frac{1}{2 d n} (A-i B) \operatorname{Hypergeometric2F1}\left[1, n, 1+n, \frac{1}{2} (1+i \tan [c+d x])\right] (a+i a \tan [c+d x])^n - \frac{i B (a+i a \tan [c+d x])^{1+n}}{a d (1+n)}$$

Result (type 5, 295 leaves):

$$\left( 2^{-1+n} e^{-2 i d n x} (e^{i d x})^n \left( \frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}} \right)^n \left( -\frac{2 i B e^{2 i (c+d x+d n x)}}{(1+e^{2 i (c+d x)}) (1+n)} + \frac{1}{n} (A+i B) e^{2 i d n x} (1+e^{2 i (c+d x)})^n \operatorname{Hypergeometric2F1}\left[n, 2+n, 1+n, -e^{2 i (c+d x)}\right] - \frac{1}{2+n} (A-i B) e^{2 i (2 c+d (2+n) x)} (1+e^{2 i (c+d x)})^n \operatorname{Hypergeometric2F1}\left[2+n, 2+n, 3+n, -e^{2 i (c+d x)}\right] \right) \left. \right) / \left( d (A \cos [c+d x] + B \sin [c+d x]) \right)$$

**Problem 222: Result more than twice size of optimal antiderivative.**

$$\int (a+i a \tan [c+d x])^n (A+B \tan [c+d x]) d x$$

Optimal (type 5, 78 leaves, 3 steps):

$$\frac{B (a+i a \tan [c+d x])^n}{d n} - \frac{1}{2 d n} (i A+B) \operatorname{Hypergeometric2F1}\left[1, n, 1+n, \frac{1}{2} (1+i \tan [c+d x])\right] (a+i a \tan [c+d x])^n$$

Result (type 5, 171 leaves):

$$\frac{1}{d n (1+n)} 2^{-1+n} (e^{i d x})^n \left( \frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}} \right)^n \left( (-i A+B) (1+n) - i (A-i B) e^{2 i (c+d x)} (1+e^{2 i (c+d x)})^n n \operatorname{Hypergeometric2F1}\left[1+n, 1+n, 2+n, -e^{2 i (c+d x)}\right] \right) \left. \right) \operatorname{Sec}[c+d x]^{-n} (\cos [d x] + i \sin [d x])^{-n} (a+i a \tan [c+d x])^n$$

### Problem 223: Unable to integrate problem.

$$\int \text{Cot}[c + d x] (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 5, 97 leaves, 5 steps):

$$\frac{1}{2 d n} (A - i B) \text{Hypergeometric2F1}\left[1, n, 1 + n, \frac{1}{2} (1 + i \text{Tan}[c + d x])\right] (a + i a \text{Tan}[c + d x])^n - \frac{1}{d n} A \text{Hypergeometric2F1}\left[1, n, 1 + n, 1 + i \text{Tan}[c + d x]\right] (a + i a \text{Tan}[c + d x])^n$$

Result (type 8, 34 leaves):

$$\int \text{Cot}[c + d x] (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

### Problem 224: Unable to integrate problem.

$$\int \text{Cot}[c + d x]^2 (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 5, 131 leaves, 6 steps):

$$- \frac{A \text{Cot}[c + d x] (a + i a \text{Tan}[c + d x])^n}{d} + \frac{1}{2 d n} (i A + B) \text{Hypergeometric2F1}\left[1, n, 1 + n, \frac{1}{2} (1 + i \text{Tan}[c + d x])\right] (a + i a \text{Tan}[c + d x])^n - \frac{1}{d n} (B + i A n) \text{Hypergeometric2F1}\left[1, n, 1 + n, 1 + i \text{Tan}[c + d x]\right] (a + i a \text{Tan}[c + d x])^n$$

Result (type 8, 36 leaves):

$$\int \text{Cot}[c + d x]^2 (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

### Problem 225: Unable to integrate problem.

$$\int \text{Cot}[c + d x]^3 (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 5, 185 leaves, 7 steps):

$$- \frac{(2 B + i A n) \text{Cot}[c + d x] (a + i a \text{Tan}[c + d x])^n}{2 d} - \frac{A \text{Cot}[c + d x]^2 (a + i a \text{Tan}[c + d x])^n}{2 d} - \frac{1}{2 d n} (A - i B) \text{Hypergeometric2F1}\left[1, n, 1 + n, \frac{1}{2} (1 + i \text{Tan}[c + d x])\right] (a + i a \text{Tan}[c + d x])^n - \frac{1}{2 d n} (2 i B n - A (2 - n + n^2)) \text{Hypergeometric2F1}\left[1, n, 1 + n, 1 + i \text{Tan}[c + d x]\right] (a + i a \text{Tan}[c + d x])^n$$

Result (type 8, 36 leaves):

$$\int \text{Cot}[c + d x]^3 (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

### Problem 226: Unable to integrate problem.

$$\int \tan[c + dx]^{5/2} (a + ia \tan[c + dx])^n (A + B \tan[c + dx]) dx$$

Optimal (type 6, 383 leaves, 11 steps):

$$\begin{aligned} & - \left( \left( 2 (2 ia n (5 + 2n) + B (15 + 10n + 4n^2)) \sqrt{\tan[c + dx]} (a + ia \tan[c + dx])^n \right) / \right. \\ & \quad \left. (d (1 + 2n) (3 + 2n) (5 + 2n)) \right) + \frac{1}{d} \\ & 2 (ia + B) \operatorname{AppellF1} \left[ \frac{1}{2}, 1 - n, 1, \frac{3}{2}, -ia \tan[c + dx], ia \tan[c + dx] \right] \\ & (1 + ia \tan[c + dx])^{-n} \sqrt{\tan[c + dx]} (a + ia \tan[c + dx])^n - \\ & \left( 2 (4Bn (9 + 8n + 2n^2) + ia (15 + 36n + 32n^2 + 8n^3)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 - n, \frac{3}{2}, \right. \right. \\ & \quad \left. \left. -ia \tan[c + dx] \right] (1 + ia \tan[c + dx])^{-n} \sqrt{\tan[c + dx]} (a + ia \tan[c + dx])^n \right) / \\ & (d (1 + 2n) (3 + 2n) (5 + 2n)) - \frac{2 (2 ia B n - A (5 + 2n)) \tan[c + dx]^{3/2} (a + ia \tan[c + dx])^n}{d (3 + 2n) (5 + 2n)} + \\ & \frac{2B \tan[c + dx]^{5/2} (a + ia \tan[c + dx])^n}{d (5 + 2n)} \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \tan[c + dx]^{5/2} (a + ia \tan[c + dx])^n (A + B \tan[c + dx]) dx$$

### Problem 227: Unable to integrate problem.

$$\int \tan[c + dx]^{3/2} (a + ia \tan[c + dx])^n (A + B \tan[c + dx]) dx$$

Optimal (type 6, 291 leaves, 10 steps):

$$\begin{aligned} & \frac{2 (2 ia B n - A (3 + 2n)) \sqrt{\tan[c + dx]} (a + ia \tan[c + dx])^n}{d (1 + 2n) (3 + 2n)} - \\ & \frac{1}{d} 2 (A - ia B) \operatorname{AppellF1} \left[ \frac{1}{2}, 1 - n, 1, \frac{3}{2}, -ia \tan[c + dx], ia \tan[c + dx] \right] \\ & (1 + ia \tan[c + dx])^{-n} \sqrt{\tan[c + dx]} (a + ia \tan[c + dx])^n + \\ & \left( 2 (2A n (3 + 2n) - ia B (3 + 6n + 4n^2)) \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, 1 - n, \frac{3}{2}, \right. \right. \\ & \quad \left. \left. -ia \tan[c + dx] \right] (1 + ia \tan[c + dx])^{-n} \sqrt{\tan[c + dx]} (a + ia \tan[c + dx])^n \right) / \\ & (d (1 + 2n) (3 + 2n)) + \frac{2B \tan[c + dx]^{3/2} (a + ia \tan[c + dx])^n}{d (3 + 2n)} \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \text{Tan}[c + d x]^{3/2} (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

**Problem 228: Unable to integrate problem.**

$$\int \sqrt{\text{Tan}[c + d x]} (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 6, 215 leaves, 9 steps):

$$\frac{2 B \sqrt{\text{Tan}[c + d x]} (a + i a \text{Tan}[c + d x])^n}{d (1 + 2 n)} - \frac{1}{d}$$

$$2 (i A + B) \text{AppellF1}\left[\frac{1}{2}, 1 - n, 1, \frac{3}{2}, -i \text{Tan}[c + d x], i \text{Tan}[c + d x]\right]$$

$$(1 + i \text{Tan}[c + d x])^{-n} \sqrt{\text{Tan}[c + d x]} (a + i a \text{Tan}[c + d x])^n + \frac{1}{d (1 + 2 n)}$$

$$2 (2 B n + i A (1 + 2 n)) \text{Hypergeometric2F1}\left[\frac{1}{2}, 1 - n, \frac{3}{2}, -i \text{Tan}[c + d x]\right]$$

$$(1 + i \text{Tan}[c + d x])^{-n} \sqrt{\text{Tan}[c + d x]} (a + i a \text{Tan}[c + d x])^n$$

Result (type 8, 38 leaves):

$$\int \sqrt{\text{Tan}[c + d x]} (a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x]) dx$$

**Problem 229: Unable to integrate problem.**

$$\int \frac{(a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x])}{\sqrt{\text{Tan}[c + d x]}} dx$$

Optimal (type 6, 158 leaves, 8 steps):

$$\frac{1}{d} 2 (A - i B) \text{AppellF1}\left[\frac{1}{2}, 1 - n, 1, \frac{3}{2}, -i \text{Tan}[c + d x], i \text{Tan}[c + d x]\right] (1 + i \text{Tan}[c + d x])^{-n}$$

$$\sqrt{\text{Tan}[c + d x]} (a + i a \text{Tan}[c + d x])^n + \frac{1}{d} 2 i B \text{Hypergeometric2F1}\left[\frac{1}{2}, 1 - n, \frac{3}{2}, -i \text{Tan}[c + d x]\right]$$

$$(1 + i \text{Tan}[c + d x])^{-n} \sqrt{\text{Tan}[c + d x]} (a + i a \text{Tan}[c + d x])^n$$

Result (type 8, 38 leaves):

$$\int \frac{(a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x])}{\sqrt{\text{Tan}[c + d x]}} dx$$

**Problem 230: Unable to integrate problem.**

$$\int \frac{(a + i a \text{Tan}[c + d x])^n (A + B \text{Tan}[c + d x])}{\text{Tan}[c + d x]^{3/2}} dx$$

Optimal (type 6, 194 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{2A(a+ia\tan[c+dx])^n}{d\sqrt{\tan[c+dx]}} + \frac{1}{d}2(iA+B)\operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, -i\tan[c+dx], i\tan[c+dx]\right] \\
 & (1+i\tan[c+dx])^{-n}\sqrt{\tan[c+dx]}(a+ia\tan[c+dx])^n - \\
 & \frac{1}{d}2iA(1-2n)\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, -i\tan[c+dx]\right] \\
 & (1+i\tan[c+dx])^{-n}\sqrt{\tan[c+dx]}(a+ia\tan[c+dx])^n
 \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \frac{(a+ia\tan[c+dx])^n(A+B\tan[c+dx])}{\tan[c+dx]^{3/2}} dx$$

**Problem 231: Unable to integrate problem.**

$$\int \frac{(a+ia\tan[c+dx])^n(A+B\tan[c+dx])}{\tan[c+dx]^{5/2}} dx$$

Optimal (type 6, 247 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{2A(a+ia\tan[c+dx])^n}{3d\tan[c+dx]^{3/2}} - \frac{2(3B+2iAn)(a+ia\tan[c+dx])^n}{3d\sqrt{\tan[c+dx]}} - \\
 & \frac{1}{d}2(A-iB)\operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, -i\tan[c+dx], i\tan[c+dx]\right] \\
 & (1+i\tan[c+dx])^{-n}\sqrt{\tan[c+dx]}(a+ia\tan[c+dx])^n - \frac{1}{3d} \\
 & 2(1-2n)(3iB-2An)\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, -i\tan[c+dx]\right] \\
 & (1+i\tan[c+dx])^{-n}\sqrt{\tan[c+dx]}(a+ia\tan[c+dx])^n
 \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \frac{(a+ia\tan[c+dx])^n(A+B\tan[c+dx])}{\tan[c+dx]^{5/2}} dx$$

**Problem 240: Result more than twice size of optimal antiderivative.**

$$\int \tan[c+dx]^2(a+b\tan[c+dx])^2(A+B\tan[c+dx]) dx$$

Optimal (type 3, 148 leaves, 5 steps):

$$\begin{aligned}
 & -(a^2A-Ab^2-2abB)x + \frac{(2aAb+a^2B-b^2B)\operatorname{Log}[\operatorname{Cos}[c+dx]]}{d} - \frac{b(Ab+aB)\tan[c+dx]}{d} - \\
 & \frac{B(a+b\tan[c+dx])^2}{2d} + \frac{(4Ab-aB)(a+b\tan[c+dx])^3}{12b^2d} + \frac{B\tan[c+dx](a+b\tan[c+dx])^3}{4bd}
 \end{aligned}$$

Result (type 3, 560 leaves):

$$\begin{aligned} & \left( (2 a A b + a^2 B - 2 b^2 B) \cos [c + d x] (a + b \tan [c + d x])^2 (A + B \tan [c + d x]) \right) / \\ & \left( 2 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) - \\ & \left( (a^2 A - A b^2 - 2 a b B) (c + d x) \cos [c + d x]^3 (a + b \tan [c + d x])^2 (A + B \tan [c + d x]) \right) / \\ & \left( d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\ & \left( (2 a A b + a^2 B - b^2 B) \cos [c + d x]^3 \log [\cos [c + d x]] (a + b \tan [c + d x])^2 (A + B \tan [c + d x]) \right) / \\ & \left( d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\ & \frac{b^2 B \sec [c + d x] (a + b \tan [c + d x])^2 (A + B \tan [c + d x])}{4 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x])} + \\ & \left( \cos [c + d x]^2 (3 a^2 A \sin [c + d x] - 4 A b^2 \sin [c + d x] - 8 a b B \sin [c + d x]) (a + b \tan [c + d x])^2 \right. \\ & \left. (A + B \tan [c + d x]) \right) / \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\ & \left( (A b^2 \sin [c + d x] + 2 a b B \sin [c + d x]) (a + b \tan [c + d x])^2 (A + B \tan [c + d x]) \right) / \\ & \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) \end{aligned}$$

**Problem 247: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^5 (a + b \tan [c + d x])^2 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 151 leaves, 6 steps):

$$\begin{aligned} & (2 a A b + a^2 B - b^2 B) x - \frac{(b^2 B - a (2 A b + a B)) \cot [c + d x]}{d} + \frac{(a^2 A - A b^2 - 2 a b B) \cot [c + d x]^2}{2 d} - \\ & \frac{a (2 A b + a B) \cot [c + d x]^3}{3 d} - \frac{a^2 A \cot [c + d x]^4}{4 d} + \frac{(a^2 A - A b^2 - 2 a b B) \log [\sin [c + d x]]}{d} \end{aligned}$$

Result (type 3, 561 leaves):

$$\begin{aligned} & \left( (-2 a A b \cos [c + d x] - a^2 B \cos [c + d x]) (b + a \cot [c + d x])^2 (B + A \cot [c + d x]) \right) / \\ & \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) - \\ & \frac{a^2 A (b + a \cot [c + d x])^2 (B + A \cot [c + d x]) \csc [c + d x]}{4 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x])} + \\ & \left( (2 a^2 A - A b^2 - 2 a b B) (b + a \cot [c + d x])^2 (B + A \cot [c + d x]) \sin [c + d x] \right) / \\ & \left( 2 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\ & \left( (8 a A b \cos [c + d x] + 4 a^2 B \cos [c + d x] - 3 b^2 B \cos [c + d x]) \right. \\ & \left. (b + a \cot [c + d x])^2 (B + A \cot [c + d x]) \sin [c + d x]^2 \right) / \\ & \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\ & \left( (2 a A b + a^2 B - b^2 B) (c + d x) (b + a \cot [c + d x])^2 (B + A \cot [c + d x]) \sin [c + d x]^3 \right) / \\ & \left( d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\ & \left( (a^2 A - A b^2 - 2 a b B) (b + a \cot [c + d x])^2 (B + A \cot [c + d x]) \log [\sin [c + d x]] \sin [c + d x]^3 \right) / \\ & \left( d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) \end{aligned}$$



### Problem 248: Result more than twice size of optimal antiderivative.

$$\int \tan [c+d x]^2 (a+b \tan [c+d x])^3 (A+B \tan [c+d x]) d x$$

Optimal (type 3, 201 leaves, 6 steps):

$$\begin{aligned} & -\left(a^3 A-3 a A b^2-3 a^2 b B+b^3 B\right) x+\frac{\left(3 a^2 A b-A b^3+a^3 B-3 a b^2 B\right) \operatorname{Log}[\operatorname{Cos}[c+d x]]}{d}- \\ & \frac{b\left(2 a A b+a^2 B-b^2 B\right) \tan [c+d x]}{d}-\frac{(A b+a B)(a+b \tan [c+d x])^2}{2 d}-\frac{B(a+b \tan [c+d x])^3}{3 d}+ \\ & \frac{(5 A b-a B)(a+b \tan [c+d x])^4}{20 b^2 d}+\frac{B \tan [c+d x](a+b \tan [c+d x])^4}{5 b d} \end{aligned}$$

Result (type 3, 680 leaves):

$$\begin{aligned} & \left(\left(3 a^2 A b-A b^3+a^3 B-3 a b^2 B\right) \operatorname{Cos}[c+d x]^4\right. \\ & \quad \left.\operatorname{Log}[\operatorname{Cos}[c+d x]](a+b \tan [c+d x])^3(A+B \tan [c+d x])\right) / \\ & \left(d(a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^3(A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x])\right)+ \\ & \left(1 / \left(240 d(a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^3(A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x])\right)\right) \\ & \operatorname{Sec}[c+d x]\left(270 a^2 A b \operatorname{Cos}[c+d x]-120 A b^3 \operatorname{Cos}[c+d x]+90 a^3 B \operatorname{Cos}[c+d x]-\right. \\ & \quad 360 a b^2 B \operatorname{Cos}[c+d x]-150 a^3 A(c+d x) \operatorname{Cos}[c+d x]+450 a A b^2(c+d x) \operatorname{Cos}[c+d x]+ \\ & \quad 450 a^2 b B(c+d x) \operatorname{Cos}[c+d x]-150 b^3 B(c+d x) \operatorname{Cos}[c+d x]+90 a^2 A b \operatorname{Cos}[3(c+d x)]- \\ & \quad 60 A b^3 \operatorname{Cos}[3(c+d x)]+30 a^3 B \operatorname{Cos}[3(c+d x)]-180 a b^2 B \operatorname{Cos}[3(c+d x)]- \\ & \quad 75 a^3 A(c+d x) \operatorname{Cos}[3(c+d x)]+225 a A b^2(c+d x) \operatorname{Cos}[3(c+d x)]+ \\ & \quad 225 a^2 b B(c+d x) \operatorname{Cos}[3(c+d x)]-75 b^3 B(c+d x) \operatorname{Cos}[3(c+d x)]- \\ & \quad 15 a^3 A(c+d x) \operatorname{Cos}[5(c+d x)]+45 a A b^2(c+d x) \operatorname{Cos}[5(c+d x)]+ \\ & \quad 45 a^2 b B(c+d x) \operatorname{Cos}[5(c+d x)]-15 b^3 B(c+d x) \operatorname{Cos}[5(c+d x)]+ \\ & \quad 30 a^3 A \operatorname{Sin}[c+d x]-60 a A b^2 \operatorname{Sin}[c+d x]-60 a^2 b B \operatorname{Sin}[c+d x]+50 b^3 B \operatorname{Sin}[c+d x]+ \\ & \quad 45 a^3 A \operatorname{Sin}[3(c+d x)]-120 a A b^2 \operatorname{Sin}[3(c+d x)]-120 a^2 b B \operatorname{Sin}[3(c+d x)]+ \\ & \quad 25 b^3 B \operatorname{Sin}[3(c+d x)]+15 a^3 A \operatorname{Sin}[5(c+d x)]-60 a A b^2 \operatorname{Sin}[5(c+d x)]- \\ & \quad \left.60 a^2 b B \operatorname{Sin}[5(c+d x)]+23 b^3 B \operatorname{Sin}[5(c+d x)]\right)(a+b \tan [c+d x])^3(A+B \tan [c+d x]) \end{aligned}$$

### Problem 249: Result more than twice size of optimal antiderivative.

$$\int \tan [c+d x](a+b \tan [c+d x])^3(A+B \tan [c+d x]) d x$$

Optimal (type 3, 165 leaves, 5 steps):

$$\begin{aligned} & -\left(3 a^2 A b-A b^3+a^3 B-3 a b^2 B\right) x- \\ & \frac{\left(a^3 A-3 a A b^2-3 a^2 b B+b^3 B\right) \operatorname{Log}[\operatorname{Cos}[c+d x]]}{d}+\frac{b\left(a^2 A-A b^2-2 a b B\right) \tan [c+d x]}{d}+ \\ & \frac{(a A-b B)(a+b \tan [c+d x])^2}{2 d}+\frac{A(a+b \tan [c+d x])^3}{3 d}+\frac{B(a+b \tan [c+d x])^4}{4 b d} \end{aligned}$$

Result (type 3, 600 leaves):

$$\frac{b^3 B (a + b \tan [c + d x])^3 (A + B \tan [c + d x])}{4 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x])} -$$

$$\left( b (-3 a A b - 3 a^2 B + 2 b^2 B) \cos [c + d x]^2 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) /$$

$$\left( 2 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) -$$

$$\left( (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) (c + d x) \cos [c + d x]^4 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) /$$

$$\left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) +$$

$$\left( (-a^3 A + 3 a A b^2 + 3 a^2 b B - b^3 B) \cos [c + d x]^4 \log [\cos [c + d x]] (a + b \tan [c + d x])^3 \right.$$

$$\left. (A + B \tan [c + d x]) \right) / \left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) +$$

$$\left( \cos [c + d x]^3 (9 a^2 A b \sin [c + d x] - 4 A b^3 \sin [c + d x] + 3 a^3 B \sin [c + d x] - 12 a b^2 B \sin [c + d x]) \right.$$

$$\left. (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) /$$

$$\left( 3 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) +$$

$$\left( \cos [c + d x] (A b^3 \sin [c + d x] + 3 a b^2 B \sin [c + d x]) (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) /$$

$$\left( 3 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right)$$

**Problem 255: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^5 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 191 leaves, 6 steps):

$$(3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) x + \frac{(3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \cot [c + d x]}{d} +$$

$$\frac{a (2 a^2 A - 5 A b^2 - 6 a b B) \cot [c + d x]^2}{4 d} - \frac{a^2 (3 A b + 2 a B) \cot [c + d x]^3}{6 d} +$$

$$\frac{(a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \log [\sin [c + d x]]}{d} - \frac{a A \cot [c + d x]^4 (a + b \tan [c + d x])^2}{4 d}$$

Result (type 3, 598 leaves):

$$\begin{aligned}
 & - \left( \left( a^3 A (b + a \cot [c + d x])^3 (B + A \cot [c + d x]) \right) / \right. \\
 & \quad \left. \left( 4 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) \right) + \\
 & \left( (-3 a^2 A b \cos [c + d x] - a^3 B \cos [c + d x]) (b + a \cot [c + d x])^3 (B + A \cot [c + d x]) \sin [c + d x] \right) / \\
 & \quad \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( a (2 a^2 A - 3 A b^2 - 3 a b B) (b + a \cot [c + d x])^3 (B + A \cot [c + d x]) \sin [c + d x]^2 \right) / \\
 & \quad \left( 2 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (12 a^2 A b \cos [c + d x] - 3 A b^3 \cos [c + d x] + 4 a^3 B \cos [c + d x] - 9 a b^2 B \cos [c + d x]) \right. \\
 & \quad \left. (b + a \cot [c + d x])^3 (B + A \cot [c + d x]) \sin [c + d x]^3 \right) / \\
 & \quad \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) (c + d x) (b + a \cot [c + d x])^3 (B + A \cot [c + d x]) \sin [c + d x]^4 \right) / \\
 & \quad \left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) (b + a \cot [c + d x])^3 (B + A \cot [c + d x]) \log [\sin [c + d x]] \right. \\
 & \quad \left. \sin [c + d x]^4 \right) / \left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

**Problem 256: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^6 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 233 leaves, 7 steps):

$$\begin{aligned}
 & - (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) x - \\
 & \frac{(a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \cot [c + d x]}{d} + \frac{(3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \cot [c + d x]^2}{2 d} + \\
 & \frac{a (5 a^2 A - 12 A b^2 - 15 a b B) \cot [c + d x]^3}{15 d} - \frac{a^2 (7 A b + 5 a B) \cot [c + d x]^4}{20 d} + \\
 & \frac{(3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \log [\sin [c + d x]]}{d} - \frac{a A \cot [c + d x]^5 (a + b \tan [c + d x])^2}{5 d}
 \end{aligned}$$

Result (type 3, 680 leaves):

$$\begin{aligned} & \left( (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) (b + a \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \operatorname{Log}[\operatorname{Sin}[c + d x]] \right. \\ & \quad \left. \operatorname{Sin}[c + d x]^4 \right) / \left( d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \left( 1 / \left( 240 d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) \\ & \left( (b + a \operatorname{Cot}[c + d x])^3 (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] \right. \\ & \quad (-50 a^3 A \operatorname{Cos}[c + d x] + 60 a A b^2 \operatorname{Cos}[c + d x] + 60 a^2 b B \operatorname{Cos}[c + d x] - \\ & \quad 30 b^3 B \operatorname{Cos}[c + d x] + 25 a^3 A \operatorname{Cos}[3(c + d x)] - 120 a A b^2 \operatorname{Cos}[3(c + d x)] - \\ & \quad 120 a^2 b B \operatorname{Cos}[3(c + d x)] + 45 b^3 B \operatorname{Cos}[3(c + d x)] - 23 a^3 A \operatorname{Cos}[5(c + d x)] + \\ & \quad 60 a A b^2 \operatorname{Cos}[5(c + d x)] + 60 a^2 b B \operatorname{Cos}[5(c + d x)] - 15 b^3 B \operatorname{Cos}[5(c + d x)] + \\ & \quad 360 a^2 A b \operatorname{Sin}[c + d x] - 90 A b^3 \operatorname{Sin}[c + d x] + 120 a^3 B \operatorname{Sin}[c + d x] - \\ & \quad 270 a b^2 B \operatorname{Sin}[c + d x] - 150 a^3 A (c + d x) \operatorname{Sin}[c + d x] + 450 a A b^2 (c + d x) \operatorname{Sin}[c + d x] + \\ & \quad 450 a^2 b B (c + d x) \operatorname{Sin}[c + d x] - 150 b^3 B (c + d x) \operatorname{Sin}[c + d x] - 180 a^2 A b \operatorname{Sin}[3(c + d x)] + \\ & \quad 30 A b^3 \operatorname{Sin}[3(c + d x)] - 60 a^3 B \operatorname{Sin}[3(c + d x)] + 90 a b^2 B \operatorname{Sin}[3(c + d x)] + \\ & \quad 75 a^3 A (c + d x) \operatorname{Sin}[3(c + d x)] - 225 a A b^2 (c + d x) \operatorname{Sin}[3(c + d x)] - \\ & \quad 225 a^2 b B (c + d x) \operatorname{Sin}[3(c + d x)] + 75 b^3 B (c + d x) \operatorname{Sin}[3(c + d x)] - \\ & \quad 15 a^3 A (c + d x) \operatorname{Sin}[5(c + d x)] + 45 a A b^2 (c + d x) \operatorname{Sin}[5(c + d x)] + \\ & \quad \left. 45 a^2 b B (c + d x) \operatorname{Sin}[5(c + d x)] - 15 b^3 B (c + d x) \operatorname{Sin}[5(c + d x)] \right) \end{aligned}$$

**Problem 257: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Tan}[c + d x]^2 (a + b \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 263 leaves, 7 steps):

$$\begin{aligned} & - (a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) x + \\ & \frac{(4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{d} - \\ & \frac{b (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{Tan}[c + d x]}{d} - \frac{(2 a A b + a^2 B - b^2 B) (a + b \operatorname{Tan}[c + d x])^2}{2 d} - \\ & \frac{(A b + a B) (a + b \operatorname{Tan}[c + d x])^3}{3 d} - \frac{B (a + b \operatorname{Tan}[c + d x])^4}{4 d} + \\ & \frac{(6 A b - a B) (a + b \operatorname{Tan}[c + d x])^5}{30 b^2 d} + \frac{B \operatorname{Tan}[c + d x] (a + b \operatorname{Tan}[c + d x])^5}{6 b d} \end{aligned}$$

Result (type 3, 958 leaves):

$$\begin{aligned}
 & \left( (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) \right. \\
 & \quad \left. \cos [c+d x]^5 \log [\cos [c+d x]] (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) \right) / \\
 & \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( 1 / \left( 480 d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) \right) \\
 & \sec [c+d x] \left( 360 a^3 A b - 480 a A b^3 + 90 a^4 B - 720 a^2 b^2 B + 170 b^4 B - 150 a^4 A (c+d x) + \right. \\
 & \quad 900 a^2 A b^2 (c+d x) - 150 A b^4 (c+d x) + 600 a^3 b B (c+d x) - 600 a b^3 B (c+d x) + \\
 & \quad 480 a^3 A b \cos [2(c+d x)] - 720 a A b^3 \cos [2(c+d x)] + 120 a^4 B \cos [2(c+d x)] - \\
 & \quad 1080 a^2 b^2 B \cos [2(c+d x)] + 180 b^4 B \cos [2(c+d x)] - 225 a^4 A (c+d x) \cos [2(c+d x)] + \\
 & \quad 1350 a^2 A b^2 (c+d x) \cos [2(c+d x)] - 225 A b^4 (c+d x) \cos [2(c+d x)] + \\
 & \quad 900 a^3 b B (c+d x) \cos [2(c+d x)] - 900 a b^3 B (c+d x) \cos [2(c+d x)] + \\
 & \quad 120 a^3 A b \cos [4(c+d x)] - 240 a A b^3 \cos [4(c+d x)] + 30 a^4 B \cos [4(c+d x)] - \\
 & \quad 360 a^2 b^2 B \cos [4(c+d x)] + 90 b^4 B \cos [4(c+d x)] - 90 a^4 A (c+d x) \cos [4(c+d x)] + \\
 & \quad 540 a^2 A b^2 (c+d x) \cos [4(c+d x)] - 90 A b^4 (c+d x) \cos [4(c+d x)] + \\
 & \quad 360 a^3 b B (c+d x) \cos [4(c+d x)] - 360 a b^3 B (c+d x) \cos [4(c+d x)] - \\
 & \quad 15 a^4 A (c+d x) \cos [6(c+d x)] + 90 a^2 A b^2 (c+d x) \cos [6(c+d x)] - \\
 & \quad 15 A b^4 (c+d x) \cos [6(c+d x)] + 60 a^3 b B (c+d x) \cos [6(c+d x)] - \\
 & \quad 60 a b^3 B (c+d x) \cos [6(c+d x)] + 75 a^4 A \sin [2(c+d x)] - 360 a^2 A b^2 \sin [2(c+d x)] + \\
 & \quad 75 A b^4 \sin [2(c+d x)] - 240 a^3 b B \sin [2(c+d x)] + 300 a b^3 B \sin [2(c+d x)] + \\
 & \quad 60 a^4 A \sin [4(c+d x)] - 360 a^2 A b^2 \sin [4(c+d x)] + 48 A b^4 \sin [4(c+d x)] - \\
 & \quad 240 a^3 b B \sin [4(c+d x)] + 192 a b^3 B \sin [4(c+d x)] + 15 a^4 A \sin [6(c+d x)] - \\
 & \quad 120 a^2 A b^2 \sin [6(c+d x)] + 23 A b^4 \sin [6(c+d x)] - 80 a^3 b B \sin [6(c+d x)] + \\
 & \quad \left. 92 a b^3 B \sin [6(c+d x)] \right) (a+b \tan [c+d x])^4 (A+B \tan [c+d x])
 \end{aligned}$$

### Problem 258: Result more than twice size of optimal antiderivative.

$$\int \tan [c+d x] (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) dx$$

Optimal (type 3, 226 leaves, 6 steps):

$$\begin{aligned}
 & - (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) x - \\
 & \frac{(a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) \log [\cos [c+d x]]}{d} + \\
 & \frac{b (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \tan [c+d x]}{d} + \frac{(a^2 A - A b^2 - 2 a b B) (a+b \tan [c+d x])^2}{2 d} + \\
 & \frac{(a A - b B) (a+b \tan [c+d x])^3}{3 d} + \frac{A (a+b \tan [c+d x])^4}{4 d} + \frac{B (a+b \tan [c+d x])^5}{5 b d}
 \end{aligned}$$

Result (type 3, 803 leaves):

$$\begin{aligned} & \left( (-a^4 A + 6 a^2 A b^2 - A b^4 + 4 a^3 b B - 4 a b^3 B) \right. \\ & \quad \left. \text{Cos}[c + d x]^5 \text{Log}[\text{Cos}[c + d x]] (a + b \text{Tan}[c + d x])^4 (A + B \text{Tan}[c + d x]) \right) / \\ & \left( d (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) + \\ & \left( 1 / \left( 240 d (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^4 (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \right) \right) \\ & \left( 540 a^2 A b^2 \text{Cos}[c + d x] - 120 A b^4 \text{Cos}[c + d x] + 360 a^3 b B \text{Cos}[c + d x] - \right. \\ & \quad 480 a b^3 B \text{Cos}[c + d x] - 600 a^3 A b (c + d x) \text{Cos}[c + d x] + 600 a A b^3 (c + d x) \text{Cos}[c + d x] - \\ & \quad 150 a^4 B (c + d x) \text{Cos}[c + d x] + 900 a^2 b^2 B (c + d x) \text{Cos}[c + d x] - \\ & \quad 150 b^4 B (c + d x) \text{Cos}[c + d x] + 180 a^2 A b^2 \text{Cos}[3(c + d x)] - 60 A b^4 \text{Cos}[3(c + d x)] + \\ & \quad 120 a^3 b B \text{Cos}[3(c + d x)] - 240 a b^3 B \text{Cos}[3(c + d x)] - 300 a^3 A b (c + d x) \text{Cos}[3(c + d x)] + \\ & \quad 300 a A b^3 (c + d x) \text{Cos}[3(c + d x)] - 75 a^4 B (c + d x) \text{Cos}[3(c + d x)] + \\ & \quad 450 a^2 b^2 B (c + d x) \text{Cos}[3(c + d x)] - 75 b^4 B (c + d x) \text{Cos}[3(c + d x)] - \\ & \quad 60 a^3 A b (c + d x) \text{Cos}[5(c + d x)] + 60 a A b^3 (c + d x) \text{Cos}[5(c + d x)] - \\ & \quad 15 a^4 B (c + d x) \text{Cos}[5(c + d x)] + 90 a^2 b^2 B (c + d x) \text{Cos}[5(c + d x)] - \\ & \quad 15 b^4 B (c + d x) \text{Cos}[5(c + d x)] + 120 a^3 A b \text{Sin}[c + d x] - 80 a A b^3 \text{Sin}[c + d x] + \\ & \quad 30 a^4 B \text{Sin}[c + d x] - 120 a^2 b^2 B \text{Sin}[c + d x] + 50 b^4 B \text{Sin}[c + d x] + 180 a^3 A b \text{Sin}[3(c + d x)] - \\ & \quad 160 a A b^3 \text{Sin}[3(c + d x)] + 45 a^4 B \text{Sin}[3(c + d x)] - 240 a^2 b^2 B \text{Sin}[3(c + d x)] + \\ & \quad 25 b^4 B \text{Sin}[3(c + d x)] + 60 a^3 A b \text{Sin}[5(c + d x)] - 80 a A b^3 \text{Sin}[5(c + d x)] + \\ & \quad \left. 15 a^4 B \text{Sin}[5(c + d x)] - 120 a^2 b^2 B \text{Sin}[5(c + d x)] + 23 b^4 B \text{Sin}[5(c + d x)] \right) \\ & (a + b \text{Tan}[c + d x])^4 (A + B \text{Tan}[c + d x]) \end{aligned}$$

**Problem 259: Result more than twice size of optimal antiderivative.**

$$\int (a + b \text{Tan}[c + d x])^4 (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 202 leaves, 5 steps):

$$\begin{aligned} & (a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) x - \\ & \frac{(4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) \text{Log}[\text{Cos}[c + d x]]}{d} + \\ & \frac{b (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \text{Tan}[c + d x]}{d} + \frac{(2 a A b + a^2 B - b^2 B) (a + b \text{Tan}[c + d x])^2}{2 d} + \\ & \frac{(A b + a B) (a + b \text{Tan}[c + d x])^3}{3 d} + \frac{B (a + b \text{Tan}[c + d x])^4}{4 d} \end{aligned}$$

Result (type 3, 626 leaves):

$$\frac{b^4 B \cos [c+d x] (a+b \tan [c+d x])^4 (A+B \tan [c+d x])}{4 d (a \cos [c+d x]+b \sin [c+d x])^4 (A \cos [c+d x]+B \sin [c+d x])} -$$

$$\left( b^2 (-2 a A b-3 a^2 B+b^2 B) \cos [c+d x]^3 (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) \right) /$$

$$\left( d (a \cos [c+d x]+b \sin [c+d x])^4 (A \cos [c+d x]+B \sin [c+d x]) \right) +$$

$$\left( (a^4 A-6 a^2 A b^2+A b^4-4 a^3 b B+4 a b^3 B) (c+d x) \cos [c+d x]^5 (a+b \tan [c+d x])^4 \right.$$

$$\left. (A+B \tan [c+d x]) \right) / \left( d (a \cos [c+d x]+b \sin [c+d x])^4 (A \cos [c+d x]+B \sin [c+d x]) \right) +$$

$$\left( (-4 a^3 A b+4 a A b^3-a^4 B+6 a^2 b^2 B-b^4 B) \cos [c+d x]^5 \log [\cos [c+d x]] (a+b \tan [c+d x])^4 \right.$$

$$\left. (A+B \tan [c+d x]) \right) / \left( d (a \cos [c+d x]+b \sin [c+d x])^4 (A \cos [c+d x]+B \sin [c+d x]) \right) +$$

$$\left( 2 \cos [c+d x]^4 (9 a^2 A b^2 \sin [c+d x]-2 A b^4 \sin [c+d x]+6 a^3 b B \sin [c+d x]- \right.$$

$$\left. 8 a b^3 B \sin [c+d x]) (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) \right) /$$

$$\left( 3 d (a \cos [c+d x]+b \sin [c+d x])^4 (A \cos [c+d x]+B \sin [c+d x]) \right) +$$

$$\left( \cos [c+d x]^2 (A b^4 \sin [c+d x]+4 a b^3 B \sin [c+d x]) (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) \right) /$$

$$\left( 3 d (a \cos [c+d x]+b \sin [c+d x])^4 (A \cos [c+d x]+B \sin [c+d x]) \right)$$

### Problem 260: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x] (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) dx$$

Optimal (type 3, 172 leaves, 6 steps):

$$(4 a^3 A b-4 a A b^3+a^4 B-6 a^2 b^2 B+b^4 B) x - \frac{b (6 a^2 A b-A b^3+4 a^3 B-4 a b^2 B) \log [\cos [c+d x]]}{d} +$$

$$\frac{a^4 A \log [\sin [c+d x]]}{d} + \frac{b^2 (3 a A b+3 a^2 B-b^2 B) \tan [c+d x]}{d} +$$

$$\frac{b (A b+2 a B) (a+b \tan [c+d x])^2}{2 d} + \frac{b B (a+b \tan [c+d x])^3}{3 d}$$

Result (type 3, 590 leaves):

$$\begin{aligned}
 & \frac{b^3 (A b + 4 a B) \cos [c + d x]^3 (a + b \tan [c + d x])^4 (A + B \tan [c + d x])}{2 d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x])} + \\
 & \left( (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) (c + d x) \cos [c + d x]^5 (a + b \tan [c + d x])^4 \right. \\
 & \quad \left. (A + B \tan [c + d x]) \right) / \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (-6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) \cos [c + d x]^5 \operatorname{Log}[\cos [c + d x]] (a + b \tan [c + d x])^4 \right. \\
 & \quad \left. (A + B \tan [c + d x]) \right) / \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( a^4 A \cos [c + d x]^5 \operatorname{Log}[\sin [c + d x]] (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) \right) / \\
 & \quad \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( b^4 B \cos [c + d x]^2 \sin [c + d x] (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) \right) / \\
 & \quad \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) - \\
 & \left( 2 \cos [c + d x]^4 (-6 a A b^3 \sin [c + d x] - 9 a^2 b^2 B \sin [c + d x] + 2 b^4 B \sin [c + d x]) \right. \\
 & \quad \left. (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) \right) / \\
 & \quad \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

**Problem 261: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^2 (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 175 leaves, 6 steps):

$$\begin{aligned}
 & - (a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) x - \frac{b^2 (4 a A b + 6 a^2 B - b^2 B) \operatorname{Log}[\cos [c + d x]]}{d} + \\
 & \frac{a^3 (4 A b + a B) \operatorname{Log}[\sin [c + d x]]}{d} + \frac{b^2 (a^2 A + A b^2 + 3 a b B) \tan [c + d x]}{d} + \\
 & \frac{b (2 a A + b B) (a + b \tan [c + d x])^2}{2 d} - \frac{a A \cot [c + d x] (a + b \tan [c + d x])^3}{d}
 \end{aligned}$$

Result (type 3, 579 leaves):



$$\begin{aligned}
 & - \left( \left( a^4 A \cos [c+d x] (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \sin [c+d x]^4 \right) / \right. \\
 & \quad \left. \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) \right) - \\
 & \left( \left( a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B \right) (c+d x) (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \right. \\
 & \quad \left. \sin [c+d x]^5 \right) / \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( \left( -4 a A b^3 - 6 a^2 b^2 B + b^4 B \right) (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \log [\cos [c+d x]] \right. \\
 & \quad \left. \sin [c+d x]^5 \right) / \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( \left( 4 a^3 A b + a^4 B \right) (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \log [\sin [c+d x]] \sin [c+d x]^5 \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \sin [c+d x]^4 (A b^4 \sin [c+d x] + 4 a b^3 B \sin [c+d x]) \right. \\
 & \quad \left. \tan [c+d x] \right) / \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( b^4 B (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \sin [c+d x]^3 \tan [c+d x]^2 \right) / \\
 & \quad \left( 2 d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right)
 \end{aligned}$$

### Problem 262: Result more than twice size of optimal antiderivative.

$$\int \cot [c+d x]^3 (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) dx$$

Optimal (type 3, 186 leaves, 6 steps):

$$\begin{aligned}
 & - \left( 4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B \right) x - \frac{b^3 (A b + 4 a B) \log [\cos [c+d x]]}{d} - \\
 & \frac{a^2 (a^2 A - 6 A b^2 - 4 a b B) \log [\sin [c+d x]]}{d} + \frac{b^2 (3 a A b + a^2 B + b^2 B) \tan [c+d x]}{d} - \\
 & \frac{a (5 A b + 2 a B) \cot [c+d x] (a+b \tan [c+d x])^2}{2 d} - \frac{a A \cot [c+d x]^2 (a+b \tan [c+d x])^3}{2 d}
 \end{aligned}$$

Result (type 3, 567 leaves):

$$\begin{aligned}
 & - \left( \left( a^4 A (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \sin [c + d x]^3 \right) / \right. \\
 & \quad \left. \left( 2 d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) \right) + \\
 & \left( (-4 a^3 A b \cos [c + d x] - a^4 B \cos [c + d x]) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \sin [c + d x]^4 \right) / \\
 & \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) - \\
 & \left( 4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B \right) (c + d x) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \\
 & \quad \sin [c + d x]^5 \Big/ \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (-A b^4 - 4 a b^3 B) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \log [\cos [c + d x]] \sin [c + d x]^5 \right) / \\
 & \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (-a^4 A + 6 a^2 A b^2 + 4 a^3 b B) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \log [\sin [c + d x]] \right. \\
 & \quad \left. \sin [c + d x]^5 \right) / \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( b^4 B (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \sin [c + d x]^5 \tan [c + d x] \right) / \\
 & \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

**Problem 263: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^4 (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 187 leaves, 6 steps):

$$\begin{aligned}
 & (a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) x + \frac{a^2 (a^2 A - 3 A b^2 - 3 a b B) \cot [c + d x]}{d} - \\
 & \frac{b^4 B \log [\cos [c + d x]]}{d} - \frac{a (4 a^2 A b - 4 A b^3 + a^3 B - 6 a b^2 B) \log [\sin [c + d x]]}{d} - \\
 & \frac{a (2 A b + a B) \cot [c + d x]^2 (a + b \tan [c + d x])^2}{2 d} - \frac{a A \cot [c + d x]^3 (a + b \tan [c + d x])^3}{3 d}
 \end{aligned}$$

Result (type 3, 592 leaves):

$$\begin{aligned}
 & - \left( \left( a^4 A \cos [c+d x] (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \sin [c+d x]^2 \right) / \right. \\
 & \quad \left. \left( 3 d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) \right) - \\
 & \frac{a^3 (4 A b + a B) (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \sin [c+d x]^3}{2 d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x])} + \\
 & \frac{\left( 2 (2 a^4 A \cos [c+d x] - 9 a^2 A b^2 \cos [c+d x] - 6 a^3 b B \cos [c+d x]) \right.}{\left. (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \sin [c+d x]^4 \right) /} \\
 & \left( 3 d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B \right) (c+d x) (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \\
 & \sin [c+d x]^5 \Big/ \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) - \\
 & \left( b^4 B (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \log [\cos [c+d x]] \sin [c+d x]^5 \right) / \\
 & \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( -4 a^3 A b + 4 a A b^3 - a^4 B + 6 a^2 b^2 B \right) (b+a \cot [c+d x])^4 (B+A \cot [c+d x]) \log [\sin [c+d x]] \\
 & \sin [c+d x]^5 \Big/ \left( d (a \cos [c+d x] + b \sin [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]) \right)
 \end{aligned}$$

**Problem 264: Result more than twice size of optimal antiderivative.**

$$\int \cot [c+d x]^5 (a+b \tan [c+d x])^4 (A+B \tan [c+d x]) dx$$

Optimal (type 3, 225 leaves, 6 steps):

$$\begin{aligned}
 & (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) x + \\
 & \frac{a (24 a^2 A b - 19 A b^3 + 6 a^3 B - 34 a b^2 B) \cot [c+d x]}{6 d} + \frac{a^2 (6 a^2 A - 13 A b^2 - 16 a b B) \cot [c+d x]^2}{12 d} + \\
 & \frac{(a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) \log [\sin [c+d x]]}{d} - \\
 & \frac{a (7 A b + 4 a B) \cot [c+d x]^3 (a+b \tan [c+d x])^2}{12 d} - \frac{a A \cot [c+d x]^4 (a+b \tan [c+d x])^3}{4 d}
 \end{aligned}$$

Result (type 3, 624 leaves):

$$\begin{aligned}
 & - \left( \left( a^4 A (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \sin [c + d x] \right) / \right. \\
 & \quad \left. \left( 4 d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) \right) + \\
 & \left( (-4 a^3 A b \cos [c + d x] - a^4 B \cos [c + d x]) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \sin [c + d x]^2 \right) / \\
 & \quad \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( a^2 (a^2 A - 3 A b^2 - 2 a b B) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \sin [c + d x]^3 \right) / \\
 & \quad \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( 2 (8 a^3 A b \cos [c + d x] - 6 a A b^3 \cos [c + d x] + 2 a^4 B \cos [c + d x] - 9 a^2 b^2 B \cos [c + d x]) \right. \\
 & \quad \left. (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \sin [c + d x]^4 \right) / \\
 & \quad \left( 3 d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) (c + d x) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \right. \\
 & \quad \left. \sin [c + d x]^5 \right) / \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) (b + a \cot [c + d x])^4 (B + A \cot [c + d x]) \log [\sin [c + d x]] \right. \\
 & \quad \left. \sin [c + d x]^5 \right) / \left( d (a \cos [c + d x] + b \sin [c + d x])^4 (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

**Problem 265: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^6 (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 273 leaves, 7 steps):

$$\begin{aligned}
 & - (a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) x - \frac{(a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) \cot [c + d x]}{d} + \\
 & \frac{a (40 a^2 A b - 28 A b^3 + 10 a^3 B - 55 a b^2 B) \cot [c + d x]^2}{20 d} + \frac{a^2 (10 a^2 A - 18 A b^2 - 25 a b B) \cot [c + d x]^3}{30 d} + \\
 & \frac{(4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) \log [\sin [c + d x]]}{d} - \\
 & \frac{a (8 A b + 5 a B) \cot [c + d x]^4 (a + b \tan [c + d x])^2}{20 d} - \frac{a A \cot [c + d x]^5 (a + b \tan [c + d x])^3}{5 d}
 \end{aligned}$$

Result (type 3, 801 leaves):

$$\begin{aligned}
 & \left( (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) \right. \\
 & \quad \left. (b + a \operatorname{Cot}[c + d x])^4 (B + A \operatorname{Cot}[c + d x]) \operatorname{Log}[\operatorname{Sin}[c + d x]] \operatorname{Sin}[c + d x]^5 \right) / \\
 & \left( d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( 1 / \left( 240 d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) \\
 & \left( b + a \operatorname{Cot}[c + d x] \right)^4 (B + A \operatorname{Cot}[c + d x]) \\
 & (-50 a^4 A \operatorname{Cos}[c + d x] + 120 a^2 A b^2 \operatorname{Cos}[c + d x] - 30 A b^4 \operatorname{Cos}[c + d x] + 80 a^3 b B \operatorname{Cos}[c + d x] - \\
 & 120 a b^3 B \operatorname{Cos}[c + d x] + 25 a^4 A \operatorname{Cos}[3(c + d x)] - 240 a^2 A b^2 \operatorname{Cos}[3(c + d x)] + \\
 & 45 A b^4 \operatorname{Cos}[3(c + d x)] - 160 a^3 b B \operatorname{Cos}[3(c + d x)] + 180 a b^3 B \operatorname{Cos}[3(c + d x)] - \\
 & 23 a^4 A \operatorname{Cos}[5(c + d x)] + 120 a^2 A b^2 \operatorname{Cos}[5(c + d x)] - 15 A b^4 \operatorname{Cos}[5(c + d x)] + \\
 & 80 a^3 b B \operatorname{Cos}[5(c + d x)] - 60 a b^3 B \operatorname{Cos}[5(c + d x)] + 480 a^3 A b \operatorname{Sin}[c + d x] - \\
 & 360 a A b^3 \operatorname{Sin}[c + d x] + 120 a^4 B \operatorname{Sin}[c + d x] - 540 a^2 b^2 B \operatorname{Sin}[c + d x] - \\
 & 150 a^4 A (c + d x) \operatorname{Sin}[c + d x] + 900 a^2 A b^2 (c + d x) \operatorname{Sin}[c + d x] - 150 A b^4 (c + d x) \operatorname{Sin}[c + d x] + \\
 & 600 a^3 b B (c + d x) \operatorname{Sin}[c + d x] - 600 a b^3 B (c + d x) \operatorname{Sin}[c + d x] - 240 a^3 A b \operatorname{Sin}[3(c + d x)] + \\
 & 120 a A b^3 \operatorname{Sin}[3(c + d x)] - 60 a^4 B \operatorname{Sin}[3(c + d x)] + 180 a^2 b^2 B \operatorname{Sin}[3(c + d x)] + \\
 & 75 a^4 A (c + d x) \operatorname{Sin}[3(c + d x)] - 450 a^2 A b^2 (c + d x) \operatorname{Sin}[3(c + d x)] + \\
 & 75 A b^4 (c + d x) \operatorname{Sin}[3(c + d x)] - 300 a^3 b B (c + d x) \operatorname{Sin}[3(c + d x)] + \\
 & 300 a b^3 B (c + d x) \operatorname{Sin}[3(c + d x)] - 15 a^4 A (c + d x) \operatorname{Sin}[5(c + d x)] + \\
 & 90 a^2 A b^2 (c + d x) \operatorname{Sin}[5(c + d x)] - 15 A b^4 (c + d x) \operatorname{Sin}[5(c + d x)] + \\
 & 60 a^3 b B (c + d x) \operatorname{Sin}[5(c + d x)] - 60 a b^3 B (c + d x) \operatorname{Sin}[5(c + d x)] \left. \right)
 \end{aligned}$$

**Problem 266: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + d x]^7 (a + b \operatorname{Tan}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 323 leaves, 8 steps):

$$\begin{aligned}
 & - (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) x - \frac{(4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) \operatorname{Cot}[c + d x]}{d} - \\
 & \frac{(a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) \operatorname{Cot}[c + d x]^2}{2 d} + \\
 & \frac{a (20 a^2 A b - 13 A b^3 + 5 a^3 B - 27 a b^2 B) \operatorname{Cot}[c + d x]^3}{15 d} + \frac{a^2 (5 a^2 A - 8 A b^2 - 12 a b B) \operatorname{Cot}[c + d x]^4}{20 d} - \\
 & \frac{(a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{d} - \\
 & \frac{a (3 A b + 2 a B) \operatorname{Cot}[c + d x]^5 (a + b \operatorname{Tan}[c + d x])^2}{10 d} - \frac{a A \operatorname{Cot}[c + d x]^6 (a + b \operatorname{Tan}[c + d x])^3}{6 d}
 \end{aligned}$$

Result (type 3, 960 leaves):

$$\begin{aligned} & \left( (-a^4 A + 6 a^2 A b^2 - A b^4 + 4 a^3 b B - 4 a b^3 B) \right. \\ & \quad \left. (b + a \operatorname{Cot}[c + d x])^4 (B + A \operatorname{Cot}[c + d x]) \operatorname{Log}[\operatorname{Sin}[c + d x]] \operatorname{Sin}[c + d x]^5 \right) / \\ & \quad \left( d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \left( 1 / \left( 480 d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) \\ & \quad (b + a \operatorname{Cot}[c + d x])^4 (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] \\ & \quad (-170 a^4 A + 720 a^2 A b^2 - 90 A b^4 + 480 a^3 b B - 360 a b^3 B - 600 a^3 A b (c + d x) + \\ & \quad 600 a A b^3 (c + d x) - 150 a^4 B (c + d x) + 900 a^2 b^2 B (c + d x) - 150 b^4 B (c + d x) + \\ & \quad 180 a^4 A \operatorname{Cos}[2(c + d x)] - 1080 a^2 A b^2 \operatorname{Cos}[2(c + d x)] + 120 A b^4 \operatorname{Cos}[2(c + d x)] - \\ & \quad 720 a^3 b B \operatorname{Cos}[2(c + d x)] + 480 a b^3 B \operatorname{Cos}[2(c + d x)] + 900 a^3 A b (c + d x) \operatorname{Cos}[2(c + d x)] - \\ & \quad 900 a A b^3 (c + d x) \operatorname{Cos}[2(c + d x)] + 225 a^4 B (c + d x) \operatorname{Cos}[2(c + d x)] - \\ & \quad 1350 a^2 b^2 B (c + d x) \operatorname{Cos}[2(c + d x)] + 225 b^4 B (c + d x) \operatorname{Cos}[2(c + d x)] - \\ & \quad 90 a^4 A \operatorname{Cos}[4(c + d x)] + 360 a^2 A b^2 \operatorname{Cos}[4(c + d x)] - 30 A b^4 \operatorname{Cos}[4(c + d x)] + \\ & \quad 240 a^3 b B \operatorname{Cos}[4(c + d x)] - 120 a b^3 B \operatorname{Cos}[4(c + d x)] - 360 a^3 A b (c + d x) \operatorname{Cos}[4(c + d x)] + \\ & \quad 360 a A b^3 (c + d x) \operatorname{Cos}[4(c + d x)] - 90 a^4 B (c + d x) \operatorname{Cos}[4(c + d x)] + \\ & \quad 540 a^2 b^2 B (c + d x) \operatorname{Cos}[4(c + d x)] - 90 b^4 B (c + d x) \operatorname{Cos}[4(c + d x)] + \\ & \quad 60 a^3 A b (c + d x) \operatorname{Cos}[6(c + d x)] - 60 a A b^3 (c + d x) \operatorname{Cos}[6(c + d x)] + 15 a^4 B (c + d x) \\ & \quad \operatorname{Cos}[6(c + d x)] - 90 a^2 b^2 B (c + d x) \operatorname{Cos}[6(c + d x)] + 15 b^4 B (c + d x) \operatorname{Cos}[6(c + d x)] - \\ & \quad 300 a^3 A b \operatorname{Sin}[2(c + d x)] + 240 a A b^3 \operatorname{Sin}[2(c + d x)] - 75 a^4 B \operatorname{Sin}[2(c + d x)] + \\ & \quad 360 a^2 b^2 B \operatorname{Sin}[2(c + d x)] - 75 b^4 B \operatorname{Sin}[2(c + d x)] + 192 a^3 A b \operatorname{Sin}[4(c + d x)] - \\ & \quad 240 a A b^3 \operatorname{Sin}[4(c + d x)] + 48 a^4 B \operatorname{Sin}[4(c + d x)] - 360 a^2 b^2 B \operatorname{Sin}[4(c + d x)] + \\ & \quad 60 b^4 B \operatorname{Sin}[4(c + d x)] - 92 a^3 A b \operatorname{Sin}[6(c + d x)] + 80 a A b^3 \operatorname{Sin}[6(c + d x)] - \\ & \quad 23 a^4 B \operatorname{Sin}[6(c + d x)] + 120 a^2 b^2 B \operatorname{Sin}[6(c + d x)] - 15 b^4 B \operatorname{Sin}[6(c + d x)]) \end{aligned}$$

**Problem 268: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{a + b \operatorname{Tan}[c + d x]} dx$$

Optimal (type 3, 101 leaves, 5 steps):

$$-\frac{(aA + bB)x}{a^2 + b^2} - \frac{(Ab - aB) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{(a^2 + b^2)d} + \frac{a^2 (Ab - aB) \operatorname{Log}[a + b \operatorname{Tan}[c + d x]]}{b^2 (a^2 + b^2)d} + \frac{B \operatorname{Tan}[c + d x]}{bd}$$

Result (type 3, 203 leaves):

$$\begin{aligned} & \left( (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (A + B \operatorname{Tan}[c + d x]) (-a A b^2 c - b^3 B c - a A b^2 d x - b^3 B d x + \right. \\ & \quad (a^2 + b^2) (-A b + a B) \operatorname{Log}[\operatorname{Cos}[c + d x]] + a^2 A b \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] - \\ & \quad \left. a^3 B \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] + b (a^2 + b^2) B \operatorname{Tan}[c + d x] \right) / \\ & \quad \left( (a - i b) (a + i b) b^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x]) \right) \end{aligned}$$

**Problem 272: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\operatorname{Cot}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{a + b \operatorname{Tan}[c + d x]} dx$$

Optimal (type 3, 103 leaves, 4 steps):

$$-\frac{(aA + bB)x}{a^2 + b^2} - \frac{A \cot[c + dx]}{ad} - \frac{(Ab - aB) \operatorname{Log}[\operatorname{Sin}[c + dx]]}{a^2 d} + \frac{b^2 (Ab - aB) \operatorname{Log}[a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]]}{a^2 (a^2 + b^2) d}$$

Result (type 3, 201 leaves):

$$- \left( (B + A \cot[c + dx]) (a^3 A c + a^2 b B c + a^3 A d x + a^2 b B d x + a A (a^2 + b^2) \cot[c + dx] - (a^2 + b^2) (-Ab + aB) \operatorname{Log}[\operatorname{Sin}[c + dx]] - A b^3 \operatorname{Log}[a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]] + a b^2 B \operatorname{Log}[a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]]) (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]) \right) / (a^2 (a - i b) (a + i b) d (b + a \cot[c + dx]) (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]))$$

**Problem 275: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c + dx]^3 (A + B \operatorname{Tan}[c + dx])}{(a + b \operatorname{Tan}[c + dx])^2} dx$$

Optimal (type 3, 208 leaves, 6 steps):

$$-\frac{(2aAb - a^2B + b^2B)x}{(a^2 + b^2)^2} + \frac{(a^2A - Ab^2 + 2abB) \operatorname{Log}[\operatorname{Cos}[c + dx]]}{(a^2 + b^2)^2 d} + \frac{a^2 (a^2Ab + 3Ab^3 - 2a^3B - 4ab^2B) \operatorname{Log}[a + b \operatorname{Tan}[c + dx]]}{b^3 (a^2 + b^2)^2 d} - \frac{(aAb - 2a^2B - b^2B) \operatorname{Tan}[c + dx]}{b^2 (a^2 + b^2) d} + \frac{a (Ab - aB) \operatorname{Tan}[c + dx]^2}{b (a^2 + b^2) d (a + b \operatorname{Tan}[c + dx])}$$

Result (type 3, 869 leaves):

$$\begin{aligned} & \left( (-2 a A b + a^2 B - b^2 B) (c + d x) \operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 (A + B \operatorname{Tan}[c + d x]) \right) / \\ & \left( (a - i b)^2 (a + i b)^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^2 \right) + \\ & \left( i a^7 A b^3 + a^6 A b^4 + 4 i a^5 A b^5 + 4 a^4 A b^6 + 3 i a^3 A b^7 + 3 a^2 A b^8 - \right. \\ & \quad \left. 2 i a^8 b^2 B - 2 a^7 b^3 B - 6 i a^6 b^4 B - 6 a^5 b^5 B - 4 i a^4 b^6 B - 4 a^3 b^7 B \right) / \\ & (c + d x) \operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 (A + B \operatorname{Tan}[c + d x]) \Big/ \\ & \left( (a - i b)^4 (a + i b)^3 b^5 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^2 \right) - \\ & \left( i (a^4 A b + 3 a^2 A b^3 - 2 a^5 B - 4 a^3 b^2 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right) \\ & \operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 (A + B \operatorname{Tan}[c + d x]) \Big/ \\ & \left( b^3 (a^2 + b^2)^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^2 \right) + \\ & \left( (-A b + 2 a B) \operatorname{Log}[\operatorname{Cos}[c + d x]] \operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right. \\ & \quad \left. (A + B \operatorname{Tan}[c + d x]) \right) / \left( b^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^2 \right) + \\ & \left( (a^4 A b + 3 a^2 A b^3 - 2 a^5 B - 4 a^3 b^2 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right. \\ & \quad \left. \operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 (A + B \operatorname{Tan}[c + d x]) \right) / \\ & \left( 2 b^3 (a^2 + b^2)^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^2 \right) + \\ & \left( \operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \right. \\ & \quad \left. (-a^2 A b \operatorname{Sin}[c + d x] + a^3 B \operatorname{Sin}[c + d x]) (A + B \operatorname{Tan}[c + d x]) \right) / \\ & \left( (a - i b) (a + i b) b^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^2 \right) + \\ & \left( B \operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \operatorname{Tan}[c + d x] (A + B \operatorname{Tan}[c + d x]) \right) / \\ & \left( b^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^2 \right) \end{aligned}$$

**Problem 276: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 3, 157 leaves, 5 steps):

$$\begin{aligned} & - \frac{(a^2 A - A b^2 + 2 a b B) x}{(a^2 + b^2)^2} - \frac{(2 a A b - a^2 B + b^2 B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{(a^2 + b^2)^2 d} - \\ & \frac{a (2 A b^3 - a (a^2 + 3 b^2) B) \operatorname{Log}[a + b \operatorname{Tan}[c + d x]]}{b^2 (a^2 + b^2)^2 d} - \frac{a^2 (A b - a B)}{b^2 (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])} \end{aligned}$$

Result (type 3, 323 leaves):



$$\frac{1}{2 b^2 (a^2 + b^2)^2 d (a + b \tan [c + d x])} \left( a \left( 2 (a + i b)^2 (-A b^2 + a (i a + 2 b) B) (c + d x) - 2 (a^2 + b^2)^2 B \operatorname{Log} [\operatorname{Cos} [c + d x]] + a (-2 A b^3 + a (a^2 + 3 b^2) B) \operatorname{Log} [(a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2] \right) + b \left( 2 (a + i b) (-i A b^3 (c + d x) + i a^3 B (i + c + d x) - a b^2 (-2 i B (c + d x) + A (i + c + d x))) + a^2 b (A + B (i + c + d x)) - 2 (a^2 + b^2)^2 B \operatorname{Log} [\operatorname{Cos} [c + d x]] + a (-2 A b^3 + a (a^2 + 3 b^2) B) \operatorname{Log} [(a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2] \right) \tan [c + d x] - 2 i a (-2 A b^3 + a (a^2 + 3 b^2) B) \operatorname{ArcTan} [\tan [c + d x]] (a + b \tan [c + d x]) \right)$$

**Problem 277: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\tan [c + d x] (A + B \tan [c + d x])}{(a + b \tan [c + d x])^2} dx$$

Optimal (type 3, 115 leaves, 3 steps):

$$\frac{(2 a A b - a^2 B + b^2 B) x}{(a^2 + b^2)^2} - \frac{(a^2 A - A b^2 + 2 a b B) \operatorname{Log} [a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]]}{(a^2 + b^2)^2 d} + \frac{a (A b - a B)}{b (a^2 + b^2) d (a + b \tan [c + d x])}$$

Result (type 3, 252 leaves):

$$\frac{1}{2 (a^2 + b^2)^2 d (a + b \tan [c + d x])} \left( a \left( -2 i (a + i b)^2 (A - i B) (c + d x) + (-a^2 A + A b^2 - 2 a b B) \operatorname{Log} [(a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2] \right) + (-2 i (a + i b) (i a^2 B + b^2 (B (c + d x) + i A (i + c + d x))) + a b (A (-i + c + d x) - i B (i + c + d x))) + b (-a^2 A + A b^2 - 2 a b B) \operatorname{Log} [(a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2] \right) \tan [c + d x] + 2 i (a^2 A - A b^2 + 2 a b B) \operatorname{ArcTan} [\tan [c + d x]] (a + b \tan [c + d x]) \right)$$

**Problem 278: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \tan [c + d x]}{(a + b \tan [c + d x])^2} dx$$

Optimal (type 3, 111 leaves, 3 steps):

$$\frac{(a^2 A - A b^2 + 2 a b B) x}{(a^2 + b^2)^2} + \frac{(2 a A b - a^2 B + b^2 B) \operatorname{Log} [a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]]}{(a^2 + b^2)^2 d} - \frac{A b - a B}{(a^2 + b^2) d (a + b \tan [c + d x])}$$

Result (type 3, 257 leaves):

$$\frac{1}{2 a (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])} \left( a^2 \left( 2 (a + i b)^2 (A - i B) (c + d x) + (2 a A b - a^2 B + b^2 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right) + b \left( 2 (a + i b) \left( -i A b^2 + a^2 (A (c + d x) - i B (-i + c + d x)) + a b (A (1 + i c + i d x) + B (i + c + d x)) \right) + a (2 a A b - a^2 B + b^2 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right) \operatorname{Tan}[c + d x] + 2 i a (-2 a A b + a^2 B - b^2 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] (a + b \operatorname{Tan}[c + d x]) \right)$$

**Problem 279: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x] (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 3, 137 leaves, 4 steps):

$$-\frac{(2 a A b - a^2 B + b^2 B) x}{(a^2 + b^2)^2} + \frac{A \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^2 d} - \frac{b (3 a^2 A b + A b^3 - 2 a^3 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]]}{a^2 (a^2 + b^2)^2 d} + \frac{b (A b - a B)}{a (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])}$$

Result (type 3, 325 leaves):

$$\frac{1}{2 a^2 (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])} \left( a \left( 2 (a + i b)^2 (-2 a A b + i A b^2 + a^2 B) (c + d x) + 2 A (a^2 + b^2)^2 \operatorname{Log}[\operatorname{Sin}[c + d x]] - b (3 a^2 A b + A b^3 - 2 a^3 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right) + b \left( 2 (a + i b) (a^3 B (c + d x) - A b^3 (-i + c + d x) + a^2 b (B (1 + i c + i d x) - 2 A (c + d x)) - i a b^2 (B + A (-i + c + d x))) + 2 A (a^2 + b^2)^2 \operatorname{Log}[\operatorname{Sin}[c + d x]] - b (3 a^2 A b + A b^3 - 2 a^3 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right) \operatorname{Tan}[c + d x] + 2 i b (3 a^2 A b + A b^3 - 2 a^3 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] (a + b \operatorname{Tan}[c + d x]) \right)$$

**Problem 280: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 3, 192 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{(a^2 A - A b^2 + 2 a b B) x}{(a^2 + b^2)^2} - \frac{(2 A b - a B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^3 d} + \frac{1}{a^3 (a^2 + b^2)^2 d} \\
 & b^2 (4 a^2 A b + 2 A b^3 - 3 a^3 B - a b^2 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] - \\
 & \frac{b (a^2 A + 2 A b^2 - a b B)}{a^2 (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])} - \frac{A \operatorname{Cot}[c + d x]}{a d (a + b \operatorname{Tan}[c + d x])}
 \end{aligned}$$

Result (type 3, 873 leaves):

$$\begin{aligned}
 & - \left( \left( (a^2 A - A b^2 + 2 a b B) (c + d x) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) / \right. \\
 & \left. \left( (a - i b)^2 (a + i b)^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) + \\
 & \left( (4 i a^{10} A b^3 + 4 a^9 A b^4 + 6 i a^8 A b^5 + 6 a^7 A b^6 + 2 i a^6 A b^7 + 2 a^5 A b^8 - \right. \\
 & \quad \left. 3 i a^{11} b^2 B - 3 a^{10} b^3 B - 4 i a^9 b^4 B - 4 a^8 b^5 B - i a^7 b^6 B - a^6 b^7 B) \right. \\
 & \quad \left. (c + d x) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) / \\
 & \left( a^8 (a - i b)^4 (a + i b)^3 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) - \\
 & \left( i (4 a^2 A b^3 + 2 A b^5 - 3 a^3 b^2 B - a b^4 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right. \\
 & \quad \left. (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) / \\
 & \left( a^3 (a^2 + b^2)^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) - \\
 & \left( A \operatorname{Cot}[c + d x] (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) / \\
 & \left( a^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( (-2 A b + a B) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] \operatorname{Log}[\operatorname{Sin}[c + d x]] \right. \\
 & \quad \left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) / \left( a^3 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( (4 a^2 A b^3 + 2 A b^5 - 3 a^3 b^2 B - a b^4 B) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] \right. \\
 & \quad \left. \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) / \\
 & \left( 2 a^3 (a^2 + b^2)^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \right. \\
 & \quad \left. (A b^4 \operatorname{Sin}[c + d x] - a b^3 B \operatorname{Sin}[c + d x]) \right) / \\
 & \left( a^3 (a - i b) (a + i b) d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right)
 \end{aligned}$$

**Problem 281: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^3 (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^2} dx$$

Optimal (type 3, 250 leaves, 6 steps):

$$\frac{(2 a A b - a^2 B + b^2 B) x}{(a^2 + b^2)^2} - \frac{(a^2 A - 3 A b^2 + 2 a b B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^4 d} - \frac{1}{a^4 (a^2 + b^2)^2 d}$$

$$b^3 (5 a^2 A b + 3 A b^3 - 4 a^3 B - 2 a b^2 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] +$$

$$\frac{b (2 a^2 A b + 3 A b^3 - a^3 B - 2 a b^2 B)}{a^3 (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])} + \frac{(3 A b - 2 a B) \operatorname{Cot}[c + d x]}{2 a^2 d (a + b \operatorname{Tan}[c + d x])} - \frac{A \operatorname{Cot}[c + d x]^2}{2 a d (a + b \operatorname{Tan}[c + d x])}$$

Result (type 3, 977 leaves):

$$- \left( \left( (-2 a A b + a^2 B - b^2 B) (c + d x) \right. \right.$$

$$\left. \left. (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) / \right.$$

$$\left. \left( (a - i b)^2 (a + i b)^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \right) +$$

$$\left( (-5 i a^{11} A b^4 - 5 a^{10} A b^5 - 8 i a^9 A b^6 - 8 a^8 A b^7 - 3 i a^7 A b^8 - 3 a^6 A b^9 + \right.$$

$$\left. 4 i a^{12} b^3 B + 4 a^{11} b^4 B + 6 i a^{10} b^5 B + 6 a^9 b^6 B + 2 i a^8 b^7 B + 2 a^7 b^8 B) \right.$$

$$\left. (c + d x) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) /$$

$$\left( a^{10} (a - i b)^4 (a + i b)^3 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) -$$

$$\left( i (-5 a^2 A b^4 - 3 A b^6 + 4 a^3 b^3 B + 2 a b^5 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right.$$

$$\left. (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) /$$

$$\left( a^4 (a^2 + b^2)^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) +$$

$$\left( (2 A b \operatorname{Cos}[c + d x] - A B \operatorname{Cos}[c + d x]) (B + A \operatorname{Cot}[c + d x]) \right.$$

$$\left. \operatorname{Csc}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) /$$

$$\left( a^3 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) -$$

$$A (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2$$

$$+ \frac{2 a^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])}{( - a^2 A + 3 A b^2 - 2 a b B) (B + A \operatorname{Cot}[c + d x])}$$

$$\operatorname{Csc}[c + d x] \operatorname{Log}[\operatorname{Sin}[c + d x]] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) /$$

$$\left( a^4 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) +$$

$$\left( (-5 a^2 A b^4 - 3 A b^6 + 4 a^3 b^3 B + 2 a b^5 B) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] \right.$$

$$\left. \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right) /$$

$$\left( 2 a^4 (a^2 + b^2)^2 d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) +$$

$$\left( (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \right.$$

$$\left. (-A b^5 \operatorname{Sin}[c + d x] + a b^4 B \operatorname{Sin}[c + d x]) \right) /$$

$$\left( a^4 (a - i b) (a + i b) d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right)$$

**Problem 282: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c + d x]^4 (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^3} dx$$

Optimal (type 3, 331 leaves, 7 steps):

$$\frac{(a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) x}{(a^2 + b^2)^3} + \frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{(a^2 + b^2)^3 d} +$$

$$\frac{1}{b^4 (a^2 + b^2)^3 d} a^2 (a^4 A b + 3 a^2 A b^3 + 6 A b^5 - 3 a^5 B - 9 a^3 b^2 B - 10 a b^4 B) \operatorname{Log}[a + b \operatorname{Tan}[c + d x]] -$$

$$\frac{(a^3 A b + 3 a A b^3 - 3 a^4 B - 6 a^2 b^2 B - b^4 B) \operatorname{Tan}[c + d x]}{b^3 (a^2 + b^2)^2 d} +$$

$$\frac{a (A b - a B) \operatorname{Tan}[c + d x]^3}{2 b (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^2} + \frac{a (a^2 A b + 5 A b^3 - 3 a^3 B - 7 a b^2 B) \operatorname{Tan}[c + d x]^2}{2 b^2 (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])}$$

Result (type 3, 1146 leaves):

$$(a^4 (-A b + a B) \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (A + B \operatorname{Tan}[c + d x])) /$$

$$(2 (a - i b)^2 (a + i b)^2 b^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) +$$

$$((a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) (c + d x) \operatorname{Sec}[c + d x]^2$$

$$(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x])) /$$

$$((a - i b)^3 (a + i b)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) +$$

$$((i a^{11} A b^4 + a^{10} A b^5 + 5 i a^9 A b^6 + 5 a^8 A b^7 + 13 i a^7 A b^8 + 13 a^6 A b^9 + 15 i a^5 A b^{10} +$$

$$15 a^4 A b^{11} + 6 i a^3 A b^{12} + 6 a^2 A b^{13} - 3 i a^{12} b^3 B - 3 a^{11} b^4 B - 15 i a^{10} b^5 B - 15 a^9 b^6 B -$$

$$31 i a^8 b^7 B - 31 a^7 b^8 B - 29 i a^6 b^9 B - 29 a^5 b^{10} B - 10 i a^4 b^{11} B - 10 a^3 b^{12} B)$$

$$(c + d x) \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x])) /$$

$$((a - i b)^6 (a + i b)^5 b^7 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) -$$

$$(i (a^6 A b + 3 a^4 A b^3 + 6 a^2 A b^5 - 3 a^7 B - 9 a^5 b^2 B - 10 a^3 b^4 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]]$$

$$\operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x])) /$$

$$(b^4 (a^2 + b^2)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) +$$

$$((-A b + 3 a B) \operatorname{Log}[\operatorname{Cos}[c + d x]] \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3$$

$$(A + B \operatorname{Tan}[c + d x])) / (b^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) +$$

$$((a^6 A b + 3 a^4 A b^3 + 6 a^2 A b^5 - 3 a^7 B - 9 a^5 b^2 B - 10 a^3 b^4 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2]$$

$$\operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x])) /$$

$$(2 b^4 (a^2 + b^2)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) +$$

$$(\operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 (-a^4 A b \operatorname{Sin}[c + d x] -$$

$$4 a^2 A b^3 \operatorname{Sin}[c + d x] + 2 a^5 B \operatorname{Sin}[c + d x] + 5 a^3 b^2 B \operatorname{Sin}[c + d x]) (A + B \operatorname{Tan}[c + d x])) /$$

$$((a - i b)^2 (a + i b)^2 b^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) +$$

$$(B \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \operatorname{Tan}[c + d x] (A + B \operatorname{Tan}[c + d x])) /$$

$$(b^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3)$$

**Problem 283: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\tan [c+d x]^3 (A+B \tan [c+d x])}{(a+b \tan [c+d x])^3} dx$$

Optimal (type 3, 250 leaves, 6 steps):

$$\begin{aligned} & - \frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) x}{(a^2 + b^2)^3} + \frac{(a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) \operatorname{Log}[\operatorname{Cos}[c+d x]]}{(a^2 + b^2)^3 d} + \\ & \frac{a (a^2 A b^3 - 3 A b^5 + a^5 B + 3 a^3 b^2 B + 6 a b^4 B) \operatorname{Log}[a+b \tan [c+d x]]}{b^3 (a^2 + b^2)^3 d} + \\ & \frac{a (A b - a B) \tan [c+d x]^2}{2 b (a^2 + b^2) d (a+b \tan [c+d x])^2} - \frac{a^2 (2 A b^3 - a (a^2 + 3 b^2) B)}{b^3 (a^2 + b^2)^2 d (a+b \tan [c+d x])} \end{aligned}$$

Result (type 3, 998 leaves):

$$\begin{aligned} & - \left( (a^3 (-A b + a B) \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]) (A+B \tan [c+d x])) / \right. \\ & \left. (2 (a - i b)^2 (a + i b)^2 b d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3) \right) + \\ & \left( (-3 a^2 A b + A b^3 + a^3 B - 3 a b^2 B) (c+d x) \operatorname{Sec}[c+d x]^2 \right. \\ & \left. (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( (a - i b)^3 (a + i b)^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) + \\ & \left( (i a^8 A b^5 + a^7 A b^6 - i a^6 A b^7 - a^5 A b^8 - 5 i a^4 A b^9 - 5 a^3 A b^{10} - 3 i a^2 A b^{11} - 3 a A b^{12} + i a^{11} b^2 B + \right. \\ & \left. a^{10} b^3 B + 5 i a^9 b^4 B + 5 a^8 b^5 B + 13 i a^7 b^6 B + 13 a^6 b^7 B + 15 i a^5 b^8 B + 15 a^4 b^9 B + 6 i a^3 b^{10} B + \right. \\ & \left. 6 a^2 b^{11} B) (c+d x) \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( (a - i b)^6 (a + i b)^5 b^5 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) - \\ & \left( i (a^3 A b^3 - 3 a A b^5 + a^6 B + 3 a^4 b^2 B + 6 a^2 b^4 B) \operatorname{ArcTan}[\tan [c+d x]] \right. \\ & \left. \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( b^3 (a^2 + b^2)^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) - \\ & \left( B \operatorname{Log}[\operatorname{Cos}[c+d x]] \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( b^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) + \\ & \left( (a^3 A b^3 - 3 a A b^5 + a^6 B + 3 a^4 b^2 B + 6 a^2 b^4 B) \operatorname{Log}[(a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^2] \right. \\ & \left. \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( 2 b^3 (a^2 + b^2)^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) + \\ & \left( \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^2 \right. \\ & \left. (3 a A b^3 \operatorname{Sin}[c+d x] - a^4 B \operatorname{Sin}[c+d x] - 4 a^2 b^2 B \operatorname{Sin}[c+d x]) (A+B \tan [c+d x]) \right) / \\ & \left( (a - i b)^2 (a + i b)^2 b^2 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) \end{aligned}$$

Problem 284: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\tan [c+d x]^2 (A+B \tan [c+d x])}{(a+b \tan [c+d x])^3} dx$$

Optimal (type 3, 189 leaves, 4 steps):

$$\frac{(a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) x}{(a^2 + b^2)^3} - \frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \operatorname{Log}[a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]]}{(a^2 + b^2)^3 d} - \frac{a^2 (A b - a B)}{2 b^2 (a^2 + b^2) d (a+b \tan [c+d x])^2} + \frac{a (2 A b^3 - a (a^2 + 3 b^2) B)}{b^2 (a^2 + b^2)^2 d (a+b \tan [c+d x])}$$

Result (type 3, 845 leaves):

$$\begin{aligned} & \left( a^2 (-A b + a B) \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]) (A+B \tan [c+d x]) \right) / \\ & \left( 2 (a - i b)^2 (a + i b)^2 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) - \\ & \left( (a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) (c+d x) \operatorname{Sec}[c+d x]^2 \right. \\ & \quad \left. (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( (a - i b)^3 (a + i b)^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) + \\ & \left( (-3 i a^9 A b - 3 a^8 A b^2 - 5 i a^7 A b^3 - 5 a^6 A b^4 - i a^5 A b^5 - a^4 A b^6 + i a^3 A b^7 + a^2 A b^8 + \right. \\ & \quad \left. i a^{10} B + a^9 b B - i a^8 b^2 B - a^7 b^3 B - 5 i a^6 b^4 B - 5 a^5 b^5 B - 3 i a^4 b^6 B - 3 a^3 b^7 B) \right. \\ & \quad \left. (c+d x) \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( a^2 (a - i b)^6 (a + i b)^5 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) - \\ & \left( i (-3 a^2 A b + A b^3 + a^3 B - 3 a b^2 B) \operatorname{ArcTan}[\tan [c+d x]] \operatorname{Sec}[c+d x]^2 \right. \\ & \quad \left. (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( (a^2 + b^2)^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) + \\ & \left( (-3 a^2 A b + A b^3 + a^3 B - 3 a b^2 B) \operatorname{Log}[(a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^2] \right. \\ & \quad \left. \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 (A+B \tan [c+d x]) \right) / \\ & \left( 2 (a^2 + b^2)^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) + \\ & \left( \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^2 \right. \\ & \quad \left. (a^2 A \operatorname{Sin}[c+d x] - 2 A b^2 \operatorname{Sin}[c+d x] + 3 a b B \operatorname{Sin}[c+d x]) (A+B \tan [c+d x]) \right) / \\ & \left( (a - i b)^2 (a + i b)^2 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right) \end{aligned}$$

**Problem 285: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Tan}[c + d x] (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^3} dx$$

Optimal (type 3, 179 leaves, 4 steps):

$$\frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) x}{(a^2 + b^2)^3} - \frac{(a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) \text{Log}[a \text{Cos}[c + d x] + b \text{Sin}[c + d x]]}{(a^2 + b^2)^3 d} + \frac{a (A b - a B)}{2 b (a^2 + b^2) d (a + b \text{Tan}[c + d x])^2} + \frac{a^2 A - A b^2 + 2 a b B}{(a^2 + b^2)^2 d (a + b \text{Tan}[c + d x])}$$

Result (type 3, 587 leaves):

$$\left( B \text{Sec}[c + d x]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^3 \left( -\frac{8 a (a^2 - 3 b^2) (c + d x)}{(a^2 + b^2)^3} + \frac{8 b (-3 a^2 + b^2) \text{Log}[a \text{Cos}[c + d x] + b \text{Sin}[c + d x]]}{(a^2 + b^2)^3} + \frac{-3 a^2 b + b^3}{(a - i b)^2 (a + i b)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2} + \frac{6 (a^2 - 3 b^2) \text{Sin}[c + d x]}{(a^2 + b^2)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])} + \frac{-b \text{Cos}[2 (c + d x)] + a \text{Sin}[2 (c + d x)]}{(a^2 + b^2) (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2} \right) \right) / \left( 8 d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \text{Tan}[c + d x])^3 \right) + \left( A \text{Sec}[c + d x]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^3 \left( -\frac{8 b (-3 a^2 + b^2) (c + d x)}{(a^2 + b^2)^3} - \frac{8 a (a^2 - 3 b^2) \text{Log}[a \text{Cos}[c + d x] + b \text{Sin}[c + d x]]}{(a^2 + b^2)^3} - \frac{a (a^2 - 3 b^2)}{(a - i b)^2 (a + i b)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2} + \frac{6 b (-3 a^2 + b^2) \text{Sin}[c + d x]}{a (a^2 + b^2)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])} + \frac{2 b^2 \text{Sin}[c + d x]^2 + a (a + b \text{Sin}[2 (c + d x)])}{a (a^2 + b^2) (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2} \right) \right) / \left( 8 d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \text{Tan}[c + d x])^3 \right)$$

**Problem 286: Result unnecessarily involves complex numbers and more than**



twice size of optimal antiderivative.

$$\int \frac{A + B \tan [c + d x]}{(a + b \tan [c + d x])^3} dx$$

Optimal (type 3, 175 leaves, 4 steps):

$$\frac{(a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) x}{(a^2 + b^2)^3} + \frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]]}{(a^2 + b^2)^3 d} - \frac{A b - a B}{2 (a^2 + b^2) d (a + b \tan [c + d x])^2} - \frac{2 a A b - a^2 B + b^2 B}{(a^2 + b^2)^2 d (a + b \tan [c + d x])}$$

Result (type 3, 854 leaves):

$$\begin{aligned} & (b^2 (-A b + a B) \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (A + B \tan [c + d x])) / \\ & \left( 2 (a - i b)^2 (a + i b)^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan [c + d x])^3 \right) + \\ & \left( (a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) (c + d x) \operatorname{Sec}[c + d x]^2 \right. \\ & \quad \left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \tan [c + d x]) \right) / \\ & \left( (a - i b)^3 (a + i b)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan [c + d x])^3 \right) + \\ & \left( (3 i a^9 A b + 3 a^8 A b^2 + 5 i a^7 A b^3 + 5 a^6 A b^4 + i a^5 A b^5 + a^4 A b^6 - i a^3 A b^7 - a^2 A b^8 - \right. \\ & \quad \left. i a^{10} B - a^9 b B + i a^8 b^2 B + a^7 b^3 B + 5 i a^6 b^4 B + 5 a^5 b^5 B + 3 i a^4 b^6 B + 3 a^3 b^7 B) \right. \\ & \quad \left. (c + d x) \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \tan [c + d x]) \right) / \\ & \left( a^2 (a - i b)^6 (a + i b)^5 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan [c + d x])^3 \right) - \\ & \left( i (3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \operatorname{ArcTan}[\tan [c + d x]] \operatorname{Sec}[c + d x]^2 \right. \\ & \quad \left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \tan [c + d x]) \right) / \\ & \left( (a^2 + b^2)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan [c + d x])^3 \right) + \\ & \left( (3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right. \\ & \quad \left. \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \tan [c + d x]) \right) / \\ & \left( 2 (a^2 + b^2)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan [c + d x])^3 \right) + \\ & \left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right. \\ & \quad \left. (3 a A b^2 \operatorname{Sin}[c + d x] - 2 a^2 b B \operatorname{Sin}[c + d x] + b^3 B \operatorname{Sin}[c + d x]) (A + B \tan [c + d x]) \right) / \\ & \left( a (a - i b)^2 (a + i b)^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan [c + d x])^3 \right) \end{aligned}$$

Problem 287: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x] (A + B \tan [c + d x])}{(a + b \tan [c + d x])^3} dx$$

Optimal (type 3, 215 leaves, 5 steps):

$$-\frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) x}{(a^2 + b^2)^3} + \frac{A \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^3 d} - \frac{1}{a^3 (a^2 + b^2)^3 d}$$

$$b (6 a^4 A b + 3 a^2 A b^3 + A b^5 - 3 a^5 B + a^3 b^2 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] +$$

$$\frac{b (A b - a B)}{2 a (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^2} + \frac{b (3 a^2 A b + A b^3 - 2 a^3 B)}{a^2 (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])}$$

Result (type 3, 1004 leaves):

$$-\left( (b^3 (-A b + a B) \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (A + B \operatorname{Tan}[c + d x])) / \right.$$

$$\left. (2 a (a - i b)^2 (a + i b)^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3) \right) +$$

$$\left( (-3 a^2 A b + A b^3 + a^3 B - 3 a b^2 B) (c + d x) \operatorname{Sec}[c + d x]^2 \right.$$

$$\left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( (a - i b)^3 (a + i b)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3 \right) +$$

$$\left( (-6 i a^{14} A b^2 - 6 a^{13} A b^3 - 15 i a^{12} A b^4 - 15 a^{11} A b^5 - 13 i a^{10} A b^6 - \right.$$

$$\left. 13 a^9 A b^7 - 5 i a^8 A b^8 - 5 a^7 A b^9 - i a^6 A b^{10} - a^5 A b^{11} + 3 i a^{15} b B + \right.$$

$$\left. 3 a^{14} b^2 B + 5 i a^{13} b^3 B + 5 a^{12} b^4 B + i a^{11} b^5 B + a^{10} b^6 B - i a^9 b^7 B - a^8 b^8 B) \right.$$

$$\left. (c + d x) \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( a^8 (a - i b)^6 (a + i b)^5 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3 \right) -$$

$$\left( i (-6 a^4 A b^2 - 3 a^2 A b^4 - A b^6 + 3 a^5 b B - a^3 b^3 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right.$$

$$\left. \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( a^3 (a^2 + b^2)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3 \right) +$$

$$\left( A \operatorname{Log}[\operatorname{Sin}[c + d x]] \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( a^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3 \right) +$$

$$\left( (-6 a^4 A b^2 - 3 a^2 A b^4 - A b^6 + 3 a^5 b B - a^3 b^3 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right.$$

$$\left. \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( 2 a^3 (a^2 + b^2)^3 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3 \right) +$$

$$\left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right.$$

$$\left. (-4 a^2 A b^3 \operatorname{Sin}[c + d x] - A b^5 \operatorname{Sin}[c + d x] + 3 a^3 b^2 B \operatorname{Sin}[c + d x]) (A + B \operatorname{Tan}[c + d x]) \right) /$$

$$\left( a^3 (a - i b)^2 (a + i b)^2 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3 \right)$$

**Problem 288: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^3} dx$$

Optimal (type 3, 287 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{(a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) x}{(a^2 + b^2)^3} - \frac{(3 A b - a B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^4 d} + \frac{1}{a^4 (a^2 + b^2)^3 d} \\
 & b^2 (10 a^4 A b + 9 a^2 A b^3 + 3 A b^5 - 6 a^5 B - 3 a^3 b^2 B - a b^4 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] - \\
 & \frac{b (2 a^2 A + 3 A b^2 - a b B)}{2 a^2 (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^2} - \frac{A \operatorname{Cot}[c + d x]}{a d (a + b \operatorname{Tan}[c + d x])^2} - \\
 & \frac{b (a^4 A + 6 a^2 A b^2 + 3 A b^4 - 3 a^3 b B - a b^3 B)}{a^3 (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])}
 \end{aligned}$$

Result(type 3, 1150 leaves):

$$\begin{aligned}
 & (b^4 (-A b + a B) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])) / \\
 & \left( 2 a^2 (a - i b)^2 (a + i b)^2 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) - \\
 & \left( (a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) (c + d x) (B + A \operatorname{Cot}[c + d x]) \right. \\
 & \quad \left. \operatorname{Csc}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right) / \\
 & \left( (a - i b)^3 (a + i b)^3 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( 10 i a^{15} A b^3 + 10 a^{14} A b^4 + 29 i a^{13} A b^5 + 29 a^{12} A b^6 + 31 i a^{11} A b^7 + 31 a^{10} A b^8 + \right. \\
 & \quad \left. 15 i a^9 A b^9 + 15 a^8 A b^{10} + 3 i a^7 A b^{11} + 3 a^6 A b^{12} - 6 i a^{16} b^2 B - 6 a^{15} b^3 B - 15 i a^{14} b^4 B - \right. \\
 & \quad \left. 15 a^{13} b^5 B - 13 i a^{12} b^6 B - 13 a^{11} b^7 B - 5 i a^{10} b^8 B - 5 a^9 b^9 B - i a^8 b^{10} B - a^7 b^{11} B \right) \\
 & (c + d x) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 / \\
 & \left( a^{10} (a - i b)^6 (a + i b)^5 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) - \\
 & \left( i (10 a^4 A b^3 + 9 a^2 A b^5 + 3 A b^7 - 6 a^5 b^2 B - 3 a^3 b^4 B - a b^6 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right. \\
 & \quad \left. (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right) / \\
 & \left( a^4 (a^2 + b^2)^3 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) - \\
 & \left( A \operatorname{Cot}[c + d x] (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right) / \\
 & \left( a^3 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( (-3 A b + a B) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^2 \operatorname{Log}[\operatorname{Sin}[c + d x]] \right. \\
 & \quad \left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right) / \left( a^4 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( 10 a^4 A b^3 + 9 a^2 A b^5 + 3 A b^7 - 6 a^5 b^2 B - 3 a^3 b^4 B - a b^6 B \right) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^2 \\
 & \quad \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 / \\
 & \left( 2 a^4 (a^2 + b^2)^3 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\
 & \left( (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right. \\
 & \quad \left. (5 a^2 A b^4 \operatorname{Sin}[c + d x] + 2 A b^6 \operatorname{Sin}[c + d x] - 4 a^3 b^3 B \operatorname{Sin}[c + d x] - a b^5 B \operatorname{Sin}[c + d x]) \right) / \\
 & \left( a^4 (a - i b)^2 (a + i b)^2 d (b + a \operatorname{Cot}[c + d x])^3 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right)
 \end{aligned}$$

**Problem 289: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cot}[c + d x]^3 (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^3} dx$$

Optimal (type 3, 352 leaves, 7 steps):

$$\begin{aligned} & \frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) x}{(a^2 + b^2)^3} - \frac{(a^2 A - 6 A b^2 + 3 a b B) \text{Log}[\text{Sin}[c + d x]]}{a^5 d} - \frac{1}{a^5 (a^2 + b^2)^3 d} \\ & + \frac{b^3 (15 a^4 A b + 17 a^2 A b^3 + 6 A b^5 - 10 a^5 B - 9 a^3 b^2 B - 3 a b^4 B) \text{Log}[a \text{Cos}[c + d x] + b \text{Sin}[c + d x]]}{2 a^3 (a^2 + b^2) d (a + b \text{Tan}[c + d x])^2} + \frac{(2 A b - a B) \text{Cot}[c + d x]}{a^2 d (a + b \text{Tan}[c + d x])^2} \\ & - \frac{A \text{Cot}[c + d x]^2}{2 a d (a + b \text{Tan}[c + d x])^2} + \frac{b (3 a^4 A b + 11 a^2 A b^3 + 6 A b^5 - a^5 B - 6 a^3 b^2 B - 3 a b^4 B)}{a^4 (a^2 + b^2)^2 d (a + b \text{Tan}[c + d x])} \end{aligned}$$

Result (type 3, 1923 leaves):

$$\begin{aligned}
 & \left( (-15 i a^{16} A b^4 - 15 a^{15} A b^5 - 47 i a^{14} A b^6 - 47 a^{13} A b^7 - 55 i a^{12} A b^8 - 55 a^{11} A b^9 - 29 i a^{10} A b^{10} - \right. \\
 & \quad \left. 29 a^9 A b^{11} - 6 i a^8 A b^{12} - 6 a^7 A b^{13} + 10 i a^{17} b^3 B + 10 a^{16} b^4 B + 29 i a^{15} b^5 B + 29 a^{14} b^6 B + \right. \\
 & \quad \left. 31 i a^{13} b^7 B + 31 a^{12} b^8 B + 15 i a^{11} b^9 B + 15 a^{10} b^{10} B + 3 i a^9 b^{11} B + 3 a^8 b^{12} B \right) \\
 & \quad (c + d x) (B + A \cot [c + d x]) \operatorname{Csc}[c + d x]^2 (a \cos [c + d x] + b \sin [c + d x])^3 \Big/ \\
 & \quad \left( a^{12} (a - i b)^6 (a + i b)^5 d (b + a \cot [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) - \\
 & \quad \left( i (-15 a^4 A b^4 - 17 a^2 A b^6 - 6 A b^8 + 10 a^5 b^3 B + 9 a^3 b^5 B + 3 a b^7 B) \operatorname{ArcTan}[\tan [c + d x]] \right) \\
 & \quad (B + A \cot [c + d x]) \operatorname{Csc}[c + d x]^2 (a \cos [c + d x] + b \sin [c + d x])^3 \Big/ \\
 & \quad \left( a^5 (a^2 + b^2)^3 d (b + a \cot [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \quad \left( -a^2 A + 6 A b^2 - 3 a b B \right) (B + A \cot [c + d x]) \operatorname{Csc}[c + d x]^2 \\
 & \quad \operatorname{Log}[\sin [c + d x]] (a \cos [c + d x] + b \sin [c + d x])^3 \Big/ \\
 & \quad \left( a^5 d (b + a \cot [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \quad \left( -15 a^4 A b^4 - 17 a^2 A b^6 - 6 A b^8 + 10 a^5 b^3 B + 9 a^3 b^5 B + 3 a b^7 B \right) (B + A \cot [c + d x]) \\
 & \quad \operatorname{Csc}[c + d x]^2 \operatorname{Log}[(a \cos [c + d x] + b \sin [c + d x])^2] (a \cos [c + d x] + b \sin [c + d x])^3 \Big/ \\
 & \quad \left( 2 a^5 (a^2 + b^2)^3 d (b + a \cot [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \quad \left( (B + A \cot [c + d x]) \operatorname{Csc}[c + d x]^4 (a \cos [c + d x] + b \sin [c + d x]) \right) \\
 & \quad \left( -2 a^{10} A - 2 a^8 A b^2 + 6 a^6 A b^4 - 6 a^4 A b^6 - 21 a^2 A b^8 - 9 A b^{10} - 2 a^9 b B - 6 a^7 b^3 B + \right. \\
 & \quad \left. 7 a^5 b^5 B + 17 a^3 b^7 B + 6 a b^9 B + 3 a^9 A b (c + d x) + 8 a^7 A b^3 (c + d x) - 3 a^5 A b^5 (c + d x) - \right. \\
 & \quad \left. a^{10} B (c + d x) + 9 a^6 b^4 B (c + d x) - 2 a^{10} A \cos [2 (c + d x)] - 4 a^8 A b^2 \cos [2 (c + d x)] + \right. \\
 & \quad \left. 26 a^4 A b^6 \cos [2 (c + d x)] + 36 a^2 A b^8 \cos [2 (c + d x)] + 12 A b^{10} \cos [2 (c + d x)] - \right. \\
 & \quad \left. 18 a^5 b^5 B \cos [2 (c + d x)] - 26 a^3 b^7 B \cos [2 (c + d x)] - 8 a b^9 B \cos [2 (c + d x)] - \right. \\
 & \quad \left. 12 a^7 A b^3 (c + d x) \cos [2 (c + d x)] + 4 a^5 A b^5 (c + d x) \cos [2 (c + d x)] + \right. \\
 & \quad \left. 4 a^8 b^2 B (c + d x) \cos [2 (c + d x)] - 12 a^6 b^4 B (c + d x) \cos [2 (c + d x)] - \right. \\
 & \quad \left. 6 a^8 A b^2 \cos [4 (c + d x)] - 18 a^6 A b^4 \cos [4 (c + d x)] - 24 a^4 A b^6 \cos [4 (c + d x)] - \right. \\
 & \quad \left. 15 a^2 A b^8 \cos [4 (c + d x)] - 3 A b^{10} \cos [4 (c + d x)] + 2 a^9 b B \cos [4 (c + d x)] + \right. \\
 & \quad \left. 6 a^7 b^3 B \cos [4 (c + d x)] + 11 a^5 b^5 B \cos [4 (c + d x)] + 9 a^3 b^7 B \cos [4 (c + d x)] + \right. \\
 & \quad \left. 2 a b^9 B \cos [4 (c + d x)] - 3 a^9 A b (c + d x) \cos [4 (c + d x)] + 4 a^7 A b^3 (c + d x) \right. \\
 & \quad \left. \cos [4 (c + d x)] - a^5 A b^5 (c + d x) \cos [4 (c + d x)] + a^{10} B (c + d x) \cos [4 (c + d x)] - \right. \\
 & \quad \left. 4 a^8 b^2 B (c + d x) \cos [4 (c + d x)] + 3 a^6 b^4 B (c + d x) \cos [4 (c + d x)] + \right. \\
 & \quad \left. 2 a^9 A b \sin [2 (c + d x)] + 12 a^7 A b^3 \sin [2 (c + d x)] + 12 a^5 A b^5 \sin [2 (c + d x)] + \right. \\
 & \quad \left. 2 a^3 A b^7 \sin [2 (c + d x)] - 2 a^{10} B \sin [2 (c + d x)] - 8 a^8 b^2 B \sin [2 (c + d x)] - \right. \\
 & \quad \left. 2 a^6 b^4 B \sin [2 (c + d x)] + 6 a^4 b^6 B \sin [2 (c + d x)] + 2 a^2 b^8 B \sin [2 (c + d x)] + \right. \\
 & \quad \left. 12 a^8 A b^2 (c + d x) \sin [2 (c + d x)] - 4 a^6 A b^4 (c + d x) \sin [2 (c + d x)] - \right. \\
 & \quad \left. 4 a^9 b B (c + d x) \sin [2 (c + d x)] + 12 a^7 b^3 B (c + d x) \sin [2 (c + d x)] + \right. \\
 & \quad \left. 3 a^9 A b \sin [4 (c + d x)] + 6 a^7 A b^3 \sin [4 (c + d x)] + 6 a^5 A b^5 \sin [4 (c + d x)] + \right. \\
 & \quad \left. 3 a^3 A b^7 \sin [4 (c + d x)] - a^{10} B \sin [4 (c + d x)] - 2 a^8 b^2 B \sin [4 (c + d x)] - \right. \\
 & \quad \left. 5 a^6 b^4 B \sin [4 (c + d x)] - 5 a^4 b^6 B \sin [4 (c + d x)] - a^2 b^8 B \sin [4 (c + d x)] - \right. \\
 & \quad \left. 6 a^8 A b^2 (c + d x) \sin [4 (c + d x)] + 2 a^6 A b^4 (c + d x) \sin [4 (c + d x)] + \right. \\
 & \quad \left. 2 a^9 b B (c + d x) \sin [4 (c + d x)] - 6 a^7 b^3 B (c + d x) \sin [4 (c + d x)] \right) \Big/ \\
 & \quad \left( 8 a^5 (a - i b)^3 (a + i b)^3 d (b + a \cot [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

Problem 290: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int \frac{\text{Tan}[c + d x]^4 (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^4} dx$$

Optimal (type 3, 351 leaves, 7 steps):

$$\begin{aligned} & \frac{(a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) x}{(a^2 + b^2)^4} + \\ & \frac{(4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) \text{Log}[\text{Cos}[c + d x]]}{(a^2 + b^2)^4 d} + \frac{1}{b^4 (a^2 + b^2)^4 d} \\ & a (4 a^2 A b^5 - 4 A b^7 + a^7 B + 4 a^5 b^2 B + 5 a^3 b^4 B + 10 a b^6 B) \text{Log}[a + b \text{Tan}[c + d x]] + \\ & \frac{a (A b - a B) \text{Tan}[c + d x]^3}{3 b (a^2 + b^2) d (a + b \text{Tan}[c + d x])^3} + \frac{a (2 A b^3 - a (a^2 + 3 b^2) B) \text{Tan}[c + d x]^2}{2 b^2 (a^2 + b^2)^2 d (a + b \text{Tan}[c + d x])^2} + \\ & \frac{a^2 (a^2 A b^3 - 3 A b^5 + a^5 B + 3 a^3 b^2 B + 6 a b^4 B)}{b^4 (a^2 + b^2)^3 d (a + b \text{Tan}[c + d x])} \end{aligned}$$

Result (type 3, 1812 leaves):

$$\begin{aligned}
 & \left( (4 i a^{10} A b^8 + 4 a^9 A b^9 + 8 i a^8 A b^{10} + 8 a^7 A b^{11} - 8 i a^4 A b^{14} - 8 a^3 A b^{15} - 4 i a^2 A b^{16} - 4 a A b^{17} + \right. \\
 & \quad i a^{15} b^3 B + a^{14} b^4 B + 7 i a^{13} b^5 B + 7 a^{12} b^6 B + 20 i a^{11} b^7 B + 20 a^{10} b^8 B + 38 i a^9 b^9 B + \\
 & \quad \left. 38 a^8 b^{10} B + 49 i a^7 b^{11} B + 49 a^6 b^{12} B + 35 i a^5 b^{13} B + 35 a^4 b^{14} B + 10 i a^3 b^{15} B + 10 a^2 b^{16} B \right) \\
 & \quad (c+d x) \operatorname{Sec}[c+d x]^3 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^4 (A+B \operatorname{Tan}[c+d x]) \Big/ \\
 & \quad \left( (a-i b)^8 (a+i b)^7 b^7 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^4 \right) - \\
 & \quad \left( i (4 a^3 A b^5 - 4 a A b^7 + a^8 B + 4 a^6 b^2 B + 5 a^4 b^4 B + 10 a^2 b^6 B) \operatorname{ArcTan}[\operatorname{Tan}[c+d x]] \right) \\
 & \quad \operatorname{Sec}[c+d x]^3 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^4 (A+B \operatorname{Tan}[c+d x]) \Big/ \\
 & \quad \left( b^4 (a^2+b^2)^4 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^4 \right) - \\
 & \quad \left( B \operatorname{Log}[\operatorname{Cos}[c+d x]] \operatorname{Sec}[c+d x]^3 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^4 (A+B \operatorname{Tan}[c+d x]) \right) \Big/ \\
 & \quad \left( b^4 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^4 \right) + \\
 & \quad \left( (4 a^3 A b^5 - 4 a A b^7 + a^8 B + 4 a^6 b^2 B + 5 a^4 b^4 B + 10 a^2 b^6 B) \operatorname{Log}[(a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^2] \right) \\
 & \quad \operatorname{Sec}[c+d x]^3 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^4 (A+B \operatorname{Tan}[c+d x]) \Big/ \\
 & \quad \left( 2 b^4 (a^2+b^2)^4 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^4 \right) + \\
 & \quad \left( \operatorname{Sec}[c+d x]^3 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]) (12 a^6 A b^4 \operatorname{Cos}[c+d x] + 48 a^4 A b^6 \operatorname{Cos}[c+d x] + \right. \\
 & \quad 36 a^2 A b^8 \operatorname{Cos}[c+d x] - 12 a^9 b B \operatorname{Cos}[c+d x] - 60 a^7 b^3 B \operatorname{Cos}[c+d x] - 108 a^5 b^5 B \operatorname{Cos}[c+d x] - \\
 & \quad 60 a^3 b^7 B \operatorname{Cos}[c+d x] + 9 a^7 A b^3 (c+d x) \operatorname{Cos}[c+d x] - 45 a^5 A b^5 (c+d x) \operatorname{Cos}[c+d x] - \\
 & \quad 45 a^3 A b^7 (c+d x) \operatorname{Cos}[c+d x] + 9 a A b^9 (c+d x) \operatorname{Cos}[c+d x] + \\
 & \quad 36 a^6 b^4 B (c+d x) \operatorname{Cos}[c+d x] - 36 a^2 b^8 B (c+d x) \operatorname{Cos}[c+d x] + 8 a^6 A b^4 \operatorname{Cos}[3(c+d x)] - \\
 & \quad 28 a^4 A b^6 \operatorname{Cos}[3(c+d x)] - 36 a^2 A b^8 \operatorname{Cos}[3(c+d x)] + 6 a^9 b B \operatorname{Cos}[3(c+d x)] + \\
 & \quad 28 a^7 b^3 B \operatorname{Cos}[3(c+d x)] + 82 a^5 b^5 B \operatorname{Cos}[3(c+d x)] + 60 a^3 b^7 B \operatorname{Cos}[3(c+d x)] + \\
 & \quad 3 a^7 A b^3 (c+d x) \operatorname{Cos}[3(c+d x)] - 27 a^5 A b^5 (c+d x) \operatorname{Cos}[3(c+d x)] + \\
 & \quad 57 a^3 A b^7 (c+d x) \operatorname{Cos}[3(c+d x)] - 9 a A b^9 (c+d x) \operatorname{Cos}[3(c+d x)] + \\
 & \quad 12 a^6 b^4 B (c+d x) \operatorname{Cos}[3(c+d x)] - 48 a^4 b^6 B (c+d x) \operatorname{Cos}[3(c+d x)] + \\
 & \quad 36 a^2 b^8 B (c+d x) \operatorname{Cos}[3(c+d x)] + 30 a^5 A b^5 \operatorname{Sin}[c+d x] + 84 a^3 A b^7 \operatorname{Sin}[c+d x] + \\
 & \quad 54 a A b^9 \operatorname{Sin}[c+d x] - 3 a^{10} B \operatorname{Sin}[c+d x] - 33 a^8 b^2 B \operatorname{Sin}[c+d x] - 123 a^6 b^4 B \operatorname{Sin}[c+d x] - \\
 & \quad 183 a^4 b^6 B \operatorname{Sin}[c+d x] - 90 a^2 b^8 B \operatorname{Sin}[c+d x] + 9 a^6 A b^4 (c+d x) \operatorname{Sin}[c+d x] - \\
 & \quad 45 a^4 A b^6 (c+d x) \operatorname{Sin}[c+d x] - 45 a^2 A b^8 (c+d x) \operatorname{Sin}[c+d x] + 9 A b^{10} (c+d x) \operatorname{Sin}[c+d x] + \\
 & \quad 36 a^5 b^5 B (c+d x) \operatorname{Sin}[c+d x] - 36 a b^9 B (c+d x) \operatorname{Sin}[c+d x] - 4 a^7 A b^3 \operatorname{Sin}[3(c+d x)] + \\
 & \quad 18 a^5 A b^5 \operatorname{Sin}[3(c+d x)] + 4 a^3 A b^7 \operatorname{Sin}[3(c+d x)] - 18 a A b^9 \operatorname{Sin}[3(c+d x)] - \\
 & \quad 3 a^{10} B \operatorname{Sin}[3(c+d x)] - 11 a^8 b^2 B \operatorname{Sin}[3(c+d x)] - 27 a^6 b^4 B \operatorname{Sin}[3(c+d x)] + \\
 & \quad 11 a^4 b^6 B \operatorname{Sin}[3(c+d x)] + 30 a^2 b^8 B \operatorname{Sin}[3(c+d x)] + 9 a^6 A b^4 (c+d x) \operatorname{Sin}[3(c+d x)] - \\
 & \quad 57 a^4 A b^6 (c+d x) \operatorname{Sin}[3(c+d x)] + 27 a^2 A b^8 (c+d x) \operatorname{Sin}[3(c+d x)] - \\
 & \quad 3 A b^{10} (c+d x) \operatorname{Sin}[3(c+d x)] + 36 a^5 b^5 B (c+d x) \operatorname{Sin}[3(c+d x)] - \\
 & \quad \left. 48 a^3 b^7 B (c+d x) \operatorname{Sin}[3(c+d x)] + 12 a b^9 B (c+d x) \operatorname{Sin}[3(c+d x)] \right) (A+B \operatorname{Tan}[c+d x]) \Big/ \\
 & \quad \left( 12 (a-i b)^4 (a+i b)^4 b^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^4 \right)
 \end{aligned}$$

**Problem 291: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c+d x]^3 (A+B \operatorname{Tan}[c+d x])}{(a+b \operatorname{Tan}[c+d x])^4} dx$$

Optimal (type 3, 298 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{(4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) x}{(a^2 + b^2)^4} + \frac{1}{(a^2 + b^2)^4 d} \\
 & \frac{(a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] +}{a (A b - a B) \operatorname{Tan}[c + d x]^2} + \frac{a^2 (a^2 A b - 5 A b^3 + 2 a^3 B + 8 a b^2 B)}{3 b (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^3} - \\
 & \frac{a (a^4 A b + 5 a^2 A b^3 - 8 A b^5 + 2 a^5 B + 7 a^3 b^2 B + 17 a b^4 B)}{3 b^3 (a^2 + b^2)^3 d (a + b \operatorname{Tan}[c + d x])^2}
 \end{aligned}$$

Result (type 3, 1586 leaves):



$$\begin{aligned}
 & \left( (i a^{13} A + a^{12} A b - 3 i a^{11} A b^2 - 3 a^{10} A b^3 - 14 i a^9 A b^4 - 14 a^8 A b^5 - \right. \\
 & \quad 14 i a^7 A b^6 - 14 a^6 A b^7 - 3 i a^5 A b^8 - 3 a^4 A b^9 + i a^3 A b^{10} + a^2 A b^{11} + 4 i a^{12} b B + \\
 & \quad \left. 4 a^{11} b^2 B + 8 i a^{10} b^3 B + 8 a^9 b^4 B - 8 i a^6 b^7 B - 8 a^5 b^8 B - 4 i a^4 b^9 B - 4 a^3 b^{10} B) \right) / \\
 & \quad (c + d x) \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( a^2 (a - i b)^8 (a + i b)^7 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) - \\
 & \quad \left( i (a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right) \\
 & \quad \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( (a^2 + b^2)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) + \\
 & \quad \left( (a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right) \\
 & \quad \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( 2 (a^2 + b^2)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) + \\
 & \quad \left( \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (6 a^7 A \operatorname{Cos}[c + d x] + 18 a^5 A b^2 \operatorname{Cos}[c + d x] - \right. \\
 & \quad 6 a^3 A b^4 \operatorname{Cos}[c + d x] - 18 a A b^6 \operatorname{Cos}[c + d x] + 12 a^6 b B \operatorname{Cos}[c + d x] + \\
 & \quad 48 a^4 b^3 B \operatorname{Cos}[c + d x] + 36 a^2 b^5 B \operatorname{Cos}[c + d x] - 36 a^6 A b (c + d x) \operatorname{Cos}[c + d x] + \\
 & \quad 36 a^2 A b^5 (c + d x) \operatorname{Cos}[c + d x] + 9 a^7 B (c + d x) \operatorname{Cos}[c + d x] - 45 a^5 b^2 B (c + d x) \operatorname{Cos}[c + d x] - \\
 & \quad 45 a^3 b^4 B (c + d x) \operatorname{Cos}[c + d x] + 9 a b^6 B (c + d x) \operatorname{Cos}[c + d x] - 26 a^5 A b^2 \operatorname{Cos}[3 (c + d x)] - \\
 & \quad 8 a^3 A b^4 \operatorname{Cos}[3 (c + d x)] + 18 a A b^6 \operatorname{Cos}[3 (c + d x)] + 8 a^6 b B \operatorname{Cos}[3 (c + d x)] - \\
 & \quad 28 a^4 b^3 B \operatorname{Cos}[3 (c + d x)] - 36 a^2 b^5 B \operatorname{Cos}[3 (c + d x)] - 12 a^6 A b (c + d x) \operatorname{Cos}[3 (c + d x)] + \\
 & \quad 48 a^4 A b^3 (c + d x) \operatorname{Cos}[3 (c + d x)] - 36 a^2 A b^5 (c + d x) \operatorname{Cos}[3 (c + d x)] + \\
 & \quad 3 a^7 B (c + d x) \operatorname{Cos}[3 (c + d x)] - 27 a^5 b^2 B (c + d x) \operatorname{Cos}[3 (c + d x)] + \\
 & \quad 57 a^3 b^4 B (c + d x) \operatorname{Cos}[3 (c + d x)] - 9 a b^6 B (c + d x) \operatorname{Cos}[3 (c + d x)] + \\
 & \quad 15 a^6 A b \operatorname{Sin}[c + d x] + 27 a^4 A b^3 \operatorname{Sin}[c + d x] - 15 a^2 A b^5 \operatorname{Sin}[c + d x] - 27 A b^7 \operatorname{Sin}[c + d x] + \\
 & \quad 30 a^5 b^2 B \operatorname{Sin}[c + d x] + 84 a^3 b^4 B \operatorname{Sin}[c + d x] + 54 a b^6 B \operatorname{Sin}[c + d x] - \\
 & \quad 36 a^5 A b^2 (c + d x) \operatorname{Sin}[c + d x] + 36 a A b^6 (c + d x) \operatorname{Sin}[c + d x] + 9 a^6 b B (c + d x) \operatorname{Sin}[c + d x] - \\
 & \quad 45 a^4 b^3 B (c + d x) \operatorname{Sin}[c + d x] - 45 a^2 b^5 B (c + d x) \operatorname{Sin}[c + d x] + 9 b^7 B (c + d x) \operatorname{Sin}[c + d x] + \\
 & \quad 13 a^6 A b \operatorname{Sin}[3 (c + d x)] - 9 a^4 A b^3 \operatorname{Sin}[3 (c + d x)] - 13 a^2 A b^5 \operatorname{Sin}[3 (c + d x)] + \\
 & \quad 9 A b^7 \operatorname{Sin}[3 (c + d x)] - 4 a^7 B \operatorname{Sin}[3 (c + d x)] + 18 a^5 b^2 B \operatorname{Sin}[3 (c + d x)] + \\
 & \quad 4 a^3 b^4 B \operatorname{Sin}[3 (c + d x)] - 18 a b^6 B \operatorname{Sin}[3 (c + d x)] - 36 a^5 A b^2 (c + d x) \operatorname{Sin}[3 (c + d x)] + \\
 & \quad 48 a^3 A b^4 (c + d x) \operatorname{Sin}[3 (c + d x)] - 12 a A b^6 (c + d x) \operatorname{Sin}[3 (c + d x)] + \\
 & \quad 9 a^6 b B (c + d x) \operatorname{Sin}[3 (c + d x)] - 57 a^4 b^3 B (c + d x) \operatorname{Sin}[3 (c + d x)] + \\
 & \quad \left. \left. 27 a^2 b^5 B (c + d x) \operatorname{Sin}[3 (c + d x)] - 3 b^7 B (c + d x) \operatorname{Sin}[3 (c + d x)] \right) (A + B \operatorname{Tan}[c + d x]) \right) \Big/ \\
 & \quad \left( 12 (a - i b)^4 (a + i b)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right)
 \end{aligned}$$

**Problem 292: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^4} dx$$

Optimal (type 3, 261 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{(a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) x}{(a^2 + b^2)^4} - \frac{1}{(a^2 + b^2)^4 d} \\
 & \frac{(4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] - a^2 (A b - a B)}{3 b^2 (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^3} + \\
 & \frac{a (2 A b^3 - a (a^2 + 3 b^2) B)}{2 b^2 (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])^2} + \frac{3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B}{(a^2 + b^2)^3 d (a + b \operatorname{Tan}[c + d x])}
 \end{aligned}$$

Result(type 3, 1336 leaves):

$$\begin{aligned}
 & \left( A \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) \right. \\
 & \quad \left. (-3ab(a^2+b^2) \operatorname{Cos}[c+dx] + (-3a^3b+ab^3) \operatorname{Cos}[3(c+dx)]) + \right. \\
 & \quad \left. (a^2-b^2)(3a^2+b^2+(3a^2-b^2) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx] (A+B \operatorname{Tan}[c+dx]) \right) / \\
 & \left( 24a(a^2+b^2)^2 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4 + \right. \\
 & \left. (B \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) (3a(a^2+b^2) \operatorname{Cos}[c+dx] + \right. \\
 & \quad \left. b(-4ab \operatorname{Cos}[3(c+dx)] + (5a^2+b^2+4(a^2-b^2) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx])) \right. \\
 & \quad \left. (A+B \operatorname{Tan}[c+dx]) \right) / \left( 24(a^2+b^2)^2 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4 \right) - \\
 & \quad \frac{1}{24(a^2+b^2)^4 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4} \\
 & \quad B \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^4 \\
 & \quad \left( 96a(a-b)b(a+b)(c+dx) - 24i(a^4-6a^2b^2+b^4)(c+dx) + 24i(a^4-6a^2b^2+b^4) \right. \\
 & \quad \operatorname{ArcTan}[\operatorname{Tan}[c+dx]] - 12(a^4-6a^2b^2+b^4) \operatorname{Log}[(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2] + \\
 & \quad \frac{4b(a^2-b^2)(a^2+b^2)^2 \operatorname{Sin}[c+dx]}{(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3} - \frac{2(a^2+b^2)(3a^4-16a^2b^2+b^4)}{(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2} + \\
 & \quad \frac{88b(-a^4+b^4) \operatorname{Sin}[c+dx]}{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} - \left. \left( (a^2+b^2)^2 (3a(a^2+b^2) \operatorname{Cos}[c+dx] + \right. \right. \\
 & \quad \left. \left. b(-4ab \operatorname{Cos}[3(c+dx)] + (5a^2+b^2+4(a^2-b^2) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx]) \right) \right) / \\
 & \quad \left. (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) (A+B \operatorname{Tan}[c+dx]) - \\
 & \quad \frac{1}{24a(a^2+b^2)^4 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4} \\
 & \quad A \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^4 \\
 & \quad \left( 96ia^2b(a^2-b^2)(c+dx) - 96ia^2b(a^2-b^2) \operatorname{ArcTan}[\operatorname{Tan}[c+dx]] + \right. \\
 & \quad \frac{48a^2b(a^2-b^2) \operatorname{Log}[(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2]}{(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3} + \\
 & \quad \left( 6a(a^2+b^2)(2a^4b+8a^2b^3-2b^5+3a^5(c+dx)-18a^3b^2(c+dx)+3ab^4(c+dx)) \right. \\
 & \quad \operatorname{Cos}[c+dx] + a(a^4-6a^2b^2+b^4)(11a^2b+11b^3+6a^3(c+dx)-18ab^2(c+dx)) \\
 & \quad \operatorname{Cos}[3(c+dx)] - (10a^8-63a^6b^2-105a^4b^4-21a^2b^6+11b^8-36a^7b(c+dx)+ \\
 & \quad 204a^5b^3(c+dx)+36a^3b^5(c+dx)-12ab^7(c+dx)+(a^4-6a^2b^2+b^4) \\
 & \quad \left. (11a^4-11b^4-36a^3b(c+dx)+12ab^3(c+dx)) \operatorname{Cos}[2(c+dx)] \right) \operatorname{Sin}[c+dx] + \\
 & \quad \left. \left( (a^2+b^2)^2 (-3ab(a^2+b^2) \operatorname{Cos}[c+dx] - 2ab(a^2-b^2) \operatorname{Cos}[3(c+dx)] - 3a^2b^2 \operatorname{Sin}[c+dx] - \right. \right. \\
 & \quad \left. \left. 3b^4 \operatorname{Sin}[c+dx] + a^4 \operatorname{Sin}[3(c+dx)] - 2a^2b^2 \operatorname{Sin}[3(c+dx)] + b^4 \operatorname{Sin}[3(c+dx)]) \right) \right) / \\
 & \quad \left. (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) (A+B \operatorname{Tan}[c+dx])
 \end{aligned}$$

**Problem 293: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Tan}[c + d x] (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^4} dx$$

Optimal (type 3, 250 leaves, 5 steps):

$$\begin{aligned} & \frac{(4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) x}{(a^2 + b^2)^4} - \frac{1}{(a^2 + b^2)^4 d} \\ & \frac{(a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) \text{Log}[a \text{Cos}[c + d x] + b \text{Sin}[c + d x]] + a (A b - a B)}{3 b (a^2 + b^2) d (a + b \text{Tan}[c + d x])^3} + \\ & \frac{a^2 A - A b^2 + 2 a b B}{2 (a^2 + b^2)^2 d (a + b \text{Tan}[c + d x])^2} + \frac{a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B}{(a^2 + b^2)^3 d (a + b \text{Tan}[c + d x])} \end{aligned}$$

Result (type 3, 1355 leaves):

$$\begin{aligned}
 & \left( A \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) (3a(a^2+b^2) \operatorname{Cos}[c+dx] + \right. \\
 & \quad \left. b(-4ab \operatorname{Cos}[3(c+dx)] + (5a^2+b^2+4(a^2-b^2) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx])) \right. \\
 & \quad \left. (A+B \operatorname{Tan}[c+dx]) \right) / \left( 24(a^2+b^2)^2 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4 \right) + \\
 & \left( B \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) \right. \\
 & \quad \left. (-a^2(a^2-3b^2) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx] + 2ab \operatorname{Cos}[c+dx] (a^2 - (a^2-3b^2) \operatorname{Sin}[c+dx]^2) + \right. \\
 & \quad \left. \operatorname{Sin}[c+dx] (a^4 + 3a^2b^2 + b^2(-a^2+3b^2) \operatorname{Sin}[c+dx]^2)) (A+B \operatorname{Tan}[c+dx]) \right) / \\
 & \left( 12a(a^2+b^2)^2 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4 \right) + \\
 & \frac{1}{24(a^2+b^2)^4 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4} \\
 & A \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^4 \\
 & \left( 96a(a-b)b(a+b)(c+dx) - 24i(a^4-6a^2b^2+b^4)(c+dx) + 24i(a^4-6a^2b^2+b^4) \right. \\
 & \quad \operatorname{ArcTan}[\operatorname{Tan}[c+dx]] - 12(a^4-6a^2b^2+b^4) \operatorname{Log}[(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2] + \\
 & \quad \frac{4b(a^2-b^2)(a^2+b^2)^2 \operatorname{Sin}[c+dx]}{(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3} - \frac{2(a^2+b^2)(3a^4-16a^2b^2+b^4)}{(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2} + \\
 & \quad \frac{88b(-a^4+b^4) \operatorname{Sin}[c+dx]}{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} + \left. \left( (a^2+b^2)^2 (3a(a^2+b^2) \operatorname{Cos}[c+dx] + \right. \right. \\
 & \quad \left. \left. b(-4ab \operatorname{Cos}[3(c+dx)] + (5a^2+b^2+4(a^2-b^2) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx])) \right) \right) / \\
 & \left. (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) (A+B \operatorname{Tan}[c+dx]) + \\
 & \frac{1}{24a(a^2+b^2)^4 d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \operatorname{Tan}[c+dx])^4} \\
 & B \operatorname{Sec}[c+dx]^3 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^4 \\
 & \left( -96i a^2 b (a^2-b^2)(c+dx) + 96i a^2 b (a^2-b^2) \operatorname{ArcTan}[\operatorname{Tan}[c+dx]] - \right. \\
 & \quad \frac{48a^2 b (a^2-b^2) \operatorname{Log}[(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2]}{(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3} + \\
 & \quad (-6a(a^2+b^2)(2a^4b+8a^2b^3-2b^5+3a^5(c+dx)-18a^3b^2(c+dx)+3ab^4(c+dx)) \\
 & \quad \operatorname{Cos}[c+dx] - a(a^4-6a^2b^2+b^4)(11a^2b+11b^3+6a^3(c+dx)-18ab^2(c+dx)) \\
 & \quad \operatorname{Cos}[3(c+dx)] + (10a^8-63a^6b^2-105a^4b^4-21a^2b^6+11b^8-36a^7b(c+dx)+ \\
 & \quad 204a^5b^3(c+dx)+36a^3b^5(c+dx)-12ab^7(c+dx)+(a^4-6a^2b^2+b^4) \\
 & \quad (11a^4-11b^4-36a^3b(c+dx)+12ab^3(c+dx)) \operatorname{Cos}[2(c+dx)]) \operatorname{Sin}[c+dx] + \\
 & \quad \left. \left( (a^2+b^2)^2 (-3ab(a^2+b^2) \operatorname{Cos}[c+dx] - 2ab(a^2-b^2) \operatorname{Cos}[3(c+dx)] - 3a^2b^2 \operatorname{Sin}[c+dx] - \right. \right. \\
 & \quad \left. \left. 3b^4 \operatorname{Sin}[c+dx] + a^4 \operatorname{Sin}[3(c+dx)] - 2a^2b^2 \operatorname{Sin}[3(c+dx)] + b^4 \operatorname{Sin}[3(c+dx)]) \right) \right) / \\
 & \left. (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right) (A+B \operatorname{Tan}[c+dx])
 \end{aligned}$$

**Problem 294: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \tan [c + d x]}{(a + b \tan [c + d x])^4} dx$$

Optimal (type 3, 247 leaves, 5 steps):

$$\frac{(a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) x}{(a^2 + b^2)^4} + \frac{1}{(a^2 + b^2)^4 d}$$

$$\frac{(4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] - A b - a B}{3 (a^2 + b^2) d (a + b \tan [c + d x])^3} -$$

$$\frac{2 a A b - a^2 B + b^2 B}{2 (a^2 + b^2)^2 d (a + b \tan [c + d x])^2} - \frac{3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B}{(a^2 + b^2)^3 d (a + b \tan [c + d x])}$$

Result (type 3, 1585 leaves):

$$\begin{aligned}
 & \left( (4 \operatorname{Re} a^{12} A b + 4 \operatorname{Re} a^{11} A b^2 + 8 \operatorname{Re} a^{10} A b^3 + 8 \operatorname{Re} a^9 A b^4 - 8 \operatorname{Re} a^6 A b^7 - 8 \operatorname{Re} a^5 A b^8 - \right. \\
 & \quad \left. 4 \operatorname{Re} a^4 A b^9 - 4 \operatorname{Re} a^3 A b^{10} - \operatorname{Re} a^{13} B - a^{12} b B + 3 \operatorname{Re} a^{11} b^2 B + 3 \operatorname{Re} a^{10} b^3 B + 14 \operatorname{Re} a^9 b^4 B + \right. \\
 & \quad \left. 14 \operatorname{Re} a^8 b^5 B + 14 \operatorname{Re} a^7 b^6 B + 14 \operatorname{Re} a^6 b^7 B + 3 \operatorname{Re} a^5 b^8 B + 3 \operatorname{Re} a^4 b^9 B - \operatorname{Re} a^3 b^{10} B - a^2 b^{11} B) \right) / \\
 & \quad (c + d x) \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( a^2 (a - \operatorname{Re} b)^8 (a + \operatorname{Re} b)^7 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) - \\
 & \quad \left( \operatorname{Re} (4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right) \\
 & \quad \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( (a^2 + b^2)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) + \\
 & \quad \left( (4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right) / \\
 & \quad \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( 2 (a^2 + b^2)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) + \\
 & \quad \left( \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \right) \\
 & \quad \left( 12 a^5 A b^3 \operatorname{Cos}[c + d x] - 12 a A b^7 \operatorname{Cos}[c + d x] + 24 a^4 b^4 B \operatorname{Cos}[c + d x] + 24 a^2 b^6 B \operatorname{Cos}[c + d x] + \right. \\
 & \quad \left. 9 a^8 A (c + d x) \operatorname{Cos}[c + d x] - 45 a^6 A b^2 (c + d x) \operatorname{Cos}[c + d x] - 45 a^4 A b^4 (c + d x) \operatorname{Cos}[c + d x] + \right. \\
 & \quad \left. 9 a^2 A b^6 (c + d x) \operatorname{Cos}[c + d x] + 36 a^7 b B (c + d x) \operatorname{Cos}[c + d x] - \right. \\
 & \quad \left. 36 a^3 b^5 B (c + d x) \operatorname{Cos}[c + d x] - 36 a^5 A b^3 \operatorname{Cos}[3(c + d x)] - 28 a^3 A b^5 \operatorname{Cos}[3(c + d x)] + \right. \\
 & \quad \left. 8 a A b^7 \operatorname{Cos}[3(c + d x)] + 18 a^6 b^2 B \operatorname{Cos}[3(c + d x)] - 8 a^4 b^4 B \operatorname{Cos}[3(c + d x)] - \right. \\
 & \quad \left. 26 a^2 b^6 B \operatorname{Cos}[3(c + d x)] + 3 a^8 A (c + d x) \operatorname{Cos}[3(c + d x)] - \right. \\
 & \quad \left. 27 a^6 A b^2 (c + d x) \operatorname{Cos}[3(c + d x)] + 57 a^4 A b^4 (c + d x) \operatorname{Cos}[3(c + d x)] - \right. \\
 & \quad \left. 9 a^2 A b^6 (c + d x) \operatorname{Cos}[3(c + d x)] + 12 a^7 b B (c + d x) \operatorname{Cos}[3(c + d x)] - \right. \\
 & \quad \left. 48 a^5 b^3 B (c + d x) \operatorname{Cos}[3(c + d x)] + 36 a^3 b^5 B (c + d x) \operatorname{Cos}[3(c + d x)] + \right. \\
 & \quad \left. 18 a^6 A b^2 \operatorname{Sin}[c + d x] + 48 a^4 A b^4 \operatorname{Sin}[c + d x] + 18 a^2 A b^6 \operatorname{Sin}[c + d x] - \right. \\
 & \quad \left. 12 A b^8 \operatorname{Sin}[c + d x] - 9 a^7 b B \operatorname{Sin}[c + d x] - 9 a^5 b^3 B \operatorname{Sin}[c + d x] + 33 a^3 b^5 B \operatorname{Sin}[c + d x] + \right. \\
 & \quad \left. 33 a b^7 B \operatorname{Sin}[c + d x] + 9 a^7 A b (c + d x) \operatorname{Sin}[c + d x] - 45 a^5 A b^3 (c + d x) \operatorname{Sin}[c + d x] - \right. \\
 & \quad \left. 45 a^3 A b^5 (c + d x) \operatorname{Sin}[c + d x] + 9 a A b^7 (c + d x) \operatorname{Sin}[c + d x] + \right. \\
 & \quad \left. 36 a^6 b^2 B (c + d x) \operatorname{Sin}[c + d x] - 36 a^2 b^6 B (c + d x) \operatorname{Sin}[c + d x] + \right. \\
 & \quad \left. 18 a^6 A b^2 \operatorname{Sin}[3(c + d x)] - 4 a^4 A b^4 \operatorname{Sin}[3(c + d x)] - 18 a^2 A b^6 \operatorname{Sin}[3(c + d x)] + \right. \\
 & \quad \left. 4 A b^8 \operatorname{Sin}[3(c + d x)] - 9 a^7 b B \operatorname{Sin}[3(c + d x)] + 13 a^5 b^3 B \operatorname{Sin}[3(c + d x)] + \right. \\
 & \quad \left. 9 a^3 b^5 B \operatorname{Sin}[3(c + d x)] - 13 a b^7 B \operatorname{Sin}[3(c + d x)] + 9 a^7 A b (c + d x) \operatorname{Sin}[3(c + d x)] - \right. \\
 & \quad \left. 57 a^5 A b^3 (c + d x) \operatorname{Sin}[3(c + d x)] + 27 a^3 A b^5 (c + d x) \operatorname{Sin}[3(c + d x)] - \right. \\
 & \quad \left. 3 a A b^7 (c + d x) \operatorname{Sin}[3(c + d x)] + 36 a^6 b^2 B (c + d x) \operatorname{Sin}[3(c + d x)] - 48 a^4 b^4 B \right. \\
 & \quad \left. (c + d x) \operatorname{Sin}[3(c + d x)] + 12 a^2 b^6 B (c + d x) \operatorname{Sin}[3(c + d x)] \right) (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( 12 a (a - \operatorname{Re} b)^4 (a + \operatorname{Re} b)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right)
 \end{aligned}$$

**Problem 295: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x] (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^4} dx$$

Optimal (type 3, 302 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{(4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) x}{(a^2 + b^2)^4} + \frac{A \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^4 d} - \frac{1}{a^4 (a^2 + b^2)^4 d} \\
 & b (10 a^6 A b + 5 a^4 A b^3 + 4 a^2 A b^5 + A b^7 - 4 a^7 B + 4 a^5 b^2 B) \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] + \\
 & \frac{b (A b - a B)}{3 a (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^3} + \frac{b (3 a^2 A b + A b^3 - 2 a^3 B)}{2 a^2 (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])^2} + \\
 & \frac{b (6 a^4 A b + 3 a^2 A b^3 + A b^5 - 3 a^5 B + a^3 b^2 B)}{a^3 (a^2 + b^2)^3 d (a + b \operatorname{Tan}[c + d x])}
 \end{aligned}$$

Result (type 3, 1818 leaves):



$$\begin{aligned}
 & \left( (-10 i a^{19} A b^2 - 10 a^{18} A b^3 - 35 i a^{17} A b^4 - 35 a^{16} A b^5 - 49 i a^{15} A b^6 - 49 a^{14} A b^7 - 38 i a^{13} A b^8 - \right. \\
 & \quad 38 a^{12} A b^9 - 20 i a^{11} A b^{10} - 20 a^{10} A b^{11} - 7 i a^9 A b^{12} - 7 a^8 A b^{13} - i a^7 A b^{14} - a^6 A b^{15} + \\
 & \quad \left. 4 i a^{20} b B + 4 a^{19} b^2 B + 8 i a^{18} b^3 B + 8 a^{17} b^4 B - 8 i a^{14} b^7 B - 8 a^{13} b^8 B - 4 i a^{12} b^9 B - 4 a^{11} b^{10} B \right) \\
 & \quad (c + d x) \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( a^{10} (a - i b)^8 (a + i b)^7 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) - \\
 & \quad \left( i (-10 a^6 A b^2 - 5 a^4 A b^4 - 4 a^2 A b^6 - A b^8 + 4 a^7 b B - 4 a^5 b^3 B) \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] \right) \\
 & \quad \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( a^4 (a^2 + b^2)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) + \\
 & \quad \left( A \operatorname{Log}[\operatorname{Sin}[c + d x]] \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \right) \Big/ \\
 & \quad \left( a^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) + \\
 & \quad \left( (-10 a^6 A b^2 - 5 a^4 A b^4 - 4 a^2 A b^6 - A b^8 + 4 a^7 b B - 4 a^5 b^3 B) \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \right) \\
 & \quad \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( 2 a^4 (a^2 + b^2)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right) + \\
 & \quad \left( \operatorname{Sec}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \right) \\
 & \quad \left( -30 a^7 A b^4 \operatorname{Cos}[c + d x] - 42 a^5 A b^6 \operatorname{Cos}[c + d x] - 18 a^3 A b^8 \operatorname{Cos}[c + d x] - 6 a A b^{10} \operatorname{Cos}[c + d x] + \right. \\
 & \quad 12 a^8 b^3 B \operatorname{Cos}[c + d x] - 12 a^4 b^7 B \operatorname{Cos}[c + d x] - 36 a^{10} A b (c + d x) \operatorname{Cos}[c + d x] + \\
 & \quad 36 a^6 A b^5 (c + d x) \operatorname{Cos}[c + d x] + 9 a^{11} B (c + d x) \operatorname{Cos}[c + d x] - 45 a^9 b^2 B (c + d x) \operatorname{Cos}[c + d x] - \\
 & \quad 45 a^7 b^4 B (c + d x) \operatorname{Cos}[c + d x] + 9 a^5 b^6 B (c + d x) \operatorname{Cos}[c + d x] + 60 a^7 A b^4 \operatorname{Cos}[3(c + d x)] + \\
 & \quad 82 a^5 A b^6 \operatorname{Cos}[3(c + d x)] + 28 a^3 A b^8 \operatorname{Cos}[3(c + d x)] + 6 a A b^{10} \operatorname{Cos}[3(c + d x)] - \\
 & \quad 36 a^8 b^3 B \operatorname{Cos}[3(c + d x)] - 28 a^6 b^5 B \operatorname{Cos}[3(c + d x)] + 8 a^4 b^7 B \operatorname{Cos}[3(c + d x)] - \\
 & \quad 12 a^{10} A b (c + d x) \operatorname{Cos}[3(c + d x)] + 48 a^8 A b^3 (c + d x) \operatorname{Cos}[3(c + d x)] - \\
 & \quad 36 a^6 A b^5 (c + d x) \operatorname{Cos}[3(c + d x)] + 3 a^{11} B (c + d x) \operatorname{Cos}[3(c + d x)] - \\
 & \quad 27 a^9 b^2 B (c + d x) \operatorname{Cos}[3(c + d x)] + 57 a^7 b^4 B (c + d x) \operatorname{Cos}[3(c + d x)] - \\
 & \quad 9 a^5 b^6 B (c + d x) \operatorname{Cos}[3(c + d x)] - 30 a^8 A b^3 \operatorname{Sin}[c + d x] - 105 a^6 A b^5 \operatorname{Sin}[c + d x] - \\
 & \quad 105 a^4 A b^7 \operatorname{Sin}[c + d x] - 39 a^2 A b^9 \operatorname{Sin}[c + d x] - 9 A b^{11} \operatorname{Sin}[c + d x] + \\
 & \quad 18 a^9 b^2 B \operatorname{Sin}[c + d x] + 48 a^7 b^4 B \operatorname{Sin}[c + d x] + 18 a^5 b^6 B \operatorname{Sin}[c + d x] - \\
 & \quad 12 a^3 b^8 B \operatorname{Sin}[c + d x] - 36 a^9 A b^2 (c + d x) \operatorname{Sin}[c + d x] + 36 a^5 A b^6 (c + d x) \operatorname{Sin}[c + d x] + \\
 & \quad 9 a^{10} b B (c + d x) \operatorname{Sin}[c + d x] - 45 a^8 b^3 B (c + d x) \operatorname{Sin}[c + d x] - \\
 & \quad 45 a^6 b^5 B (c + d x) \operatorname{Sin}[c + d x] + 9 a^4 b^7 B (c + d x) \operatorname{Sin}[c + d x] - 30 a^8 A b^3 \operatorname{Sin}[3(c + d x)] - \\
 & \quad 11 a^6 A b^5 \operatorname{Sin}[3(c + d x)] + 27 a^4 A b^7 \operatorname{Sin}[3(c + d x)] + 11 a^2 A b^9 \operatorname{Sin}[3(c + d x)] + \\
 & \quad 3 A b^{11} \operatorname{Sin}[3(c + d x)] + 18 a^9 b^2 B \operatorname{Sin}[3(c + d x)] - 4 a^7 b^4 B \operatorname{Sin}[3(c + d x)] - \\
 & \quad 18 a^5 b^6 B \operatorname{Sin}[3(c + d x)] + 4 a^3 b^8 B \operatorname{Sin}[3(c + d x)] - 36 a^9 A b^2 (c + d x) \operatorname{Sin}[3(c + d x)] + \\
 & \quad 48 a^7 A b^4 (c + d x) \operatorname{Sin}[3(c + d x)] - 12 a^5 A b^6 (c + d x) \operatorname{Sin}[3(c + d x)] + \\
 & \quad 9 a^{10} b B (c + d x) \operatorname{Sin}[3(c + d x)] - 57 a^8 b^3 B (c + d x) \operatorname{Sin}[3(c + d x)] + \\
 & \quad \left. 27 a^6 b^5 B (c + d x) \operatorname{Sin}[3(c + d x)] - 3 a^4 b^7 B (c + d x) \operatorname{Sin}[3(c + d x)] \right) (A + B \operatorname{Tan}[c + d x]) \Big/ \\
 & \quad \left( 12 a^4 (a - i b)^4 (a + i b)^4 d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^4 \right)
 \end{aligned}$$

**Problem 296: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^2 (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^4} dx$$

Optimal (type 3, 399 leaves, 7 steps):

$$\begin{aligned} & - \frac{(a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) x}{(a^2 + b^2)^4} - \frac{(4 A b - a B) \operatorname{Log}[\operatorname{Sin}[c + d x]]}{a^5 d} + \frac{1}{a^5 (a^2 + b^2)^4 d} \\ & b^2 (20 a^6 A b + 24 a^4 A b^3 + 16 a^2 A b^5 + 4 A b^7 - 10 a^7 B - 5 a^5 b^2 B - 4 a^3 b^4 B - a b^6 B) \\ & \operatorname{Log}[a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]] - \frac{b (3 a^2 A + 4 A b^2 - a b B)}{3 a^2 (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^3} - \\ & \frac{A \operatorname{Cot}[c + d x]}{a d (a + b \operatorname{Tan}[c + d x])^3} - \frac{b (2 a^4 A + 8 a^2 A b^2 + 4 A b^4 - 3 a^3 b B - a b^3 B)}{2 a^3 (a^2 + b^2)^2 d (a + b \operatorname{Tan}[c + d x])^2} - \\ & \frac{b (a^6 A + 13 a^4 A b^2 + 12 a^2 A b^4 + 4 A b^6 - 6 a^5 b B - 3 a^3 b^3 B - a b^5 B)}{a^4 (a^2 + b^2)^3 d (a + b \operatorname{Tan}[c + d x])} \end{aligned}$$

Result (type 3, 2351 leaves):

$$\begin{aligned} & \left( (20 a^{20} A b^3 + 20 a^{19} A b^4 + 84 a^{18} A b^5 + 84 a^{17} A b^6 + 148 a^{16} A b^7 + 148 a^{15} A b^8 + 144 a^{14} A b^9 + \right. \\ & \quad 144 a^{13} A b^{10} + 84 a^{12} A b^{11} + 84 a^{11} A b^{12} + 28 a^{10} A b^{13} + 28 a^9 A b^{14} + 4 a^8 A b^{15} + 4 a^7 A b^{16} - \\ & \quad 10 a^{21} b^2 B - 10 a^{20} b^3 B - 35 a^{19} b^4 B - 35 a^{18} b^5 B - 49 a^{17} b^6 B - 49 a^{16} b^7 B - 38 a^{15} b^8 B - \\ & \quad \left. 38 a^{14} b^9 B - 20 a^{13} b^{10} B - 20 a^{12} b^{11} B - 7 a^{11} b^{12} B - 7 a^{10} b^{13} B - a^9 b^{14} B - a^8 b^{15} B) \right) \\ & \quad (c + d x) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 \Big/ \\ & \quad \left( a^{12} (a - b)^8 (a + b)^7 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) - \\ & \quad \left( (20 a^6 A b^3 + 24 a^4 A b^5 + 16 a^2 A b^7 + 4 A b^9 - 10 a^7 b^2 B - 5 a^5 b^4 B - 4 a^3 b^6 B - a b^8 B) \right) \\ & \quad \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 \Big/ \\ & \quad \left( a^5 (a^2 + b^2)^4 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \left( (-4 A b + a B) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 \right. \\ & \quad \quad \left. \operatorname{Log}[\operatorname{Sin}[c + d x]] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 \right) \Big/ \\ & \quad \left( a^5 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \left( (20 a^6 A b^3 + 24 a^4 A b^5 + 16 a^2 A b^7 + 4 A b^9 - 10 a^7 b^2 B - 5 a^5 b^4 B - 4 a^3 b^6 B - a b^8 B) (B + A \operatorname{Cot}[c + d x]) \right) \\ & \quad \operatorname{Csc}[c + d x]^3 \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4 \Big/ \\ & \quad \left( 2 a^5 (a^2 + b^2)^4 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) + \\ & \quad \left( (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^4 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \right) \\ & \quad \left( -9 a^{12} A - 45 a^{10} A b^2 - 45 a^8 A b^4 + 90 a^6 A b^6 + 183 a^4 A b^8 + 111 a^2 A b^{10} + 27 A b^{12} - 30 a^9 b^3 B - \right. \\ & \quad 105 a^7 b^5 B - 105 a^5 b^7 B - 39 a^3 b^9 B - 9 a b^{11} B - 9 a^{11} A b (c + d x) + 45 a^9 A b^3 (c + d x) + \\ & \quad 45 a^7 A b^5 (c + d x) - 9 a^5 A b^7 (c + d x) - 36 a^{10} b^2 B (c + d x) + 36 a^6 b^6 B (c + d x) - \\ & \quad 12 a^{12} A \operatorname{Cos}[2(c + d x)] - 48 a^{10} A b^2 \operatorname{Cos}[2(c + d x)] - 72 a^8 A b^4 \operatorname{Cos}[2(c + d x)] - \\ & \quad 196 a^6 A b^6 \operatorname{Cos}[2(c + d x)] - 276 a^4 A b^8 \operatorname{Cos}[2(c + d x)] - 152 a^2 A b^{10} \operatorname{Cos}[2(c + d x)] - \\ & \quad 36 A b^{12} \operatorname{Cos}[2(c + d x)] + 94 a^7 b^5 B \operatorname{Cos}[2(c + d x)] + 132 a^5 b^7 B \operatorname{Cos}[2(c + d x)] + \\ & \quad 50 a^3 b^9 B \operatorname{Cos}[2(c + d x)] + 12 a b^{11} B \operatorname{Cos}[2(c + d x)] + 12 a^9 A b^3 (c + d x) \operatorname{Cos}[2(c + d x)] - \\ & \quad 72 a^7 A b^5 (c + d x) \operatorname{Cos}[2(c + d x)] + 12 a^5 A b^7 (c + d x) \operatorname{Cos}[2(c + d x)] + \\ & \quad 48 a^8 b^4 B (c + d x) \operatorname{Cos}[2(c + d x)] - 48 a^6 b^6 B (c + d x) \operatorname{Cos}[2(c + d x)] - \\ & \quad 3 a^{12} A \operatorname{Cos}[4(c + d x)] - 3 a^{10} A b^2 \operatorname{Cos}[4(c + d x)] - 27 a^8 A b^4 \operatorname{Cos}[4(c + d x)] + \\ & \quad 10 a^6 A b^6 \operatorname{Cos}[4(c + d x)] + 69 a^4 A b^8 \operatorname{Cos}[4(c + d x)] + 41 a^2 A b^{10} \operatorname{Cos}[4(c + d x)] + \\ & \quad 9 A b^{12} \operatorname{Cos}[4(c + d x)] + 30 a^9 b^3 B \operatorname{Cos}[4(c + d x)] + 11 a^7 b^5 B \operatorname{Cos}[4(c + d x)] - \\ & \quad \left. 27 a^5 b^7 B \operatorname{Cos}[4(c + d x)] - 11 a^3 b^9 B \operatorname{Cos}[4(c + d x)] - 3 a b^{11} B \operatorname{Cos}[4(c + d x)] \right) + \end{aligned}$$

$$\begin{aligned}
 & 9 a^{11} A b (c+d x) \cos [4 (c+d x)] - 57 a^9 A b^3 (c+d x) \cos [4 (c+d x)] + \\
 & 27 a^7 A b^5 (c+d x) \cos [4 (c+d x)] - 3 a^5 A b^7 (c+d x) \cos [4 (c+d x)] + \\
 & 36 a^{10} b^2 B (c+d x) \cos [4 (c+d x)] - 48 a^8 b^4 B (c+d x) \cos [4 (c+d x)] + \\
 & 12 a^6 b^6 B (c+d x) \cos [4 (c+d x)] - 18 a^{11} A b \sin [2 (c+d x)] - 78 a^9 A b^3 \sin [2 (c+d x)] + \\
 & 12 a^7 A b^5 \sin [2 (c+d x)] + 148 a^5 A b^7 \sin [2 (c+d x)] + 106 a^3 A b^9 \sin [2 (c+d x)] + \\
 & 30 a A b^{11} \sin [2 (c+d x)] - 90 a^8 b^4 B \sin [2 (c+d x)] - 124 a^6 b^6 B \sin [2 (c+d x)] - \\
 & 46 a^4 b^8 B \sin [2 (c+d x)] - 12 a^2 b^{10} B \sin [2 (c+d x)] - 6 a^{12} A (c+d x) \sin [2 (c+d x)] + \\
 & 18 a^{10} A b^2 (c+d x) \sin [2 (c+d x)] + 102 a^8 A b^4 (c+d x) \sin [2 (c+d x)] - 18 a^6 A b^6 (c+d x) \\
 & \sin [2 (c+d x)] - 24 a^{11} b B (c+d x) \sin [2 (c+d x)] - 48 a^9 b^3 B (c+d x) \sin [2 (c+d x)] + \\
 & 72 a^7 b^5 B (c+d x) \sin [2 (c+d x)] - 9 a^{11} A b \sin [4 (c+d x)] - 33 a^9 A b^3 \sin [4 (c+d x)] - \\
 & 132 a^7 A b^5 \sin [4 (c+d x)] - 172 a^5 A b^7 \sin [4 (c+d x)] - 79 a^3 A b^9 \sin [4 (c+d x)] - \\
 & 15 a A b^{11} \sin [4 (c+d x)] + 60 a^8 b^4 B \sin [4 (c+d x)] + 82 a^6 b^6 B \sin [4 (c+d x)] + \\
 & 28 a^4 b^8 B \sin [4 (c+d x)] + 6 a^2 b^{10} B \sin [4 (c+d x)] - 3 a^{12} A (c+d x) \sin [4 (c+d x)] + \\
 & 27 a^{10} A b^2 (c+d x) \sin [4 (c+d x)] - 57 a^8 A b^4 (c+d x) \sin [4 (c+d x)] + \\
 & 9 a^6 A b^6 (c+d x) \sin [4 (c+d x)] - 12 a^{11} b B (c+d x) \sin [4 (c+d x)] + \\
 & 48 a^9 b^3 B (c+d x) \sin [4 (c+d x)] - 36 a^7 b^5 B (c+d x) \sin [4 (c+d x)] \Big) / \\
 & (24 a^5 (a-i b)^4 (a+i b)^4 d (b+a \cot [c+d x])^4 (A \cos [c+d x] + B \sin [c+d x]))
 \end{aligned}$$

**Problem 297: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cot [c+d x]^3 (A+B \tan [c+d x])}{(a+b \tan [c+d x])^4} dx$$

Optimal (type 3, 477 leaves, 8 steps):

$$\begin{aligned}
 & \frac{(4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) x}{(a^2 + b^2)^4} - \frac{(a^2 A - 10 A b^2 + 4 a b B) \log [\sin [c+d x]]}{a^6 d} \\
 & \frac{1}{a^6 (a^2 + b^2)^4 d} b^3 (35 a^6 A b + 56 a^4 A b^3 + 39 a^2 A b^5 + 10 A b^7 - 20 a^7 B - 24 a^5 b^2 B - 16 a^3 b^4 B - 4 a b^6 B) \\
 & \log [a \cos [c+d x] + b \sin [c+d x]] + \frac{b (9 a^2 A b + 10 A b^3 - 3 a^3 B - 4 a b^2 B)}{3 a^3 (a^2 + b^2) d (a+b \tan [c+d x])^3} + \\
 & \frac{(5 A b - 2 a B) \cot [c+d x]}{2 a^2 d (a+b \tan [c+d x])^3} - \frac{A \cot [c+d x]^2}{2 a d (a+b \tan [c+d x])^3} + \\
 & \frac{b (7 a^4 A b + 19 a^2 A b^3 + 10 A b^5 - 2 a^5 B - 8 a^3 b^2 B - 4 a b^4 B)}{2 a^4 (a^2 + b^2)^2 d (a+b \tan [c+d x])^2} + \\
 & (b (4 a^6 A b + 27 a^4 A b^3 + 29 a^2 A b^5 + 10 A b^7 - a^7 B - 13 a^5 b^2 B - 12 a^3 b^4 B - 4 a b^6 B)) / \\
 & (a^5 (a^2 + b^2)^3 d (a+b \tan [c+d x]))
 \end{aligned}$$

Result (type 3, 3045 leaves):

$$\begin{aligned}
 & ((-35 i a^{21} A b^4 - 35 a^{20} A b^5 - 161 i a^{19} A b^6 - 161 a^{18} A b^7 - 312 i a^{17} A b^8 - \\
 & 312 a^{16} A b^9 - 330 i a^{15} A b^{10} - 330 a^{14} A b^{11} - 203 i a^{13} A b^{12} - 203 a^{12} A b^{13} - \\
 & 69 i a^{11} A b^{14} - 69 a^{10} A b^{15} - 10 i a^9 A b^{16} - 10 a^8 A b^{17} + 20 i a^{22} b^3 B + 20 a^{21} b^4 B +
 \end{aligned}$$

$$\begin{aligned}
& 84 \, i \, a^{20} b^5 B + 84 \, a^{19} b^6 B + 148 \, i \, a^{18} b^7 B + 148 \, a^{17} b^8 B + 144 \, i \, a^{16} b^9 B + 144 \, a^{15} b^{10} B + \\
& 84 \, i \, a^{14} b^{11} B + 84 \, a^{13} b^{12} B + 28 \, i \, a^{12} b^{13} B + 28 \, a^{11} b^{14} B + 4 \, i \, a^{10} b^{15} B + 4 \, a^9 b^{16} B) \\
& (c + d x) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4) / \\
& (a^{14} (a - i b)^8 (a + i b)^7 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])) - \\
& (i (-35 a^6 A b^4 - 56 a^4 A b^6 - 39 a^2 A b^8 - 10 A b^{10} + 20 a^7 b^3 B + 24 a^5 b^5 B + 16 a^3 b^7 B + 4 a b^9 B) \\
& \operatorname{ArcTan}[\operatorname{Tan}[c + d x]] (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4) / \\
& (a^6 (a^2 + b^2)^4 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])) + \\
& (-a^2 A + 10 A b^2 - 4 a b B) (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 \\
& \operatorname{Log}[\operatorname{Sin}[c + d x]] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4) / \\
& (a^6 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])) + \\
& (-35 a^6 A b^4 - 56 a^4 A b^6 - 39 a^2 A b^8 - 10 A b^{10} + 20 a^7 b^3 B + 24 a^5 b^5 B + 16 a^3 b^7 B + 4 a b^9 B) \\
& (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^3 \operatorname{Log}[(a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2] \\
& (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^4) / \\
& (2 a^6 (a^2 + b^2)^4 d (b + a \operatorname{Cot}[c + d x])^4 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])) + \\
& (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]^5 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \\
& (-18 a^{13} A \operatorname{Cos}[c + d x] - 18 a^{11} A b^2 \operatorname{Cos}[c + d x] + 132 a^9 A b^4 \operatorname{Cos}[c + d x] + \\
& 138 a^7 A b^6 \operatorname{Cos}[c + d x] - 82 a^5 A b^8 \operatorname{Cos}[c + d x] - 136 a^3 A b^{10} \operatorname{Cos}[c + d x] - \\
& 48 a A b^{12} \operatorname{Cos}[c + d x] - 18 a^{12} b B \operatorname{Cos}[c + d x] - 78 a^{10} b^3 B \operatorname{Cos}[c + d x] + 12 a^8 b^5 B \operatorname{Cos}[c + d x] + \\
& 148 a^6 b^7 B \operatorname{Cos}[c + d x] + 106 a^4 b^9 B \operatorname{Cos}[c + d x] + 30 a^2 b^{11} B \operatorname{Cos}[c + d x] + \\
& 24 a^{12} A b (c + d x) \operatorname{Cos}[c + d x] + 48 a^{10} A b^3 (c + d x) \operatorname{Cos}[c + d x] - 72 a^8 A b^5 (c + d x) \\
& \operatorname{Cos}[c + d x] - 6 a^{13} B (c + d x) \operatorname{Cos}[c + d x] + 18 a^{11} b^2 B (c + d x) \operatorname{Cos}[c + d x] + \\
& 102 a^9 b^4 B (c + d x) \operatorname{Cos}[c + d x] - 18 a^7 b^6 B (c + d x) \operatorname{Cos}[c + d x] - 6 a^{13} A \operatorname{Cos}[3 (c + d x)] - \\
& 42 a^{11} A b^2 \operatorname{Cos}[3 (c + d x)] - 144 a^9 A b^4 \operatorname{Cos}[3 (c + d x)] + 60 a^7 A b^6 \operatorname{Cos}[3 (c + d x)] + \\
& 374 a^5 A b^8 \operatorname{Cos}[3 (c + d x)] + 278 a^3 A b^{10} \operatorname{Cos}[3 (c + d x)] + 72 a A b^{12} \operatorname{Cos}[3 (c + d x)] + \\
& 9 a^{12} b B \operatorname{Cos}[3 (c + d x)] + 45 a^{10} b^3 B \operatorname{Cos}[3 (c + d x)] - 144 a^8 b^5 B \operatorname{Cos}[3 (c + d x)] - \\
& 320 a^6 b^7 B \operatorname{Cos}[3 (c + d x)] - 185 a^4 b^9 B \operatorname{Cos}[3 (c + d x)] - 45 a^2 b^{11} B \operatorname{Cos}[3 (c + d x)] - \\
& 12 a^{12} A b (c + d x) \operatorname{Cos}[3 (c + d x)] - 96 a^{10} A b^3 (c + d x) \operatorname{Cos}[3 (c + d x)] + \\
& 108 a^8 A b^5 (c + d x) \operatorname{Cos}[3 (c + d x)] + 3 a^{13} B (c + d x) \operatorname{Cos}[3 (c + d x)] + \\
& 9 a^{11} b^2 B (c + d x) \operatorname{Cos}[3 (c + d x)] - 159 a^9 b^4 B (c + d x) \operatorname{Cos}[3 (c + d x)] + \\
& 27 a^7 b^6 B (c + d x) \operatorname{Cos}[3 (c + d x)] - 36 a^{11} A b^2 \operatorname{Cos}[5 (c + d x)] - \\
& 132 a^9 A b^4 \operatorname{Cos}[5 (c + d x)] - 294 a^7 A b^6 \operatorname{Cos}[5 (c + d x)] - 316 a^5 A b^8 \operatorname{Cos}[5 (c + d x)] - \\
& 142 a^3 A b^{10} \operatorname{Cos}[5 (c + d x)] - 24 a A b^{12} \operatorname{Cos}[5 (c + d x)] + 9 a^{12} b B \operatorname{Cos}[5 (c + d x)] + \\
& 33 a^{10} b^3 B \operatorname{Cos}[5 (c + d x)] + 132 a^8 b^5 B \operatorname{Cos}[5 (c + d x)] + 172 a^6 b^7 B \operatorname{Cos}[5 (c + d x)] + \\
& 79 a^4 b^9 B \operatorname{Cos}[5 (c + d x)] + 15 a^2 b^{11} B \operatorname{Cos}[5 (c + d x)] - 12 a^{12} A b (c + d x) \operatorname{Cos}[5 (c + d x)] + \\
& 48 a^{10} A b^3 (c + d x) \operatorname{Cos}[5 (c + d x)] - 36 a^8 A b^5 (c + d x) \operatorname{Cos}[5 (c + d x)] + \\
& 3 a^{13} B (c + d x) \operatorname{Cos}[5 (c + d x)] - 27 a^{11} b^2 B (c + d x) \operatorname{Cos}[5 (c + d x)] + \\
& 57 a^9 b^4 B (c + d x) \operatorname{Cos}[5 (c + d x)] - 9 a^7 b^6 B (c + d x) \operatorname{Cos}[5 (c + d x)] + \\
& 6 a^{12} A b \operatorname{Sin}[c + d x] + 78 a^{10} A b^3 \operatorname{Sin}[c + d x] + 126 a^8 A b^5 \operatorname{Sin}[c + d x] - \\
& 412 a^6 A b^7 \operatorname{Sin}[c + d x] - 984 a^4 A b^9 \operatorname{Sin}[c + d x] - 698 a^2 A b^{11} \operatorname{Sin}[c + d x] - \\
& 180 A b^{13} \operatorname{Sin}[c + d x] - 6 a^{13} B \operatorname{Sin}[c + d x] - 42 a^{11} b^2 B \operatorname{Sin}[c + d x] - 18 a^9 b^4 B \operatorname{Sin}[c + d x] + \\
& 376 a^7 b^6 B \operatorname{Sin}[c + d x] + 642 a^5 b^8 B \operatorname{Sin}[c + d x] + 374 a^3 b^{10} B \operatorname{Sin}[c + d x] + \\
& 90 a b^{12} B \operatorname{Sin}[c + d x] + 72 a^{11} A b^2 (c + d x) \operatorname{Sin}[c + d x] + 48 a^9 A b^4 (c + d x) \operatorname{Sin}[c + d x] - \\
& 120 a^7 A b^6 (c + d x) \operatorname{Sin}[c + d x] - 18 a^{12} b B (c + d x) \operatorname{Sin}[c + d x] + 78 a^{10} b^3 B (c + d x) \\
& \operatorname{Sin}[c + d x] + 162 a^8 b^5 B (c + d x) \operatorname{Sin}[c + d x] - 30 a^6 b^7 B (c + d x) \operatorname{Sin}[c + d x] +
\end{aligned}$$

$$\begin{aligned}
 & 18 a^{12} A b \sin[3(c+dx)] + 114 a^{10} A b^3 \sin[3(c+dx)] + 213 a^8 A b^5 \sin[3(c+dx)] + \\
 & 479 a^6 A b^7 \sin[3(c+dx)] + 663 a^4 A b^9 \sin[3(c+dx)] + 391 a^2 A b^{11} \sin[3(c+dx)] + \\
 & 90 A b^{13} \sin[3(c+dx)] - 9 a^{13} B \sin[3(c+dx)] - 45 a^{11} b^2 B \sin[3(c+dx)] - \\
 & 45 a^9 b^4 B \sin[3(c+dx)] - 206 a^7 b^6 B \sin[3(c+dx)] - 345 a^5 b^8 B \sin[3(c+dx)] - \\
 & 193 a^3 b^{10} B \sin[3(c+dx)] - 45 a b^{12} B \sin[3(c+dx)] + 36 a^{11} A b^2 (c+dx) \sin[3(c+dx)] - \\
 & 96 a^9 A b^4 (c+dx) \sin[3(c+dx)] + 60 a^7 A b^6 (c+dx) \sin[3(c+dx)] - \\
 & 9 a^{12} b B (c+dx) \sin[3(c+dx)] + 69 a^{10} b^3 B (c+dx) \sin[3(c+dx)] - \\
 & 99 a^8 b^5 B (c+dx) \sin[3(c+dx)] + 15 a^6 b^7 B (c+dx) \sin[3(c+dx)] + \\
 & 12 a^{12} A b \sin[5(c+dx)] + 12 a^{10} A b^3 \sin[5(c+dx)] - 9 a^8 A b^5 \sin[5(c+dx)] - \\
 & 109 a^6 A b^7 \sin[5(c+dx)] - 177 a^4 A b^9 \sin[5(c+dx)] - 95 a^2 A b^{11} \sin[5(c+dx)] - \\
 & 18 A b^{13} \sin[5(c+dx)] - 3 a^{13} B \sin[5(c+dx)] - 3 a^{11} b^2 B \sin[5(c+dx)] - \\
 & 27 a^9 b^4 B \sin[5(c+dx)] + 10 a^7 b^6 B \sin[5(c+dx)] + 69 a^5 b^8 B \sin[5(c+dx)] + \\
 & 41 a^3 b^{10} B \sin[5(c+dx)] + 9 a b^{12} B \sin[5(c+dx)] - 36 a^{11} A b^2 (c+dx) \sin[5(c+dx)] + \\
 & 48 a^9 A b^4 (c+dx) \sin[5(c+dx)] - 12 a^7 A b^6 (c+dx) \sin[5(c+dx)] + \\
 & 9 a^{12} b B (c+dx) \sin[5(c+dx)] - 57 a^{10} b^3 B (c+dx) \sin[5(c+dx)] + \\
 & 27 a^8 b^5 B (c+dx) \sin[5(c+dx)] - 3 a^6 b^7 B (c+dx) \sin[5(c+dx)] \Big) / \\
 & (48 a^6 (a - ib)^4 (a + ib)^4 d (b + a \cot[c+dx])^4 (A \cos[c+dx] + B \sin[c+dx]))
 \end{aligned}$$

**Problem 309: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\tan[c+dx] (aB + bB \tan[c+dx])}{(a + b \tan[c+dx])^2} dx$$

Optimal (type 3, 48 leaves, 3 steps):

$$\frac{b B x}{a^2 + b^2} - \frac{a B \log[a \cos[c+dx] + b \sin[c+dx]]}{(a^2 + b^2) d}$$

Result (type 3, 67 leaves):

$$\frac{1}{2(a^2 + b^2)d} B \left( 2(-ia + b)(c+dx) + 2ia \operatorname{ArcTan}[\tan[c+dx]] - a \log[(a \cos[c+dx] + b \sin[c+dx])^2] \right)$$

**Problem 314: Result more than twice size of optimal antiderivative.**

$$\int \frac{3 + \tan[c+dx]}{2 - \tan[c+dx]} dx$$

Optimal (type 3, 25 leaves, 2 steps):

$$x - \frac{\log[2 \cos[c+dx] - \sin[c+dx]]}{d}$$

Result (type 3, 62 leaves):

$$\frac{\operatorname{ArcTan}[\tan[c+dx]]}{d} + \frac{\log[5 - 4(2 - \tan[c+dx]) + (2 - \tan[c+dx])^2]}{2d} - \frac{\log[2 - \tan[c+dx]]}{d}$$

**Problem 316: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{a + b \tan [c + d x]}{(b + a \tan [c + d x])^2} dx$$

Optimal (type 3, 101 leaves, 3 steps):

$$-\frac{a (a^2 - 3 b^2) x}{(a^2 + b^2)^2} + \frac{b (3 a^2 - b^2) \operatorname{Log}[b \operatorname{Cos}[c + d x] + a \operatorname{Sin}[c + d x]]}{(a^2 + b^2)^2 d} - \frac{a^2 - b^2}{(a^2 + b^2) d (b + a \tan [c + d x])}$$

Result (type 3, 219 leaves):

$$\frac{1}{2 b (a^2 + b^2)^2 d (b + a \tan [c + d x])} \left( b^2 \left( -2 (a - i b)^3 (c + d x) - b (-3 a^2 + b^2) \operatorname{Log}[(b \operatorname{Cos}[c + d x] + a \operatorname{Sin}[c + d x])^2] \right) + a \left( 2 (a - i b) (a^3 - a^2 b (-i + c + d x) + b^3 (-i + c + d x) + i a b^2 (i + 2 c + 2 d x)) - b^2 (-3 a^2 + b^2) \operatorname{Log}[(b \operatorname{Cos}[c + d x] + a \operatorname{Sin}[c + d x])^2] \right) \tan [c + d x] + 2 i b^2 (-3 a^2 + b^2) \operatorname{ArcTan}[\tan [c + d x]] (b + a \tan [c + d x]) \right)$$

**Problem 317: Result more than twice size of optimal antiderivative.**

$$\int \tan [c + d x]^3 \sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 233 leaves, 11 steps):

$$\frac{\sqrt{a - i b} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a - i b}}\right]}{d} + \frac{\sqrt{a + i b} (A + i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a + i b}}\right]}{d} - \frac{2 A \sqrt{a + b \tan [c + d x]}}{d} - \frac{2 (14 a A b - 8 a^2 B + 35 b^2 B) (a + b \tan [c + d x])^{3/2}}{105 b^3 d} + \frac{2 (7 A b - 4 a B) \tan [c + d x] (a + b \tan [c + d x])^{3/2}}{35 b^2 d} + \frac{2 B \tan [c + d x]^2 (a + b \tan [c + d x])^{3/2}}{7 b d}$$

Result (type 3, 498 leaves):

$$\begin{aligned}
 & - \left( \left( i (A b + a B) \left( \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan[c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} - \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan[c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \right) \right. \\
 & \quad \left. \cos [c+d x]^2 (a+b \tan [c+d x]) (A+B \tan [c+d x]) \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x]) (A \cos [c+d x] + B \sin [c+d x]) \right) - \\
 & \left( (-a A + b B) \left( \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan[c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} + \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan[c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \right) \\
 & \quad \left. \cos [c+d x]^2 (a+b \tan [c+d x]) (A+B \tan [c+d x]) \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x]) (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \quad \left( \cos [c+d x] \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x]) \right. \\
 & \quad \left( -\frac{4 (7 a^2 A b + 63 A b^3 - 4 a^3 B + 19 a b^2 B)}{105 b^3} + \frac{2 (7 A b + a B) \sec [c+d x]^2}{35 b} - \frac{1}{105 b^2} \right. \\
 & \quad \left. \left. 2 \sec [c+d x] (-7 a A b \sin [c+d x] + 4 a^2 B \sin [c+d x] + 50 b^2 B \sin [c+d x]) + \frac{2}{7} B \sec [c+d x]^2 \tan [c+d x] \right) \right) / (d (A \cos [c+d x] + B \sin [c+d x]))
 \end{aligned}$$

**Problem 318: Result more than twice size of optimal antiderivative.**

$$\int \tan [c+d x]^2 \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 186 leaves, 10 steps):

$$\begin{aligned}
 & \frac{\sqrt{a-i b} (i A + B) \text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{d} - \\
 & \frac{\sqrt{a+i b} (i A - B) \text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{d} - \frac{2 B \sqrt{a+b \tan [c+d x]}}{d} + \\
 & \frac{2 (5 A b - 2 a B) (a+b \tan [c+d x])^{3/2}}{15 b^2 d} + \frac{2 B \tan [c+d x] (a+b \tan [c+d x])^{3/2}}{5 b d}
 \end{aligned}$$

Result (type 3, 443 leaves):

$$\left( \cos [c+d x] \left( -\frac{2(-5 a A b+2 a^2 B+18 b^2 B)}{15 b^2} + \frac{2}{5} B \sec [c+d x]^2 + \frac{2 \sec [c+d x](5 A b \sin [c+d x]+a B \sin [c+d x])}{15 b} \right) \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x]) \right) / (d(A \cos [c+d x]+B \sin [c+d x])) + \left( i(a A-b B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \cos [c+d x]^2 (a+b \tan [c+d x])(A+B \tan [c+d x]) \right) / (d(a \cos [c+d x]+b \sin [c+d x])(A \cos [c+d x]+B \sin [c+d x])) + \left( (A b+a B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \cos [c+d x]^2 (a+b \tan [c+d x])(A+B \tan [c+d x]) \right) / (d(a \cos [c+d x]+b \sin [c+d x])(A \cos [c+d x]+B \sin [c+d x]))$$

**Problem 322: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c+d x]^2 \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 167 leaves, 12 steps):

$$-\frac{(A b+2 a B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}}\right]}{\sqrt{a} d} + \frac{\sqrt{a-i b}(i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{\sqrt{a+i b}(i A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} - \frac{A \cot [c+d x] \sqrt{a+b \tan [c+d x]}}{d}$$

Result (type 4, 23646 leaves): Display of huge result suppressed!

**Problem 323: Result unnecessarily involves higher level functions and more**



than twice size of optimal antiderivative.

$$\int \text{Cot}[c + d x]^3 \sqrt{a + b \text{Tan}[c + d x]} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 219 leaves, 13 steps):

$$\frac{(8 a^2 A + A b^2 - 4 a b B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{4 a^{3/2} d} - \frac{\sqrt{a-i b} (A-i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{\sqrt{a+i b} (A+i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} - \frac{(A b + 4 a B) \text{Cot}[c + d x] \sqrt{a + b \text{Tan}[c + d x]}}{4 a d} - \frac{A \text{Cot}[c + d x]^2 \sqrt{a + b \text{Tan}[c + d x]}}{2 d}$$

Result (type 4, 25731 leaves): Display of huge result suppressed!

**Problem 324:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Cot}[c + d x]^4 \sqrt{a + b \text{Tan}[c + d x]} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 279 leaves, 14 steps):

$$\frac{(8 a^2 A b - A b^3 + 16 a^3 B + 2 a b^2 B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{8 a^{5/2} d} - \frac{\sqrt{a-i b} (i A + B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} + \frac{\sqrt{a+i b} (i A - B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} + \frac{(8 a^2 A + A b^2 - 2 a b B) \text{Cot}[c + d x] \sqrt{a + b \text{Tan}[c + d x]}}{8 a^2 d} - \frac{(A b + 6 a B) \text{Cot}[c + d x]^2 \sqrt{a + b \text{Tan}[c + d x]}}{12 a d} - \frac{A \text{Cot}[c + d x]^3 \sqrt{a + b \text{Tan}[c + d x]}}{3 d}$$

Result (type 4, 27748 leaves): Display of huge result suppressed!

**Problem 325:** Result more than twice size of optimal antiderivative.

$$\int \text{Tan}[c + d x]^2 (a + b \text{Tan}[c + d x])^{3/2} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 214 leaves, 11 steps):

$$\frac{(a - i b)^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{(a + i b)^{3/2} (i A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} -$$

$$\frac{2 (A b + a B) \sqrt{a+b \tan [c+d x]}}{d} - \frac{2 B (a+b \tan [c+d x])^{3/2}}{3 d} +$$

$$\frac{2 (7 A b - 2 a B) (a+b \tan [c+d x])^{5/2}}{35 b^2 d} + \frac{2 B \tan [c+d x] (a+b \tan [c+d x])^{5/2}}{7 b d}$$

Result (type 3, 540 leaves):

$$\left( i (a^2 A - A b^2 - 2 a b B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \right.$$

$$\left. \cos [c+d x]^3 (a+b \tan [c+d x])^2 (A+B \tan [c+d x]) \right) /$$

$$\left( d (a \cos [c+d x] + b \sin [c+d x])^2 (A \cos [c+d x] + B \sin [c+d x]) \right) +$$

$$\left( (2 a A b + a^2 B - b^2 B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \right.$$

$$\left. \cos [c+d x]^3 (a+b \tan [c+d x])^2 (A+B \tan [c+d x]) \right) /$$

$$\left( d (a \cos [c+d x] + b \sin [c+d x])^2 (A \cos [c+d x] + B \sin [c+d x]) \right) +$$

$$\left( \cos [c+d x]^2 (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) \right.$$

$$\left( -\frac{2 (-21 a^2 A b + 126 A b^3 + 6 a^3 B + 164 a b^2 B)}{105 b^2} + \frac{2}{35} (7 A b + 8 a B) \sec [c+d x]^2 - \frac{1}{105 b} \right.$$

$$\left. \left. 2 \sec [c+d x] (-42 a A b \sin [c+d x] - 3 a^2 B \sin [c+d x] + 50 b^2 B \sin [c+d x]) + \frac{2}{7} b B \sec [c+d x]^2 \tan [c+d x] \right) \right) /$$

$$\left( d (a \cos [c+d x] + b \sin [c+d x]) (A \cos [c+d x] + B \sin [c+d x]) \right)$$

**Problem 326: Result more than twice size of optimal antiderivative.**

$$\int \tan [c+d x] (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 175 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{(a - i b)^{3/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{(a + i b)^{3/2} (A + i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} + \\
 & \frac{2(a A - b B) \sqrt{a+b \tan [c+d x]}}{d} + \frac{2 A (a+b \tan [c+d x])^{3/2}}{3 d} + \frac{2 B (a+b \tan [c+d x])^{5/2}}{5 b d}
 \end{aligned}$$

Result (type 3, 487 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^2 \left( \frac{2(20 a A b + 3 a^2 B - 18 b^2 B)}{15 b} + \frac{2}{5} b B \sec [c+d x]^2 + \frac{2}{15} \sec [c+d x] \right. \right. \\
 & \quad \left. \left. (5 A b \sin [c+d x] + 6 a B \sin [c+d x]) \right) (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) \right) / \\
 & (d(a \cos [c+d x] + b \sin [c+d x]) (A \cos [c+d x] + B \sin [c+d x])) - \\
 & \left( i(-2 a A b - a^2 B + b^2 B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \right. \\
 & \quad \left. \cos [c+d x]^3 (a+b \tan [c+d x])^2 (A+B \tan [c+d x]) \right) / \\
 & (d(a \cos [c+d x] + b \sin [c+d x])^2 (A \cos [c+d x] + B \sin [c+d x])) - \\
 & \left( (a^2 A - A b^2 - 2 a b B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \right. \\
 & \quad \left. \cos [c+d x]^3 (a+b \tan [c+d x])^2 (A+B \tan [c+d x]) \right) / \\
 & (d(a \cos [c+d x] + b \sin [c+d x])^2 (A \cos [c+d x] + B \sin [c+d x]))
 \end{aligned}$$

**Problem 327: Result more than twice size of optimal antiderivative.**

$$\int (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 150 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{(a - i b)^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} + \frac{(a + i b)^{3/2} (i A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} + \\
 & \frac{2(A b + a B) \sqrt{a+b \tan [c+d x]}}{d} + \frac{2 B (a+b \tan [c+d x])^{3/2}}{3 d}
 \end{aligned}$$

Result (type 3, 442 leaves):

$$\begin{aligned}
 & - \left( \left( i (a^2 A - A b^2 - 2 a b B) \left( \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} - \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \right. \right. \\
 & \quad \left. \left. \cos [c+d x]^3 (a+b \tan [c+d x])^2 (A+B \tan [c+d x]) \right) / \right. \\
 & \quad \left. \left( d (a \cos [c+d x] + b \sin [c+d x])^2 (A \cos [c+d x] + B \sin [c+d x]) \right) \right) - \\
 & \left( (2 a A b + a^2 B - b^2 B) \left( \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} + \frac{\text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \right. \\
 & \quad \left. \cos [c+d x]^3 (a+b \tan [c+d x])^2 (A+B \tan [c+d x]) \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x])^2 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \left( \cos [c+d x]^2 (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) \left( \frac{2}{3} (3 A b + 4 a B) + \frac{2}{3} b B \tan [c+d x] \right) \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x]) (A \cos [c+d x] + B \sin [c+d x]) \right)
 \end{aligned}$$

**Problem 328: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c+d x] (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 152 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{2 a^{3/2} A \text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}} \right]}{d} + \frac{(a-i b)^{3/2} (A-i B) \text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{d} + \\
 & \frac{(a+i b)^{3/2} (A+i B) \text{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{d} + \frac{2 b B \sqrt{a+b \tan [c+d x]}}{d}
 \end{aligned}$$

Result (type 4, 29055 leaves): Display of huge result suppressed!

**Problem 329: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x]^2 (a + b \text{Tan}[c + d x])^{3/2} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 169 leaves, 12 steps):

$$\frac{\sqrt{a} (3 A b + 2 a B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{d} + \frac{(a - i b)^{3/2} (i A + B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{(a + i b)^{3/2} (i A - B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} - \frac{a A \text{Cot}[c + d x] \sqrt{a + b \text{Tan}[c + d x]}}{d}$$

Result (type 4, 30 728 leaves): Display of huge result suppressed!

**Problem 330: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x]^3 (a + b \text{Tan}[c + d x])^{3/2} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 219 leaves, 13 steps):

$$\frac{(8 a^2 A - 3 A b^2 - 12 a b B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{4 \sqrt{a} d} - \frac{(a - i b)^{3/2} (A - i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{(a + i b)^{3/2} (A + i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} - \frac{(5 A b + 4 a B) \text{Cot}[c + d x] \sqrt{a + b \text{Tan}[c + d x]}}{4 d} - \frac{a A \text{Cot}[c + d x]^2 \sqrt{a + b \text{Tan}[c + d x]}}{2 d}$$

Result (type 4, 32 510 leaves): Display of huge result suppressed!

**Problem 331: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x]^4 (a + b \text{Tan}[c + d x])^{3/2} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 278 leaves, 14 steps):

$$\frac{(24 a^2 A b + A b^3 + 16 a^3 B - 6 a b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}}\right]}{8 a^{3/2} d} -$$

$$\frac{(a-i b)^{3/2} (i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} + \frac{(a+i b)^{3/2} (i A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} +$$

$$\frac{(8 a^2 A - A b^2 - 10 a b B) \operatorname{Cot}[c+d x] \sqrt{a+b \tan [c+d x]}}{8 a d} -$$

$$\frac{(7 A b + 6 a B) \operatorname{Cot}[c+d x]^2 \sqrt{a+b \tan [c+d x]}}{12 d} - \frac{a A \operatorname{Cot}[c+d x]^3 \sqrt{a+b \tan [c+d x]}}{3 d}$$

Result (type 4, 34 557 leaves): Display of huge result suppressed!

### Problem 332: Result more than twice size of optimal antiderivative.

$$\int \tan [c+d x]^2 (a+b \tan [c+d x])^{5/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 252 leaves, 12 steps):

$$\frac{(a-i b)^{5/2} (i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} -$$

$$\frac{(a+i b)^{5/2} (i A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} - \frac{2(2 a A b + a^2 B - b^2 B) \sqrt{a+b \tan [c+d x]}}{d} -$$

$$\frac{2(A b + a B) (a+b \tan [c+d x])^{3/2}}{3 d} - \frac{2 B (a+b \tan [c+d x])^{5/2}}{5 d} +$$

$$\frac{2(9 A b - 2 a B) (a+b \tan [c+d x])^{7/2}}{63 b^2 d} + \frac{2 B \tan [c+d x] (a+b \tan [c+d x])^{7/2}}{9 b d}$$

Result (type 3, 622 leaves):

$$\begin{aligned}
 & \frac{1}{d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x])} \\
 & \cos [c + d x]^3 \left( -\frac{2 (-45 a^3 A b + 870 a A b^3 + 10 a^4 B + 558 a^2 b^2 B - 413 b^4 B)}{315 b^2} + \right. \\
 & \quad \frac{2}{315} (135 a A b + 75 a^2 B - 133 b^2 B) \sec [c + d x]^2 + \frac{2}{9} b^2 B \sec [c + d x]^4 + \\
 & \quad \left. \frac{2}{63} \sec [c + d x]^3 (9 A b^2 \sin [c + d x] + 19 a b B \sin [c + d x]) - \frac{1}{315 b} 2 \sec [c + d x] \right. \\
 & \quad \left. (-135 a^2 A b \sin [c + d x] + 150 A b^3 \sin [c + d x] - 5 a^3 B \sin [c + d x] + 326 a b^2 B \sin [c + d x]) \right) \\
 & (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) + \\
 & \left( i (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \left( \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \right. \\
 & \quad \left. \cos [c + d x]^4 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\
 & \left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) + \\
 & \left( (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \left( \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \right. \\
 & \quad \left. \cos [c + d x]^4 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\
 & \left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

**Problem 333: Result more than twice size of optimal antiderivative.**

$$\int \tan [c + d x] (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 213 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{(a - i b)^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} - \\
 & \frac{(a + i b)^{5/2} (A + i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} + \frac{2 (a^2 A - A b^2 - 2 a b B) \sqrt{a+b \tan [c+d x]}}{d} + \\
 & \frac{2 (a A - b B) (a+b \tan [c+d x])^{3/2}}{3 d} + \frac{2 A (a+b \tan [c+d x])^{5/2}}{5 d} + \frac{2 B (a+b \tan [c+d x])^{7/2}}{7 b d}
 \end{aligned}$$

Result (type 3, 558 leaves):

$$\begin{aligned}
 & - \left( \left( i (-3 a^2 A b + A b^3 - a^3 B + 3 a b^2 B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}}\right) \right) \right. \\
 & \quad \left. \cos [c+d x]^4 (a+b \tan [c+d x])^3 (A+B \tan [c+d x]) \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x])^3 (A \cos [c+d x] + B \sin [c+d x]) \right) - \\
 & \quad \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}}\right) \right) \right. \\
 & \quad \left. \cos [c+d x]^4 (a+b \tan [c+d x])^3 (A+B \tan [c+d x]) \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x])^3 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \quad \left( \cos [c+d x]^3 (a+b \tan [c+d x])^{5/2} (A+B \tan [c+d x]) \right. \\
 & \quad \left( \frac{2 (161 a^2 A b - 126 A b^3 + 15 a^3 B - 290 a b^2 B)}{105 b} + \frac{2}{35} b (7 A b + 15 a B) \sec [c+d x]^2 + \right. \\
 & \quad \left. \frac{2}{105} \sec [c+d x] (77 a A b \sin [c+d x] + 45 a^2 B \sin [c+d x] - 50 b^2 B \sin [c+d x]) + \right. \\
 & \quad \left. \left. \frac{2}{7} b^2 B \sec [c+d x]^2 \tan [c+d x] \right) \right) / \\
 & \quad \left( d (a \cos [c+d x] + b \sin [c+d x])^2 (A \cos [c+d x] + B \sin [c+d x]) \right)
 \end{aligned}$$



### Problem 334: Result more than twice size of optimal antiderivative.

$$\int (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 188 leaves, 10 steps):

$$\begin{aligned} & - \frac{(a - i b)^{5/2} (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a - i b}} \right]}{d} + \\ & \frac{(a + i b)^{5/2} (i A - B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a + i b}} \right]}{d} + \frac{2 (2 a A b + a^2 B - b^2 B) \sqrt{a + b \tan [c + d x]}}{d} + \\ & \frac{2 (A b + a B) (a + b \tan [c + d x])^{3/2}}{3 d} + \frac{2 B (a + b \tan [c + d x])^{5/2}}{5 d} \end{aligned}$$

Result (type 3, 506 leaves):

$$\begin{aligned} & \left( \cos [c + d x]^3 \left( \frac{2}{15} (35 a A b + 23 a^2 B - 18 b^2 B) + \frac{2}{5} b^2 B \sec [c + d x]^2 + \frac{2}{15} \sec [c + d x] \right. \right. \\ & \quad \left. \left. (5 A b^2 \sin [c + d x] + 11 a b B \sin [c + d x]) \right) (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) \right) / \\ & \left( d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) - \\ & \left( i (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \left( \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a - i b}} \right]}{\sqrt{a - i b}} - \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a + i b}} \right]}{\sqrt{a + i b}} \right) \right. \\ & \quad \left. \cos [c + d x]^4 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\ & \left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) - \\ & \left( (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \left( \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a - i b}} \right]}{\sqrt{a - i b}} + \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a + i b}} \right]}{\sqrt{a + i b}} \right) \right. \\ & \quad \left. \cos [c + d x]^4 (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) \right) / \\ & \left( d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) \end{aligned}$$

**Problem 335: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x] (a + b \text{Tan}[c + d x])^{5/2} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 182 leaves, 13 steps):

$$\begin{aligned} & -\frac{2 a^{5/2} A \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{d} + \frac{(a-i b)^{5/2} (A-i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} + \\ & \frac{(a+i b)^{5/2} (A+i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} + \\ & \frac{2 b (A b+2 a B) \sqrt{a+b \text{Tan}[c+d x]}}{d} + \frac{2 b B (a+b \text{Tan}[c+d x])^{3/2}}{3 d} \end{aligned}$$

Result (type 4, 36 102 leaves): Display of huge result suppressed!

**Problem 336: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x]^2 (a + b \text{Tan}[c + d x])^{5/2} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 196 leaves, 13 steps):

$$\begin{aligned} & -\frac{a^{3/2} (5 A b+2 a B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{d} + \\ & \frac{(a-i b)^{5/2} (i A+B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{(a+i b)^{5/2} (i A-B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} + \\ & \frac{b (a A+2 b B) \sqrt{a+b \text{Tan}[c+d x]}}{d} - \frac{a A \text{Cot}[c+d x] (a+b \text{Tan}[c+d x])^{3/2}}{d} \end{aligned}$$

Result (type 4, 37 767 leaves): Display of huge result suppressed!

**Problem 337: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + d x]^3 (a + b \text{Tan}[c + d x])^{5/2} (A + B \text{Tan}[c + d x]) dx$$

Optimal (type 3, 220 leaves, 13 steps):

$$\frac{\sqrt{a} (8 a^2 A - 15 A b^2 - 20 a b B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}}\right]}{4 d} -$$

$$\frac{(a - i b)^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{(a + i b)^{5/2} (A + i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} -$$

$$\frac{a (7 A b + 4 a B) \operatorname{Cot}[c+d x] \sqrt{a+b \tan [c+d x]}}{4 d} - \frac{a A \operatorname{Cot}[c+d x]^2 (a+b \tan [c+d x])^{3/2}}{2 d}$$

Result (type 4, 39536 leaves): Display of huge result suppressed!

**Problem 338: Humongous result has more than 200000 leaves.**

$$\int \operatorname{Cot}[c+d x]^4 (a+b \tan [c+d x])^{5/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 277 leaves, 14 steps):

$$\frac{(40 a^2 A b - 5 A b^3 + 16 a^3 B - 30 a b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}}\right]}{8 \sqrt{a} d} -$$

$$\frac{(a - i b)^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{d} + \frac{(a + i b)^{5/2} (i A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{d} +$$

$$\frac{(8 a^2 A - 11 A b^2 - 18 a b B) \operatorname{Cot}[c+d x] \sqrt{a+b \tan [c+d x]}}{8 d} -$$

$$\frac{a (3 A b + 2 a B) \operatorname{Cot}[c+d x]^2 \sqrt{a+b \tan [c+d x]}}{4 d} - \frac{a A \operatorname{Cot}[c+d x]^3 (a+b \tan [c+d x])^{3/2}}{3 d}$$

Result (type ?, 240294 leaves): Display of huge result suppressed!

**Problem 339: Humongous result has more than 200000 leaves.**

$$\int \operatorname{Cot}[c+d x]^5 (a+b \tan [c+d x])^{5/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 342 leaves, 15 steps):

$$\begin{aligned}
 & -\frac{1}{64 a^{3/2} d} (128 a^4 A - 240 a^2 A b^2 - 5 A b^4 - 320 a^3 b B + 40 a b^3 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a}}\right] + \\
 & \frac{(a-i b)^{5/2} (A-i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} + \frac{(a+i b)^{5/2} (A+i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} + \\
 & \frac{1}{64 a d} (144 a^2 A b - 5 A b^3 + 64 a^3 B - 88 a b^2 B) \operatorname{Cot}[c+d x] \sqrt{a+b \operatorname{Tan}[c+d x]} + \\
 & \frac{(48 a^2 A - 59 A b^2 - 104 a b B) \operatorname{Cot}[c+d x]^2 \sqrt{a+b \operatorname{Tan}[c+d x]}}{96 d} - \\
 & \frac{a (11 A b + 8 a B) \operatorname{Cot}[c+d x]^3 \sqrt{a+b \operatorname{Tan}[c+d x]}}{24 d} - \frac{a A \operatorname{Cot}[c+d x]^4 (a+b \operatorname{Tan}[c+d x])^{3/2}}{4 d}
 \end{aligned}$$

Result (type ?, 258206 leaves): Display of huge result suppressed!

### Problem 340: Result more than twice size of optimal antiderivative.

$$\int (-a+b \operatorname{Tan}[c+d x]) (a+b \operatorname{Tan}[c+d x])^{5/2} dx$$

Optimal (type 3, 151 leaves, 10 steps):

$$\begin{aligned}
 & \frac{(i a-b) (a-i b)^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{d} - \frac{(a+i b)^{5/2} (i a+b) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{d} - \\
 & \frac{2 b (a^2+b^2) \sqrt{a+b \operatorname{Tan}[c+d x]}}{d} + \frac{2 b (a+b \operatorname{Tan}[c+d x])^{5/2}}{5 d}
 \end{aligned}$$

Result (type 3, 479 leaves):

$$\begin{aligned}
 & \left( \cos [c + d x]^3 (-a + b \tan [c + d x]) (a + b \tan [c + d x])^{5/2} \right. \\
 & \quad \left. \left( \frac{4}{5} b (2 a^2 + 3 b^2) - \frac{2}{5} b^3 \sec [c + d x]^2 - \frac{4}{5} a b^2 \tan [c + d x] \right) \right) / \\
 & \quad \left( d (a \cos [c + d x] - b \sin [c + d x]) (a \cos [c + d x] + b \sin [c + d x])^2 \right) + \\
 & \quad \left( (a^2 + b^2) (-a + b \tan [c + d x]) (a + b \tan [c + d x])^{5/2} \right. \\
 & \quad \left. \left( - \left( \left( i (a^2 - b^2) \left( \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \sqrt{a+b \tan [c+d x]} \right) \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right) \right) - \\
 & \quad \left( 2 a b \left( \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{\sqrt{a+i b}} \right) \sqrt{a+b \tan [c+d x]} \right) / \\
 & \quad \left. \left( \sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right) \right) \right) / \\
 & \quad \left( d \sec [c + d x]^{7/2} (a \cos [c + d x] - b \sin [c + d x]) (a \cos [c + d x] + b \sin [c + d x])^{5/2} \right)
 \end{aligned}$$

**Problem 341: Result unnecessarily involves imaginary or complex numbers.**

$$\int (-a + b \tan [c + d x]) (a + b \tan [c + d x])^{3/2} dx$$

Optimal (type 3, 408 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{b (a^2 + b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} - \sqrt{2} \sqrt{a + b \operatorname{Tan}[c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right]}{\sqrt{2} \sqrt{a - \sqrt{a^2 + b^2}} d} + \\
 & \frac{b (a^2 + b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} + \sqrt{2} \sqrt{a + b \operatorname{Tan}[c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right]}{\sqrt{2} \sqrt{a - \sqrt{a^2 + b^2}} d} - \\
 & \left( b (a^2 + b^2) \operatorname{Log} \left[ a + \sqrt{a^2 + b^2} + b \operatorname{Tan}[c + d x] - \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} \sqrt{a + b \operatorname{Tan}[c + d x]} \right] \right) / \\
 & \left( 2 \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} d \right) + \\
 & \left( b (a^2 + b^2) \operatorname{Log} \left[ a + \sqrt{a^2 + b^2} + b \operatorname{Tan}[c + d x] + \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} \sqrt{a + b \operatorname{Tan}[c + d x]} \right] \right) / \\
 & \left( 2 \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} d \right) + \frac{2 b (a + b \operatorname{Tan}[c + d x])^{3/2}}{3 d}
 \end{aligned}$$

Result (type 3, 180 leaves):

$$\begin{aligned}
 & \left( \operatorname{Cos}[c + d x]^2 (a - b \operatorname{Tan}[c + d x]) \right. \\
 & (a + b \operatorname{Tan}[c + d x]) \left( 3 i \sqrt{a - i b} (a^2 + b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \operatorname{Tan}[c + d x]}}{\sqrt{a - i b}} \right] - \right. \\
 & \left. \left. 3 i \sqrt{a + i b} (a^2 + b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \operatorname{Tan}[c + d x]}}{\sqrt{a + i b}} \right] + 2 b (a + b \operatorname{Tan}[c + d x])^{3/2} \right) \right) / \\
 & (3 d (a^2 \operatorname{Cos}[c + d x]^2 - b^2 \operatorname{Sin}[c + d x]^2))
 \end{aligned}$$

**Problem 342: Result unnecessarily involves imaginary or complex numbers.**

$$\int (-a + b \operatorname{Tan}[c + d x]) \sqrt{a + b \operatorname{Tan}[c + d x]} dx$$

Optimal (type 3, 422 leaves, 13 steps):

$$\begin{aligned}
 & \frac{b \sqrt{a^2 + b^2} \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} - \sqrt{2} \sqrt{a + b \tan[c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right]}{\sqrt{2} \sqrt{a - \sqrt{a^2 + b^2}} d} + \\
 & \frac{b \sqrt{a^2 + b^2} \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} + \sqrt{2} \sqrt{a + b \tan[c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right]}{\sqrt{2} \sqrt{a - \sqrt{a^2 + b^2}} d} + \\
 & \left( b \sqrt{a^2 + b^2} \operatorname{Log} \left[ a + \sqrt{a^2 + b^2} + b \tan[c + d x] - \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} \sqrt{a + b \tan[c + d x]} \right] \right) / \\
 & \left( 2 \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} d \right) - \\
 & \left( b \sqrt{a^2 + b^2} \operatorname{Log} \left[ a + \sqrt{a^2 + b^2} + b \tan[c + d x] + \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} \sqrt{a + b \tan[c + d x]} \right] \right) / \\
 & \left( 2 \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} d \right) + \frac{2 b \sqrt{a + b \tan[c + d x]}}{d}
 \end{aligned}$$

Result (type 3, 120 leaves):

$$\frac{1}{d} \operatorname{Im} \left( \frac{(a^2 + b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan[c + d x]}}{\sqrt{a - i b}} \right]}{\sqrt{a - i b}} - \frac{(a^2 + b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan[c + d x]}}{\sqrt{a + i b}} \right]}{\sqrt{a + i b}} - 2 i b \sqrt{a + b \tan[c + d x]} \right)$$

**Problem 348:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cot}[c + d x]^2 (A + B \tan[c + d x])}{\sqrt{a + b \tan[c + d x]}} dx$$

Optimal (type 3, 169 leaves, 12 steps):

$$\frac{(A b - 2 a B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}}\right]}{a^{3/2} d} + \frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b} d} - \frac{(i A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b} d} - \frac{A \operatorname{Cot}[c+d x] \sqrt{a+b \tan [c+d x]}}{a d}$$

Result (type 4, 17 098 leaves):

$$\frac{A (B + A \operatorname{Cot}[c+d x]) (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])}{a d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) \sqrt{a+b \tan [c+d x]}} + \left( 2 (B + A \operatorname{Cot}[c+d x]) \left( -A b \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right]} \right), \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + (A b - 2 a B) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}} \right], \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + 2 i a A \operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}} \right], \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + 2 a B \operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}} \right], \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - 2 i a A \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}} \right], \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + 2 a B \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}} \right], \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + A b \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}} \right], \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \right),$$



$$\begin{aligned}
 & \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \Big] - 2 a B \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] \\
 & \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \\
 & \left( -\frac{A b \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]}}{2 a \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} + \frac{B \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]}}{2 \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} + \right. \\
 & \frac{B \text{Cos}[2 (c + d x)] \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]}}{2 \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} - \\
 & \left. \frac{A \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \text{Sin}[2 (c + d x)]}{2 \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} \right) \\
 & \left( -1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \left( 1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{(-a - b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]\right)}} \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]\right)}} \\
 & \sqrt{\frac{1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}} \\
 & \sqrt{\frac{a + 2 b \text{Tan} \left[ \frac{1}{2} (c + d x) \right] - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}} \Big/ \\
 & \left( a d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]\right)}} \right. \\
 & \left. \left( -2 b \text{Tan} \left[ \frac{1}{2} (c + d x) \right] + a \left( -1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \\
 & \left( - \left( \left( \left( \left( -A b \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + \right. \right. \right. \right. \\
 & \left. \left. \left. \left. (A b - 2 a B) \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + \\
 & 2i a A \text{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \\
 & 2 a B \text{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - \\
 & 2i a A \text{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \\
 & 2 a B \text{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + A b \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 2 a B \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}} \\
 & \left(-b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 + a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right) \\
 & \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}} \sqrt{\frac{a + 2b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}} \Big/ \\
 & \left( a \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}} \right. \\
 & \left. \left(-2b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right)^2\right) \right) + \\
 & \left( \left( -A b \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + \right. \right. \\
 & (A b - 2 a B) \operatorname{EllipticPi}\left[\frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + 2 i a A \operatorname{EllipticPi}\left[ \right. \\
 & \left. -\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}}\right], \right. \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + 2 a B \operatorname{EllipticPi}\left[-\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] - 2 i a A \operatorname{EllipticPi}\left[ \right. \\
 & \left. \frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}}\right], \right. \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + 2 a B \operatorname{EllipticPi}\left[\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right]
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + A b \text{EllipticPi} [ \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - 2 a B \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \right. \\
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \right) \\
 & \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 (-1+\tan[\frac{1}{2}(c+dx)]) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)]}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \sqrt{\frac{1+\tan[\frac{1}{2}(c+dx)]^2}{1-\tan[\frac{1}{2}(c+dx)]^2}} \\
 & \sqrt{\frac{a+2 b \tan[\frac{1}{2}(c+dx)]-a \tan[\frac{1}{2}(c+dx)]^2}{1+\tan[\frac{1}{2}(c+dx)]^2}} \Big/ \\
 & \left( a \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right. \\
 & \left. \left( -2 b \tan[\frac{1}{2}(c+dx)] + a \left( -1+\tan[\frac{1}{2}(c+dx)]^2 \right) \right) \right) + \\
 & \left( \left( -A b \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \right) + \right. \\
 & \left. (A b - 2 a B) \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \right. \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \right] + 2 i a A \text{EllipticPi} [
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 2aB \operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 2iaA \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right], \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 2aB \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + Ab \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right], \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} - 2aB \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \Big/
 \end{aligned}$$

$$\left( a \sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right. \\ \left. \left( -2b \tan\left[\frac{1}{2}(c+dx)\right] + a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \right) - \\ \left( \left( -Ab \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \right. \right. \\ \left. \left( Ab - 2aB \right) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 2i a A \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 2i a A \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right]\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 2aB \operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right]\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 2i a A \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right]\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 2aB \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right]\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + Ab \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + Ab \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right]\right], \frac{a+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}\right] \right) \right)$$

$$\begin{aligned}
 & \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \Big] - 2 a B \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] \\
 & \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right) \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \text{Tan} \left[\frac{1}{2} (c + d x)\right]}{(-a - b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \\
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[\frac{1}{2} (c + d x)\right]}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \sqrt{\frac{1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}{1 - \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}} \\
 & \sqrt{\frac{a + 2 b \text{Tan} \left[\frac{1}{2} (c + d x)\right] - a \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}{1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}} \\
 & \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \text{Sec} \left[\frac{1}{2} (c + d x)\right]^2}{2 (a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)} - \left( (-a + b + \sqrt{a^2 + b^2}) \text{Sec} \left[\frac{1}{2} (c + d x)\right]^2 \right. \right. \\
 & \left. \left. \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right) \right) / \left( 2 (a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)^2 \right) \right) / \\
 & \left( a \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)} \right)^{3/2} \left( -2 b \text{Tan} \left[\frac{1}{2} (c + d x)\right] + \right. \right. \\
 & \left. \left. a \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)^2 \right) \right) + \\
 & \left( \left( -A b \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + \right. \right. \\
 & \left. \left. (A b - 2 a B) \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + 2 i a A \text{EllipticPi} \left[ \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 2aB \operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 2iA \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 2aB \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + A \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} - 2aB \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}\right] \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left(-\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}\right) -
 \end{aligned}$$



$$\left. \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(b - \sqrt{a^2+b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{2 \left(-a-b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2}\right) \Bigg/$$

$$\left( a \sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \right.$$

$$\sqrt{\frac{b - \sqrt{a^2+b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\left(-a-b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}$$

$$\left. \left(-2b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + a \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) +$$

$$\left( \left( -A b \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \right.$$

$$(A b - 2 a B) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 2 i a A \operatorname{EllipticPi}\left[\frac{i \left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 2 a B \operatorname{EllipticPi}\left[-\frac{i \left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 2 i a A \operatorname{EllipticPi}\left[\frac{i \left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 2 a B \operatorname{EllipticPi}\left[-\frac{i \left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right]$$

$$\begin{aligned} & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + A b \text{EllipticPi}\left[ \right. \\ & \left. \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \right. \right. \\ & \left. \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 2 a B \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \right. \right. \\ & \left. \left. \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \right) \right. \\ & \left. \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \right. \\ & \left. \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\ & \left. \sqrt{\frac{a+2 b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\ & \left. \left(\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)} + \right. \right. \\ & \left. \left. \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2(b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right])}{2(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2}\right)\right) \Bigg/ \\ & \left(a \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right. \\ & \left. \sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right. \\ & \left. \left(-2 b \tan\left[\frac{1}{2}(c+dx)\right]+a\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) \Bigg) + \end{aligned}$$

$$\left( \left( -A b \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \right.$$

$$(A b - 2 a B) \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + 2 i a A \operatorname{EllipticPi} \left[ \right.$$

$$-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]},$$

$$\left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + 2 a B \operatorname{EllipticPi} \left[ -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - 2 i a A \operatorname{EllipticPi} \left[ \right.$$

$$\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]},$$

$$\left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + 2 a B \operatorname{EllipticPi} \left[ \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + A b \operatorname{EllipticPi} \left[ \right.$$

$$\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]},$$

$$\left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - 2 a B \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right]$$

$$\left. \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right]$$

$$\left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)$$

$$\begin{aligned}
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{(-a - b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}} \\
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}} \\
 & \sqrt{\frac{a + 2b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}} \\
 & \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2} + \left( \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] \right. \right. \\
 & \quad \left. \left. \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right) \right) / \left(1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right)^2 \right) / \\
 & \left( a \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}} \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2}} \right. \\
 & \quad \left. \left(-2b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right)\right) \right) + \\
 & \left( \left( -Ab \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + \right. \\
 & \quad (Ab - 2aB) \operatorname{EllipticPi}\left[\frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + 2i a \operatorname{EllipticPi}\left[\right. \\
 & \quad \left. -\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right] \right), \\
 & \quad \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + 2aB \operatorname{EllipticPi}\left[-\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - 2i a A \text{EllipticPi}[ \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + 2 a B \text{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + A b \text{EllipticPi}\left[ \right. \right. \\
 & \left. \left. \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \right] \right], \\
 & \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 2 a B \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \right. \\
 & \left. \left. \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \right) \right) \\
 & \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left(\frac{b \sec\left[\frac{1}{2}(c+dx)\right]^2 - a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2} - \right. \\
 & \left. \left(\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\left(a+2 b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) / \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \Bigg) / \left(a \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a + 2 b \tan\left[\frac{1}{2}(c + d x)\right] - a \tan\left[\frac{1}{2}(c + d x)\right]^2}{1 + \tan\left[\frac{1}{2}(c + d x)\right]^2}} \\
 & \left(-2 b \tan\left[\frac{1}{2}(c + d x)\right] + a \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]^2\right)\right) + \\
 & \left(2 \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right) \left(1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)\right. \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}{(-a - b + \sqrt{a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)}} \\
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)}} \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c + d x)\right]^2}{1 - \tan\left[\frac{1}{2}(c + d x)\right]^2}} \\
 & \sqrt{\frac{a + 2 b \tan\left[\frac{1}{2}(c + d x)\right] - a \tan\left[\frac{1}{2}(c + d x)\right]^2}{1 + \tan\left[\frac{1}{2}(c + d x)\right]^2}} \\
 & \left(-\left(\left(A b \left(\frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2}{2(a + b + \sqrt{a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)} - \left((-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \left(1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)\right) / \left(2(a + b + \sqrt{a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)\right)\right)\right) / \left(2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)}}\right.\right. \\
 & \left.\left.\sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)}} \sqrt{\left(1 - \frac{((a + \sqrt{a^2 + b^2}) (-a + b + \sqrt{a^2 + b^2}) \left(1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)) / \left((a - \sqrt{a^2 + b^2}) (a + b + \sqrt{a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(c + d x)\right]\right)\right)}{2}\right)}\right)\right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( A b \left( \frac{(-a+b+\sqrt{a^2+b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \left( (-a+b+\sqrt{a^2+b^2}) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \right. \\
 & \quad \left. \left. \left. \left( 2(a+b+\sqrt{a^2+b^2}) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \right) \right) / \right. \\
 & \left( 2 \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \left( 1 - \frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) \right) \\
 & \sqrt{1 - \frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \\
 & \sqrt{\left( 1 - \left( (a+\sqrt{a^2+b^2}) \left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) /} \\
 & \quad \left. \left. \left. \left( (a-\sqrt{a^2+b^2}) \left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) \right) - \right. \\
 & \left( a B \left( \frac{(-a+b+\sqrt{a^2+b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \left( (-a+b+\sqrt{a^2+b^2}) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \right. \\
 & \quad \left. \left. \left. \left( 2(a+b+\sqrt{a^2+b^2}) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \right) \right) / \right. \\
 & \left( \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \left( 1 - \frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) \right) \\
 & \sqrt{1 - \frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \\
 & \sqrt{\left( 1 - \left( (a+\sqrt{a^2+b^2}) \left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) /} \\
 & \quad \left. \left. \left. \left( (a-\sqrt{a^2+b^2}) \left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( i a A \left( \frac{(-a+b+\sqrt{a^2+b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \left( (-a+b+\sqrt{a^2+b^2}) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \right. \\
 & \quad \left. \left. \left. \left( 2(a+b+\sqrt{a^2+b^2}) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right)^2 \right) \right) \right) / \\
 & \left( \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \left(1 - \frac{i\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}\right)} \right. \\
 & \quad \left. \sqrt{1 - \frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \right. \right. \\
 & \quad \left. \left. \sqrt{\left(1 - \left( (a+\sqrt{a^2+b^2}) \left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \right. \right. \\
 & \quad \left. \left. \left. \left( (a-\sqrt{a^2+b^2}) \left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) \right) \right) + \\
 & \left( a B \left( \frac{(-a+b+\sqrt{a^2+b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \left( (-a+b+\sqrt{a^2+b^2}) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \right. \\
 & \quad \left. \left. \left. \left( 2(a+b+\sqrt{a^2+b^2}) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right)^2 \right) \right) \right) / \\
 & \left( \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \left(1 - \frac{i\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}\right)} \right. \\
 & \quad \left. \sqrt{1 - \frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \right. \right. \\
 & \quad \left. \left. \sqrt{\left(1 - \left( (a+\sqrt{a^2+b^2}) \left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) / \right. \right. \\
 & \quad \left. \left. \left. \left( (a-\sqrt{a^2+b^2}) \left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) \right) \right) +
 \end{aligned}$$



$$\begin{aligned}
 & \left( i a A \left( \frac{(-a+b+\sqrt{a^2+b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])} - \left( (-a+b+\sqrt{a^2+b^2}) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \right. \\
 & \quad \left. \left. \left. \left( 2(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \right) \right) / \\
 & \left( \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}} \left( 1 + \frac{i(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) \right) \\
 & \sqrt{1 - \frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}} \\
 & \sqrt{\left( 1 - \left( (a+\sqrt{a^2+b^2})(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]) \right) \right) /} \\
 & \quad \left. \left( (a-\sqrt{a^2+b^2})(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]) \right) \right) \right) + \\
 & \left( a B \left( \frac{(-a+b+\sqrt{a^2+b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])} - \left( (-a+b+\sqrt{a^2+b^2}) \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \right. \\
 & \quad \left. \left. \left. \left( 2(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \right) \right) / \\
 & \left( \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}} \left( 1 + \frac{i(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) \right) \\
 & \sqrt{1 - \frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}} \\
 & \sqrt{\left( 1 - \left( (a+\sqrt{a^2+b^2})(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]) \right) \right) /} \\
 & \quad \left. \left( (a-\sqrt{a^2+b^2})(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]) \right) \right) \right) +
 \end{aligned}$$

$$\left( (A b - 2 a B) \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2}{2(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])} - \right. \right. \\ \left. \left( (-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right) \right) \right) / \\ \left. \left( 2(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])^2 \right) \right) / \\ \left( 2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])}} \right. \\ \left. \left( 1 - \frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])}{(a - b - \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])} \right) \right. \\ \left. \sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])}} \right. \\ \left. \sqrt{\left( 1 - \left( (a + \sqrt{a^2 + b^2})(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]) \right) \right) / \right. \\ \left. \left. \left( (a - \sqrt{a^2 + b^2})(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]) \right) \right) \right) \right) / \\ \left( a \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])}{(a + b + \sqrt{a^2 + b^2})(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right])}} \left( -2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + \right. \right. \\ \left. \left. a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right) \right) \sqrt{a + b \operatorname{Tan}[c + d x]} \right)$$

**Problem 349: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^3 (A + B \operatorname{Tan}[c + d x])}{\sqrt{a + b \operatorname{Tan}[c + d x]}} dx$$

Optimal (type 3, 224 leaves, 13 steps):

$$\frac{(8 a^2 A - 3 A b^2 + 4 a b B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}}\right]}{4 a^{5/2} d} -$$

$$\frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b} d} - \frac{(A + i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b} d} +$$

$$\frac{(3 A b - 4 a B) \operatorname{Cot}[c+d x] \sqrt{a+b \tan [c+d x]}}{4 a^2 d} - \frac{A \operatorname{Cot}[c+d x]^2 \sqrt{a+b \tan [c+d x]}}{2 a d}$$

Result (type 4, 19139 leaves):

$$\left( (B + A \operatorname{Cot}[c+d x]) \right.$$

$$\left. \left( b (3 A b - 4 a B) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right]} \right], \right.$$

$$\frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \left. \right] + (8 a^2 A - 3 A b^2 + 4 a b B) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \right.$$

$$\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \left. \right] - 8 a^2 A$$

$$\operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right] \right],$$

$$\frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \left. \right] + 8 i a^2 B \operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \right.$$

$$\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \left. \right] - 8 a^2 A$$

$$\operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right] \right],$$

$$\frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \left. \right] - 8 i a^2 B \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \right.$$

$$\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+d x)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \left. \right] + 8 a^2 A \operatorname{EllipticPi}\left[ \right.$$

$$\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] -$$

$$3 A b^2 \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right]\right],$$

$$\frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + 4 a b B \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}},$$

$$\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right]$$

$$\sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx] \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}$$

$$\left(-\frac{A \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}} + \frac{3 A b^2 \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]}}{8 a^2 \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}} -$$

$$\frac{b B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]}}{2 a \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}} - \frac{A \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}} -$$

$$\frac{B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)]}{2 \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}}\right)$$

$$\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)$$

$$\sqrt{\frac{b-\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}$$

$$\sqrt{\frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}$$

$$\sqrt{\frac{a+2 b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}}\right) /$$

$$\left(2 a^2 d (A \operatorname{Cos}[c+dx]+B \operatorname{Sin}[c+dx]) \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}\right)$$

$$\begin{aligned}
 & \left( -2 b \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right] + a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) \\
 & \left( - \left( \left( \left( b (3 A b - 4 a B) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}} \right]} \right), \right. \right. \right. \\
 & \quad \left. \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + (8 a^2 A - 3 A b^2 + 4 a b B) \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - \right. \\
 & \quad \left. 8 a^2 A \operatorname{EllipticPi} \left[ -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \right. \\
 & \quad \left. 8 i a^2 B \operatorname{EllipticPi} \left[ -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - \right. \\
 & \quad \left. 8 a^2 A \operatorname{EllipticPi} \left[ \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - \right. \\
 & \quad \left. 8 i a^2 B \operatorname{EllipticPi} \left[ \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \right. \\
 & \quad \left. 8 a^2 A \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \right. \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}[\frac{1}{2}(c+d x)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3 A b^2 \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \\
 & 4 a b B \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right) \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)]}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \left( -b \sec^2 \left[ \frac{1}{2}(c+dx) \right] + a \sec^2 \left[ \frac{1}{2}(c+dx) \right] \tan^2 \left[ \frac{1}{2}(c+dx) \right] \right) \\
 & \sqrt{\frac{1+\tan[\frac{1}{2}(c+dx)]^2}{1-\tan[\frac{1}{2}(c+dx)]^2}} \sqrt{\frac{a+2b \tan[\frac{1}{2}(c+dx)]-a \tan^2[\frac{1}{2}(c+dx)]}{1+\tan[\frac{1}{2}(c+dx)]^2}} \Big/ \\
 & \left( 2 a^2 \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right. \\
 & \left. \left( -2 b \tan \left[ \frac{1}{2}(c+dx) \right] + a \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right]^2 \right)^2 \right) \right) \Bigg] + \\
 & \left( \left( b (3 A b - 4 a B) \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \right. \right. \\
 & \left. \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + (8 a^2 A - 3 A b^2 + 4 a b B) \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - 8 a^2 A \text{EllipticPi} \left[ \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 8i a^2 \operatorname{B EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8a^2 \operatorname{A EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right], \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} - 8i a^2 \operatorname{B EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \\
 & \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \\
 & 8a^2 \operatorname{A EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 3Ab^2 \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right], \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 4ab \operatorname{B EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}}
 \end{aligned}$$

$$\sqrt{\frac{a + 2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \Big/$$

$$\left( 4 a^2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)} \right. \right.$$

$$\left. \left. \left(-2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2\right)\right) \right) +$$

$$\left( \left( b (3 A b - 4 a B) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)} \right]\right], \right.$$

$$\frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + (8 a^2 A - 3 A b^2 + 4 a b B) \operatorname{EllipticPi}\left[\frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\right.$$

$$\left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - 8 a^2 A \operatorname{EllipticPi}\left[\right.$$

$$\left. -\frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)} \right]\right],$$

$$\frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + 8 i a^2 B \operatorname{EllipticPi}\left[-\frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\right.$$

$$\left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - 8 a^2 A \operatorname{EllipticPi}\left[\right.$$

$$\left. \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)} \right]\right],$$

$$\frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - 8 i a^2 B \operatorname{EllipticPi}\left[\frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \right.$$

$$\left. \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]\right)} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] +$$



$$\begin{aligned}
 & 8 a^2 A \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - 3 A b^2 \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \\
 & + 4 a b B \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \\
 & + \operatorname{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan \left[ \frac{1}{2}(c+dx) \right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan \left[ \frac{1}{2}(c+dx) \right])}} \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan \left[ \frac{1}{2}(c+dx) \right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan \left[ \frac{1}{2}(c+dx) \right])}} \sqrt{\frac{1+\tan \left[ \frac{1}{2}(c+dx) \right]^2}{1-\tan \left[ \frac{1}{2}(c+dx) \right]^2}} \\
 & \sqrt{\frac{a+2 b \tan \left[ \frac{1}{2}(c+dx) \right]-a \tan \left[ \frac{1}{2}(c+dx) \right]^2}{1+\tan \left[ \frac{1}{2}(c+dx) \right]^2}} \left/ \right. \\
 & \left( 4 a^2 \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan \left[ \frac{1}{2}(c+dx) \right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan \left[ \frac{1}{2}(c+dx) \right])}} \right. \\
 & \left. \left. \left( -2 b \tan \left[ \frac{1}{2}(c+dx) \right] + a \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right]^2 \right) \right) \right) \right) - \\
 & \left( \left( b (3 A b - 4 a B) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan \left[ \frac{1}{2}(c+dx) \right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan \left[ \frac{1}{2}(c+dx) \right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \right. \right. \\
 & \left. \left. + (8 a^2 A - 3 A b^2 + 4 a b B) \operatorname{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan \left[ \frac{1}{2}(c+dx) \right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan \left[ \frac{1}{2}(c+dx) \right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - 8 a^2 A \text{EllipticPi} [ \\
 & -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + 8 i a^2 B \text{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8 a^2 A \text{EllipticPi} [ \right. \\
 & \left. \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right] \right], \\
 & \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8 i a^2 B \text{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 8 a^2 A \text{EllipticPi} [ \right. \\
 & \left. \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right] \right], \\
 & \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 3 A b^2 \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 4 a b B \text{EllipticPi} [ \right. \\
 & \left. \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right] \right], \\
 & \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{(-a - b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \\
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \\
 & \sqrt{\frac{a + 2 b \tan \left[ \frac{1}{2} (c + d x) \right] - a \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \\
 & \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 (a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])} - \right. \\
 & \left. \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (1 + \tan \left[ \frac{1}{2} (c + d x) \right])}{2 (a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])^2} \right) \right) / \\
 & \left( 4 a^2 \left( \frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (c + d x) \right])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])} \right)^{3/2} \right. \\
 & \left. \left( -2 b \tan \left[ \frac{1}{2} (c + d x) \right] + a (-1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2) \right) \right) + \\
 & \left( \left( b (3 A b - 4 a B) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (c + d x) \right])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \right] \right), \right. \right. \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + (8 a^2 A - 3 A b^2 + 4 a b B) \operatorname{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (c + d x) \right])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \right] \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - 8 a^2 A \operatorname{EllipticPi} \left[ \right. \\
 & \left. - \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (c + d x) \right])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \right] \right], \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + 8 i a^2 B \operatorname{EllipticPi} \left[ -\frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - 8a^2 A \text{EllipticPi}\left[ \right. \\
 & \left. \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \right. \right. \\
 & \left. \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8i a^2 B \text{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \right. \right. \\
 & \left. \left. 8a^2 A \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 3A b^2 \text{EllipticPi}\left[ \right. \right. \\
 & \left. \left. \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \right. \right. \\
 & \left. \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 4ab B \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \right) \\
 & \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a\tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a+2b\tan\left[\frac{1}{2}(c+dx)\right]-a\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left(-\frac{a\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(-a-b+\sqrt{a^2+b^2})\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}\right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(b - \sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]\right)}{2 \left(-a-b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2} \right) \Bigg/ \\
 & \left( 4a^2 \sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right. \\
 & \sqrt{\frac{b - \sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\left(-a-b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \\
 & \left. \left(-2b \tan\left[\frac{1}{2}(c+dx)\right] + a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right) + \\
 & \left( \left( b(3Ab-4aB) \text{EllipticF}\left[\text{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \right. \right. \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \left. \left. + (8a^2A-3Ab^2+4abB) \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8a^2A \text{EllipticPi}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8a^2A \text{EllipticPi}\left[-\frac{i\left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 8ia^2B \text{EllipticPi}\left[-\frac{i\left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8a^2A \text{EllipticPi}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8ia^2B \text{EllipticPi}\left[-\frac{i\left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \Big] + \\
 & 8 a^2 A \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - 3 A b^2 \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}} + 4 a b B \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \\
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \right) \\
 & \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
 & \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a+2 b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left( \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])} + \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2(b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right])}{2(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])^2} \right) \Big/ \\
 & \left( 4 a^2 \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right. \\
 & \left. \sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right)
 \end{aligned}$$

$$\left( -2 b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \right) +$$

$$\left( b \left( 3 A b - 4 a B \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \right.$$

$$\left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \left( 8 a^2 A - 3 A b^2 + 4 a b B \right) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8 a^2 A \operatorname{EllipticPi}\left[\frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - \frac{i\left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 8 i a^2 B \operatorname{EllipticPi}\left[-\frac{i\left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8 a^2 A \operatorname{EllipticPi}\left[\frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - \frac{i\left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8 i a^2 B \operatorname{EllipticPi}\left[\frac{i\left(a+b+\sqrt{a^2+b^2}\right)}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + 8 a^2 A \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 3 A b^2 \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right], \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right)}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right],$$

$$\begin{aligned}
 & \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} + 4 a b B \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] \\
 & \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right) \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \text{Tan} \left[\frac{1}{2} (c + d x)\right]}{(-a - b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \\
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[\frac{1}{2} (c + d x)\right]}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \\
 & \sqrt{\frac{a + 2 b \text{Tan} \left[\frac{1}{2} (c + d x)\right] - a \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}{1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}} \\
 & \left(\frac{\text{Sec} \left[\frac{1}{2} (c + d x)\right]^2 \text{Tan} \left[\frac{1}{2} (c + d x)\right]}{1 - \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2} + \left(\text{Sec} \left[\frac{1}{2} (c + d x)\right]\right)^2 \text{Tan} \left[\frac{1}{2} (c + d x)\right] \right. \\
 & \left. \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2\right) \right) / \left(1 - \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2\right)^2 \Bigg) / \\
 & \left(4 a^2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \sqrt{\frac{1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}{1 - \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2}} \right. \\
 & \left. \left(-2 b \text{Tan} \left[\frac{1}{2} (c + d x)\right] + a \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]^2\right)\right) \right) + \\
 & \left( \left( b (3 A b - 4 a B) \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \right] \right), \right. \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} + (8 a^2 A - 3 A b^2 + 4 a b B) \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \right. \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left(1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \text{Tan} \left[\frac{1}{2} (c + d x)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - 8 a^2 A \text{EllipticPi} \left[ \right.
 \end{aligned}$$



$$\begin{aligned}
 & -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 8i a^2 \operatorname{B EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 8a^2 \operatorname{A EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right], \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} - 8i a^2 \operatorname{B EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \\
 & \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + \\
 & 8a^2 \operatorname{A EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - 3Ab^2 \operatorname{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right], \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} + 4ab \operatorname{B EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \sqrt{\frac{b-\sqrt{a^2+b^2}-a\tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)}} \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}} \\
 & \left( \frac{b \sec\left[\frac{1}{2}(c + dx)\right]^2 - a \sec\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2} - \right. \\
 & \left. \left( \sec\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \left( a + 2b \tan\left[\frac{1}{2}(c + dx)\right] - a \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \right) / \\
 & \left. \left( 1 + \tan\left[\frac{1}{2}(c + dx)\right]^2 \right)^2 \right) / \\
 & \left( 4a^2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})\left(1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)}} \right. \\
 & \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(c + dx)\right] - a \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}} \\
 & \left. \left( -2b \tan\left[\frac{1}{2}(c + dx)\right] + a \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) \right) + \\
 & \left( \left( -1 + \tan\left[\frac{1}{2}(c + dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c + dx)\right] \right) \right. \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{(-a - b + \sqrt{a^2 + b^2})\left(-1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)}} \\
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)}} \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c + dx)\right]^2}} \\
 & \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(c + dx)\right] - a \tan\left[\frac{1}{2}(c + dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c + dx)\right]^2}} \\
 & \left. \left( b(3Ab - 4aB) \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \sec\left[\frac{1}{2}(c + dx)\right]^2}{2(a + b + \sqrt{a^2 + b^2})\left(-1 + \tan\left[\frac{1}{2}(c + dx)\right]\right)} - \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
 & \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}} \right. \\
 & \sqrt{1 - \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \left. \sqrt{\left( 1 - \left( \left( a + \sqrt{a^2 + b^2} \right) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) /} \right. \\
 & \left. \left( \left( a - \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) + \\
 & \left( 4 a^2 A \left( \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)} - \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) / \right. \\
 & \left. \left. \left. \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \right) \Bigg) / \\
 & \left( \sqrt{\frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( 1 - \frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{-1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) \right. \\
 & \sqrt{1 - \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \left. \sqrt{\left( 1 - \left( \left( a + \sqrt{a^2 + b^2} \right) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) /} \right. \\
 & \left. \left( \left( a - \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) - \\
 & \left( 3 A b^2 \left( \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)} - \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned} & \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{2 \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2} \right) / \\ & \left( 2 \sqrt{\frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \left(1 - \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}\right)}{\sqrt{1 - \frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}} \right. \\ & \left. \sqrt{\left(1 - \left(\left(a + \sqrt{a^2+b^2}\right) \left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)} \right) / \right. \\ & \left. \left(\left(a - \sqrt{a^2+b^2}\right) \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) \right) + \\ & \left( 2 a b B \left( \frac{\left(-a+b + \sqrt{a^2+b^2}\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2 \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \left(\left(-a+b + \sqrt{a^2+b^2}\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) / \right. \right. \\ & \left. \left. \left(2 \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2\right) \right) \right) / \\ & \left( \sqrt{\frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \left(1 - \frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}\right)}{\sqrt{1 - \frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}}} \right. \\ & \left. \sqrt{\left(1 - \left(\left(a + \sqrt{a^2+b^2}\right) \left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)} \right) / \right. \\ & \left. \left(\left(a - \sqrt{a^2+b^2}\right) \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) \right) - \\ & \left( 4 a^2 A \left( \frac{\left(-a+b + \sqrt{a^2+b^2}\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2 \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \left(\left(-a+b + \sqrt{a^2+b^2}\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) / \right. \right. \\ & \left. \left. \left(2 \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2\right) \right) \right) / \right. \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(2\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2\right)} \right) / \\
 & \left( \sqrt{\frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)} \left(1 - \frac{i \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right)}{\sqrt{1 - \frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}}} \right) / \\
 & \sqrt{\left(1 - \left(\left(a + \sqrt{a^2+b^2}\right) \left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)} / \\
 & \left. \left(\left(\left(a - \sqrt{a^2+b^2}\right) \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)\right) - \\
 & \left(4 i a^2 B \left(\frac{\left(-a+b + \sqrt{a^2+b^2}\right) \sec\left[\frac{1}{2}(c+dx)\right]^2}{2\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)} - \right. \right. \\
 & \left. \left(\left(-a+b + \sqrt{a^2+b^2}\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) / \\
 & \left. \left(2\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2\right)\right) / \\
 & \left( \sqrt{\frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)} \left(1 - \frac{i \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]}\right)}{\sqrt{1 - \frac{\left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)}}} \right) / \\
 & \sqrt{\left(1 - \left(\left(a + \sqrt{a^2+b^2}\right) \left(-a+b + \sqrt{a^2+b^2}\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)} / \\
 & \left. \left(\left(\left(a - \sqrt{a^2+b^2}\right) \left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)\right) - \\
 & \left(4 a^2 A \left(\frac{\left(-a+b + \sqrt{a^2+b^2}\right) \sec\left[\frac{1}{2}(c+dx)\right]^2}{2\left(a+b + \sqrt{a^2+b^2}\right) \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)} - \left(\left(-a+b + \sqrt{a^2+b^2}\right)\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(2\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2\right)} \right) / \\
 & \left( \sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \left(1+\frac{i\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}\right)} \right. \\
 & \left. \sqrt{1-\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \right. \\
 & \left. \sqrt{\left(1-\left(\left(a+\sqrt{a^2+b^2}\right)\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)} / \right. \\
 & \left. \left(\left(a-\sqrt{a^2+b^2}\right)\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) + \\
 & \left(4 i a^2 B \left(\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \right. \right. \\
 & \left. \left(\left(-a+b+\sqrt{a^2+b^2}\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right) / \right. \\
 & \left. \left. \left(2\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2\right)\right)\right) / \\
 & \left( \sqrt{\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \left(1+\frac{i\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}\right)} \right. \\
 & \left. \sqrt{1-\frac{\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}{\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \right. \\
 & \left. \sqrt{\left(1-\left(\left(a+\sqrt{a^2+b^2}\right)\left(-a+b+\sqrt{a^2+b^2}\right)\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)\right)} / \right. \\
 & \left. \left(\left(a-\sqrt{a^2+b^2}\right)\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) + \\
 & \left( \left(8 a^2 A-3 A b^2+4 a b B\right) \left(\frac{\left(-a+b+\sqrt{a^2+b^2}\right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2\left(a+b+\sqrt{a^2+b^2}\right)\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
 & \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}} \right. \\
 & \left( 1 - \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a - b - \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)} \right) \\
 & \sqrt{1 - \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \sqrt{\left( 1 - \left( \left( a + \sqrt{a^2 + b^2} \right) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) / \\
 & \left( \left( a - \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Bigg) \Bigg) / \\
 & \left( 2 a^2 \sqrt{\frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( -2 b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + \right. \right. \\
 & \left. \left. a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \Bigg) \\
 & \left. \sqrt{a + b \operatorname{Tan} [c + d x]} \right) + \left( (B + A \operatorname{Cot} [c + d x]) \right. \\
 & \left( \frac{A}{2 a} + \frac{(3 A b \operatorname{Cos} [c + d x] - 4 a B \operatorname{Cos} [c + d x]) \operatorname{Csc} [c + d x]}{4 a^2} - \frac{A \operatorname{Csc} [c + d x]^2}{2 a} \right) \\
 & (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]) \operatorname{Tan} [ \\
 & c + \\
 & d
 \end{aligned}$$

$$\left. x \right) / \left( d \left( A \cos [c + d x] + B \sin [c + d x] \right) \sqrt{a + b \tan [c + d x]} \right)$$

**Problem 350: Result more than twice size of optimal antiderivative.**

$$\int \frac{\tan [c + d x]^3 (A + B \tan [c + d x])}{(a + b \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 264 leaves, 10 steps):

$$\frac{(A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{(a - i b)^{3/2} d} + \frac{(A + i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{(a + i b)^{3/2} d} + \frac{2 a (A b - a B) \tan [c + d x]^2}{b (a^2 + b^2) d \sqrt{a + b \tan [c + d x]}} + \frac{2 (6 a^2 A b + 3 A b^3 - 8 a^3 B - 5 a b^2 B) \sqrt{a + b \tan [c + d x]}}{3 b^3 (a^2 + b^2) d} - \frac{2 (3 a A b - 4 a^2 B - b^2 B) \tan [c + d x] \sqrt{a + b \tan [c + d x]}}{3 b^2 (a^2 + b^2) d}$$

Result (type 3, 575 leaves):



$$\begin{aligned}
 & \left( \sec [c+d x] (a \cos [c+d x]+b \sin [c+d x])^2 \right. \\
 & \quad (A+B \tan [c+d x]) \left( -\frac{2(-6 a^2 A b-3 A b^3+8 a^3 B+5 a b^2 B)}{3(a-i b)(a+i b) b^3} + \right. \\
 & \quad \left. \frac{2(-a^2 A b \sin [c+d x]+a^3 B \sin [c+d x])}{(a-i b)(a+i b) b^2(a \cos [c+d x]+b \sin [c+d x])} + \frac{2 B \tan [c+d x]}{3 b^2} \right) \Bigg) / \\
 & \left( d(A \cos [c+d x]+B \sin [c+d x])(a+b \tan [c+d x])^{3 / 2} \right) - \\
 & \left( \sqrt{\sec [c+d x]}(a \cos [c+d x]+b \sin [c+d x])^{3 / 2}(A+B \tan [c+d x]) \right. \\
 & \quad \left( -\left( \left( i(A b-a B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \sqrt{a+b \tan [c+d x]} \right) \right. \right. \\
 & \quad \left. \left. \left( \sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right) \right) - \right. \\
 & \quad \left( (a A+b B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \sqrt{a+b \tan [c+d x]} \right) / \\
 & \quad \left. \left( \sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right) \right) \Bigg) / \\
 & \left( (a-i b)(a+i b) d(A \cos [c+d x]+B \sin [c+d x])(a+b \tan [c+d x])^{3 / 2} \right)
 \end{aligned}$$

**Problem 351: Result more than twice size of optimal antiderivative.**

$$\int \frac{\tan [c+d x]^2(A+B \tan [c+d x])}{(a+b \tan [c+d x])^{3 / 2}} d x$$

Optimal (type 3, 167 leaves, 9 steps):

$$\begin{aligned}
 & \frac{(i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{(a-i b)^{3 / 2} d} - \frac{(i A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{(a+i b)^{3 / 2} d} - \\
 & \frac{2 a^2(A b-a B)}{b^2\left(a^2+b^2\right) d \sqrt{a+b \tan [c+d x]}} + \frac{2 B \sqrt{a+b \tan [c+d x]}}{b^2 d}
 \end{aligned}$$

Result (type 3, 547 leaves):

$$\left( \text{Sec}[c+dx] (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2 \right. \\ \left. \left( \frac{2(-aAb + 2a^2B + b^2B)}{(a-ib)(a+ib)b^2} - \frac{2(-aAb \text{Sin}[c+dx] + a^2B \text{Sin}[c+dx])}{(a-ib)(a+ib)b(a \text{Cos}[c+dx] + b \text{Sin}[c+dx])} \right) \right. \\ \left. (A+B \text{Tan}[c+dx]) \right) / \left( d (A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a+b \text{Tan}[c+dx])^{3/2} \right) - \\ \left( \sqrt{\text{Sec}[c+dx]} (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^{3/2} (A+B \text{Tan}[c+dx]) \right. \\ \left. \left( - \left( \left( i (aA + bB) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} - \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \text{Tan}[c+dx]} \right) / \right. \right. \right. \\ \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) - \right. \\ \left. \left( (-Ab + aB) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \text{Tan}[c+dx]} \right) / \right. \\ \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) \right) \right) / \\ \left( (a-ib)(a+ib)d (A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a+b \text{Tan}[c+dx])^{3/2} \right)$$

**Problem 352: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Tan}[c+dx] (A+B \text{Tan}[c+dx])}{(a+b \text{Tan}[c+dx])^{3/2}} dx$$

Optimal (type 3, 141 leaves, 8 steps):

$$- \frac{(A-ib) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{(a-ib)^{3/2} d} - \\ \frac{(A+ib) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{(a+ib)^{3/2} d} + \frac{2a(Ab-aB)}{b(a^2+b^2)d \sqrt{a+b \text{Tan}[c+dx]}}$$

Result (type 3, 531 leaves):

$$\begin{aligned}
 & \left( \text{Sec}[c+dx] (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2 \right. \\
 & \quad \left( \frac{2(Ab - aB)}{b(-ia + b)(ia + b)} + \frac{2(-Ab \text{Sin}[c+dx] + aB \text{Sin}[c+dx])}{(a - ib)(a + ib)(a \text{Cos}[c+dx] + b \text{Sin}[c+dx])} \right) \\
 & \quad \left. (A + B \text{Tan}[c+dx]) \right) / \left( d(A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a + b \text{Tan}[c+dx])^{3/2} \right) + \\
 & \left( \sqrt{\text{Sec}[c+dx]} (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^{3/2} (A + B \text{Tan}[c+dx]) \right. \\
 & \quad \left. - \left( \left( ia(Ab - aB) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} - \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \text{Tan}[c+dx]} \right) \right. \right. \\
 & \quad \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) - \right. \\
 & \quad \left. \left( (aA + bB) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \text{Tan}[c+dx]} \right) \right. \right. \\
 & \quad \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) \right) / \\
 & \left( (a - ib)(a + ib)d(A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a + b \text{Tan}[c+dx])^{3/2} \right)
 \end{aligned}$$

**Problem 353: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \text{Tan}[c+dx]}{(a + b \text{Tan}[c+dx])^{3/2}} dx$$

Optimal (type 3, 138 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(ia + B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{(a - ib)^{3/2} d} + \\
 & \frac{(ia - B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{(a + ib)^{3/2} d} - \frac{2(Ab - aB)}{(a^2 + b^2) d \sqrt{a + b \text{Tan}[c+dx]}}
 \end{aligned}$$

Result (type 3, 537 leaves):

$$\left( \text{Sec}[c+dx] (a \cos[c+dx] + b \sin[c+dx])^2 \right. \\ \left. \left( -\frac{2(Ab-aB)}{a(-ia+b)(ia+b)} - \frac{2(-Ab^2 \sin[c+dx] + aB \sin[c+dx])}{a(a-ib)(a+ib)(a \cos[c+dx] + b \sin[c+dx])} \right) \right. \\ \left. (A+B \tan[c+dx]) \right) / \left( d(A \cos[c+dx] + B \sin[c+dx]) (a+b \tan[c+dx])^{3/2} \right) + \\ \left( \sqrt{\text{Sec}[c+dx]} (a \cos[c+dx] + b \sin[c+dx])^{3/2} (A+B \tan[c+dx]) \right. \\ \left. \left( -\left( \left( ia(A+B) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \tan[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} - \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \tan[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \tan[c+dx]} \right) \right) \right. \right. \\ \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \right) \right) - \right. \\ \left. \left( (-Ab+aB) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \tan[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \tan[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \tan[c+dx]} \right) \right) / \\ \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \right) \right) \right) / \\ \left( (a-ib)(a+ib)d(A \cos[c+dx] + B \sin[c+dx]) (a+b \tan[c+dx])^{3/2} \right)$$

**Problem 354: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cot}[c+dx] (A+B \tan[c+dx])}{(a+b \tan[c+dx])^{3/2}} dx$$

Optimal (type 3, 171 leaves, 12 steps):

$$-\frac{2A \text{ArcTanh}\left[\frac{\sqrt{a+b \tan[c+dx]}}{\sqrt{a}}\right]}{a^{3/2}d} + \frac{(A-ib) \text{ArcTanh}\left[\frac{\sqrt{a+b \tan[c+dx]}}{\sqrt{a-ib}}\right]}{(a-ib)^{3/2}d} + \\ \frac{(A+ib) \text{ArcTanh}\left[\frac{\sqrt{a+b \tan[c+dx]}}{\sqrt{a+ib}}\right]}{(a+ib)^{3/2}d} + \frac{2b(Ab-aB)}{a(a^2+b^2)d \sqrt{a+b \tan[c+dx]}}$$

Result (type 4, 24 431 leaves): Display of huge result suppressed!

**Problem 355: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cot}[c + d x]^2 (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{3/2}} dx$$

Optimal (type 3, 219 leaves, 13 steps):

$$\frac{(3 A b - 2 a B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{a^{5/2} d} + \frac{(i A + B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{(a-i b)^{3/2} d} - \frac{(i A - B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{(a+i b)^{3/2} d} - \frac{b (a^2 A + 3 A b^2 - 2 a b B)}{a^2 (a^2 + b^2) d \sqrt{a+b \text{Tan}[c+d x]}} - \frac{A \text{Cot}[c+d x]}{a d \sqrt{a+b \text{Tan}[c+d x]}}$$

Result (type 4, 27 988 leaves): Display of huge result suppressed!

**Problem 356: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\text{Cot}[c + d x]^3 (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{3/2}} dx$$

Optimal (type 3, 285 leaves, 14 steps):

$$\frac{(8 a^2 A - 15 A b^2 + 12 a b B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{4 a^{7/2} d} - \frac{(A-i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{(a-i b)^{3/2} d} - \frac{(A+i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{(a+i b)^{3/2} d} + \frac{b (7 a^2 A b + 15 A b^3 - 4 a^3 B - 12 a b^2 B)}{4 a^3 (a^2 + b^2) d \sqrt{a+b \text{Tan}[c+d x]}} + \frac{(5 A b - 4 a B) \text{Cot}[c+d x]}{4 a^2 d \sqrt{a+b \text{Tan}[c+d x]}} - \frac{A \text{Cot}[c+d x]^2}{2 a d \sqrt{a+b \text{Tan}[c+d x]}}$$

Result (type 4, 29 982 leaves): Display of huge result suppressed!

**Problem 358: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Tan}[c + d x]^3 (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 261 leaves, 10 steps):

$$\frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{(a-i b)^{5/2} d} + \frac{(A+i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{(a+i b)^{5/2} d} + \frac{2 a (A b - a B) \tan [c+d x]^2}{3 b (a^2 + b^2) d (a+b \tan [c+d x])^{3/2}} - \frac{2 a^2 (a^2 A b + 7 A b^3 - 4 a^3 B - 10 a b^2 B)}{3 b^3 (a^2 + b^2)^2 d \sqrt{a+b \tan [c+d x]}} - \frac{2 (a A b - 4 a^2 B - 3 b^2 B) \sqrt{a+b \tan [c+d x]}}{3 b^3 (a^2 + b^2) d}$$

Result (type 3, 677 leaves):

$$\left( \operatorname{Sec}[c+d x]^2 (a \cos [c+d x] + b \sin [c+d x])^3 \left( \frac{2 (-2 a^3 A b - 9 a A b^3 + 8 a^4 B + 18 a^2 b^2 B + 3 b^4 B)}{3 (a-i b)^2 (a+i b)^2 b^3} - \frac{2 a^3 (-A b + a B)}{3 (a-i b)^2 (a+i b)^2 b (a \cos [c+d x] + b \sin [c+d x])^2} - \frac{2 (-a^3 A b \sin [c+d x] - 9 a A b^3 \sin [c+d x] + 4 a^4 B \sin [c+d x] + 12 a^2 b^2 B \sin [c+d x])}{3 (a-i b)^2 (a+i b)^2 b^2 (a \cos [c+d x] + b \sin [c+d x])} \right) (A+B \tan [c+d x]) \right) / \left( d (A \cos [c+d x] + B \sin [c+d x]) (a+b \tan [c+d x])^{5/2} - \operatorname{Sec}[c+d x]^{3/2} (a \cos [c+d x] + b \sin [c+d x])^{5/2} (A+B \tan [c+d x]) - \left( \left( \left( i (2 a A b - a^2 B + b^2 B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right)}{\sqrt{a+b \tan [c+d x]}} \right) / \left( \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a \cos [c+d x] + b \sin [c+d x]} \right) - \left( (a^2 A - A b^2 + 2 a b B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right)}{\sqrt{a+b \tan [c+d x]}} \right) / \left( \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a \cos [c+d x] + b \sin [c+d x]} \right) \right) \right) / \left( (a-i b)^2 (a+i b)^2 d (A \cos [c+d x] + B \sin [c+d x]) (a+b \tan [c+d x])^{5/2} \right)$$

### Problem 359: Result more than twice size of optimal antiderivative.

$$\int \frac{\tan [c+d x]^2 (A+B \tan [c+d x])}{(a+b \tan [c+d x])^{5/2}} dx$$

Optimal (type 3, 198 leaves, 9 steps):

$$\frac{(i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{(a-i b)^{5/2} d} - \frac{(i A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{(a+i b)^{5/2} d} - \frac{2 a^2 (A b-a B)}{3 b^2 (a^2+b^2) d (a+b \tan [c+d x])^{3/2}} + \frac{2 a (2 A b^3-a (a^2+3 b^2) B)}{b^2 (a^2+b^2)^2 d \sqrt{a+b \tan [c+d x]}}$$

Result (type 3, 660 leaves):

$$\left( \text{Sec}[c+dx]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^3 \right. \\ \left. - \frac{2(a^2 A b - 6 A b^3 + 2 a^3 B + 9 a b^2 B)}{3(a-ib)^2(a+ib)^2 b^2} + \frac{2 a^2(-A b + a B)}{3(a-ib)^2(a+ib)^2(a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2} + \right. \\ \left. (2(2 a^2 A b \text{Sin}[c+dx] - 6 A b^3 \text{Sin}[c+dx] + a^3 B \text{Sin}[c+dx] + 9 a b^2 B \text{Sin}[c+dx])) / \right. \\ \left. (3(a-ib)^2(a+ib)^2 b(a \text{Cos}[c+dx] + b \text{Sin}[c+dx])) \right) (A+B \text{Tan}[c+dx]) \Big/ \\ (d(A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a+b \text{Tan}[c+dx])^{5/2}) - \\ \left( \text{Sec}[c+dx]^{3/2} (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^{5/2} (A+B \text{Tan}[c+dx]) \right. \\ \left. - \left( \left( \left( i(a^2 A - A b^2 + 2 a b B) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} - \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{a+b \text{Tan}[c+dx]} \right) / \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) - \right. \\ \left. \left( (-2 a A b + a^2 B - b^2 B) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \right. \right. \\ \left. \left. \sqrt{a+b \text{Tan}[c+dx]} \right) / \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) \Big/ \\ \left. (a-ib)^2 (a+ib)^2 d(A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a+b \text{Tan}[c+dx])^{5/2} \right)$$

**Problem 360: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Tan}[c+dx] (A+B \text{Tan}[c+dx])}{(a+b \text{Tan}[c+dx])^{5/2}} dx$$

Optimal (type 3, 188 leaves, 9 steps):

$$- \frac{(A-ib) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{(a-ib)^{5/2} d} - \frac{(A+ib) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{(a+ib)^{5/2} d} + \\ \frac{2 a (A b - a B)}{3 b (a^2 + b^2) d (a+b \text{Tan}[c+dx])^{3/2}} + \frac{2 (a^2 A - A b^2 + 2 a b B)}{(a^2 + b^2)^2 d \sqrt{a+b \text{Tan}[c+dx]}}$$



Result (type 3, 662 leaves):

$$\begin{aligned}
 & \left( \sec [c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
 & \left. \left( -\frac{2(-4 a^2 A b+3 A b^3+a^3 B-6 a b^2 B)}{3 a(a-i b)^2(a+i b)^2 b}-\frac{2 a b(-A b+a B)}{3(a-i b)^2(a+i b)^2(a \cos [c+d x]+b \sin [c+d x])^2} \right. \right. \\
 & \left. \left. +\frac{2(-5 a^2 A b \sin [c+d x]+3 A b^3 \sin [c+d x]+2 a^3 B \sin [c+d x]-6 a b^2 B \sin [c+d x])}{3 a(a-i b)^2(a+i b)^2(a \cos [c+d x]+b \sin [c+d x])} \right) \right) (A+B \tan [c+d x]) \Big/ \\
 & \left( d(A \cos [c+d x]+B \sin [c+d x])(a+b \tan [c+d x])^{5 / 2} \right)+ \\
 & \left( \sec [c+d x]^{3 / 2}(a \cos [c+d x]+b \sin [c+d x])^{5 / 2}(A+B \tan [c+d x]) \right. \\
 & \left. \left( -\left( \left( i\left( 2 a A b-a^2 B+b^2 B \right) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}}-\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}}\right) \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{a+b \tan [c+d x]} \right) \Big/ \left( \sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right) \right) - \right. \\
 & \left. \left( \left( a^2 A-A b^2+2 a b B \right) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}}+\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}}\right) \right. \right. \\
 & \left. \left. \sqrt{a+b \tan [c+d x]} \right) \Big/ \left( \sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right) \right) \Big/ \\
 & \left. \left( (a-i b)^2(a+i b)^2 d(A \cos [c+d x]+B \sin [c+d x])(a+b \tan [c+d x])^{5 / 2} \right) \right)
 \end{aligned}$$

**Problem 361: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \tan [c+d x]}{(a+b \tan [c+d x])^{5 / 2}} d x$$

Optimal (type 3, 185 leaves, 9 steps):

$$-\frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{(a-i b)^{5/2} d} + \frac{(i A - B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{(a+i b)^{5/2} d} - \frac{2(A b - a B)}{3(a^2 + b^2) d (a+b \operatorname{Tan}[c+d x])^{3/2}} - \frac{2(2 a A b - a^2 B + b^2 B)}{(a^2 + b^2)^2 d \sqrt{a+b \operatorname{Tan}[c+d x]}}$$

Result(type 3, 640 leaves):

$$\left( \operatorname{Sec}[c+d x]^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^3 \left( \frac{2(-7 a A b + 4 a^2 B - 3 b^2 B)}{3 a (a-i b)^2 (a+i b)^2} + \frac{2 b^2 (-A b + a B)}{3 (a-i b)^2 (a+i b)^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^2} - (2(-8 a A b^2 \operatorname{Sin}[c+d x] + 5 a^2 b B \operatorname{Sin}[c+d x] - 3 b^3 B \operatorname{Sin}[c+d x])) / (3 a (a-i b)^2 (a+i b)^2 (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])) \right) (A+B \operatorname{Tan}[c+d x]) \right) / \left( d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^{5/2} \right) + \left( \operatorname{Sec}[c+d x]^{3/2} (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^{5/2} (A+B \operatorname{Tan}[c+d x]) \left( - \left( \left( i (a^2 A - A b^2 + 2 a b B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} - \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \sqrt{a+b \operatorname{Tan}[c+d x]} \right) / \left( \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]} \right) \right) - \left( (-2 a A b + a^2 B - b^2 B) \left( \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{\sqrt{a-i b}} + \frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+b \operatorname{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{\sqrt{a+i b}} \right) \sqrt{a+b \operatorname{Tan}[c+d x]} \right) / \left( \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]} \right) \right) \right) / \left( (a-i b)^2 (a+i b)^2 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^{5/2} \right)$$

**Problem 362:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x] (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 224 leaves, 13 steps):

$$\begin{aligned} & -\frac{2 A \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{a^{5/2} d} + \\ & \frac{(A - i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{(a - i b)^{5/2} d} + \frac{(A + i B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{(a + i b)^{5/2} d} + \\ & \frac{2 b (A b - a B)}{3 a (a^2 + b^2) d (a + b \text{Tan}[c + d x])^{3/2}} + \frac{2 b (3 a^2 A b + A b^3 - 2 a^3 B)}{a^2 (a^2 + b^2)^2 d \sqrt{a + b \text{Tan}[c + d x]}} \end{aligned}$$

Result (type 4, 33211 leaves): Display of huge result suppressed!

**Problem 363:** Humongous result has more than 200000 leaves.

$$\int \frac{\text{Cot}[c + d x]^2 (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 289 leaves, 14 steps):

$$\begin{aligned} & \frac{(5 A b - 2 a B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a}}\right]}{a^{7/2} d} + \frac{(i A + B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a-i b}}\right]}{(a - i b)^{5/2} d} - \\ & \frac{(i A - B) \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+d x]}}{\sqrt{a+i b}}\right]}{(a + i b)^{5/2} d} - \frac{b (3 a^2 A + 5 A b^2 - 2 a b B)}{3 a^2 (a^2 + b^2) d (a + b \text{Tan}[c + d x])^{3/2}} - \\ & \frac{A \text{Cot}[c + d x]}{a d (a + b \text{Tan}[c + d x])^{3/2}} - \frac{b (a^4 A + 10 a^2 A b^2 + 5 A b^4 - 6 a^3 b B - 2 a b^3 B)}{a^3 (a^2 + b^2)^2 d \sqrt{a + b \text{Tan}[c + d x]}} \end{aligned}$$

Result (type ?, 234 114 leaves): Display of huge result suppressed!

**Problem 364:** Humongous result has more than 200000 leaves.

$$\int \frac{\text{Cot}[c + d x]^3 (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 364 leaves, 15 steps):

$$\frac{(8 a^2 A - 35 A b^2 + 20 a b B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a}}\right]}{4 a^{9/2} d} -$$

$$\frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right]}{(a-i b)^{5/2} d} - \frac{(A + i B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right]}{(a+i b)^{5/2} d} +$$

$$\frac{b(27 a^2 A b + 35 A b^3 - 12 a^3 B - 20 a b^2 B)}{12 a^3 (a^2 + b^2) d (a+b \tan [c+d x])^{3/2}} + \frac{(7 A b - 4 a B) \operatorname{Cot}[c+d x]}{4 a^2 d (a+b \tan [c+d x])^{3/2}} -$$

$$\frac{A \operatorname{Cot}[c+d x]^2}{2 a d (a+b \tan [c+d x])^{3/2}} + \frac{b(11 a^4 A b + 62 a^2 A b^3 + 35 A b^5 - 4 a^5 B - 40 a^3 b^2 B - 20 a b^4 B)}{4 a^4 (a^2 + b^2)^2 d \sqrt{a+b \tan [c+d x]}}$$

Result (type ?, 251 836 leaves): Display of huge result suppressed!

### Problem 365: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{a B + b B \tan [c+d x]}{\sqrt{a+b \tan [c+d x]}} dx$$

Optimal (type 3, 362 leaves, 12 steps):

$$\frac{b B \operatorname{ArcTanh}\left[\frac{\sqrt{a+\sqrt{a^2+b^2}}-\sqrt{2} \sqrt{a+b \tan [c+d x]}}{\sqrt{a-\sqrt{a^2+b^2}}}\right]}{\sqrt{2} \sqrt{a-\sqrt{a^2+b^2}} d} - \frac{b B \operatorname{ArcTanh}\left[\frac{\sqrt{a+\sqrt{a^2+b^2}}+\sqrt{2} \sqrt{a+b \tan [c+d x]}}{\sqrt{a-\sqrt{a^2+b^2}}}\right]}{\sqrt{2} \sqrt{a-\sqrt{a^2+b^2}} d} +$$

$$\left( b B \operatorname{Log}\left[ a + \sqrt{a^2+b^2} + b \tan [c+d x] - \sqrt{2} \sqrt{a+\sqrt{a^2+b^2}} \sqrt{a+b \tan [c+d x]} \right] \right) /$$

$$\left( 2 \sqrt{2} \sqrt{a+\sqrt{a^2+b^2}} d \right) -$$

$$\left( b B \operatorname{Log}\left[ a + \sqrt{a^2+b^2} + b \tan [c+d x] + \sqrt{2} \sqrt{a+\sqrt{a^2+b^2}} \sqrt{a+b \tan [c+d x]} \right] \right) /$$

$$\left( 2 \sqrt{2} \sqrt{a+\sqrt{a^2+b^2}} d \right)$$

Result (type 3, 88 leaves):

$$-\frac{1}{d} i B \left( \sqrt{a-i b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}}\right] - \sqrt{a+i b} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}}\right] \right)$$

**Problem 366: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{a B + b B \tan [c + d x]}{(a + b \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 406 leaves, 12 steps):

$$\frac{b B \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} - \sqrt{2} \sqrt{a + b \tan [c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right] + b B \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} + \sqrt{2} \sqrt{a + b \tan [c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right]}{\sqrt{2} \sqrt{a^2 + b^2} \sqrt{a - \sqrt{a^2 + b^2}} d} - \frac{b B \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} - \sqrt{2} \sqrt{a + b \tan [c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right] + b B \operatorname{ArcTanh} \left[ \frac{\sqrt{a + \sqrt{a^2 + b^2}} + \sqrt{2} \sqrt{a + b \tan [c + d x]}}{\sqrt{a - \sqrt{a^2 + b^2}}} \right]}{\sqrt{2} \sqrt{a^2 + b^2} \sqrt{a - \sqrt{a^2 + b^2}} d} - \left( b B \operatorname{Log} \left[ a + \sqrt{a^2 + b^2} + b \tan [c + d x] - \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} \sqrt{a + b \tan [c + d x]} \right] \right) / \left( 2 \sqrt{2} \sqrt{a^2 + b^2} \sqrt{a + \sqrt{a^2 + b^2}} d \right) + \left( b B \operatorname{Log} \left[ a + \sqrt{a^2 + b^2} + b \tan [c + d x] + \sqrt{2} \sqrt{a + \sqrt{a^2 + b^2}} \sqrt{a + b \tan [c + d x]} \right] \right) / \left( 2 \sqrt{2} \sqrt{a^2 + b^2} \sqrt{a + \sqrt{a^2 + b^2}} d \right)$$

Result (type 3, 88 leaves):

$$\frac{i B \left( \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a - i b}} \right]}{\sqrt{a - i b}} - \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a + i b}} \right]}{\sqrt{a + i b}} \right)}{d}$$

**Problem 369: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cot [c + d x] (a B + b B \tan [c + d x])}{(a + b \tan [c + d x])^{5/2}} dx$$

Optimal (type 3, 154 leaves, 13 steps):

$$-\frac{2 B \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a}} \right]}{a^{3/2} d} + \frac{B \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a - i b}} \right]}{(a - i b)^{3/2} d} + \frac{B \operatorname{ArcTanh} \left[ \frac{\sqrt{a + b \tan [c + d x]}}{\sqrt{a + i b}} \right]}{(a + i b)^{3/2} d} + \frac{2 b^2 B}{a (a^2 + b^2) d \sqrt{a + b \tan [c + d x]}}$$

Result (type 4, 17418 leaves):

$$\begin{aligned}
 & B \left( \left( \text{Sec}[c + dx]^2 (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])^2 \left( \frac{2b^2}{a^2(a - ib)(a + ib)} - \right. \right. \right. \\
 & \left. \left. \left. \frac{2b^3 \text{Sin}[c + dx]}{a^2(a - ib)(a + ib)(a \text{Cos}[c + dx] + b \text{Sin}[c + dx])} \right) \right) / (d(a + b \text{Tan}[c + dx])^{3/2}) - \right. \\
 & \left. 4 \left( -b^2 \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \text{Tan}[\frac{1}{2}(c + dx)])}{(a + b + \sqrt{a^2 + b^2})(-1 + \text{Tan}[\frac{1}{2}(c + dx)])}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + \right. \right. \\
 & \left. (a^2 + b^2) \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \text{Tan}[\frac{1}{2}(c + dx)])}{(a + b + \sqrt{a^2 + b^2})(-1 + \text{Tan}[\frac{1}{2}(c + dx)])}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - a^2 \text{EllipticPi} \left[ \right. \right. \\
 & \left. \left. - \frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \text{Tan}[\frac{1}{2}(c + dx)])}{(a + b + \sqrt{a^2 + b^2})(-1 + \text{Tan}[\frac{1}{2}(c + dx)])}} \right], \right. \right. \\
 & \left. \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - iab \text{EllipticPi} \left[ -\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \text{Tan}[\frac{1}{2}(c + dx)])}{(a + b + \sqrt{a^2 + b^2})(-1 + \text{Tan}[\frac{1}{2}(c + dx)])}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - a^2 \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \text{Tan}[\frac{1}{2}(c + dx)])}{(a + b + \sqrt{a^2 + b^2})(-1 + \text{Tan}[\frac{1}{2}(c + dx)])}} \right], \right. \right. \\
 & \left. \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + iab \text{EllipticPi} \left[ \frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \text{Tan}[\frac{1}{2}(c + dx)])}{(a + b + \sqrt{a^2 + b^2})(-1 + \text{Tan}[\frac{1}{2}(c + dx)])}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + \right. \right. \\
 & \left. \left. a^2 \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \text{Tan}[\frac{1}{2}(c + dx)])}{(a + b + \sqrt{a^2 + b^2})(-1 + \text{Tan}[\frac{1}{2}(c + dx)])}} \right], \right. \right. \\
 & \left. \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + b^2 \text{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \Bigg) \\
 & \text{Sec}[c+dx]^{3/2} (a \cos[c+dx] + b \sin[c+dx])^{3/2} \\
 & \left( \frac{a \csc[c+dx] \sqrt{\sec[c+dx]}}{2(a-ib)(a+ib)\sqrt{a \cos[c+dx] + b \sin[c+dx]}} + \right. \\
 & \quad \frac{b^2 \csc[c+dx] \sqrt{\sec[c+dx]}}{a(a-ib)(a+ib)\sqrt{a \cos[c+dx] + b \sin[c+dx]}} + \\
 & \quad \frac{a \cos[2(c+dx)] \csc[c+dx] \sqrt{\sec[c+dx]}}{2(a-ib)(a+ib)\sqrt{a \cos[c+dx] + b \sin[c+dx]}} - \\
 & \quad \left. \frac{b \csc[c+dx] \sqrt{\sec[c+dx]} \sin[2(c+dx)]}{2(a-ib)(a+ib)\sqrt{a \cos[c+dx] + b \sin[c+dx]}} \right) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \\
 & \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \Bigg) / \\
 & \left( a(a-ib)(a+ib) d \sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right. \\
 & \quad \left. \left(-2b \tan\left[\frac{1}{2}(c+dx)\right] + a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)^2\right) \right) \\
 & \left( \left( 4 \left( -b^2 \text{EllipticF} \left[ \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2}) \left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}{(a+b+\sqrt{a^2+b^2}) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \right. \right. \\
 & \quad \left. \left. (a^2+b^2) \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - a^2 \text{EllipticPi} [ \\
 & -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - i a b \text{EllipticPi} \left[ -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \text{EllipticPi} [ \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + i a b \text{EllipticPi} \left[ \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + a^2 \text{EllipticPi} [ \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + b^2 \text{EllipticPi} \left[ \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2}(c+dx) \right] \right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)]}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \\
 & \left( -b \text{Sec} \left[ \frac{1}{2}(c+dx) \right] \right)^2 + a \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \tan \left[ \frac{1}{2}(c+dx) \right] \right)
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(c+dx)\right] - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \Big/ \\
 & \left( a(a-ib)(a+ib) \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right. \\
 & \quad \left. \left( -2b \tan\left[\frac{1}{2}(c+dx)\right] + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right)^2 \right) - \\
 & \left( 2 \left( -b^2 \operatorname{EllipticF}\left[ \operatorname{ArcSin}\left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \right. \right. \\
 & \quad (a^2+b^2) \operatorname{EllipticPi}\left[ \frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[ \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \operatorname{EllipticPi}\left[ \right. \\
 & \quad \left. -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right] \right], \\
 & \quad \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - iab \operatorname{EllipticPi}\left[ -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[ \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \operatorname{EllipticPi}\left[ \right. \\
 & \quad \left. \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[ \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right] \right], \\
 & \quad \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + iab \operatorname{EllipticPi}\left[ \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[ \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + a^2 \operatorname{EllipticPi}\left[ \right.
 \end{aligned}$$

$$\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right],$$

$$\frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + b^2 \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \operatorname{Sec}\left[\frac{1}{2}\right.$$

$$(c+dx)]^2 \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}$$

$$\sqrt{-\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}}$$

$$\sqrt{\frac{a+2b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \Bigg/$$

$$\left(a(a-ib)(a+ib) \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}\right.$$

$$\left.(-2b \tan\left[\frac{1}{2}(c+dx)\right]+a(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2)\right) \Bigg) -$$

$$\left(2 \left(-b^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] +\right.$$

$$(a^2+b^2) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - a^2 \operatorname{EllipticPi}\left[\right.$$

$$\left.-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}}\right]\right],$$

$$\begin{aligned}
 & \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \Big] - i a b \operatorname{EllipticPi} \left[ -\frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan[\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan[\frac{1}{2} (c + d x)])}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - a^2 \operatorname{EllipticPi} \left[ \right. \\
 & \left. \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan[\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan[\frac{1}{2} (c + d x)])}} \right] \right], \\
 & \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \Big] + i a b \operatorname{EllipticPi} \left[ \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan[\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan[\frac{1}{2} (c + d x)])}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + a^2 \operatorname{EllipticPi} \left[ \right. \\
 & \left. \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan[\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan[\frac{1}{2} (c + d x)])}} \right] \right], \\
 & \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \Big] + b^2 \operatorname{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan[\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan[\frac{1}{2} (c + d x)])}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] \Big) \operatorname{Sec} \left[ \right. \\
 & \left. \frac{1}{2} (c + d x) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{(-a - b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \\
 & \sqrt{-\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \\
 & \sqrt{\frac{a + 2 b \tan \left[ \frac{1}{2} (c + d x) \right] - a \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \Big/ \\
 & \left( a (a - i b) (a + i b) \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (c + d x) \right])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (c + d x) \right])}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -2 b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] + a \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) + \\
 & \left( 2 \left( -b^2 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right]}, \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + \right. \\
 & (a^2 + b^2) \operatorname{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right]}, \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - a^2 \operatorname{EllipticPi} \left[ \right. \\
 & \left. - \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right] \right], \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - i a b \operatorname{EllipticPi} \left[ - \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right]}, \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - a^2 \operatorname{EllipticPi} \left[ \right. \\
 & \left. \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right] \right], \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + i a b \operatorname{EllipticPi} \left[ \frac{i (a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right]}, \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + a^2 \operatorname{EllipticPi} \left[ \right. \\
 & \left. \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right] \right], \\
 & \left. \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + b^2 \operatorname{EllipticPi} \left[ \frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \right. \right. \\
 & \left. \left. \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) (1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}{(a + b + \sqrt{a^2 + b^2}) (-1 + \operatorname{Tan} [\frac{1}{2} (c + d x)])}} \right]}, \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] \left. \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{(-a - b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \sqrt{\frac{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 - \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a + 2b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} - \left( (-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
 & \left. \left. \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left( 2(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) \right) / \\
 & \left( a(a - ib)(a + ib) \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)} \right)^{3/2} \right. \\
 & \left. \left( -2b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + a \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) - \\
 & \left( 2 \left( -b^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] + \right. \\
 & (a^2 + b^2) \operatorname{EllipticPi}\left[\frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - a^2 \operatorname{EllipticPi}\left[\frac{ib(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] - ia b \operatorname{EllipticPi}\left[-\frac{ib(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right)}} \right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - a^2 \text{EllipticPi}[ \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + i a b \text{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + a^2 \text{EllipticPi}[ \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + b^2 \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & (-1+\tan[\frac{1}{2}(c+dx)]) \left(1+\tan[\frac{1}{2}(c+dx)]\right) \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)]}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}} \sqrt{\frac{1+\tan[\frac{1}{2}(c+dx)]^2}{1-\tan[\frac{1}{2}(c+dx)]^2}} \\
 & \sqrt{\frac{a+2b \tan[\frac{1}{2}(c+dx)]-a \tan[\frac{1}{2}(c+dx)]^2}{1+\tan[\frac{1}{2}(c+dx)]^2}} \\
 & \left(-\frac{a \text{Sec}[\frac{1}{2}(c+dx)]^2}{2(-a-b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])} - \frac{\text{Sec}[\frac{1}{2}(c+dx)]^2(b-\sqrt{a^2+b^2}-a \tan[\frac{1}{2}(c+dx)])}{2(-a-b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])^2}\right) \Bigg) \Bigg) \Bigg) \\
 & \left(a(a-ib)(a+ib) \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{(-a - b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}} \\
 & \left(-2b \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right] + a\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^2\right)\right) - \\
 & \left(2 \left(-b^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + \right. \\
 & (a^2 + b^2) \operatorname{EllipticPi}\left[\frac{a + b + \sqrt{a^2 + b^2}}{a - b - \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] - a^2 \operatorname{EllipticPi}\left[\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] - i a b \operatorname{EllipticPi}\left[-\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] - a^2 \operatorname{EllipticPi}\left[\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + i a b \operatorname{EllipticPi}\left[\frac{i(a + b + \sqrt{a^2 + b^2})}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + a^2 \operatorname{EllipticPi}\left[\frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] + b^2 \operatorname{EllipticPi}\left[\frac{a + b + \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a + b + \sqrt{a^2 + b^2})(1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right])}{(a + b + \sqrt{a^2 + b^2})\left(-1 + \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]\right)}}\right], \frac{a + \sqrt{a^2 + b^2}}{a - \sqrt{a^2 + b^2}}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right) \\
 & \left( -1+\tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1+\tan\left[\frac{1}{2}(c+dx)\right] \right) \\
 & \sqrt{\frac{b-\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left( \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])} + \right. \\
 & \left. \left. \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2(b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right])}{2(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])^2} \right) \right) \Bigg/ \\
 & \left( a(a-ib)(a+ib) \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right. \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \\
 & \left. \left( -2b \tan\left[\frac{1}{2}(c+dx)\right] + a(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2) \right) \right) - \\
 & \left( 2 \left( -b^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \right. \right. \\
 & (a^2+b^2) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \operatorname{EllipticPi}\left[ \right. \\
 & \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \operatorname{EllipticPi}\left[ \right.
 \end{aligned}$$



$$\begin{aligned}
 & -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] - i a b \text{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] - a^2 \text{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + i a b \text{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] + a^2 \text{EllipticPi}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + b^2 \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right]}, \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \sqrt{\frac{b-\sqrt{a^2+b^2}-a\tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a\tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \\
 & \sqrt{\frac{a+2b\tan\left[\frac{1}{2}(c+dx)\right]-a\tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}}
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} + \left( \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
 & \quad \left. \left. \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \left(1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right) / \\
 & \left( a(a-ib)(a+ib) \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}} \right. \\
 & \quad \left. \sqrt{\frac{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \left(-2b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] + a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right) - \\
 & \left( 2 \left( -b^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + \right. \\
 & \quad (a^2+b^2) \operatorname{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{a-b-\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \operatorname{EllipticPi}\left[\right. \\
 & \quad \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \operatorname{EllipticPi}\left[\right. \\
 & \quad \left. -\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - iab \operatorname{EllipticPi}\left[-\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\right. \right. \\
 & \quad \left. \left. \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] - a^2 \operatorname{EllipticPi}\left[\right. \\
 & \quad \left. \frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + iab \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\right. \right. \\
 & \quad \left. \left. \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}} \right] + iab \operatorname{EllipticPi}\left[\frac{i(a+b+\sqrt{a^2+b^2})}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + a^2 \text{EllipticPi}[ \\
 & \frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \\
 & \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}] + b^2 \text{EllipticPi}\left[\frac{a+b+\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin}\left[\sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan[\frac{1}{2}(c+dx)])}{(a+b+\sqrt{a^2+b^2})(-1+\tan[\frac{1}{2}(c+dx)])}}\right], \frac{a+\sqrt{a^2+b^2}}{a-\sqrt{a^2+b^2}}\right] \\
 & \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]\right)\left(1+\tan\left[\frac{1}{2}(c+dx)\right]\right) \\
 & \sqrt{\frac{b-\sqrt{a^2+b^2}-a\tan\left[\frac{1}{2}(c+dx)\right]}{(-a-b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \\
 & \sqrt{-\frac{b+\sqrt{a^2+b^2}-a\tan\left[\frac{1}{2}(c+dx)\right]}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left(\left(b \sec\left[\frac{1}{2}(c+dx)\right]^2 - a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) / \right. \\
 & \quad \left.\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \left(\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right. \\
 & \quad \left.\left.\left(a+2b \tan\left[\frac{1}{2}(c+dx)\right] - a \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right) / \right. \\
 & \left. \left(a(a-ib)(a+ib) \sqrt{\frac{(-a+b+\sqrt{a^2+b^2})(1+\tan\left[\frac{1}{2}(c+dx)\right])}{(a+b+\sqrt{a^2+b^2})(-1+\tan\left[\frac{1}{2}(c+dx)\right])}} \right. \right. \\
 & \quad \left. \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(c+dx)\right] - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \quad \left. \left(-2b \tan\left[\frac{1}{2}(c+dx)\right] + a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \right. \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{(-a - b + \sqrt{a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)}} \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)}} \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \sqrt{\frac{a + 2b \tan\left[\frac{1}{2}(c+dx)\right] - a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
 & \left. - \left( \left( b^2 \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)} - \right. \right. \right. \\
 & \left. \left. \left( (-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \Bigg) \Bigg) / \\
 & \left. \left( 2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)}} \right. \right. \\
 & \sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)}} \\
 & \left. \sqrt{\left( 1 - \left( (a + \sqrt{a^2 + b^2}) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \Bigg) \Bigg) / \\
 & \left. \left( \left( (a - \sqrt{a^2 + b^2}) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \right) \Bigg) \Bigg) + \\
 & \left( a^2 \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{2(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right] \right)} - \left( (-a + b + \sqrt{a^2 + b^2}) \right. \right. \right. \\
 & \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Bigg) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( 1 - \frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right. \\
 & \quad \sqrt{1 - \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \quad \left. \sqrt{\left( 1 - \left( \left( a + \sqrt{a^2 + b^2} \right) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) /} \right. \\
 & \quad \left. \left( \left( a - \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) + \\
 & \left( b^2 \left( \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)} - \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) / \\
 & \quad \left. \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( 1 - \frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right. \\
 & \quad \sqrt{1 - \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{\left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \quad \left. \sqrt{\left( 1 - \left( \left( a + \sqrt{a^2 + b^2} \right) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) /} \right. \\
 & \quad \left. \left( \left( a - \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) - \\
 & \left( a^2 \left( \frac{\left( -a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)} - \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( 1 - \frac{i \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right. \\
 & \quad \sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \quad \left. \sqrt{\left( 1 - \left( (a + \sqrt{a^2 + b^2}) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right)} / \right. \\
 & \quad \left. \left( \left( a - \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) + \\
 & \left( i a b \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)} - \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) / \right. \\
 & \quad \left. \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( 1 - \frac{i \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right. \\
 & \quad \sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \quad \left. \sqrt{\left( 1 - \left( (a + \sqrt{a^2 + b^2}) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right)} / \right. \\
 & \quad \left. \left( \left( a - \sqrt{a^2 + b^2} \right) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) - \\
 & \left( a^2 \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)} - \left( \left( -a + b + \sqrt{a^2 + b^2} \right) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) / \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( 1 + \frac{i \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right. \\
 & \quad \sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \quad \left. \sqrt{\left( 1 - \left( (a + \sqrt{a^2 + b^2}) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right)} / \right. \\
 & \quad \left. \left( (a - \sqrt{a^2 + b^2}) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) - \\
 & \left( i a b \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)} - \left( (-a + b + \sqrt{a^2 + b^2}) \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) / \\
 & \quad \left. \left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \Bigg) / \\
 & \left( 2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \left( 1 + \frac{i \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right. \\
 & \quad \sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \\
 & \quad \left. \sqrt{\left( 1 - \left( (a + \sqrt{a^2 + b^2}) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right)} / \right. \\
 & \quad \left. \left( (a - \sqrt{a^2 + b^2}) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) + \\
 & \left( (a^2 + b^2) \left( \frac{(-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)} - \right. \right. \\
 & \quad \left. \left. \left( (-a + b + \sqrt{a^2 + b^2}) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \right) /
 \end{aligned}$$

$$\left( 2 \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \Bigg) /$$

$$\left( 2 \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \right.$$

$$\left( 1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a - b - \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)} \right)$$

$$\sqrt{1 - \frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \right.$$

$$\left. \sqrt{\left( 1 - \left( (a + \sqrt{a^2 + b^2}) \left( -a + b + \sqrt{a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) / \right.$$

$$\left. \left( (a - \sqrt{a^2 + b^2}) \left( a + b + \sqrt{a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \Bigg) \Bigg) /$$

$$\left( a (a - i b) (a + i b) \sqrt{\frac{(-a + b + \sqrt{a^2 + b^2}) \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}{(a + b + \sqrt{a^2 + b^2}) \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)}} \right.$$

$$\left. \left( -2 b \tan \left[ \frac{1}{2} (c + d x) \right] + a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \Bigg) (a + b \tan [c + d x])^{3/2} \Bigg)$$

**Problem 372: Result more than twice size of optimal antiderivative.**

$$\int \frac{-a + b \tan [c + d x]}{(a + b \tan [c + d x])^{5/2}} dx$$

Optimal (type 3, 174 leaves, 9 steps):

$$\frac{(i a - b) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a-i b}} \right]}{(a - i b)^{5/2} d} - \frac{(i a + b) \operatorname{ArcTanh} \left[ \frac{\sqrt{a+b \tan [c+d x]}}{\sqrt{a+i b}} \right]}{(a + i b)^{5/2} d} +$$

$$\frac{4 a b}{3 (a^2 + b^2) d (a + b \tan [c + d x])^{3/2}} + \frac{2 b (3 a^2 - b^2)}{(a^2 + b^2)^2 d \sqrt{a + b \tan [c + d x]}}$$

Result (type 3, 606 leaves):



$$\begin{aligned}
 & \left( \text{Sec}[c+dx]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^3 \right. \\
 & \left( -\frac{2b(11a^2 - 3b^2)}{3a(a-ib)^2(a+ib)^2} - \frac{4ab^3}{3(a-ib)^2(a+ib)^2(a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2} + \right. \\
 & \left. \frac{2(13a^2b^2 \text{Sin}[c+dx] - 3b^4 \text{Sin}[c+dx])}{3a(a-ib)^2(a+ib)^2(a \text{Cos}[c+dx] + b \text{Sin}[c+dx])} \right) (-a + b \text{Tan}[c+dx]) \Big/ \\
 & \left( d(a \text{Cos}[c+dx] - b \text{Sin}[c+dx]) (a + b \text{Tan}[c+dx])^{5/2} + \right. \\
 & \left. \text{Sec}[c+dx]^{3/2} (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^{5/2} (-a + b \text{Tan}[c+dx]) \right. \\
 & \left. \left( -\left( \left( i(a^3 - 3ab^2) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} - \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \text{Tan}[c+dx]} \right) \right) \right. \right. \\
 & \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) - \right. \\
 & \left. \left( (-3a^2b + b^3) \left( \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib}} + \frac{\text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a+ib}}\right]}{\sqrt{a+ib}} \right) \sqrt{a+b \text{Tan}[c+dx]} \right) \right. \right. \\
 & \left. \left. \left( \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right) \right) \right) \Big/ \\
 & \left. \left( (a-ib)^2 (a+ib)^2 d (a \text{Cos}[c+dx] - b \text{Sin}[c+dx]) (a + b \text{Tan}[c+dx])^{5/2} \right) \right)
 \end{aligned}$$

**Problem 373: Result more than twice size of optimal antiderivative.**

$$\int \frac{1 + i \text{Tan}[c+dx]}{\sqrt{a+b \text{Tan}[c+dx]}} dx$$

Optimal (type 3, 45 leaves, 3 steps):

$$\frac{2i \text{ArcTanh}\left[\frac{\sqrt{a+b \text{Tan}[c+dx]}}{\sqrt{a-ib}}\right]}{\sqrt{a-ib} d}$$

Result (type 3, 128 leaves):

$$-\frac{1}{\sqrt{a-ib}d}i \operatorname{Log}\left[\frac{1}{\sqrt{a-ib}}\right. \\ \left.2\left(-ib e^{2i(c+dx)} + a(1+e^{2i(c+dx)}) + \sqrt{a-ib}(1+e^{2i(c+dx)})\sqrt{a-\frac{ib(-1+e^{2i(c+dx)})}{1+e^{2i(c+dx)}}}\right)\right]$$

**Problem 375:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{3 + \tan[x]}{\sqrt{4 + 3 \tan[x]}} dx$$

Optimal (type 3, 30 leaves, 2 steps):

$$-\sqrt{2} \operatorname{ArcTan}\left[\frac{1 - 3 \tan[x]}{\sqrt{2} \sqrt{4 + 3 \tan[x]}}\right]$$

Result (type 3, 69 leaves):

$$\left(\frac{1}{5} - \frac{3i}{5}\right) \sqrt{4-3i} \operatorname{ArcTanh}\left[\frac{\sqrt{4+3 \tan[x]}}{\sqrt{4-3i}}\right] + \left(\frac{1}{5} + \frac{3i}{5}\right) \sqrt{4+3i} \operatorname{ArcTanh}\left[\frac{\sqrt{4+3 \tan[x]}}{\sqrt{4+3i}}\right]$$

**Problem 376:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{1 - 3 \tan[x]}{\sqrt{4 + 3 \tan[x]}} dx$$

Optimal (type 3, 27 leaves, 2 steps):

$$\sqrt{2} \operatorname{ArcTanh}\left[\frac{3 + \tan[x]}{\sqrt{2} \sqrt{4 + 3 \tan[x]}}\right]$$

Result (type 3, 65 leaves):

$$\frac{1}{5} \left( (3+i) \sqrt{4-3i} \operatorname{ArcTanh}\left[\frac{\sqrt{4+3 \tan[x]}}{\sqrt{4-3i}}\right] + (3-i) \sqrt{4+3i} \operatorname{ArcTanh}\left[\frac{\sqrt{4+3 \tan[x]}}{\sqrt{4+3i}}\right] \right)$$

**Problem 377:** Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{4 - 3 \tan[a + bx]}{\sqrt{4 + 3 \tan[a + bx]}} dx$$

Optimal (type 3, 85 leaves, 5 steps):

$$-\frac{9 \operatorname{ArcTan}\left[\frac{1-3 \tan[a+bx]}{\sqrt{2} \sqrt{4+3 \tan[a+bx]}}\right]}{5 \sqrt{2} b} + \frac{13 \operatorname{ArcTanh}\left[\frac{3+\tan[a+bx]}{\sqrt{2} \sqrt{4+3 \tan[a+bx]}}\right]}{5 \sqrt{2} b}$$

Result (type 3, 76 leaves):

$$\frac{1}{25 b} \left( (24 - 7 i) \sqrt{4 - 3 i} \operatorname{ArcTanh} \left[ \frac{\sqrt{4 + 3 \operatorname{Tan}[a + b x]}}{\sqrt{4 - 3 i}} \right] + (24 + 7 i) \sqrt{4 + 3 i} \operatorname{ArcTanh} \left[ \frac{\sqrt{4 + 3 \operatorname{Tan}[a + b x]}}{\sqrt{4 + 3 i}} \right] \right)$$

**Problem 398: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Tan}[c + d x]^{5/2} (A + B \operatorname{Tan}[c + d x])}{a + b \operatorname{Tan}[c + d x]} dx$$

Optimal (type 3, 325 leaves, 16 steps):

$$\begin{aligned} & \frac{(a(A - B) + b(A + B)) \operatorname{ArcTan} \left[ 1 - \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]} \right]}{\sqrt{2} (a^2 + b^2) d} - \\ & \frac{(a(A - B) + b(A + B)) \operatorname{ArcTan} \left[ 1 + \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]} \right]}{\sqrt{2} (a^2 + b^2) d} - \frac{2 a^{5/2} (A b - a B) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a}} \right]}{b^{5/2} (a^2 + b^2) d} + \\ & \frac{(b(A - B) - a(A + B)) \operatorname{Log} \left[ 1 - \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]} + \operatorname{Tan}[c + d x] \right]}{2 \sqrt{2} (a^2 + b^2) d} - \\ & \frac{(b(A - B) - a(A + B)) \operatorname{Log} \left[ 1 + \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]} + \operatorname{Tan}[c + d x] \right]}{2 \sqrt{2} (a^2 + b^2) d} + \\ & \frac{2 (A b - a B) \sqrt{\operatorname{Tan}[c + d x]}}{b^2 d} + \frac{2 B \operatorname{Tan}[c + d x]^{3/2}}{3 b d} \end{aligned}$$

Result (type 3, 744 leaves):

$$\left( (a \cos [c + d x] + b \sin [c + d x]) \sqrt{\tan [c + d x]} (A + B \tan [c + d x]) \left( \frac{2 (A b - a B)}{b^2} + \frac{2 B \tan [c + d x]}{3 b} \right) \right) / (d (A \cos [c + d x] + B \sin [c + d x]) (a + b \tan [c + d x])) -$$

$$\frac{1}{2 b^2 d (A \cos [c + d x] + B \sin [c + d x]) (a + b \tan [c + d x]) (a \cos [c + d x] + b \sin [c + d x]) (A + B \tan [c + d x])}$$

$$\left( 2 (2 a A b - 2 a^2 B + b^2 B) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a}} \right] \operatorname{Csc} [c + d x] \operatorname{Sec} [c + d x]^3 \right.$$

$$\left. (a + b \tan [c + d x]) \right) / (\sqrt{a} \sqrt{b} (b + a \cot [c + d x]) (1 + \tan [c + d x]^2)^2) +$$

$$\frac{1}{4 (a^2 + b^2) (b + a \cot [c + d x]) (1 + \tan [c + d x]^2)}$$

$$A b^2 \operatorname{Csc} [c + d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a}} \right] + \sqrt{2} \right.$$

$$\left( -2 (a + b) \operatorname{ArcTan} [1 - \sqrt{2} \sqrt{\tan [c + d x]}] + 2 (a + b) \operatorname{ArcTan} [1 + \sqrt{2} \sqrt{\tan [c + d x]}] + \right.$$

$$\left. (a - b) (\operatorname{Log} [1 - \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]] - \operatorname{Log} [1 + \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]]) \right) \operatorname{Sec} [c + d x]^2 \sin [2 (c + d x)] (a + b \tan [c + d x]) +$$

$$(1 / (2 (a^2 + b^2) (b + a \cot [c + d x]) (1 - \tan [c + d x]^2) (1 + \tan [c + d x]^2)))$$

$$b^2 B \cos [2 (c + d x)] \operatorname{Csc} [c + d x] \left( \frac{4 (a^2 - b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a}} \right]}{\sqrt{a} \sqrt{b}} + \right.$$

$$\sqrt{2} (2 (a - b) \operatorname{ArcTan} [1 - \sqrt{2} \sqrt{\tan [c + d x]}] - 2 (a - b) \operatorname{ArcTan} [1 + \sqrt{2} \sqrt{\tan [c + d x]}] +$$

$$(a + b) (\operatorname{Log} [1 - \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]] - \operatorname{Log} [1 + \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]]) \left. \right) \operatorname{Sec} [c + d x]^3 (a + b \tan [c + d x])$$

**Problem 403: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \tan [c + d x]}{\tan [c + d x]^{5/2} (a + b \tan [c + d x])} dx$$

Optimal (type 3, 325 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{(b(A-B) - a(A+B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]}\right]}{\sqrt{2} (a^2 + b^2) d} + \\
 & \frac{(b(A-B) - a(A+B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]}\right]}{\sqrt{2} (a^2 + b^2) d} + \frac{2 b^{5/2} (Ab - aB) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a}}\right]}{a^{5/2} (a^2 + b^2) d} + \\
 & \frac{(a(A-B) + b(A+B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]\right]}{2 \sqrt{2} (a^2 + b^2) d} - \\
 & \frac{(a(A-B) + b(A+B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]\right]}{2 \sqrt{2} (a^2 + b^2) d} - \\
 & \frac{2A}{3 a d \tan[c+dx]^{3/2}} + \frac{2(Ab - aB)}{a^2 d \sqrt{\tan[c+dx]}}
 \end{aligned}$$

Result (type 3, 773 leaves):

$$\begin{aligned}
& \left( \left( \frac{2A}{3a} - \frac{2(-Ab \cos[c+dx] + aB \cos[c+dx]) \csc[c+dx]}{a^2} - \frac{2A \csc[c+dx]^2}{3a} \right) \right. \\
& \quad \left. (a \cos[c+dx] + b \sin[c+dx]) \sqrt{\tan[c+dx]} (A + B \tan[c+dx]) \right) / \\
& \quad \frac{(d(A \cos[c+dx] + B \sin[c+dx]) (a + b \tan[c+dx])) + 1}{2a^2 d (A \cos[c+dx] + B \sin[c+dx]) (a + b \tan[c+dx])} \\
& \quad (a \cos[c+dx] + b \sin[c+dx]) (A + B \tan[c+dx]) \\
& \quad \left( \left( 2(-a^2 A + 2Ab^2 - 2abB) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a}} \right] \csc[c+dx] \sec[c+dx]^3 \right. \right. \\
& \quad \left. \left. (a + b \tan[c+dx]) \right) / \left( \sqrt{a} \sqrt{b} (b + a \cot[c+dx]) (1 + \tan[c+dx]^2)^2 \right) - \right. \\
& \quad \left. \frac{1}{4(a^2 + b^2) (b + a \cot[c+dx]) (1 + \tan[c+dx]^2)} \right. \\
& \quad \left. a^2 B \csc[c+dx]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a}} \right] + \sqrt{2} \right. \right. \\
& \quad \left. \left. (-2(a+b) \operatorname{ArcTan} [1 - \sqrt{2} \sqrt{\tan[c+dx]}] + 2(a+b) \operatorname{ArcTan} [1 + \sqrt{2} \sqrt{\tan[c+dx]}] + \right. \right. \\
& \quad \left. \left. (a-b) (\log [1 - \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]] - \log [1 + \sqrt{2} \sqrt{\tan[c+dx]} + \right. \right. \\
& \quad \left. \left. \tan[c+dx]) \right) \right) \sec[c+dx]^2 \sin[2(c+dx)] (a + b \tan[c+dx]) + \\
& \quad \left. (1 / (2(a^2 + b^2) (b + a \cot[c+dx]) (1 - \tan[c+dx]^2) (1 + \tan[c+dx]^2))) \right. \\
& \quad \left. a^2 A \cos[2(c+dx)] \csc[c+dx] \left( \frac{4(a^2 - b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a}} \right]}{\sqrt{a} \sqrt{b}} + \right. \right. \\
& \quad \left. \left. \sqrt{2} (2(a-b) \operatorname{ArcTan} [1 - \sqrt{2} \sqrt{\tan[c+dx]}] - 2(a-b) \operatorname{ArcTan} [1 + \sqrt{2} \sqrt{\tan[c+dx]}] + \right. \right. \\
& \quad \left. \left. (a+b) (\log [1 - \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]] - \log [ \right. \right. \\
& \quad \left. \left. 1 + \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx] \right) \right) \right) \sec[c+dx]^3 (a + b \tan[c+dx]) \left. \right)
\end{aligned}$$

**Problem 404: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\tan[c+dx]^{5/2} (A + B \tan[c+dx])}{(a + b \tan[c+dx])^2} dx$$

Optimal (type 3, 436 leaves, 16 steps):

$$\begin{aligned}
 & \frac{(a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]}\right]}{\sqrt{2} (a^2 + b^2)^2 d} - \\
 & \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]}\right] + \\
 & \frac{a^{3/2} (a^2 A b + 5 A b^3 - 3 a^3 B - 7 a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a}}\right]}{b^{5/2} (a^2 + b^2)^2 d} + \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} \\
 & (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] - \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] - \\
 & \frac{(a A b - 3 a^2 B - 2 b^2 B) \sqrt{\tan[c + d x]}}{b^2 (a^2 + b^2) d} + \frac{a (A b - a B) \tan[c + d x]^{3/2}}{b (a^2 + b^2) d (a + b \tan[c + d x])}
 \end{aligned}$$

Result (type 3, 882 leaves):

$$\begin{aligned}
 & \left( \text{Sec}[c + d x] (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2 \right. \\
 & \quad \left( \frac{-a A b + 3 a^2 B + 2 b^2 B}{(a - i b) (a + i b) b^2} + \frac{a A b \text{Sin}[c + d x] - a^2 B \text{Sin}[c + d x]}{(a - i b) (a + i b) b (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])} \right) \sqrt{\text{Tan}[c + d x]} \\
 & \quad \left. (A + B \text{Tan}[c + d x]) \right) / \left( d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \text{Tan}[c + d x])^2 \right) - \\
 & \left( \text{Sec}[c + d x] (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2 (A + B \text{Tan}[c + d x]) \right. \\
 & \quad \left( \left( 2 (-a^2 A b - A b^3 + 3 a^3 B + 3 a b^2 B) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a}}\right] \text{Csc}[c + d x] \text{Sec}[c + d x]^3 \right. \right. \\
 & \quad \left. \left. (a + b \text{Tan}[c + d x]) \right) / \left( \sqrt{a} \sqrt{b} (b + a \text{Cot}[c + d x]) (1 + \text{Tan}[c + d x]^2)^2 \right) + \right. \\
 & \quad \frac{1}{4 (a^2 + b^2) (b + a \text{Cot}[c + d x]) (1 + \text{Tan}[c + d x]^2)} (a A b^2 + b^3 B) \text{Csc}[c + d x]^2 \\
 & \quad \left( -8 \sqrt{a} \sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a}}\right] + \sqrt{2} \right. \\
 & \quad \left( -2 (a + b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]}] + 2 (a + b) \text{ArcTan}[1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]}] \right) + \\
 & \quad \left. (a - b) \left( \text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \text{Tan}[c + d x]] - \text{Log}[1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \right. \right. \\
 & \quad \left. \left. \text{Tan}[c + d x]] \right) \right) \text{Sec}[c + d x]^2 \text{Sin}[2 (c + d x)] (a + b \text{Tan}[c + d x]) - \\
 & \quad \left( 1 / (2 (a^2 + b^2) (b + a \text{Cot}[c + d x]) (1 - \text{Tan}[c + d x]^2) (1 + \text{Tan}[c + d x]^2)) \right) \\
 & \quad (A b^3 - a b^2 B) \text{Cos}[2 (c + d x)] \text{Csc}[c + d x] \left( \frac{4 (a^2 - b^2) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right. \\
 & \quad \left. \left( 2 (a - b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]}] - 2 (a - b) \text{ArcTan}[1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]}] \right) + \right. \\
 & \quad \left. (a + b) \left( \text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \text{Tan}[c + d x]] - \text{Log}[1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \right. \right. \\
 & \quad \left. \left. \text{Tan}[c + d x]] \right) \right) \text{Sec}[c + d x]^3 (a + b \text{Tan}[c + d x]) \right) / \\
 & \left( 2 (a - i b) (a + i b) b^2 d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \text{Tan}[c + d x])^2 \right)
 \end{aligned}$$



Problem 405: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\tan [c+d x]^{3 / 2}(A+B \tan [c+d x])}{(a+b \tan [c+d x])^2} d x$$

Optimal (type 3, 391 leaves, 15 steps):

$$\begin{aligned} & -\frac{1}{\sqrt{2}\left(a^2+b^2\right)^2 d}\left(2 a b(A-B)-a^2(A+B)+b^2(A+B)\right) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\tan [c+d x]}\right]+ \\ & \frac{1}{\sqrt{2}\left(a^2+b^2\right)^2 d}\left(2 a b(A-B)-a^2(A+B)+b^2(A+B)\right) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\tan [c+d x]}\right]+ \\ & \frac{\sqrt{a}\left(a^2 A b-3 A b^3+a^3 B+5 a b^2 B\right) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}}\right]}{b^{3 / 2}\left(a^2+b^2\right)^2 d}+\frac{1}{2 \sqrt{2}\left(a^2+b^2\right)^2 d} \\ & \left(a^2(A-B)-b^2(A-B)+2 a b(A+B)\right) \operatorname{Log}\left[1-\sqrt{2} \sqrt{\tan [c+d x]}+\tan [c+d x]\right]- \\ & \frac{1}{2 \sqrt{2}\left(a^2+b^2\right)^2 d}\left(a^2(A-B)-b^2(A-B)+2 a b(A+B)\right) \operatorname{Log}\left[1+\sqrt{2} \sqrt{\tan [c+d x]}+\tan [c+d x]\right]+ \\ & \frac{a(A b-a B) \sqrt{\tan [c+d x]}}{b\left(a^2+b^2\right) d(a+b \tan [c+d x])} \end{aligned}$$

Result (type 3, 849 leaves):

$$\begin{aligned}
 & \left( \text{Sec}[c + d x] (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2 \right. \\
 & \left. \left( -\frac{-A b + a B}{(a - i b) (a + i b) b} + \frac{-A b \text{Sin}[c + d x] + a B \text{Sin}[c + d x]}{(a - i b) (a + i b) (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])} \right) \sqrt{\text{Tan}[c + d x]} \right. \\
 & \left. (A + B \text{Tan}[c + d x]) \right) / \left( d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \text{Tan}[c + d x])^2 \right) - \\
 & \left( \text{Sec}[c + d x] (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2 (A + B \text{Tan}[c + d x]) \right. \\
 & \left. \left( \left( 2 (-a^2 B - b^2 B) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a}}\right] \text{Csc}[c + d x] \text{Sec}[c + d x]^3 (a + b \text{Tan}[c + d x]) \right) \right) / \right. \\
 & \left. \left( \sqrt{a} \sqrt{b} (b + a \text{Cot}[c + d x]) (1 + \text{Tan}[c + d x])^2 \right) + \right. \\
 & \left. \frac{1}{4 (a^2 + b^2) (b + a \text{Cot}[c + d x]) (1 + \text{Tan}[c + d x])^2} \right. \\
 & \left. (-A b^2 + a b B) \text{Csc}[c + d x]^2 \left( -8 \sqrt{a} \sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a}}\right] + \sqrt{2} \right. \right. \\
 & \left. \left( -2 (a + b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]}] + 2 (a + b) \text{ArcTan}[1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]}] \right) + \right. \\
 & \left. (a - b) \left( \text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \text{Tan}[c + d x]] - \text{Log}[1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \right. \right. \\
 & \left. \left. \text{Tan}[c + d x] \right) \right) \left. \right) \text{Sec}[c + d x]^2 \text{Sin}[2 (c + d x)] (a + b \text{Tan}[c + d x]) - \\
 & \left( 1 / (2 (a^2 + b^2) (b + a \text{Cot}[c + d x]) (1 - \text{Tan}[c + d x])^2 (1 + \text{Tan}[c + d x])^2) \right) \\
 & (a A b + b^2 B) \text{Cos}[2 (c + d x)] \text{Csc}[c + d x] \left( \frac{4 (a^2 - b^2) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right. \\
 & \left. \left( 2 (a - b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]}] - 2 (a - b) \text{ArcTan}[1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]}] \right) + \right. \\
 & \left. (a + b) \left( \text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \text{Tan}[c + d x]] - \text{Log}[ \right. \right. \\
 & \left. \left. 1 + \sqrt{2} \sqrt{\text{Tan}[c + d x]} + \text{Tan}[c + d x] \right) \right) \left. \right) \text{Sec}[c + d x]^3 (a + b \text{Tan}[c + d x]) \left. \right) / \\
 & \left( 2 (a - i b) (a + i b) b d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \text{Tan}[c + d x])^2 \right)
 \end{aligned}$$

**Problem 406: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sqrt{\text{Tan}[c + d x]} (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^2} dx$$

Optimal (type 3, 391 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]}\right] + \\
 & \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]}\right] - \\
 & \frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b} (a^2 + b^2)^2 d} - \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} \\
 & (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] + \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] - \\
 & \frac{(A b - a B) \sqrt{\tan[c + d x]}}{(a^2 + b^2) d (a + b \tan[c + d x])}
 \end{aligned}$$

Result (type 3, 750 leaves):

$$\left( \text{Sec}[c+dx] (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2 \right. \\ \left. \left( \frac{-Ab + aB}{a(a-ib)(a+ib)} + \frac{Ab^2 \text{Sin}[c+dx] - aBb \text{Sin}[c+dx]}{a(a-ib)(a+ib)(a \text{Cos}[c+dx] + b \text{Sin}[c+dx])} \right) \sqrt{\text{Tan}[c+dx]} \right. \\ \left. (A+B \text{Tan}[c+dx]) \right) / \left( d (A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a+b \text{Tan}[c+dx])^2 \right) + \\ \left( \text{Sec}[c+dx] (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2 (A+B \text{Tan}[c+dx]) \right. \\ \left. \left( \frac{1}{4(a^2+b^2)(b+a \text{Cot}[c+dx])(1+\text{Tan}[c+dx]^2)} \right. \right. \\ \left. \left. (aA+bB) \text{Csc}[c+dx]^2 \left( -8\sqrt{a}\sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b}\sqrt{\text{Tan}[c+dx]}}{\sqrt{a}}\right] + \sqrt{2} \right. \right. \right. \\ \left. \left. \left( -2(a+b) \text{ArcTan}[1-\sqrt{2}\sqrt{\text{Tan}[c+dx]}] + 2(a+b) \text{ArcTan}[1+\sqrt{2}\sqrt{\text{Tan}[c+dx]}] \right) + \right. \right. \\ \left. \left. (a-b) \left( \text{Log}[1-\sqrt{2}\sqrt{\text{Tan}[c+dx]} + \text{Tan}[c+dx]] - \text{Log}[1+\sqrt{2}\sqrt{\text{Tan}[c+dx]} + \right. \right. \right. \\ \left. \left. \left. \text{Tan}[c+dx] \right) \right) \right) \right) \text{Sec}[c+dx]^2 \text{Sin}[2(c+dx)] (a+b \text{Tan}[c+dx]) - \\ \left. \left( 1 / (2(a^2+b^2)(b+a \text{Cot}[c+dx])(1-\text{Tan}[c+dx]^2)(1+\text{Tan}[c+dx]^2)) \right) \right) \\ (Ab-aB) \text{Cos}[2(c+dx)] \text{Csc}[c+dx] \left( \frac{4(a^2-b^2) \text{ArcTan}\left[\frac{\sqrt{b}\sqrt{\text{Tan}[c+dx]}}{\sqrt{a}}\right]}{\sqrt{a}\sqrt{b}} + \sqrt{2} \right. \\ \left. \left( 2(a-b) \text{ArcTan}[1-\sqrt{2}\sqrt{\text{Tan}[c+dx]}] - 2(a-b) \text{ArcTan}[1+\sqrt{2}\sqrt{\text{Tan}[c+dx]}] \right) + \right. \\ \left. \left. (a+b) \left( \text{Log}[1-\sqrt{2}\sqrt{\text{Tan}[c+dx]} + \text{Tan}[c+dx]] - \text{Log}[ \right. \right. \right. \\ \left. \left. \left. 1+\sqrt{2}\sqrt{\text{Tan}[c+dx]} + \text{Tan}[c+dx] \right) \right) \right) \right) \text{Sec}[c+dx]^3 (a+b \text{Tan}[c+dx]) \left. \right) / \\ \left( 2(a-ib)(a+ib)d(A \text{Cos}[c+dx] + B \text{Sin}[c+dx])(a+b \text{Tan}[c+dx])^2 \right)$$

**Problem 407: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \text{Tan}[c+dx]}{\sqrt{\text{Tan}[c+dx]} (a+b \text{Tan}[c+dx])^2} dx$$

Optimal (type 3, 391 leaves, 15 steps):

$$\begin{aligned}
 & \frac{(2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]}\right]}{\sqrt{2} (a^2 + b^2)^2 d} - \\
 & \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]}\right] + \\
 & \frac{\sqrt{b} (5 a^2 A b + A b^3 - 3 a^3 B + a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a}}\right]}{a^{3/2} (a^2 + b^2)^2 d} - \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} \\
 & (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] + \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] + \\
 & \frac{b (A b - a B) \sqrt{\tan [c + d x]}}{a (a^2 + b^2) d (a + b \tan [c + d x])}
 \end{aligned}$$

Result (type 3, 856 leaves):

$$\begin{aligned}
 & \left( \text{Sec}[c + dx] (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])^2 \right. \\
 & \left. \left( -\frac{b(-Ab + aB)}{a^2(a - ib)(a + ib)} + \frac{-Ab^3 \text{Sin}[c + dx] + a^2 B \text{Sin}[c + dx]}{a^2(a - ib)(a + ib)(a \text{Cos}[c + dx] + b \text{Sin}[c + dx])} \right) \sqrt{\text{Tan}[c + dx]} \right. \\
 & \left. (A + B \text{Tan}[c + dx]) \right) / \left( d (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) (a + b \text{Tan}[c + dx])^2 \right) + \\
 & \left( \text{Sec}[c + dx] (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])^2 (A + B \text{Tan}[c + dx]) \right. \\
 & \left. \left( \left( 2 (a^2 A + Ab^2) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right] \text{Csc}[c + dx] \text{Sec}[c + dx]^3 (a + b \text{Tan}[c + dx]) \right) / \right. \right. \\
 & \left. \left. \frac{(\sqrt{a} \sqrt{b} (b + a \text{Cot}[c + dx]) (1 + \text{Tan}[c + dx]^2)^2)}{1} + \right. \right. \\
 & \left. \left. 4 (a^2 + b^2) (b + a \text{Cot}[c + dx]) (1 + \text{Tan}[c + dx]^2) \right. \right. \\
 & \left. \left. (-aAb + a^2 B) \text{Csc}[c + dx]^2 \left( -8 \sqrt{a} \sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right] + \sqrt{2} \right. \right. \right. \\
 & \left. \left. \left( -2 (a + b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]}] + 2 (a + b) \text{ArcTan}[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]}] \right) + \right. \right. \\
 & \left. \left. (a - b) \left( \text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx]] - \text{Log}[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \right. \right. \right. \\
 & \left. \left. \left. \text{Tan}[c + dx] \right) \right) \right) \text{Sec}[c + dx]^2 \text{Sin}[2(c + dx)] (a + b \text{Tan}[c + dx]) - \\
 & \left. \left( 1 / (2 (a^2 + b^2) (b + a \text{Cot}[c + dx]) (1 - \text{Tan}[c + dx]^2) (1 + \text{Tan}[c + dx]^2)) \right) \right. \\
 & \left. (a^2 A + a b B) \text{Cos}[2(c + dx)] \text{Csc}[c + dx] \left( \frac{4 (a^2 - b^2) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right. \right. \\
 & \left. \left. (2 (a - b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]}] - 2 (a - b) \text{ArcTan}[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]}] + \right. \right. \\
 & \left. \left. (a + b) \left( \text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx]] - \text{Log}[ \right. \right. \right. \\
 & \left. \left. \left. 1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx] \right) \right) \right) \text{Sec}[c + dx]^3 (a + b \text{Tan}[c + dx]) \right) / \\
 & \left( 2 a (a - ib) (a + ib) d (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) (a + b \text{Tan}[c + dx])^2 \right)
 \end{aligned}$$

Problem 408: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{A + B \tan [c + d x]}{\tan [c + d x]^{3/2} (a + b \tan [c + d x])^2} dx$$

Optimal (type 3, 439 leaves, 16 steps):

$$\frac{(a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]}\right]}{\sqrt{2} (a^2 + b^2)^2 d} -$$

$$\frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]}\right] -$$

$$\frac{b^{3/2} (7 a^2 A b + 3 A b^3 - 5 a^3 B - a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a}}\right]}{a^{5/2} (a^2 + b^2)^2 d} + \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d}$$

$$(2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] -$$

$$\frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] -$$

$$\frac{2 a^2 A + 3 A b^2 - a b B}{a^2 (a^2 + b^2) d \sqrt{\tan [c + d x]}} + \frac{b (A b - a B)}{a (a^2 + b^2) d \sqrt{\tan [c + d x]} (a + b \tan [c + d x])}$$

Result (type 3, 880 leaves):

$$\left( \text{Sec}[c + dx] (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])^2 \right. \\ \left. \left( \frac{b^2 (-Ab + aB)}{a^3 (a^2 + b^2)} - \frac{2A \text{Cot}[c + dx]}{a^2} + \frac{Ab^4 \text{Sin}[c + dx] - a b^3 B \text{Sin}[c + dx]}{a^3 (a - ib) (a + ib) (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])} \right) \right. \\ \left. \sqrt{\text{Tan}[c + dx]} (A + B \text{Tan}[c + dx]) \right) / \left( d (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) (a + b \text{Tan}[c + dx])^2 \right) - \\ \left( \text{Sec}[c + dx] (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])^2 (A + B \text{Tan}[c + dx]) \right. \\ \left( \left( 2 (3 a^2 A b + 3 A b^3 - a^3 B - a b^2 B) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right] \text{Csc}[c + dx] \text{Sec}[c + dx]^3 \right. \right. \\ \left. \left. (a + b \text{Tan}[c + dx]) \right) / \left( \sqrt{a} \sqrt{b} (b + a \text{Cot}[c + dx]) (1 + \text{Tan}[c + dx]^2)^2 \right) + \right. \\ \left. \frac{1}{4 (a^2 + b^2) (b + a \text{Cot}[c + dx]) (1 + \text{Tan}[c + dx]^2)} (a^3 A + a^2 b B) \text{Csc}[c + dx]^2 \right. \\ \left. \left( -8 \sqrt{a} \sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right] + \sqrt{2} \right. \right. \\ \left. \left( -2 (a + b) \text{ArcTan}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] + 2 (a + b) \text{ArcTan}\left[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] + \right. \right. \\ \left. \left. (a - b) \left( \text{Log}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx]\right] - \text{Log}\left[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \right. \right. \right. \\ \left. \left. \left. \text{Tan}[c + dx]\right] \right) \right) \right) \text{Sec}[c + dx]^2 \text{Sin}[2(c + dx)] (a + b \text{Tan}[c + dx]) - \\ (1 / (2 (a^2 + b^2) (b + a \text{Cot}[c + dx]) (1 - \text{Tan}[c + dx]^2) (1 + \text{Tan}[c + dx]^2))) \\ (a^2 A b - a^3 B) \text{Cos}[2(c + dx)] \text{Csc}[c + dx] \left( \frac{4 (a^2 - b^2) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right. \\ \left. \left( 2 (a - b) \text{ArcTan}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] - 2 (a - b) \text{ArcTan}\left[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] + \right. \right. \\ \left. \left. (a + b) \left( \text{Log}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx]\right] - \text{Log}\left[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \right. \right. \right. \\ \left. \left. \left. \text{Tan}[c + dx]\right] \right) \right) \right) \text{Sec}[c + dx]^3 (a + b \text{Tan}[c + dx]) \right) / \\ (2 a^2 (a - ib) (a + ib) d (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) (a + b \text{Tan}[c + dx])^2)$$



### Problem 409: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{A + B \tan [c + d x]}{\tan [c + d x]^{5/2} (a + b \tan [c + d x])^2} dx$$

Optimal (type 3, 493 leaves, 17 steps):

$$\begin{aligned} & - \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]}\right] + \\ & \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]}\right] + \\ & \frac{b^{5/2} (9 a^2 A b + 5 A b^3 - 7 a^3 B - 3 a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a}}\right]}{a^{7/2} (a^2 + b^2)^2 d} + \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} \\ & (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] - \\ & \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] - \\ & \frac{2 a^2 A + 5 A b^2 - 3 a b B}{3 a^2 (a^2 + b^2) d \tan [c + d x]^{3/2}} + \frac{4 a^2 A b + 5 A b^3 - 2 a^3 B - 3 a b^2 B}{a^3 (a^2 + b^2) d \sqrt{\tan [c + d x]}} + \\ & \frac{b (A b - a B)}{a (a^2 + b^2) d \tan [c + d x]^{3/2} (a + b \tan [c + d x])} \end{aligned}$$

Result (type 3, 956 leaves):

$$\begin{aligned}
 & \left( \sec [c+d x] (a \cos [c+d x]+b \sin [c+d x])^2 \right. \\
 & \left. \left( \frac{2 a^4 A+2 a^2 A b^2+3 A b^4-3 a b^3 B}{3 a^4(a-i b)(a+i b)}-\frac{2(-2 A b \cos [c+d x]+a B \cos [c+d x]) \csc [c+d x]}{a^3}-\frac{2 A \csc [c+d x]^2}{3 a^2}+\frac{-A b^5 \sin [c+d x]+a b^4 B \sin [c+d x]}{a^4(a-i b)(a+i b)(a \cos [c+d x]+b \sin [c+d x])} \right) \sqrt{\tan [c+d x]} \right. \\
 & \left. (A+B \tan [c+d x]) \right) / \left( d(A \cos [c+d x]+B \sin [c+d x])(a+b \tan [c+d x])^2 \right)+ \\
 & \left( \sec [c+d x] (a \cos [c+d x]+b \sin [c+d x])^2 (A+B \tan [c+d x]) \right. \\
 & \left. \left( \left( 2\left(-a^4 A+4 a^2 A b^2+5 A b^4-3 a^3 b B-3 a b^3 B\right) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}}\right] \csc [c+d x] \right. \right. \right. \\
 & \left. \left. \left. \sec [c+d x]^3(a+b \tan [c+d x]) \right) \right) / \left( \sqrt{a} \sqrt{b}(b+a \cot [c+d x])\left(1+\tan [c+d x]^2\right)^2 \right)+ \right. \\
 & \left. \frac{1}{4\left(a^2+b^2\right)(b+a \cot [c+d x])\left(1+\tan [c+d x]^2\right)}\left(a^3 A b-a^4 B\right) \csc [c+d x]^2 \right. \\
 & \left. \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}}\right]+\sqrt{2} \right. \right. \\
 & \left. \left. \left( -2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\tan [c+d x]}\right]+2(a+b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\tan [c+d x]}\right] \right)+ \right. \right. \\
 & \left. \left. (a-b)\left(\log \left[1-\sqrt{2} \sqrt{\tan [c+d x]}+\tan [c+d x]\right]-\log \left[1+\sqrt{2} \sqrt{\tan [c+d x]}+\right. \right. \right. \\
 & \left. \left. \left. \tan [c+d x]\right)\right] \right) \right) \sec [c+d x]^2 \sin [2(c+d x)](a+b \tan [c+d x]) - \\
 & \left. \left( 1 / \left( 2\left(a^2+b^2\right)(b+a \cot [c+d x])\left(1-\tan [c+d x]^2\right)\left(1+\tan [c+d x]^2\right) \right) \right) \right. \\
 & \left. \left( -a^4 A-a^3 b B\right) \cos [2(c+d x)] \csc [c+d x] \left( \frac{4\left(a^2-b^2\right) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}}+\sqrt{2} \right. \right. \\
 & \left. \left. \left( 2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\tan [c+d x]}\right]-2(a-b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\tan [c+d x]}\right] \right)+ \right. \right. \\
 & \left. \left. (a+b)\left(\log \left[1-\sqrt{2} \sqrt{\tan [c+d x]}+\tan [c+d x]\right]-\log \left[1+\sqrt{2} \sqrt{\tan [c+d x]}+\right. \right. \right. \\
 & \left. \left. \left. \tan [c+d x]\right)\right] \right) \right) \sec [c+d x]^3(a+b \tan [c+d x]) \right) / \\
 & \left( 2 a^3(a-i b)(a+i b) d(A \cos [c+d x]+B \sin [c+d x])(a+b \tan [c+d x])^2 \right)
 \end{aligned}$$

**Problem 410: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\tan [c+d x]^{7/2} (A+B \tan [c+d x])}{(a+b \tan [c+d x])^3} dx$$

Optimal (type 3, 600 leaves, 17 steps):

$$\frac{1}{\sqrt{2} (a^2+b^2)^3 d} (3 a^2 b (A-B) - b^3 (A-B) - a^3 (A+B) + 3 a b^2 (A+B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan [c+d x]}\right] - \frac{1}{\sqrt{2} (a^2+b^2)^3 d} (3 a^2 b (A-B) - b^3 (A-B) - a^3 (A+B) + 3 a b^2 (A+B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan [c+d x]}\right] + \frac{1}{4 b^{7/2} (a^2+b^2)^3 d} a^{3/2} (3 a^4 A b + 6 a^2 A b^3 + 35 A b^5 - 15 a^5 B - 46 a^3 b^2 B - 63 a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}}\right] - \frac{1}{2 \sqrt{2} (a^2+b^2)^3 d} (a^3 (A-B) - 3 a b^2 (A-B) + 3 a^2 b (A+B) - b^3 (A+B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan [c+d x]} + \tan [c+d x]\right] + \frac{1}{2 \sqrt{2} (a^2+b^2)^3 d} (a^3 (A-B) - 3 a b^2 (A-B) + 3 a^2 b (A+B) - b^3 (A+B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan [c+d x]} + \tan [c+d x]\right] - \frac{(3 a^3 A b + 11 a A b^3 - 15 a^4 B - 31 a^2 b^2 B - 8 b^4 B) \sqrt{\tan [c+d x]}}{4 b^3 (a^2+b^2)^2 d} + \frac{a (A b - a B) \tan [c+d x]^{5/2}}{2 b (a^2+b^2) d (a+b \tan [c+d x])^2} + \frac{a (a^2 A b + 9 A b^3 - 5 a^3 B - 13 a b^2 B) \tan [c+d x]^{3/2}}{4 b^2 (a^2+b^2)^2 d (a+b \tan [c+d x])}$$

Result (type 3, 1034 leaves):

$$\left( \sec [c+d x]^2 (a \cos [c+d x] + b \sin [c+d x])^3 \left( \frac{-3 a^3 A b - 13 a A b^3 + 15 a^4 B + 33 a^2 b^2 B + 8 b^4 B}{4 (a - i b)^2 (a + i b)^2 b^3} - \frac{a^3 (-A b + a B)}{2 (a - i b)^2 (a + i b)^2 b (a \cos [c+d x] + b \sin [c+d x])^2} + \frac{(a^3 A b \sin [c+d x] + 13 a A b^3 \sin [c+d x] - 5 a^4 B \sin [c+d x] - 17 a^2 b^2 B \sin [c+d x])}{(4 (a - i b)^2 (a + i b)^2 b^2 (a \cos [c+d x] + b \sin [c+d x]))} \right) \sqrt{\tan [c+d x]} (A+B \tan [c+d x]) \right) / \left( d (A \cos [c+d x] + B \sin [c+d x]) (a+b \tan [c+d x])^3 \right) - \left( \sec [c+d x]^2 (a \cos [c+d x] + b \sin [c+d x])^3 (A+B \tan [c+d x]) \right)$$

$$\left( \left( 2 \left( -3 a^4 A b - 7 a^2 A b^3 - 4 A b^5 + 15 a^5 B + 31 a^3 b^2 B + 16 a b^4 B \right) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}} \right] \right. \right.$$

$$\left. \left. \operatorname{Csc}[c+d x] \operatorname{Sec}[c+d x]^3 (a+b \tan [c+d x]) \right) \right) / \left( \sqrt{a} \sqrt{b} (b+a \operatorname{Cot}[c+d x]) \right)$$

$$\left( \frac{1}{4 (a^2+b^2) (b+a \operatorname{Cot}[c+d x]) (1+\tan [c+d x]^2)} \right) +$$

$$\left( 8 a A b^4 - 4 a^2 b^3 B + 4 b^5 B \right) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}} \right] + \sqrt{2} \right.$$

$$\left( -2 (a+b) \operatorname{ArcTan} \left[ 1 - \sqrt{2} \sqrt{\tan [c+d x]} \right] + 2 (a+b) \operatorname{ArcTan} \left[ 1 + \sqrt{2} \sqrt{\tan [c+d x]} \right] \right) +$$

$$\left( a-b \right) \left( \operatorname{Log} \left[ 1 - \sqrt{2} \sqrt{\tan [c+d x]} + \tan [c+d x] \right] - \operatorname{Log} \left[ 1 + \sqrt{2} \sqrt{\tan [c+d x]} + \right. \right.$$

$$\left. \left. \tan [c+d x] \right] \right) \left) \operatorname{Sec}[c+d x]^2 \operatorname{Sin} \left[ 2 (c+d x) \right] (a+b \tan [c+d x]) - \right.$$

$$\left( \frac{1}{2 (a^2+b^2) (b+a \operatorname{Cot}[c+d x]) (1-\tan [c+d x]^2) (1+\tan [c+d x]^2)} \right) \left( -4 a^2 A b^3 + 4 A b^5 - 8 a b^4 B \right) \operatorname{Cos} \left[ 2 (c+d x) \right]$$

$$\operatorname{Csc}[c+d x] \left( \frac{4 (a^2-b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a}} \right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right.$$

$$\left( 2 (a-b) \operatorname{ArcTan} \left[ 1 - \sqrt{2} \sqrt{\tan [c+d x]} \right] - 2 (a-b) \operatorname{ArcTan} \left[ 1 + \sqrt{2} \sqrt{\tan [c+d x]} \right] + \right.$$

$$\left. \left. (a+b) \left( \operatorname{Log} \left[ 1 - \sqrt{2} \sqrt{\tan [c+d x]} + \tan [c+d x] \right] - \operatorname{Log} \left[ 1 + \sqrt{2} \sqrt{\tan [c+d x]} + \tan [c+d x] \right] \right) \right) \right) \operatorname{Sec}[c+d x]^3 (a+b \tan [c+d x]) \left. \right) /$$

$$\left( 8 (a-i b)^2 (a+i b)^2 b^3 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \tan [c+d x])^3 \right)$$

**Problem 411: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\tan [c+d x]^{5/2} (A+B \tan [c+d x])}{(a+b \tan [c+d x])^3} dx$$

Optimal (type 3, 534 leaves, 16 steps):

$$\frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]}\right] - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]}\right] + \frac{1}{4 b^{5/2} (a^2 + b^2)^3 d} \sqrt{a} (a^4 A b + 18 a^2 A b^3 - 15 A b^5 + 3 a^5 B + 6 a^3 b^2 B + 35 a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a}}\right] + \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] + \frac{a (A b - a B) \tan[c + d x]^{3/2}}{2 b (a^2 + b^2) d (a + b \tan[c + d x])^2} - \frac{a (a^2 A b - 7 A b^3 + 3 a^3 B + 11 a b^2 B) \sqrt{\tan[c + d x]}}{4 b^2 (a^2 + b^2)^2 d (a + b \tan[c + d x])}$$

Result (type 3, 1007 leaves):

$$\left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \left( -\frac{a^2 A b - 9 A b^3 + 3 a^3 B + 13 a b^2 B}{4 (a - i b)^2 (a + i b)^2 b^2} + \frac{a^2 (-A b + a B)}{2 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2} + (3 a^2 A b \operatorname{Sin}[c + d x] - 9 A b^3 \operatorname{Sin}[c + d x] + a^3 B \operatorname{Sin}[c + d x] + 13 a b^2 B \operatorname{Sin}[c + d x]) \right) / \left( 4 (a - i b)^2 (a + i b)^2 b (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \right) \sqrt{\tan[c + d x]} (A + B \tan[c + d x]) \right) / \left( d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan[c + d x])^3 \right) + \left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \tan[c + d x]) \left( 2 (a^3 A b + a A b^3 + 3 a^4 B + 7 a^2 b^2 B + 4 b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a}}\right] \operatorname{Csc}[c + d x] \operatorname{Sec}[c + d x]^3 (a + b \tan[c + d x]) \right) / \left( \sqrt{a} \sqrt{b} (b + a \operatorname{Cot}[c + d x]) (1 + \tan[c + d x])^2 \right) + \frac{1}{4 (a^2 + b^2) (b + a \operatorname{Cot}[c + d x]) (1 + \tan[c + d x])^2} (-4 a^2 A b^2 + 4 A b^4 - 8 a b^3 B) \right)$$

$$\begin{aligned}
 & \text{Csc}[c + dx]^2 \left( -8 \sqrt{a} \sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right] + \sqrt{2} \right. \\
 & \quad \left( -2 (a + b) \text{ArcTan}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] + 2 (a + b) \text{ArcTan}\left[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] + \right. \\
 & \quad \left. (a - b) \left( \text{Log}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx]\right] - \text{Log}\left[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \right. \right. \\
 & \quad \left. \left. \text{Tan}[c + dx]\right]\right) \left. \right) \text{Sec}[c + dx]^2 \text{Sin}[2(c + dx)] (a + b \text{Tan}[c + dx]) - \\
 & \left( \frac{1}{2(a^2 + b^2)} (b + a \text{Cot}[c + dx]) (1 - \text{Tan}[c + dx]^2) (1 + \text{Tan}[c + dx]^2) \right) \\
 & \left( -8 a A b^3 + 4 a^2 b^2 B - 4 b^4 B \right) \text{Cos}[2(c + dx)] \\
 & \text{Csc}[c + dx] \left( \frac{4(a^2 - b^2) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right. \\
 & \quad \left( 2(a - b) \text{ArcTan}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] - 2(a - b) \text{ArcTan}\left[1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]}\right] + \right. \\
 & \quad \left. (a + b) \left( \text{Log}\left[1 - \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx]\right] - \text{Log}\left[ \right. \right. \\
 & \quad \left. \left. 1 + \sqrt{2} \sqrt{\text{Tan}[c + dx]} + \text{Tan}[c + dx]\right]\right) \left. \right) \text{Sec}[c + dx]^3 (a + b \text{Tan}[c + dx]) \left. \right) / \\
 & \left( 8(a - ib)^2 (a + ib)^2 b^2 d (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) (a + b \text{Tan}[c + dx])^3 \right)
 \end{aligned}$$

**Problem 412: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\text{Tan}[c + dx]^{3/2} (A + B \text{Tan}[c + dx])}{(a + b \text{Tan}[c + dx])^3} dx$$

Optimal (type 3, 533 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \\
 & \quad \text{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]}\right] + \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} \\
 & (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \text{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]}\right] + \\
 & \left( (3 a^4 A b - 26 a^2 A b^3 + 3 A b^5 + a^5 B + 18 a^3 b^2 B - 15 a b^4 B) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a}}\right] \right) / \\
 & \left( 4 \sqrt{a} b^{3/2} (a^2 + b^2)^3 d \right) + \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \\
 & \text{Log}\left[1 - \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \text{Log}\left[1 + \sqrt{2} \sqrt{\tan[c + d x]} + \tan[c + d x]\right] + \\
 & \frac{a (A b - a B) \sqrt{\tan[c + d x]}}{2 b (a^2 + b^2) d (a + b \tan[c + d x])^2} + \frac{(3 a^2 A b - 5 A b^3 + a^3 B + 9 a b^2 B) \sqrt{\tan[c + d x]}}{4 b (a^2 + b^2)^2 d (a + b \tan[c + d x])}
 \end{aligned}$$

Result (type 3, 997 leaves):

$$\begin{aligned}
 & \left( \text{Sec}[c + d x]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^3 \right. \\
 & \quad \left( - \frac{-5 a^2 A b + 5 A b^3 + a^3 B - 9 a b^2 B}{4 a (a - i b)^2 (a + i b)^2 b} - \frac{a b (-A b + a B)}{2 (a - i b)^2 (a + i b)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2} + \right. \\
 & \quad \left. (-7 a^2 A b \text{Sin}[c + d x] + 5 A b^3 \text{Sin}[c + d x] + 3 a^3 B \text{Sin}[c + d x] - 9 a b^2 B \text{Sin}[c + d x]) / \right. \\
 & \quad \left. (4 a (a - i b)^2 (a + i b)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])) \right) \sqrt{\tan[c + d x]} \\
 & \quad \left. (A + B \tan[c + d x]) \right) / \left( d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \tan[c + d x])^3 \right) + \\
 & \left( \text{Sec}[c + d x]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^3 (A + B \tan[c + d x]) \right. \\
 & \quad \left( \left( 2 (-a^2 A b - A b^3 + a^3 B + a b^2 B) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a}}\right] \text{Csc}[c + d x] \text{Sec}[c + d x]^3 \right. \right. \\
 & \quad \left. \left. (a + b \tan[c + d x]) \right) / \left( \sqrt{a} \sqrt{b} (b + a \text{Cot}[c + d x]) (1 + \tan[c + d x])^2 \right) \right) + \\
 & \quad \frac{1}{4 (a^2 + b^2) (b + a \text{Cot}[c + d x]) (1 + \tan[c + d x])^2} (8 a A b^2 - 4 a^2 b B + 4 b^3 B) \\
 & \quad \left. \text{Csc}[c + d x]^2 \left( -8 \sqrt{a} \sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a}}\right] + \sqrt{2} \right) \right)
 \end{aligned}$$

$$\begin{aligned} & \left( -2 (a+b) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]}\right] + 2 (a+b) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]}\right] + \right. \\ & \quad \left. (a-b) \left( \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]\right] - \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]} + \right. \right. \right. \\ & \quad \left. \left. \tan[c+dx]\right] \right) \right) \operatorname{Sec}[c+dx]^2 \operatorname{Sin}[2(c+dx)] (a+b \tan[c+dx]) - \\ & \left( \frac{1}{2} (2(a^2+b^2)(b+a \operatorname{Cot}[c+dx])(1-\tan[c+dx]^2)(1+\tan[c+dx]^2)) \right. \\ & \quad \left. (-4a^2Ab+4Ab^3-8a^2B) \operatorname{Cos}[2(c+dx)] \right) \\ & \operatorname{Csc}[c+dx] \left( \frac{4(a^2-b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right. \\ & \quad \left. \left( 2(a-b) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]}\right] - 2(a-b) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]}\right] + \right. \right. \\ & \quad \left. \left. (a+b) \left( \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]\right] - \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]} + \right. \right. \right. \right. \\ & \quad \left. \left. \tan[c+dx]\right] \right) \right) \operatorname{Sec}[c+dx]^3 (a+b \tan[c+dx]) \Bigg) / \\ & \left( 8(a-ib)^2 (a+ib)^2 bd (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) (a+b \tan[c+dx])^3 \right) \end{aligned}$$

**Problem 413: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sqrt{\tan[c+dx]} (A+B \tan[c+dx])}{(a+b \tan[c+dx])^3} dx$$

Optimal (type 3, 531 leaves, 16 steps):

$$\begin{aligned} & -\frac{1}{\sqrt{2} (a^2+b^2)^3 d} (a^3 (A-B) - 3ab^2 (A-B) + 3a^2b (A+B) - b^3 (A+B)) \\ & \quad \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]}\right] + \frac{1}{\sqrt{2} (a^2+b^2)^3 d} \\ & \quad (a^3 (A-B) - 3ab^2 (A-B) + 3a^2b (A+B) - b^3 (A+B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]}\right] - \\ & \quad \left( (15a^4Ab - 18a^2Ab^3 - Ab^5 - 3a^5B + 26a^3b^2B - 3ab^4B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a}}\right] \right) / \\ & \quad \left( 4a^{3/2} \sqrt{b} (a^2+b^2)^3 d \right) - \frac{1}{2\sqrt{2} (a^2+b^2)^3 d} (3a^2b (A-B) - b^3 (A-B) - a^3 (A+B) + 3ab^2 (A+B)) \\ & \quad \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]\right] + \frac{1}{2\sqrt{2} (a^2+b^2)^3 d} \\ & \quad (3a^2b (A-B) - b^3 (A-B) - a^3 (A+B) + 3ab^2 (A+B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan[c+dx]} + \tan[c+dx]\right] - \\ & \quad \frac{(Ab-aB) \sqrt{\tan[c+dx]}}{2(a^2+b^2)d(a+b \tan[c+dx])^2} - \frac{(7a^2Ab - Ab^3 - 3a^3B + 5ab^2B) \sqrt{\tan[c+dx]}}{4a(a^2+b^2)^2d(a+b \tan[c+dx])} \end{aligned}$$

Result (type 3, 998 leaves):



$$\begin{aligned}
 & \left( \text{Sec}[c+dx]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^3 \right. \\
 & \left. \left( \frac{-9 a^2 A b + A b^3 + 5 a^3 B - 5 a b^2 B}{4 a^2 (a - i b)^2 (a + i b)^2} + \frac{b^2 (-A b + a B)}{2 (a - i b)^2 (a + i b)^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2} + \right. \right. \\
 & \left. \left. (11 a^2 A b^2 \text{Sin}[c+dx] - A b^4 \text{Sin}[c+dx] - 7 a^3 b B \text{Sin}[c+dx] + 5 a b^3 B \text{Sin}[c+dx]) / \right. \right. \\
 & \left. \left. (4 a^2 (a - i b)^2 (a + i b)^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])) \right) \sqrt{\text{Tan}[c+dx]} \right. \\
 & \left. (A + B \text{Tan}[c+dx]) \right) / \left( d (A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a + b \text{Tan}[c+dx])^3 \right) + \\
 & \left( \text{Sec}[c+dx]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^3 (A + B \text{Tan}[c+dx]) \right. \\
 & \left. \left( \left( 2 (a^2 A b + A b^3 - a^3 B - a b^2 B) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c+dx]}}{\sqrt{a}}\right] \text{Csc}[c+dx] \text{Sec}[c+dx]^3 \right. \right. \right. \\
 & \left. \left. (a + b \text{Tan}[c+dx]) \right) / \left( \sqrt{a} \sqrt{b} (b + a \text{Cot}[c+dx]) (1 + \text{Tan}[c+dx]^2)^2 \right) + \right. \\
 & \left. \frac{1}{4 (a^2 + b^2) (b + a \text{Cot}[c+dx]) (1 + \text{Tan}[c+dx]^2)} (4 a^3 A - 4 a A b^2 + 8 a^2 b B) \right. \\
 & \left. \text{Csc}[c+dx]^2 \left( -8 \sqrt{a} \sqrt{b} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c+dx]}}{\sqrt{a}}\right] + \sqrt{2} \right. \right. \\
 & \left. \left. (-2 (a + b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c+dx]}] + 2 (a + b) \text{ArcTan}[1 + \sqrt{2} \sqrt{\text{Tan}[c+dx]}] + \right. \right. \\
 & \left. \left. (a - b) (\text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c+dx]} + \text{Tan}[c+dx]] - \text{Log}[1 + \sqrt{2} \sqrt{\text{Tan}[c+dx]} + \right. \right. \\
 & \left. \left. \text{Tan}[c+dx]) \right) \right) \text{Sec}[c+dx]^2 \text{Sin}[2(c+dx)] (a + b \text{Tan}[c+dx]) - \\
 & \left. (1 / (2 (a^2 + b^2) (b + a \text{Cot}[c+dx]) (1 - \text{Tan}[c+dx]^2) (1 + \text{Tan}[c+dx]^2))) \right. \\
 & \left. (8 a^2 A b - 4 a^3 B + 4 a b^2 B) \text{Cos}[2(c+dx)] \text{Csc}[c+dx] \left( \frac{4 (a^2 - b^2) \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c+dx]}}{\sqrt{a}}\right]}{\sqrt{a} \sqrt{b}} \right. \right. \\
 & \left. \left. \sqrt{2} (2 (a - b) \text{ArcTan}[1 - \sqrt{2} \sqrt{\text{Tan}[c+dx]}] - 2 (a - b) \text{ArcTan}[1 + \right. \right. \\
 & \left. \left. \sqrt{2} \sqrt{\text{Tan}[c+dx]}] + (a + b) (\text{Log}[1 - \sqrt{2} \sqrt{\text{Tan}[c+dx]} + \text{Tan}[c+dx]] - \text{Log}[ \right. \right. \\
 & \left. \left. 1 + \sqrt{2} \sqrt{\text{Tan}[c+dx]} + \text{Tan}[c+dx]) \right) \right) \text{Sec}[c+dx]^3 (a + b \text{Tan}[c+dx]) \right) \left. \right) / \\
 & \left( 8 a (a - i b)^2 (a + i b)^2 d (A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) (a + b \text{Tan}[c+dx])^3 \right)
 \end{aligned}$$

**Problem 414: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \tan [c + d x]}{\sqrt{\tan [c + d x]} (a + b \tan [c + d x])^3} dx$$

Optimal (type 3, 534 leaves, 16 steps):

$$\frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]}\right] - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]}\right] + \frac{1}{4 a^{5/2} (a^2 + b^2)^3 d} \sqrt{b} (35 a^4 A b + 6 a^2 A b^3 + 3 A b^5 - 15 a^5 B + 18 a^3 b^2 B + a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a}}\right] - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] + \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\tan [c + d x]} + \tan [c + d x]\right] + \frac{b (A b - a B) \sqrt{\tan [c + d x]}}{2 a (a^2 + b^2) d (a + b \tan [c + d x])^2} + \frac{b (11 a^2 A b + 3 A b^3 - 7 a^3 B + a b^2 B) \sqrt{\tan [c + d x]}}{4 a^2 (a^2 + b^2)^2 d (a + b \tan [c + d x])}$$

Result (type 3, 1018 leaves):

$$\left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \left( -\frac{b (-13 a^2 A b - 3 A b^3 + 9 a^3 B - a b^2 B)}{4 a^3 (a - i b)^2 (a + i b)^2} - \frac{b^3 (-A b + a B)}{2 a (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2} + \frac{(-15 a^2 A b^3 \operatorname{Sin}[c + d x] - 3 A b^5 \operatorname{Sin}[c + d x] + 11 a^3 b^2 B \operatorname{Sin}[c + d x] - a b^4 B \operatorname{Sin}[c + d x])}{4 a^3 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])} \right) \sqrt{\tan [c + d x]} (A + B \tan [c + d x]) \right) / \left( d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \tan [c + d x])^3 \right) + \left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \tan [c + d x]) \right)$$

$$\left( \left( 2 (4 a^4 A + 7 a^2 A b^2 + 3 A b^4 + a^3 b B + a b^3 B) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a}} \right] \operatorname{Csc}[c+d x] \right. \right.$$

$$\left. \left. \operatorname{Sec}[c+d x]^3 (a+b \operatorname{Tan}[c+d x]) \right) / \left( \sqrt{a} \sqrt{b} (b+a \operatorname{Cot}[c+d x]) (1+\operatorname{Tan}[c+d x]^2)^2 \right) + \right.$$

$$\frac{1}{4 (a^2+b^2) (b+a \operatorname{Cot}[c+d x]) (1+\operatorname{Tan}[c+d x]^2)} (-8 a^3 A b + 4 a^4 B - 4 a^2 b^2 B)$$

$$\operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a}} \right] + \sqrt{2} \right.$$

$$\left( -2 (a+b) \operatorname{ArcTan} [1-\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]}] + 2 (a+b) \operatorname{ArcTan} [1+\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]}] \right) +$$

$$(a-b) \left( \operatorname{Log} [1-\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]} + \operatorname{Tan}[c+d x]] - \operatorname{Log} [1+\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]} + \right.$$

$$\left. \left. \operatorname{Tan}[c+d x] \right] \right) \left. \right) \operatorname{Sec}[c+d x]^2 \operatorname{Sin}[2(c+d x)] (a+b \operatorname{Tan}[c+d x]) -$$

$$\left( \frac{1}{2 (a^2+b^2) (b+a \operatorname{Cot}[c+d x]) (1-\operatorname{Tan}[c+d x]^2) (1+\operatorname{Tan}[c+d x]^2)} \right)$$

$$\left( 4 a^4 A - 4 a^2 A b^2 + 8 a^3 b B \right) \operatorname{Cos}[2(c+d x)]$$

$$\operatorname{Csc}[c+d x] \left( \frac{4 (a^2-b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a}} \right]}{\sqrt{a} \sqrt{b}} + \sqrt{2} \right.$$

$$\left( 2 (a-b) \operatorname{ArcTan} [1-\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]}] - 2 (a-b) \operatorname{ArcTan} [1+\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]}] \right) +$$

$$(a+b) \left( \operatorname{Log} [1-\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]} + \operatorname{Tan}[c+d x]] - \operatorname{Log} [ \right.$$

$$\left. \left. 1+\sqrt{2} \sqrt{\operatorname{Tan}[c+d x]} + \operatorname{Tan}[c+d x] \right] \right) \left. \right) \operatorname{Sec}[c+d x]^3 (a+b \operatorname{Tan}[c+d x]) \left. \right) /$$

$$(8 a^2 (a-i b)^2 (a+i b)^2 d (A \operatorname{Cos}[c+d x] + B \operatorname{Sin}[c+d x]) (a+b \operatorname{Tan}[c+d x])^3)$$

**Problem 415: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \operatorname{Tan}[c+d x]}{\operatorname{Tan}[c+d x]^{3/2} (a+b \operatorname{Tan}[c+d x])^3} dx$$

Optimal (type 3, 601 leaves, 17 steps):

$$\frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]}\right] - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]}\right] - \frac{1}{4 a^{7/2} (a^2 + b^2)^3 d} b^{3/2} (63 a^4 A b + 46 a^2 A b^3 + 15 A b^5 - 35 a^5 B - 6 a^3 b^2 B - 3 a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a}}\right] + \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]} + \operatorname{Tan}[c + d x]\right] - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Tan}[c + d x]} + \operatorname{Tan}[c + d x]\right] - \frac{8 a^4 A + 31 a^2 A b^2 + 15 A b^4 - 11 a^3 b B - 3 a b^3 B}{4 a^3 (a^2 + b^2)^2 d \sqrt{\operatorname{Tan}[c + d x]}} + \frac{b (A b - a B)}{2 a (a^2 + b^2) d \sqrt{\operatorname{Tan}[c + d x]} (a + b \operatorname{Tan}[c + d x])^2} + \frac{b (13 a^2 A b + 5 A b^3 - 9 a^3 B - a b^2 B)}{4 a^2 (a^2 + b^2)^2 d \sqrt{\operatorname{Tan}[c + d x]} (a + b \operatorname{Tan}[c + d x])}$$

Result (type 3, 1043 leaves):

$$\left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \left( \frac{b^2 (-17 a^2 A b - 7 A b^3 + 13 a^3 B + 3 a b^2 B)}{4 a^4 (a - i b)^2 (a + i b)^2} - \frac{2 A \operatorname{Cot}[c + d x]}{a^3} + \frac{b^4 (-A b + a B)}{2 a^2 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2} + (19 a^2 A b^4 \operatorname{Sin}[c + d x] + 7 A b^6 \operatorname{Sin}[c + d x] - 15 a^3 b^3 B \operatorname{Sin}[c + d x] - 3 a b^5 B \operatorname{Sin}[c + d x]) / (4 a^4 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])) \right) \sqrt{\operatorname{Tan}[c + d x]} (A + B \operatorname{Tan}[c + d x]) \right) / \left( d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^3 \right) - \left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 (A + B \operatorname{Tan}[c + d x]) \left( 2 (16 a^4 A b + 31 a^2 A b^3 + 15 A b^5 - 4 a^5 B - 7 a^3 b^2 B - 3 a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a}}\right] \right) \right) / \left( \sqrt{a} \sqrt{b} (b + a \operatorname{Cot}[c + d x]) \right)$$

$$\begin{aligned}
 & \frac{1}{4(a^2 + b^2)(b + a \cot[c + dx])(1 + \tan[c + dx]^2)} \\
 & (4a^5A - 4a^3Ab^2 + 8a^4bB) \operatorname{Csc}[c + dx]^2 \left( -8\sqrt{a}\sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{b}\sqrt{\tan[c + dx]}}{\sqrt{a}}\right] + \sqrt{2} \right. \\
 & \left. (-2(a + b) \operatorname{ArcTan}[1 - \sqrt{2}\sqrt{\tan[c + dx]}] + 2(a + b) \operatorname{ArcTan}[1 + \sqrt{2}\sqrt{\tan[c + dx]}] + \right. \\
 & \left. (a - b) \left( \operatorname{Log}[1 - \sqrt{2}\sqrt{\tan[c + dx]} + \tan[c + dx]] - \operatorname{Log}[1 + \sqrt{2}\sqrt{\tan[c + dx]} + \right. \right. \\
 & \left. \left. \tan[c + dx]] \right) \right) \operatorname{Sec}[c + dx]^2 \operatorname{Sin}[2(c + dx)](a + b \tan[c + dx]) - \\
 & \left( \frac{1}{2(a^2 + b^2)(b + a \cot[c + dx])(1 - \tan[c + dx]^2)(1 + \tan[c + dx]^2)} \right) \\
 & (8a^4Ab - 4a^5B + 4a^3b^2B) \operatorname{Cos}[2(c + dx)] \\
 & \operatorname{Csc}[c + dx] \left( \frac{4(a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b}\sqrt{\tan[c + dx]}}{\sqrt{a}}\right]}{\sqrt{a}\sqrt{b}} + \sqrt{2} \right. \\
 & \left. (2(a - b) \operatorname{ArcTan}[1 - \sqrt{2}\sqrt{\tan[c + dx]}] - 2(a - b) \operatorname{ArcTan}[1 + \sqrt{2}\sqrt{\tan[c + dx]}] + \right. \\
 & \left. (a + b) \left( \operatorname{Log}[1 - \sqrt{2}\sqrt{\tan[c + dx]} + \tan[c + dx]] - \operatorname{Log}[ \right. \right. \\
 & \left. \left. 1 + \sqrt{2}\sqrt{\tan[c + dx]} + \tan[c + dx]] \right) \right) \operatorname{Sec}[c + dx]^3 (a + b \tan[c + dx]) \Bigg) / \\
 & (8a^3(a - ib)^2(a + ib)^2d(A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx])(a + b \tan[c + dx])^3)
 \end{aligned}$$

**Problem 427: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \tan[c + dx]^{3/2} \sqrt{a + b \tan[c + dx]} (A + B \tan[c + dx]) dx$$

Optimal (type 3, 264 leaves, 14 steps):

$$\begin{aligned}
 & \frac{\sqrt{ia - b} (iA - B) \operatorname{ArcTan}\left[\frac{\sqrt{ia - b}\sqrt{\tan[c + dx]}}{\sqrt{a + b \tan[c + dx]}}\right]}{d} + \\
 & \frac{(4aAb - a^2B - 8b^2B) \operatorname{ArcTanh}\left[\frac{\sqrt{b}\sqrt{\tan[c + dx]}}{\sqrt{a + b \tan[c + dx]}}\right]}{4b^{3/2}d} + \frac{\sqrt{ia + b} (iA + B) \operatorname{ArcTanh}\left[\frac{\sqrt{ia + b}\sqrt{\tan[c + dx]}}{\sqrt{a + b \tan[c + dx]}}\right]}{d} + \\
 & \frac{(4Ab - aB) \sqrt{\tan[c + dx]} \sqrt{a + b \tan[c + dx]}}{4bd} + \frac{B \sqrt{\tan[c + dx]} (a + b \tan[c + dx])^{3/2}}{2bd}
 \end{aligned}$$

Result (type 4, 85695 leaves): Display of huge result suppressed!

**Problem 428: Result unnecessarily involves higher level functions and more**

than twice size of optimal antiderivative.

$$\int \sqrt{\tan [c+d x]} \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x]) d x$$

Optimal (type 3, 201 leaves, 13 steps):

$$\frac{\sqrt{i a-b} (A+i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} + \frac{(2 A b+a B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{\sqrt{b} d} -$$

$$\frac{\sqrt{i a+b} (A-i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} + \frac{B \sqrt{\tan [c+d x]} \sqrt{a+b \tan [c+d x]}}{d}$$

Result (type 4, 69837 leaves): Display of huge result suppressed!

Problem 429: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x])}{\sqrt{\tan [c+d x]}} d x$$

Optimal (type 3, 169 leaves, 12 steps):

$$-\frac{\sqrt{i a-b} (i A-B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} +$$

$$\frac{2 \sqrt{b} B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} - \frac{\sqrt{i a+b} (i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d}$$

Result (type 4, 12343 leaves):

$$\left( 4 a \operatorname{Cos}[c+d x] \left( A \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] + \right. \right.$$

$$\left. \left. B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right) \right) /$$

$$\left( -a+b+\sqrt{a^2+b^2} \right) -$$

$$\left( A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right.$$

$$\left. \left( -i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left( a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right.$$

$$\left. \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) - \right.$$

$$\left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right.$$

$$\left. \left( -i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right.$$

$$\left. \left( -i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left( i a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right.$$

$$\left. \left( i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\begin{aligned}
 & \left( A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( i a + b + \sqrt{a^2 + b^2} \right) - \\
 & \left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( i a + b + \sqrt{a^2 + b^2} \right) + \\
 & \left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( i a + b + \sqrt{a^2 + b^2} \right) - \frac{1}{a + b + \sqrt{a^2 + b^2}} \\
 & \left. b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( \frac{A \operatorname{Csc} [c + d x] \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{\operatorname{Sec} [c + d x]}} + \right. \\
 & \left. B \sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]} \right)
 \end{aligned}$$



$$\left. \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x]) \right/$$

$$\left( \sqrt{a^2+b^2} d \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 (a \cos [c+d x]+b \sin [c+d x])}{a^2+b^2}} \right.$$

$$(A \cos [c+d x]+B \sin [c+d x])$$

$$\left. - \frac{1}{\sqrt{a^2+b^2} \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 (a \cos [c+d x]+b \sin [c+d x])}{a^2+b^2}} \tan [c+d x]^{3/2}} \right)$$

$$2 a \left( A \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] + \right.$$

$$\left. b B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right/ (-a+b+\sqrt{a^2+b^2}) - A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right.$$

$$\left( \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( a \text{ A EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( a + i \left( b + \sqrt{a^2+b^2} \right) \right) - \left( a \text{ B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2+b^2} \right) - \right.$$

$$\left( i b \text{ B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( -i a + b + \sqrt{a^2+b^2} \right) - \left( i a \text{ A EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( \text{A b EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( \text{a B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) +$$

$$\left( i b \text{ B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( b \text{ B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left( \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( a+b+\sqrt{a^2+b^2} \right)$$

$$\text{Sec}[c+dx]^{5/2} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} +$$

$$\left( a^2 \left( \text{AEllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) + \right.$$

$$\left. b \text{BEllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( -a+b+\sqrt{a^2+b^2} \right) - \left( \text{AbEllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( -i a+b+\sqrt{a^2+b^2} \right) -$$

$$\left( a \text{AEllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Bigg/ \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) - \left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Bigg/ \left( -i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left. \left( i b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Bigg/ \left( -i a + b + \sqrt{a^2 + b^2} \right) - \left( i a A \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Bigg/ \left( i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left. \left( A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \right.$$

$$\left( \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) - \left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( i b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) - \left( b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\left. \left. \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\text{Sec} [c + d x]} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \right) / \right.$$

$$\left( \sqrt{a^2 + b^2} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos} [c + d x] + b \text{Sin} [c + d x])}{a^2 + b^2}} \right)$$

$$\begin{aligned}
 & \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}} \sqrt{\operatorname{Tan}[c+dx]}} + \\
 & \left( 2a \left( A \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] + \right. \right. \\
 & \left. \left( b B \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \right. \right. \\
 & \left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] / \left(-a+b+\sqrt{a^2+b^2}\right) - \left( A b \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right. \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] / \left(-i a+b+\sqrt{a^2+b^2}\right) - \right. \right. \\
 & \left. \left( a A \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \right. \right. \\
 & \left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] / \left(a+i\left(b+\sqrt{a^2+b^2}\right)\right) - \left( a B \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right. \right. \right.
 \end{aligned}$$

$$\left( \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2+b^2} \right) - \right.$$

$$\left( i b \operatorname{B EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2+b^2} \right) - \left( i a \operatorname{A EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right. \right.$$

$$\left. \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2+b^2} \right) - \right. \right.$$

$$\left( a b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( a b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right. \right.$$



$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) +$$

$$\left( i b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right],$$

$$\frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}},$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( a + b + \sqrt{a^2+b^2} \right) \right)$$

$$\left. \sqrt{\text{Sec}[c+dx]} (b \text{Cos}[c+dx] - a \text{Sin}[c+dx]) \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right] \Bigg/$$

$$\left( \sqrt{a^2+b^2} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right)$$

$$\left. \sqrt{\frac{a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])}{a^2+b^2}} \sqrt{\text{Tan}[c+dx]} \right) +$$

$$\begin{aligned}
 & \frac{1}{\sqrt{a^2 + b^2} \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{a^2 + b^2}} \sqrt{\operatorname{Tan}[c+dx]}} \\
 & 2 a \left( A \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] + \right. \\
 & \left. b B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / \\
 & (-a + b + \sqrt{a^2 + b^2}) - \left( A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / (-i a + b + \sqrt{a^2 + b^2}) - \\
 & \left( a A \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right. \right. \\
 & \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / (a + i (b + \sqrt{a^2 + b^2})) - \left( a B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.
 \end{aligned}$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( i b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2+b^2} \right) - \left( i a A \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Big/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Big/$$

$$\left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( a B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Big/$$

$$\begin{aligned}
 & \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( i b \operatorname{B EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) - \\
 & \left( b \operatorname{B EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} [c + d x]^{3/2} \\
 & \frac{\operatorname{Sin} [c + d x] \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}}{1} \\
 & \frac{\sqrt{a^2 + b^2} \left( \frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2} \right)^{3/2} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a^2 + b^2}} \\
 & 2 a \left( \operatorname{A EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) +
 \end{aligned}$$

$$\left( b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$(-a + b + \sqrt{a^2 + b^2}) - \left( A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (-i a + b + \sqrt{a^2 + b^2}) -$$

$$\left( a A \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (a + i (b + \sqrt{a^2 + b^2})) - \left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (-i a + b + \sqrt{a^2 + b^2}) -$$

$$\left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) - \left( i a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) + \left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \Big/$$

$$\left( a + b + \sqrt{a^2+b^2} \right)$$

$$\frac{\sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}}{\left( \frac{a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (b \text{Cos}[c+dx] - a \text{Sin}[c+dx])}{a^2+b^2} + \frac{1}{a^2+b^2} \right) + a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx]) \tan\left[\frac{1}{2}(c+dx)\right] \right)} +$$


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$$\frac{1}{\sqrt{a^2+b^2} \sqrt{\frac{a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])}{a^2+b^2}} \sqrt{\text{Tan}[c+dx]}}$$

$$4 a \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\left( - \left( a A \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \Big/ \left( 4 \sqrt{2} \sqrt{a^2+b^2} \sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}} \right) \right)$$

$$\begin{aligned}
 & \left. \left( \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right) \right) - \\
 & \left( a b B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4\sqrt{2}\sqrt{a^2 + b^2} \left( -a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{-a + b + \sqrt{a^2 + b^2}} \right) \right) + \\
 & \left( a A b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4\sqrt{2}\sqrt{a^2 + b^2} \left( -i a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}} \right) \right) + \\
 & \left( a^2 A \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4\sqrt{2}\sqrt{a^2 + b^2} \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}} \right) \right) + \\
 & \left( a^2 B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4\sqrt{2}\sqrt{a^2 + b^2} \left( -i a + b + \sqrt{a^2 + b^2} \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(i a b B \sec\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4 \sqrt{2} \sqrt{a^2 + b^2} (-i a + b + \sqrt{a^2 + b^2})\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(i a^2 A \sec\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4 \sqrt{2} \sqrt{a^2 + b^2} (i a + b + \sqrt{a^2 + b^2})\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(a A b \sec\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4 \sqrt{2} \sqrt{a^2 + b^2} (i a + b + \sqrt{a^2 + b^2})\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( a^2 B \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \quad \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{2 \sqrt{a^2 + b^2}}} \\
 & \quad \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{i a + b + \sqrt{a^2 + b^2}} \right) \right) - \\
 & \left( i a b B \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \quad \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{2 \sqrt{a^2 + b^2}}} \\
 & \quad \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{i a + b + \sqrt{a^2 + b^2}} \right) \right) + \\
 & \left( a b B \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \left( a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \quad \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{2 \sqrt{a^2 + b^2}}} \\
 & \quad \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \\
 & \quad \left. \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{a + b + \sqrt{a^2 + b^2}} \right) \right) \sqrt{\operatorname{Tan} [c + d x]}
 \end{aligned}$$

Problem 430: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x])}{\tan [c+d x]^{3/2}} dx$$

Optimal (type 3, 154 leaves, 8 steps):

$$\frac{\sqrt{i a-b} (A+i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} +$$

$$\frac{\sqrt{i a+b} (A-i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} - \frac{2 A \sqrt{a+b \tan [c+d x]}}{d \sqrt{\tan [c+d x]}}$$

Result (type 4, 4869 leaves):

$$\frac{2 A \cos [c+d x] \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x])}{d (A \cos [c+d x]+B \sin [c+d x]) \sqrt{\tan [c+d x]}} +$$

$$\left( 4 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \cos [c+d x] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \right.$$

$$\left. i (A b+a B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b) (A+i B) \right.$$

$$\operatorname{EllipticPi}\left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b) \right.$$

$$\left. (A-i B) \operatorname{EllipticPi}\left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \left( \frac{A b \csc [c+d x] \sqrt{\sec [c+d x]} \sqrt{\tan [c+d x]}}{2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \right.$$

$$\frac{a B \csc [c+d x] \sqrt{\sec [c+d x]} \sqrt{\tan [c+d x]}}{2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} +$$

$$\frac{A b \cos [2 (c+d x)] \csc [c+d x] \sqrt{\sec [c+d x]} \sqrt{\tan [c+d x]}}{2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} +$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \frac{a B \cos [2 (c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} - \\
 & \frac{a A \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sin [2 (c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \\
 & \frac{b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sin [2 (c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \Big) \\
 & \sqrt{a+b \operatorname{Tan}[c+d x]} (A+B \operatorname{Tan}[c+d x]) \Big) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \cos [c+d x]+b \sin [c+d x]) (A \cos [c+d x]+B \sin [c+d x]) \right. \\
 & \left. - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \operatorname{Tan}[c+d x]^{3/2}} \right. \\
 & \left. 2 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2} (c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2} (c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \left( i (A b+a B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c+d x)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \\
 & \left. \left. (a+i b) (A+i B) \operatorname{EllipticPi}\left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c+d x)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b) (A-i B) \right.
 \end{aligned}
 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec}[c + d x]^{5/2} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) \\
 & \left( i (A b + a B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec}[c + d x]} \right) / \\
 & \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \right) \\
 & \left( \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\tan[c + d x]} \right) - \left( a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( i (A b + a B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a + i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right]\right], \\
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a - i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\operatorname{Sec}[c + d x]} \Bigg/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]} \sqrt{\operatorname{Tan}[c + d x]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}} \\
 & 3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( i (A b + a B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right]\right], \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a - i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} (a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx])^{3/2} \sqrt{\operatorname{Tan} [c+dx]}}} \\
 & 2 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & \left. (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2+b^2})}{a} \right], \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a - i b) (A - i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c+dx]} (b \operatorname{Cos} [c+dx] - a \operatorname{Sin} [c+dx]) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}}} \\
 & 4 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \quad i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B) \\
 & \quad \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} +}{1} \\
 & \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}} \\
 & \left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \quad (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \quad \quad i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B) \\
 & \quad \quad \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} +
 \end{aligned}$$



$$\begin{aligned}
 & \left( 4 \cos \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \sqrt{\sec [c + d x]} \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A b + a B) \sec \left[ \frac{1}{2} (c + d x) \right] \right)^2 / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right] \right)^{3/2} \right) + \\
 & \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \sec \left[ \frac{1}{2} (c + d x) \right] \right)^2 / \left( 4 \left( 1 - i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \right) \\
 & \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right] \right)^{3/2} - \\
 & \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \sec \left[ \frac{1}{2} (c + d x) \right] \right)^2 / \left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \right) \\
 & \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right] \right)^{3/2} \\
 & \tan \left[ \frac{1}{2} (c + d x) \right] \right)^{3/2} / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right. \\
 & \left. \sqrt{\tan [c + d x]} \right) \left. \sqrt{\tan [c + d x]} \right)
 \end{aligned}$$

**Problem 431:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x])}{\tan [c + d x]^{5/2}} dx$$

Optimal (type 3, 199 leaves, 9 steps):

$$\frac{\sqrt{i a - b} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} + \frac{\sqrt{i a + b} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \frac{2 A \sqrt{a + b \tan[c + d x]}}{3 d \tan[c + d x]^{3/2}} - \frac{2 (A b + 3 a B) \sqrt{a + b \tan[c + d x]}}{3 a d \sqrt{\tan[c + d x]}}$$

Result (type 4, 4932 leaves):

$$\begin{aligned} & - \left( 4 i \cos\left[\frac{1}{2}(c + d x)\right]^2 \cos[c + d x] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\ & \left( (a A - b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\ & (a + i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\ & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b) (A - i B) \\ & \left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\ & \tan\left[\frac{1}{2}(c + d x)\right]^{3/2} \left( -\frac{a A \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \right. \\ & \frac{b B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \\ & \left. \frac{(a A \cos[2(c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} + \frac{(b B \cos[2(c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} - \right. \\ & \left. \frac{(a b \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sin[2(c + d x)] \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} - \right. \\ & \left. \frac{(a B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sin[2(c + d x)] \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} \right) \end{aligned}$$

$$\left. \left( 2 \sqrt{a \cos[c+dx] + b \sin[c+dx]} \right) \sqrt{a+b \tan[c+dx]} (A+B \tan[c+dx]) \right/$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \cos[c+dx] + b \sin[c+dx]) (A \cos[c+dx] + B \sin[c+dx]) \right.$$

$$\left. \left( \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \tan[c+dx]^{3/2}} \right. \right.$$

$$\left. \left. 2 i \cos\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}}\right] \right. \right.$$

$$\left. \left( (aA-bB) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \right.$$

$$\left. (a+ib)(A+iB) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-ib)(A-ib) \right. \right.$$

$$\left. \left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right) \right)$$

$$\operatorname{Sec}[c+dx]^{5/2} \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} + \left( i a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right)$$

$$\left( (a A - b B) \operatorname{EllipticF}\left[\operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a + \operatorname{i} b) (A + \operatorname{i} B) \operatorname{EllipticPi}\left[-\frac{\operatorname{i}(b+\sqrt{a^2+b^2})}{a}, \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a - \operatorname{i} b) (A - \operatorname{i} B) \operatorname{EllipticPi}\left[\frac{\operatorname{i}(b+\sqrt{a^2+b^2})}{a}, \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\operatorname{Sec}[c+dx]} \Bigg) /$$

$$\left( (b - \sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right.$$

$$\left. \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \sqrt{\operatorname{Tan}[c+dx]} \right) + \left( \operatorname{i} a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right.$$

$$\left( (a A - b B) \operatorname{EllipticF}\left[\operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a + \operatorname{i} b) (A + \operatorname{i} B) \operatorname{EllipticPi}\left[-\frac{\operatorname{i}(b+\sqrt{a^2+b^2})}{a}, \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a - \operatorname{i} b) (A - \operatorname{i} B) \operatorname{EllipticPi}\left[\frac{\operatorname{i}(b+\sqrt{a^2+b^2})}{a}, \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\begin{aligned}
 & \left( \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \sqrt{\operatorname{Sec} [c+dx]} \Big/ \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\operatorname{Tan} [c+dx]} \right) - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}} \\
 & 3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( (aA-bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} + \\
 & \left( 1 / \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx])^{3/2} \sqrt{\operatorname{Tan} [c+dx]} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Im} \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a A - b B) \operatorname{EllipticF} \left[ \operatorname{Im} \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A - i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sqrt{\operatorname{Sec} [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}} \\
 & 4 \operatorname{Im} \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a A - b B) \operatorname{EllipticF} \left[ \operatorname{Im} \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A - i B)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}} \\
 & 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a A - b B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A - i B) \\
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sec [c + d x]^{3/2} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}} \\
 & 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\sec [c+d x]} \left( - \left( \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a A-b B) \sec \left[ \frac{1}{2}(c+d x) \right]^2 \right) / \right. \right. \\
 & \left. \left( 4 \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \right) \right) + \\
 & \left( i(a+i b) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \sec \left[ \frac{1}{2}(c+d x) \right]^2 \right) / \left( 4 \left( 1-i \cot \left[ \frac{1}{2}(c+d x) \right] \right) \right. \\
 & \left. \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \right) + \\
 & \left( i(a-i b) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A-i B) \sec \left[ \frac{1}{2}(c+d x) \right]^2 \right) / \\
 & \left( 4 \left( 1+i \cot \left[ \frac{1}{2}(c+d x) \right] \right) \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \left. \left. \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \right) \right) \right) \left. \left. \left. \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \sqrt{\tan [c+d x]} \right) \right) \right) + \\
 & \left( \cos [c+d x] \left( \frac{2 A}{3} - \frac{2(A b \cos [c+d x]+3 a B \cos [c+d x]) \operatorname{Csc}[c+d x]}{3 a} - \right. \right. \\
 & \left. \left. \frac{2}{3} A \operatorname{Csc}[c+d x]^2 \right) \right. \\
 & \left. \left( A + \sqrt{\tan [c+d x]} \sqrt{a+b \tan [c+d x]} \right. \right. \\
 & \left. \left. B \tan [c+d x] \right) \right) / \\
 & (d(A \cos [c+d x]+B \sin [c+d x]))
 \end{aligned}$$

**Problem 432:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x])}{\tan [c+d x]^{7 / 2}} d x$$



Optimal (type 3, 250 leaves, 10 steps):

$$\frac{\sqrt{i a - b} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \frac{\sqrt{i a + b} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \frac{2 A \sqrt{a + b \tan[c + d x]}}{5 d \tan[c + d x]^{5/2}} - \frac{2 (A b + 5 a B) \sqrt{a + b \tan[c + d x]}}{15 a d \tan[c + d x]^{3/2}} + \frac{2 (15 a^2 A + 2 A b^2 - 5 a b B) \sqrt{a + b \tan[c + d x]}}{15 a^2 d \sqrt{\tan[c + d x]}}$$

Result (type 4, 4972 leaves):

$$\begin{aligned} & - \left( 4 \cos\left[\frac{1}{2}(c + d x)\right]^2 \cos[c + d x] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\ & \left( i (A b + a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\ & (a + i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\ & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a - i b) (A - i B) \\ & \left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\ & \tan\left[\frac{1}{2}(c + d x)\right]^{3/2} \left( -\frac{A b \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \right. \\ & \frac{a B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \\ & \left. \frac{(A b \cos[2(c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} - \frac{(a B \cos[2(c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} + \right. \end{aligned}$$

$$\left( \frac{a A \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}\left[2(c+d x)\right] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} - \frac{b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}\left[2(c+d x)\right] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} \right) \sqrt{a+b \operatorname{Tan}[c+d x]} (A+B \operatorname{Tan}[c+d x]) \Big/$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]) (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right.$$

$$\left( \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \operatorname{Tan}[c+d x]^{3/2}} \right.$$

$$2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( i (A b+a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+i b) (A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right.$$

$$i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a-i b) (A-i B)$$

$$\left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)$$

$$\begin{aligned}
 & \text{Sec}[c+d x]^{5/2} \text{Tan}\left[\frac{1}{2}(c+d x)\right]^{3/2} + \left( a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \left( \text{I} (A b+a B) \text{EllipticF}\left[\text{I} \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \right. \\
 & \left. \left. (a+\text{I} b)(A+\text{I} B) \text{EllipticPi}\left[-\frac{\text{I}(b+\sqrt{a^2+b^2})}{a}, \text{I} \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a-\text{I} b)(A-\text{I} B) \text{EllipticPi}\left[\frac{\text{I}(b+\sqrt{a^2+b^2})}{a}, \text{I} \right. \right. \\
 & \left. \left. \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right) \sqrt{\text{Sec}[c+d x]} \Big/ \\
 & \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \text{Cos}[c+d x]+b \text{Sin}[c+d x]} \right. \\
 & \left. \sqrt{\text{Tan}\left[\frac{1}{2}(c+d x)\right]} \sqrt{\text{Tan}[c+d x]} \right) + \left( a \sqrt{1+\frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \left( \text{I} (A b+a B) \text{EllipticF}\left[\text{I} \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \right. \\
 & \left. \left. (a+\text{I} b)(A+\text{I} B) \text{EllipticPi}\left[-\frac{\text{I}(b+\sqrt{a^2+b^2})}{a}, \text{I} \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] + (a - i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \\
 & \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Big] / \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\operatorname{Tan} [c + d x]} \right) - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}} \\
 & 3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right] \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right] \right] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} +
 \end{aligned}$$

$$\left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]}} \right)$$

$$2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\frac{\sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}}$$

$$4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a-i b) (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \frac{\sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2}}{1} - \\
 & \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{1} \\
 & 2 \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & \left. (a+i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b) (A-i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \frac{\operatorname{Sec}[c+d x]^{3/2} \operatorname{Sin}[c+d x] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2}}{1} - \\
 & \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{1}
 \end{aligned}$$

$$\begin{aligned}
 & 4 \cos\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\sec[c+dx]} \left( \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (Ab+aB) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) + \right. \\
 & \left. \left( i(a+ib) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+iB) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( 1-i \cot\left[\frac{1}{2}(c+dx)\right] \right) \right) \right. \\
 & \left. \left. \sqrt{\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) - \right. \\
 & \left. \left( i(a-ib) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A-ib) \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \right. \\
 & \left. \left( 4 \left( 1+i \cot\left[\frac{1}{2}(c+dx)\right] \right) \sqrt{\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \right) \right) \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \sqrt{\tan[c+dx]} \right) + \\
 & \left( \cos[c+dx] \left( \frac{2(Ab+5aB)}{15a} + \frac{1}{15a^2} 2(18a^2 A \cos[c+dx] + 2A^2 b^2 \cos[c+dx] - 5abB \cos[c+dx]) \right. \right. \\
 & \left. \left. \frac{\csc[c+dx] - 2(Ab+5aB) \csc[c+dx]^2}{15a} - \frac{2}{5} A \cot[c+dx] \right. \right. \\
 & \left. \left. \csc[c+dx]^2 \right) \right. \\
 & \left. \left( \sqrt{\tan[c+dx]} \sqrt{a+b \tan[c+dx]} \right. \right. \\
 & \left. \left. (A + B \tan[c+dx]) \right) / \right. \\
 & \left. (d(A \cos[c+dx] + B \sin[c+dx])) \right)
 \end{aligned}$$

Problem 433: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x])}{\tan [c + d x]^{9/2}} dx$$

Optimal (type 3, 314 leaves, 11 steps):

$$\frac{\sqrt{i a - b} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right]}{d} - \frac{\sqrt{i a + b} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right]}{d} - \frac{2 A \sqrt{a + b \tan [c + d x]}}{7 d \tan [c + d x]^{7/2}} - \frac{2 (A b + 7 a B) \sqrt{a + b \tan [c + d x]}}{35 a d \tan [c + d x]^{5/2}} + \frac{2 (35 a^2 A + 4 A b^2 - 7 a b B) \sqrt{a + b \tan [c + d x]}}{105 a^2 d \tan [c + d x]^{3/2}} + \frac{2 (35 a^2 A b - 8 A b^3 + 105 a^3 B + 14 a b^2 B) \sqrt{a + b \tan [c + d x]}}{105 a^3 d \sqrt{\tan [c + d x]}}$$

Result (type 4, 5051 leaves):

$$\left( 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \cos [c + d x] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\ \left. (a A - b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A + i B) \right. \\ \left. \operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) \right. \\ \left. (A - i B) \operatorname{EllipticPi}\left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\ \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \left( \frac{a A \csc [c + d x] \sqrt{\sec [c + d x]} \sqrt{\tan [c + d x]}}{2 \sqrt{a \cos [c + d x] + b \sin [c + d x]}} - \right.$$



$$\begin{aligned}
 & \frac{b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} + \\
 & \frac{a A \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} - \\
 & \frac{b B \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} + \\
 & \frac{A b \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} + \\
 & \left. \frac{a B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} \right) \\
 & \left. \sqrt{a+b \operatorname{Tan}[c+d x]} (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]) (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right. \\
 & \left. - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \operatorname{Tan}[c+d x]^{3/2}} \right. \\
 & \left. 2 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \left( (a A-b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \right. \\
 & \left. (a+i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-i b)(A-i B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec}[c + d x]^{5/2} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) \\
 & \left( (a A - b B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec}[c + d x]} \right) / \\
 & \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \right) \\
 & \left( \sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\text{Tan}[c + d x]} \right) - \left( i a \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( (a A - b B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$(a + i b) (A + i B) \text{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right]\right],$$

$$\frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}] - (a - i b) (A - i B) \text{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a},$$

$$i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\text{Sec}[c + d x]} \Bigg/$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\ \left. \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]} \sqrt{\text{Tan}[c + d x]} \right) +$$

1

$$\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\text{Tan}[c + d x]}$$

$$3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( (a A - b B) \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) (A + i B)$$

$$\text{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a - i b) (A - i B) \text{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \sqrt{\sec [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} -$$


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$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]}}$$

$$2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( (a A - b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A + i B) \right.$$

$$\left. \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$\left. (a - i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right.$$

$$\left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} -$$


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$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}} 4 i \cos \left[ \frac{1}{2} (c + d x) \right]$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( (aA - bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+ib) (A+ib) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$(a-ib) (A-ib) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right],$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} +$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}} - 2i \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( (aA - bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+ib) (A+ib) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$(a-ib) (A-ib) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \left[ \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x] \text{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} + \right.$$

$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\text{Tan}[c + d x]}} 4 i \text{Cos}\left[\frac{1}{2}(c + d x)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}}$$

$$\sqrt{\text{Sec}[c + d x]} \left( - \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a A - b B) \text{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \right.$$

$$\left. \left( 4 \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \right) \right) +$$

$$\left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \text{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \left( 4 \left( 1 - i \text{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \right.$$

$$\left. \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \right) +$$

$$\left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \text{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \text{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left. \text{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \right) \right) \left. \text{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \sqrt{\text{Tan}[c + d x]} \right) +$$

$$\left( \text{Cos}[c + d x] \left( - \frac{2 (50 a^2 A + 4 A b^2 - 7 a b B)}{105 a^2} + \frac{1}{105 a^3} 4 (19 a^2 A b \text{Cos}[c + d x] - \right. \right.$$

$$\left. \left. 4 A b^3 \text{Cos}[c + d x] + 63 a^3 B \text{Cos}[c + d x] + 7 a b^2 B \text{Cos}[c + d x] \right) \right)$$

$$\begin{aligned} & \text{Csc}[c+dx] + \frac{2(65a^2A + 4Ab^2 - 7abB)\text{Csc}[c+dx]^2}{105a^2} - \\ & \frac{2(Ab\text{Cos}[c+dx] + 7aB\text{Cos}[c+dx])\text{Csc}[c+dx]^3}{35a} - \frac{2}{7}A\text{Csc}[c+dx]^4 \Big) \\ & \sqrt{\text{Tan}[c+dx]} \sqrt{a+b\text{Tan}[c+dx]} \\ & (A+B\text{Tan}[c+dx]) \Big) / \\ & (d(A\text{Cos}[c+dx] + B\text{Sin}[c+dx])) \end{aligned}$$

**Problem 434: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \text{Tan}[c+dx]^{3/2} (a+b\text{Tan}[c+dx])^{3/2} (A+B\text{Tan}[c+dx]) dx$$

Optimal (type 3, 323 leaves, 15 steps):

$$\begin{aligned} & \frac{(ia-b)^{3/2} (A+iB) \text{ArcTan}\left[\frac{\sqrt{ia-b}\sqrt{\text{Tan}[c+dx]}}{\sqrt{a+b\text{Tan}[c+dx]}}\right]}{d} + \\ & \frac{(6a^2Ab - 16Ab^3 - a^3B - 24a^2b^2B) \text{ArcTanh}\left[\frac{\sqrt{b}\sqrt{\text{Tan}[c+dx]}}{\sqrt{a+b\text{Tan}[c+dx]}}\right]}{8b^{3/2}d} + \\ & \frac{(ia+b)^{3/2} (A-iB) \text{ArcTanh}\left[\frac{\sqrt{ia+b}\sqrt{\text{Tan}[c+dx]}}{\sqrt{a+b\text{Tan}[c+dx]}}\right]}{d} + \\ & \frac{(6aAb - a^2B - 8b^2B) \sqrt{\text{Tan}[c+dx]} \sqrt{a+b\text{Tan}[c+dx]}}{8bd} + \\ & \frac{(6Ab - aB) \sqrt{\text{Tan}[c+dx]} (a+b\text{Tan}[c+dx])^{3/2}}{12bd} + \frac{B \sqrt{\text{Tan}[c+dx]} (a+b\text{Tan}[c+dx])^{5/2}}{3bd} \end{aligned}$$

Result (type 4, 122510 leaves): Display of huge result suppressed!

**Problem 435: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\text{Tan}[c+dx]} (a+b\text{Tan}[c+dx])^{3/2} (A+B\text{Tan}[c+dx]) dx$$

Optimal (type 3, 268 leaves, 14 steps):

$$\frac{(a + i b)^2 (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right] + (12 a A b + 3 a^2 B - 8 b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{\sqrt{i a - b} d} + \frac{(i a + b)^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} + \frac{(4 A b + 5 a B) \sqrt{\operatorname{Tan}[c + d x]} \sqrt{a + b \operatorname{Tan}[c + d x]}}{4 d} + \frac{b B \operatorname{Tan}[c + d x]^{3/2} \sqrt{a + b \operatorname{Tan}[c + d x]}}{2 d}$$

Result (type 4, 106626 leaves): Display of huge result suppressed!

**Problem 436: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x])}{\sqrt{\operatorname{Tan}[c + d x]}} dx$$

Optimal (type 3, 204 leaves, 13 steps):

$$-\frac{(i a - b)^{3/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} + \frac{\sqrt{b} (2 A b + 3 a B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} - \frac{(i a + b)^{3/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} + \frac{b B \sqrt{\operatorname{Tan}[c + d x]} \sqrt{a + b \operatorname{Tan}[c + d x]}}{d}$$

Result (type 4, 96488 leaves): Display of huge result suppressed!

**Problem 437: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x])}{\operatorname{Tan}[c + d x]^{3/2}} dx$$

Optimal (type 3, 209 leaves, 13 steps):

$$-\frac{(a + i b)^2 (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{\sqrt{i a - b} d} + \frac{2 b^{3/2} B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} - \frac{(i a + b)^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} - \frac{2 a A \sqrt{a + b \operatorname{Tan}[c + d x]}}{d \sqrt{\operatorname{Tan}[c + d x]}}$$

Result (type 4, 86483 leaves): Display of huge result suppressed!



Problem 438: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x])}{\tan [c + d x]^{5/2}} dx$$

Optimal (type 3, 196 leaves, 9 steps):

$$\frac{(i a - b)^{3/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right]}{d} + \frac{(i a + b)^{3/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right]}{d} - \frac{2 a A \sqrt{a + b \tan [c + d x]}}{3 d \tan [c + d x]^{3/2}} - \frac{2 (4 A b + 3 a B) \sqrt{a + b \tan [c + d x]}}{3 d \sqrt{\tan [c + d x]}}$$

Result (type 4, 5254 leaves):

$$\begin{aligned} & - \left( \left( 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \cos [c + d x]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \right. \\ & \left. \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\ & (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\ & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \\ & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\ & \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \left( -\frac{a^2 A \csc [c + d x] \sqrt{\sec [c + d x]} \sqrt{\tan [c + d x]}}{2 \sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \right. \\ & \left. \frac{A b^2 \csc [c + d x] \sqrt{\sec [c + d x]} \sqrt{\tan [c + d x]}}{2 \sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \right) \end{aligned}$$

$$\begin{aligned}
 & \frac{a b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} - \\
 & \left( \frac{\left( a^2 A \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]} \right)}{\left( 2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \right)} + \right. \\
 & \left( \frac{A b^2 \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left( 2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \right)} + \left( a b B \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \right. \right. \\
 & \left. \left. \frac{\sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left( \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \right)} - \right. \right. \\
 & \left. \left( \frac{A A b \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left( \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \right)} - \left( \frac{a^2 B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \right. \right. \right. \\
 & \left. \left. \left. \frac{\operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left( 2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \right)} + \right. \right. \\
 & \left. \left. \left( \frac{b^2 B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left( 2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \right)} \right) \right) \right) \\
 & \left. \left. \left. \left( 2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \right) \right) \right) (a+b \operatorname{Tan}[c+d x])^{3/2} (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2 (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right. \\
 & \left. \left( \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \operatorname{Tan}[c+d x]^{3/2}} \right. \right. \\
 & \left. \left. 2 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \right. \\
 & \left. \left( (a^2 A-A b^2-2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \right. \\
 & \left. \left. (a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-ib)^2 (A-ib) \\
 & \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \operatorname{Sec}[c+dx]^{5/2} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} + \left( i a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \\
 & \left. \left. (a+ib)^2 (A+ib) \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-ib)^2 (A-ib) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec}[c+dx]} \right) / \\
 & \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right) \\
 & \left. \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\operatorname{Tan}[c+dx]} \right) + \left( i a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \right)
 \end{aligned}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+ib)^2 (A+iB) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-ib)^2 (A-ib) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\operatorname{Sec}[c+dx]} \right) /$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \sqrt{\operatorname{Tan}[c+dx]} \right) -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}$$

$$3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+ib)^2 (A+iB) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} - (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \\
 & \left. \sqrt{\sec [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} + \left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]}} \right) \right. \\
 & 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}} \\
 & 4 i \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right]}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}\right],$$

$$i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-i b)^2 (A-i B)$$

$$\left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}\right], i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)$$

$$\frac{\sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} - 1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}$$

$$2 i \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right]}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}\right],$$

$$i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-i b)^2 (A-i B)$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\text{Tan}[c + d x]}} \\
 & 4 i \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \sqrt{\text{Sec}[c + d x]} \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^2 A - A b^2 - 2 a b B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right. \right. \\
 & \left. \left. \left( 4 \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \right) + \\
 & \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 - i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 + i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left. \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \left( \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{\text{Tan}[c + d x]} \right) \right) + \\
 & \left( \text{Cos}[c + d x]^2 \left( \frac{2 a A}{3} - \frac{2}{3} (4 A b \text{Cos}[c + d x] + 3 a B \text{Cos}[c + d x]) \text{Csc}[c + d x] - \right. \right.
 \end{aligned}$$

$$\frac{\frac{2}{3} a A \operatorname{Csc}[c+d x]^2}{\sqrt{\operatorname{Tan}[c+d x]} (a+b \operatorname{Tan}[c+d x])^{3/2} (A+B \operatorname{Tan}[c+d x])} / (d (a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]) (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]))$$

**Problem 439: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+b \operatorname{Tan}[c+d x])^{3/2} (A+B \operatorname{Tan}[c+d x])}{\operatorname{Tan}[c+d x]^{7/2}} dx$$

Optimal (type 3, 259 leaves, 10 steps):

$$\frac{(a+i b)^2 (i A-B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+b \operatorname{Tan}[c+d x]}}\right]}{\sqrt{i a-b} d} + \frac{(i a+b)^{3/2} (i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a-b} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+b \operatorname{Tan}[c+d x]}}\right]}{d} - \frac{2 a A \sqrt{a+b \operatorname{Tan}[c+d x]}}{5 d \operatorname{Tan}[c+d x]^{5/2}} - \frac{2 (6 A b+5 a B) \sqrt{a+b \operatorname{Tan}[c+d x]}}{15 d \operatorname{Tan}[c+d x]^{3/2}} + \frac{2 (15 a^2 A-3 A b^2-20 a b B) \sqrt{a+b \operatorname{Tan}[c+d x]}}{15 a d \sqrt{\operatorname{Tan}[c+d x]}}$$

Result (type 4, 5302 leaves):

$$- \left( \left( 4 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \operatorname{Cos}[c+d x]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\right) \left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i (b+\sqrt{a^2+b^2})}{a}\right], \right.$$



$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a-i b)^2 (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} \left( - \frac{a A b \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}}{\sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}} - \right. \\
 & \quad \frac{a^2 B \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}}{2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}} + \\
 & \quad \frac{b^2 B \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}}{2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}} - \\
 & \quad \left. \frac{(a A b \operatorname{Cos} [2 (c+dx)] \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}) / (\sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}) - (a^2 B \operatorname{Cos} [2 (c+dx)] \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}) / (2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})}{(2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})} + \right. \\
 & \quad \frac{(b^2 B \operatorname{Cos} [2 (c+dx)] \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}) / (2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})}{(2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})} + \\
 & \quad \frac{(a^2 A \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \operatorname{Sin} [2 (c+dx)] \sqrt{\operatorname{Tan} [c+dx]}) / (2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})}{(2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})} - \\
 & \quad \frac{(A b^2 \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \operatorname{Sin} [2 (c+dx)] \sqrt{\operatorname{Tan} [c+dx]}) / (2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})}{(2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})} - \\
 & \quad \left. \frac{(a b B \operatorname{Csc} [c+dx] \sqrt{\operatorname{Sec} [c+dx]} \operatorname{Sin} [2 (c+dx)] \sqrt{\operatorname{Tan} [c+dx]}) / (2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})}{(2 \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]})} \right) \left( a+b \operatorname{Tan} [c+dx] \right)^{3/2} (A+B \operatorname{Tan} [c+dx]) \left. \right) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx])^2 (A \operatorname{Cos} [c+dx] + B \operatorname{Sin} [c+dx]) \right)
 \end{aligned}$$

$$\left( \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \tan [c+d x]^{3/2}} \right.$$

$$2 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \left. \right] + (a-i b)^2 (A-i B)$$

$$\operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \left. \right)$$

$$\sec [c+d x]^{5/2} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} + a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}}$$

$$\left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] + (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \\
 & \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Big/ \\
 & \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right. \\
 & \left. \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\operatorname{Tan} [c + d x]} \right) + \left( a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] + (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Big/ \right. \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\operatorname{Tan} [c + d x]} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}} \\
 & 3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right. \\
 & (a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right],\right. \\
 & \left.\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(a-i b)^2 (A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right],\right. \\
 & \left.\left.\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}+ \\
 & \left.1 / \left(\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \cos [c+d x]+b \sin [c+d x])^{3 / 2} \sqrt{\tan [c+d x]}\right)\right) \\
 & 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right. \\
 & (a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a},\right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a-i b)^2 (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \sqrt{\operatorname{Sec} [c+dx]} (b \operatorname{Cos} [c+dx] - a \operatorname{Sin} [c+dx]) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}} \\
 & 4 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a-i b)^2 (A-i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c+dx]} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}}
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right. \\
 & (a+i b)^2(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a},\right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(a-i b)^2(A-i B) \\
 & \left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \\
 & \frac{\operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2}}{1}- \\
 & \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{1} \\
 & 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\operatorname{Sec}[c+dx]} \left( \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (2 a A b+a^2 B-b^2 B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) + \right. \\
 & \left. \left( i (a+i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 \left( 1 - i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) - \left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left( \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{\tan [c + d x]} \right) + \\
 & \left( \cos [c + d x]^2 \left( \frac{2}{15} (6 A b + 5 a B) + \frac{1}{15 a} 2 (18 a^2 A \cos [c + d x] - 3 A b^2 \cos [c + d x] - \right. \right. \\
 & \quad \left. \left. 20 a b B \cos [c + d x]) \csc [c + d x] - \frac{2}{15} (6 A b + 5 a B) \csc [c + d x]^2 - \frac{2}{5} a A \cot [c + d x] \csc [c + d x]^2 \right) \right. \\
 & \quad \left. \sqrt{\tan [c + d x]} (a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x]) \right) / \\
 & \left( d (a \cos [c + d x] + b \sin [c + d x]) (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

**Problem 440: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x])}{\tan [c + d x]^{9/2}} dx$$

Optimal (type 3, 311 leaves, 11 steps):

$$\begin{aligned}
 & \frac{(i a - b)^{3/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \\
 & \frac{(i a + b)^{3/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \frac{2 a A \sqrt{a + b \tan[c + d x]}}{7 d \tan[c + d x]^{7/2}} - \\
 & \frac{2 (8 A b + 7 a B) \sqrt{a + b \tan[c + d x]}}{35 d \tan[c + d x]^{5/2}} + \frac{2 (35 a^2 A - 3 A b^2 - 42 a b B) \sqrt{a + b \tan[c + d x]}}{105 a d \tan[c + d x]^{3/2}} + \\
 & \frac{2 (140 a^2 A b + 6 A b^3 + 105 a^3 B - 21 a b^2 B) \sqrt{a + b \tan[c + d x]}}{105 a^2 d \sqrt{\tan[c + d x]}}
 \end{aligned}$$

Result (type 4, 5373 leaves):

$$\begin{aligned}
 & \left( 4 i \cos\left[\frac{1}{2}(c + d x)\right]^2 \cos^2[c + d x]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 (A - i B) \\
 & \left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \tan\left[\frac{1}{2}(c + d x)\right]^{3/2} \left( \frac{a^2 A \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \right. \\
 & \frac{A b^2 \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \\
 & \left. \frac{a b B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{\sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \right)
 \end{aligned}$$



$$\begin{aligned}
 & \frac{a^2 A \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\
 & \frac{A b^2 \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\
 & \frac{a b B \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \frac{a A b \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \frac{a^2 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\
 & \left. \frac{b^2 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) \\
 & \left. (a + b \operatorname{Tan}[c+dx])^{3/2} (A + B \operatorname{Tan}[c+dx]) \right) / \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2 (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right. \\
 & \left. - \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \operatorname{Tan}[c+dx]^{3/2}} \right. \\
 & \left. 2 \operatorname{I} \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[\operatorname{I} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. \left. (a + \operatorname{I} b)^2 (A + \operatorname{I} B) \operatorname{EllipticPi}\left[-\frac{\operatorname{I} (b + \sqrt{a^2 + b^2})}{a}\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-ib)^2 (A-ib) \\
 & \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \operatorname{Sec}[c+dx]^{5/2} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} - \left( i a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \\
 & \left. \left. (a+ib)^2 (A+ib) \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-ib)^2 (A-ib) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec}[c+dx]} \right) / \\
 & \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \right. \\
 & \left. \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\operatorname{Tan}[c+dx]} \right) - \left( i a \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \right)
 \end{aligned}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+d x]} \Bigg) /$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos} [c+d x]+b \operatorname{Sin} [c+d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]} \sqrt{\operatorname{Tan} [c+d x]} \right) +$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x]+b \operatorname{Sin} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]}}$$

$$3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} - (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]}} \\
 & 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}} \\
 & 4 i \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\frac{\sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}$$

$$2 i \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B)$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\text{Tan}[c + d x]}} \\
 & 4 i \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}} \\
 & \sqrt{\text{Sec}[c + d x]} \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^2 A - A b^2 - 2 a b B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right. \right. \\
 & \left. \left. \left( 4 \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \right) + \\
 & \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \\
 & \left. \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \\
 & \left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 + i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left. \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{\text{Tan}[c + d x]} \right) + \\
 & \left( \text{Cos}[c + d x]^2 \left( - \frac{2 (50 a^2 A - 3 A b^2 - 42 a b B)}{105 a} + \frac{1}{105 a^2} 2 (164 a^2 A b \text{Cos}[c + d x] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 A b^3 \cos [c+d x]+126 a^3 B \cos [c+d x]-21 a b^2 B \cos [c+d x]) \\
 & \operatorname{Csc}[c+d x]+\frac{2\left(65 a^2 A-3 A b^2-42 a b B\right) \operatorname{Csc}[c+d x]^2}{105 a}- \\
 & \frac{2}{35}\left(8 A b \cos [c+d x]+7 a B \cos [c+d x]\right) \operatorname{Csc}[c+d x]^3- \\
 & \frac{2}{7} a A \operatorname{Csc}[c+d x]^4) \\
 & \sqrt{\tan [c+d x]}(a+b \tan [c+d x])^{3 / 2} \\
 & (A+B \tan [c+d x]) \Big/ \\
 & (d(a \cos [c+d x]+b \sin [c+d x]) \\
 & (A \cos [c+d x]+B \sin [c+d x]))
 \end{aligned}$$

**Problem 441: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+b \tan [c+d x])^{3 / 2}(A+B \tan [c+d x])}{\tan [c+d x]^{11 / 2}} d x$$

Optimal (type 3, 382 leaves, 12 steps):

$$\begin{aligned}
 & \frac{(i a-b)^{3 / 2}(i A-B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d}- \\
 & \frac{(i a+b)^{3 / 2}(i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d}-\frac{2 a A \sqrt{a+b \tan [c+d x]}}{9 d \tan [c+d x]^{9 / 2}}- \\
 & \frac{2(10 A b+9 a B) \sqrt{a+b \tan [c+d x]}}{63 d \tan [c+d x]^{7 / 2}}+\frac{2\left(21 a^2 A-A b^2-24 a b B\right) \sqrt{a+b \tan [c+d x]}}{105 a d \tan [c+d x]^{5 / 2}}+ \\
 & \frac{2\left(126 a^2 A b+4 A b^3+105 a^3 B-9 a b^2 B\right) \sqrt{a+b \tan [c+d x]}}{315 a^2 d \tan [c+d x]^{3 / 2}}- \\
 & \frac{\left(2\left(315 a^4 A-63 a^2 A b^2+8 A b^4-420 a^3 b B-18 a b^3 B\right) \sqrt{a+b \tan [c+d x]}\right)}{\left(315 a^3 d \sqrt{\tan [c+d x]}\right)} \Big/
 \end{aligned}$$

Result (type 4, 5445 leaves):

$$\left(4 \cos \left[\frac{1}{2}(c+d x)\right]^2 \cos [c+d x]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\right) \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)^2 (A-i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} \left( \frac{a A b \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]}}{\sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} + \right.$$

$$\frac{a^2 B \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]}}{2 \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} -$$

$$\frac{b^2 B \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]}}{2 \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} +$$

$$\frac{a A b \operatorname{Cos} [2 (c+d x)] \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]}}{\sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} +$$

$$\frac{a^2 B \operatorname{Cos} [2 (c+d x)] \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]}}{2 \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} -$$

$$\frac{b^2 B \operatorname{Cos} [2 (c+d x)] \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]}}{2 \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} -$$

$$\frac{a^2 A \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \operatorname{Sin} [2 (c+d x)] \sqrt{\operatorname{Tan} [c+d x]}}{2 \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} +$$

$$\frac{A b^2 \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \operatorname{Sin} [2 (c+d x)] \sqrt{\operatorname{Tan} [c+d x]}}{2 \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} +$$

$$\left. \frac{a b B \operatorname{Csc} [c+d x] \sqrt{\operatorname{Sec} [c+d x]} \operatorname{Sin} [2 (c+d x)] \sqrt{\operatorname{Tan} [c+d x]}}{\sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} \right)$$



$$\left. (a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x]) \right\} /$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right.$$

$$\left. - \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \tan [c + d x]^{3/2}} \right.$$

$$\left. 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right.$$

$$\left. (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a} \right], \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^2 (A - i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a} \right], i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right)$$

$$\operatorname{Sec} [c + d x]^{5/2} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right.$$

$$\left( \begin{aligned} & i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \\ & (a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \\ & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)^2 (A-i B) \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\ & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec}[c+dx]} \right) / \\ & \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \right. \\ & \left. \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \sqrt{\operatorname{Tan}[c+dx]} \right) - \left( a \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right. \\ & \left. i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\ & (a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \\ & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)^2 (A-i B) \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \end{aligned} \right)$$

$$\begin{aligned}
 & \left( i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \sqrt{\operatorname{Sec} [c+dx]} \Big/ \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\operatorname{Tan} [c+dx]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}} \\
 & 3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx])^{3/2} \sqrt{\operatorname{Tan} [c+dx]}}
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i(2aAb+a^2B-b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+ib)^2 (A+iB) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-ib)^2 (A-ib) \right. \\
 & \left. \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \frac{\sqrt{\operatorname{Sec}[c+dx]} (b \operatorname{Cos}[c+dx] - a \operatorname{Sin}[c+dx]) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} - 1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}} \\
 & 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i(2aAb+a^2B-b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+ib)^2 (A+iB) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-ib)^2 (A-ib) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} +}{1} \\
 & \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}}{2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}} \\
 & \left( i (2 a A b + a^2 B - b^2 B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a + i b)^2 (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^2 (A - i B) \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \frac{\sec [c + d x]^{3/2} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} +}{4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}} \\
 & \frac{\sqrt{\sec [c + d x]} \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (2 a A b + a^2 B - b^2 B) \sec \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right)}{2}
 \end{aligned}$$

$$\begin{aligned}
 & \left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) + \\
 & \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \right) \\
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} - \\
 & \left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \right) \\
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \Bigg) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \Bigg) / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right. \\
 & \left. \sqrt{\operatorname{Tan}[c+dx]} \right) \Bigg) \sqrt{\operatorname{Tan}[c+dx]} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{d (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx])} \\
 & \operatorname{Cos}[c+dx]^2 \\
 & \left( - \frac{2 (176 a^2 A b + 4 A b^3 + 150 a^3 B - 9 a b^2 B)}{315 a^2} - \right. \\
 & \frac{1}{315 a^3} \\
 & 2 (413 a^4 A \operatorname{Cos}[c+dx] - 66 a^2 A b^2 \operatorname{Cos}[c+dx] + 8 A b^4 \operatorname{Cos}[c+dx] - \\
 & \quad 492 a^3 b B \operatorname{Cos}[c+dx] - 18 a b^3 B \operatorname{Cos}[c+dx]) \operatorname{Csc}[c+dx] + \\
 & \left. \frac{2 (226 a^2 A b + 4 A b^3 + 195 a^3 B - 9 a b^2 B) \operatorname{Csc}[c+dx]^2}{315 a^2} + \right. \\
 & \frac{1}{315 a} \\
 & 2 (133 a^2 A \operatorname{Cos}[c+dx] - 3 A b^2 \operatorname{Cos}[c+dx] - 72 a b B \operatorname{Cos}[c+dx]) \operatorname{Csc}[c+dx]^3 - \\
 & \left. \frac{2}{63} (10 A b + 9 a B) \operatorname{Csc}[c+dx]^4 - \right)
 \end{aligned}$$

$$\frac{2}{9} a A \cot [c+d x] \csc [c+d x]^4 \int \sqrt{\tan [c+d x]} (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) dx$$

**Problem 442: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \tan [c+d x]^{3/2} (a+b \tan [c+d x])^{5/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 397 leaves, 16 steps):

$$\begin{aligned} & -\frac{(i a-b)^{5/2} (i A-B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} + \frac{1}{64 b^{3/2} d} \\ & (40 a^3 A b-320 a A b^3-5 a^4 B-240 a^2 b^2 B+128 b^4 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]- \\ & \frac{(i a+b)^{5/2} (i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{d} + \frac{1}{64 b d} \\ & \frac{(40 a^2 A b-64 A b^3-5 a^3 B-112 a b^2 B) \sqrt{\tan [c+d x]} \sqrt{a+b \tan [c+d x]}+(40 a A b-5 a^2 B-48 b^2 B) \sqrt{\tan [c+d x]}(a+b \tan [c+d x])^{3/2}}{96 b d} + \\ & \frac{(8 A b-a B) \sqrt{\tan [c+d x]}(a+b \tan [c+d x])^{5/2}+B \sqrt{\tan [c+d x]}(a+b \tan [c+d x])^{7/2}}{24 b d} + \frac{B \sqrt{\tan [c+d x]}(a+b \tan [c+d x])^{7/2}}{4 b d} \end{aligned}$$

Result (type 4, 159271 leaves): Display of huge result suppressed!

**Problem 443: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\tan [c+d x]} (a+b \tan [c+d x])^{5/2} (A+B \tan [c+d x]) dx$$

Optimal (type 3, 316 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{(\sqrt{-1} a - b)^{5/2} (A + \sqrt{-1} B) \operatorname{ArcTan}\left[\frac{\sqrt{-1} a - b \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right]}{d} + \\
 & \frac{(30 a^2 A b - 16 A b^3 + 5 a^3 B - 40 a b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right]}{8 \sqrt{b} d} + \\
 & \frac{(\sqrt{-1} a + b)^{5/2} (A - \sqrt{-1} B) \operatorname{ArcTanh}\left[\frac{\sqrt{-1} a + b \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right]}{d} + \\
 & \frac{(14 a A b + 5 a^2 B - 8 b^2 B) \sqrt{\operatorname{Tan}[c+dx]} \sqrt{a+b \operatorname{Tan}[c+dx]}}{8 d} + \\
 & \frac{(2 A b + 3 a B) \sqrt{\operatorname{Tan}[c+dx]} (a+b \operatorname{Tan}[c+dx])^{3/2}}{4 d} + \frac{b B \operatorname{Tan}[c+dx]^{3/2} (a+b \operatorname{Tan}[c+dx])^{3/2}}{3 d}
 \end{aligned}$$

Result (type 4, 143376 leaves): Display of huge result suppressed!

**Problem 444: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+b \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx])}{\sqrt{\operatorname{Tan}[c+dx]}} dx$$

Optimal (type 3, 260 leaves, 14 steps):

$$\begin{aligned}
 & \frac{(\sqrt{-1} a - b)^{5/2} (\sqrt{-1} A - B) \operatorname{ArcTan}\left[\frac{\sqrt{-1} a - b \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right]}{d} + \\
 & \frac{\sqrt{b} (20 a A b + 15 a^2 B - 8 b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right]}{4 d} + \\
 & \frac{(\sqrt{-1} a + b)^{5/2} (\sqrt{-1} A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{-1} a + b \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right]}{d} + \\
 & \frac{b (4 A b + 7 a B) \sqrt{\operatorname{Tan}[c+dx]} \sqrt{a+b \operatorname{Tan}[c+dx]}}{4 d} + \frac{b B \sqrt{\operatorname{Tan}[c+dx]} (a+b \operatorname{Tan}[c+dx])^{3/2}}{2 d}
 \end{aligned}$$

Result (type 4, 133239 leaves): Display of huge result suppressed!

**Problem 445: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+b \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx])}{\operatorname{Tan}[c+dx]^{3/2}} dx$$



Optimal (type 3, 241 leaves, 14 steps):

$$\frac{(i a - b)^{5/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} +$$

$$\frac{b^{3/2} (2 A b + 5 a B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \frac{(i a + b)^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} +$$

$$\frac{b (2 a A + b B) \sqrt{\tan[c + d x]} \sqrt{a + b \tan[c + d x]}}{d} - \frac{2 a A (a + b \tan[c + d x])^{3/2}}{d \sqrt{\tan[c + d x]}}$$

Result (type 4, 123 092 leaves): Display of huge result suppressed!

**Problem 446: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x])}{\tan[c + d x]^{5/2}} dx$$

Optimal (type 3, 240 leaves, 14 steps):

$$-\frac{(i a - b)^{5/2} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} +$$

$$\frac{2 b^{5/2} B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \frac{(i a + b)^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} -$$

$$\frac{2 a (2 A b + a B) \sqrt{a + b \tan[c + d x]}}{d \sqrt{\tan[c + d x]}} - \frac{2 a A (a + b \tan[c + d x])^{3/2}}{3 d \tan[c + d x]^{3/2}}$$

Result (type 4, 113 126 leaves): Display of huge result suppressed!

**Problem 447: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x])}{\tan[c + d x]^{7/2}} dx$$

Optimal (type 3, 247 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{(\mathbf{i} a - b)^{5/2} (A + \mathbf{i} B) \operatorname{ArcTan}\left[\frac{\sqrt{\mathbf{i} a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} + \\
 & \frac{(\mathbf{i} a + b)^{5/2} (A - \mathbf{i} B) \operatorname{ArcTanh}\left[\frac{\sqrt{\mathbf{i} a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{d} - \frac{2 a (8 A b + 5 a B) \sqrt{a + b \operatorname{Tan}[c + d x]}}{15 d \operatorname{Tan}[c + d x]^{3/2}} + \\
 & \frac{2 (15 a^2 A - 23 A b^2 - 35 a b B) \sqrt{a + b \operatorname{Tan}[c + d x]}}{15 d \sqrt{\operatorname{Tan}[c + d x]}} - \frac{2 a A (a + b \operatorname{Tan}[c + d x])^{3/2}}{5 d \operatorname{Tan}[c + d x]^{5/2}}
 \end{aligned}$$

Result (type 4, 5580 leaves):

$$\begin{aligned}
 & - \left( \left( 4 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \operatorname{Cos}[c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right) \right. \\
 & \left( \mathbf{i} (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{EllipticF}\left[\mathbf{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + \mathbf{i} b)^3 (A + \mathbf{i} B) \operatorname{EllipticPi}\left[-\frac{\mathbf{i} (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. \mathbf{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a - \mathbf{i} b)^3 (A - \mathbf{i} B) \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{\mathbf{i} (b + \sqrt{a^2 + b^2})}{a}, \mathbf{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \left( - \frac{3 a^2 A b \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \right. \\
 & \frac{A b^3 \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \\
 & \frac{a^3 B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \\
 & \left. \frac{3 a b^2 B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{3 a^2 A b \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} + \right. \\
 & \left( \frac{A b^3 \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} - \frac{a^3 B \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x]}{\sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}} \right) / \left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2 + \\
 & \left( \frac{3 a b^2 B \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} + \right. \\
 & \left( \frac{a^3 A \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} - \right. \\
 & \left( \frac{3 a A b^2 \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} - \right. \\
 & \left( \frac{3 a^2 b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} + \right. \\
 & \left. \left. \left( \frac{b^3 B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)^2} \right) \right) \left( a+b \operatorname{Tan}[c+d x] \right)^{5/2} (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^3 (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \operatorname{Tan}[c+d x]^{3/2}} \right. \\
 & \left. 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \left( i \left( 3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B \right) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi}\left[ -\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a} \right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a - i b)^3 (A - i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \\
 & \operatorname{Sec} [c + d x]^{5/2} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^3 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \left. \sqrt{\operatorname{Sec} [c + d x]} \right) / \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\operatorname{Tan} [c + d x]} \right) +
 \end{aligned}$$

$$\left( a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\right) \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \right.$$

$$\operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B)$$

$$\operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] +$$

$$(a - i b)^3 (A - i B) \operatorname{EllipticPi}\left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec}[c+dx]} \Big/$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \sqrt{\operatorname{Tan}[c+dx]} \right) -$$


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$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}$$

$$3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}$$

$$\sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \right)$$

$$\begin{aligned}
 & \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+\text{i}b)^3 (A+\text{i}B) \\
 & \text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + \\
 & (a-\text{i}b)^3 (A-\text{i}B) \text{EllipticPi}\left[\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]} + \\
 & \left(1/\left(\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}(a\text{Cos}[c+dx]+b\text{Sin}[c+dx])^{3/2}\sqrt{\text{Tan}[c+dx]}\right)\right) \\
 & 2\text{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a\text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a\text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left(\text{i}(3a^2Ab-Ab^3+a^3B-3ab^2B)\text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+\text{i}b)^3 (A+\text{i}B)\text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a-\text{i}b)^3 (A-\text{i}B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} +}{1} \\
 & \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}} \\
 & 4 \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^3 (A - i B) \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} -}{1} \\
 & \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}} \\
 & 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\left( i(3a^2Ab - Ab^3 + a^3B - 3ab^2B) \right. \\
 & \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + ib)^3(A + iB) \\
 & \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \\
 & (a - ib)^3(A - iB) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \right) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}} 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\sqrt{\operatorname{Sec}[c+dx]} \\
 & \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (3a^2Ab - Ab^3 + a^3B - 3ab^2B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
 & \left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) + \\
 & \left( i(a + ib)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}(A + iB) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) /
 \end{aligned}$$



$$\begin{aligned}
 & \left( 4 \left( 1 - i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \left( i (a - i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \\
 & \left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left( \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{\tan [c + d x]} \right) + \\
 & \left( \cos [c + d x]^3 \left( \frac{2}{15} a (11 A b + 5 a B) + \frac{2}{15} (18 a^2 A \cos [c + d x] - 23 A b^2 \cos [c + d x] - \right. \right. \\
 & \quad \left. \left. 35 a b B \cos [c + d x]) \csc [c + d x] - \right. \right. \\
 & \quad \left. \frac{2}{15} a (11 A b + 5 a B) \csc [c + d x]^2 - \frac{2}{5} a^2 A \cot [c + d x] \csc [c + d x]^2 \right) \\
 & \quad \left. \sqrt{\tan [c + d x]} (a + b \tan [c + d x])^{5/2} \right. \\
 & \quad \left. (A + B \tan [c + d x]) \right) / \\
 & \left( d (a \cos [c + d x] + b \sin [c + d x])^2 \right. \\
 & \quad \left. (A \cos [c + d x] + B \sin [c + d x]) \right)
 \end{aligned}$$

**Problem 448: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x])}{\tan [c + d x]^{9/2}} dx$$

Optimal (type 3, 309 leaves, 11 steps):

$$\frac{(i a - b)^{5/2} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} + \frac{(i a + b)^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} -$$

$$\frac{2 a (10 A b + 7 a B) \sqrt{a + b \tan[c + d x]}}{35 d \tan[c + d x]^{5/2}} + \frac{2 (35 a^2 A - 45 A b^2 - 77 a b B) \sqrt{a + b \tan[c + d x]}}{105 d \tan[c + d x]^{3/2}} +$$

$$\frac{2 (245 a^2 A b - 15 A b^3 + 105 a^3 B - 161 a b^2 B) \sqrt{a + b \tan[c + d x]}}{105 a d \sqrt{\tan[c + d x]}} - \frac{2 a A (a + b \tan[c + d x])^{3/2}}{7 d \tan[c + d x]^{7/2}}$$

Result (type 4, 5641 leaves):

$$\left( 4 i \cos\left[\frac{1}{2}(c + d x)\right]^2 \cos[c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right.$$

$$\left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right) \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right)$$

$$\operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^3 (A + i B)$$

$$\operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^3$$

$$\left. (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]\right)$$

$$\tan\left[\frac{1}{2}(c + d x)\right]^{3/2} \left( \frac{a^3 A \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \right.$$

$$\frac{3 a A b^2 \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} -$$

$$\left. \frac{3 a^2 b B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \right)$$

$$\begin{aligned}
 & \frac{b^3 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \frac{a^3 A \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\
 & \left( \frac{3 a A b^2 \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) - \\
 & \left( \frac{3 a^2 b B \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) + \\
 & \frac{b^3 B \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \left( \frac{3 a^2 A b \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) - \\
 & \frac{A b^3 \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \frac{a^3 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\
 & \left( \frac{3 a b^2 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) / \\
 & \left. \left( 2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right) \right) (a+b \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) \Bigg/ \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right. \\
 & \left. - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \operatorname{Tan}[c+dx]^{3/2}} \right. \\
 & \left. 2 i \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right)
 \end{aligned}$$

$$\left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^3 (A+iB) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-ib)^3 (A-ib) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)$$

$$\operatorname{Sec}[c+dx]^{5/2} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} - \left( i a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right)$$

$$\left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^3 (A+iB) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-ib)^3 (A-ib) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)$$

$$\begin{aligned}
 & \left. \sqrt{\sec [c+d x]} \right) / \left( \left( b-\sqrt{a^2+b^2} \right) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) - \\
 & \left( i a \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \left( a^3 A-3 a A b^2-3 a^2 b B+b^3 B \right) \right. \\
 & \left. \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-(a+i b)^3(A+i B) \right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & \left. (a-i b)^3(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\sec [c+d x]} \right) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \left(b+\sqrt{a^2+b^2}\right) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}}
 \end{aligned}$$

$$\begin{aligned}
 & 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^3 (A - i B) \operatorname{EllipticPi}\left[ \right. \right. \\
 & \left. \left. \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \sqrt{\operatorname{Sec}[c + d x]} \\
 & \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]} - \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^{3/2} \sqrt{\operatorname{Tan}[c + d x]}} \\
 & 2 i \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^3 (A - i B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\text{Sec} [c + d x]} (b \text{Cos} [c + d x] - a \text{Sin} [c + d x]) \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\text{Tan} [c + d x]}} \\
 & 4 i \text{Cos} \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^3 (A - i B) \right) \\
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\text{Sec} [c + d x]} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\text{Tan} [c + d x]}} \\
 & 2 i \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \right. \\
 & \operatorname{EllipticF}\left[\operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + \operatorname{i} b)^3 (A + \operatorname{i} B) \\
 & \operatorname{EllipticPi}\left[-\frac{\operatorname{i}(b + \sqrt{a^2 + b^2})}{a}, \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \\
 & (a - \operatorname{i} b)^3 (A - \operatorname{i} B) \operatorname{EllipticPi}\left[\frac{\operatorname{i}(b + \sqrt{a^2 + b^2})}{a}, \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \right) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}\sqrt{\operatorname{Tan}[c+dx]}} 4 \operatorname{i} \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\sqrt{\operatorname{Sec}[c+dx]} \\
 & \left(-\left(\operatorname{i} \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}(a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
 & \left(4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2}\right) + \\
 & \left(\operatorname{i}(a + \operatorname{i} b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}(A + \operatorname{i} B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right) / \left(4 \left(1 - \operatorname{i} \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]\right)\right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \left( \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) + \right. \\
 & \left( i (a - i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \sqrt{\operatorname{Tan}[c+dx]} \right) + \\
 & \frac{1}{d (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2 (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx])} \\
 & \operatorname{Cos}[c+dx]^3 \\
 & \left( -\frac{2}{105} (50 a^2 A - 45 A b^2 - 77 a b B) + \right. \\
 & \frac{1}{105 a} \\
 & 2 (290 a^2 A b \operatorname{Cos}[c+dx] - 15 A b^3 \operatorname{Cos}[c+dx] + 126 a^3 B \operatorname{Cos}[c+dx] - 161 a b^2 B \operatorname{Cos}[c+dx]) \\
 & \operatorname{Csc}[c+dx] + \\
 & \frac{2}{105} (65 a^2 A - 45 A b^2 - 77 a b B) \operatorname{Csc}[c+dx]^2 - \\
 & \frac{2}{35} (15 a A b \operatorname{Cos}[c+dx] + 7 a^2 B \operatorname{Cos}[c+dx]) \operatorname{Csc}[c+dx]^3 - \\
 & \left. \frac{2}{7} a^2 A \operatorname{Csc}[c+dx]^4 \right) \\
 & \sqrt{\operatorname{Tan}[c+dx]} (a + b \operatorname{Tan}[c+dx])^{5/2} \\
 & (A + \\
 & B \operatorname{Tan}[c+dx])
 \end{aligned}$$

**Problem 449: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{Tan}[c + d x])^{5/2} (A + B \operatorname{Tan}[c + d x])}{\operatorname{Tan}[c + d x]^{11/2}} dx$$

Optimal (type 3, 378 leaves, 12 steps):

$$\frac{(i a - b)^{5/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] - (i a + b)^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{d} - \frac{2 a (4 A b + 3 a B) \sqrt{a + b \tan[c + d x]} + 2 (21 a^2 A - 25 A b^2 - 45 a b B) \sqrt{a + b \tan[c + d x]}}{21 d \tan[c + d x]^{7/2} + 105 d \tan[c + d x]^{5/2}} + \frac{2 (231 a^2 A b - 5 A b^3 + 105 a^3 B - 135 a b^2 B) \sqrt{a + b \tan[c + d x]}}{315 a d \tan[c + d x]^{3/2}} - \left(2 (315 a^4 A - 483 a^2 A b^2 - 10 A b^4 - 735 a^3 b B + 45 a b^3 B) \sqrt{a + b \tan[c + d x]}\right) / \left(315 a^2 d \sqrt{\tan[c + d x]}\right) - \frac{2 a A (a + b \tan[c + d x])^{3/2}}{9 d \tan[c + d x]^{9/2}}$$

Result (type 4, 5725 leaves):

$$\left(4 \cos\left[\frac{1}{2}(c + d x)\right]^2 \cos[c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right. \\ \left.\sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right] \left(i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a - i b)^3 (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]\right) \\ \tan\left[\frac{1}{2}(c + d x)\right]^{3/2} \left(\frac{3 a^2 A b \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \frac{A b^3 \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \right)$$

$$\left. \begin{aligned} & \frac{a^3 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\ & \frac{3 a b^2 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\ & \left( \frac{3 a^2 A b \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) - \\ & \frac{A b^3 \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\ & \frac{a^3 B \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\ & \left( \frac{3 a b^2 B \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) - \\ & \frac{a^3 A \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\ & \left( \frac{3 a A b^2 \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) + \\ & \left( \frac{3 a^2 b B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) - \\ & \left. \frac{b^3 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) \Bigg) / \\ & (a + b \operatorname{Tan}[c+dx])^{5/2} (A + B \operatorname{Tan}[c+dx]) \Bigg) / \end{aligned} \right.$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right. \\ \left. (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right. \\ \left. - \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \operatorname{Tan}[c+dx]^{3/2}} \right)$$

$$\begin{aligned}
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^3 (A+ib) \operatorname{EllipticPi}\left[-\frac{ib+\sqrt{a^2+b^2}}{a}\right], \right. \\
 & \left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a-ib)^3 (A-ib) \right. \\
 & \left. \operatorname{EllipticPi}\left[\frac{ib+\sqrt{a^2+b^2}}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right) \\
 & \operatorname{Sec}[c+dx]^{5/2} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} - \left( a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^3 (A+ib) \operatorname{EllipticPi}\left[-\frac{ib+\sqrt{a^2+b^2}}{a}\right], \right. \\
 & \left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a-ib)^3 (A-ib) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right. \\
 & \left. \sqrt{\text{Sec} [c + d x]} \right) / \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\text{Tan} [c + d x]} \right) - \\
 & \left( a \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \right. \right. \\
 & \left. \left. \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \right. \\
 & \left. \left. (a - i b)^3 (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \right. \\
 & \left. \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec} [c + d x]} \right) / \right. \\
 & \left. \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}}} \\
 & 3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i\left(3 a^2 A b-A b^3+a^3 B-3 a b^2 B\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\left(a+i b\right)^3(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+\left(a-i b\right)^3(A-i B) \operatorname{EllipticPi}\left[\right. \right. \\
 & \left. \left. \frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \sqrt{\sec [c+d x]} \\
 & \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}(a \cos [c+d x]+b \sin [c+d x])^{3 / 2} \sqrt{\tan [c+d x]}}} \\
 & 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( i\left(3 a^2 A b-A b^3+a^3 B-3 a b^2 B\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] - (a + i b)^3 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^3 (A - i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c + d x]} (b \operatorname{Cos} [c + d x] - a \operatorname{Sin} [c + d x]) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}} \\
 & 4 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] - (a + i b)^3 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^3 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}}} \\
 & 2 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \\
 & \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \left( i \left( 3 a^2 A b-A b^3+a^3 B-3 a b^2 B \right) \right. \\
 & \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]-\left( a+i b \right)^3 (A+i B) \\
 & \text{EllipticPi} \left[ -\frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]+ \\
 & \left. \left( a-i b \right)^3 (A-i B) \text{EllipticPi} \left[ \frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \operatorname{Sec} [c+d x]^{3 / 2} \sin [c+d x] \tan \left[ \frac{1}{2} (c+d x) \right]^{3 / 2}+ \\
 & \left( 4 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{\operatorname{Sec} [c+d x]} \left( \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \left( 3 a^2 A b-A b^3+a^3 B-3 a b^2 B \right) \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2} (c+d x) \right]^{3 / 2} \right) \right)+
 \end{aligned}$$



$$\begin{aligned}
 & \left( i (a + i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \right. \\
 & \quad \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \right) - \\
 & \left( i (a - i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \right. \\
 & \quad \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \right) \\
 & \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \right. \\
 & \quad \left. \sqrt{\operatorname{Tan}[c + d x]} \right) \left( \sqrt{\operatorname{Tan}[c + d x]} \right) + \\
 & \frac{1}{d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])} \\
 & \operatorname{Cos}[c + d x]^3 \\
 & \left( -\frac{2 (326 a^2 A b - 5 A b^3 + 150 a^3 B - 135 a b^2 B)}{315 a} - \right. \\
 & \quad \frac{1}{315 a^2} \\
 & \quad 2 (413 a^4 A \operatorname{Cos}[c + d x] - 558 a^2 A b^2 \operatorname{Cos}[c + d x] - 10 A b^4 \operatorname{Cos}[c + d x] - \\
 & \quad \quad 870 a^3 b B \operatorname{Cos}[c + d x] + 45 a b^3 B \operatorname{Cos}[c + d x]) \operatorname{Csc}[c + d x] + \\
 & \quad \left. \frac{2 (421 a^2 A b - 5 A b^3 + 195 a^3 B - 135 a b^2 B) \operatorname{Csc}[c + d x]^2}{315 a} + \right. \\
 & \quad \frac{2}{315} (133 a^2 A \operatorname{Cos}[c + d x] - 75 A b^2 \operatorname{Cos}[c + d x] - 135 a b B \operatorname{Cos}[c + d x]) \operatorname{Csc}[c + d x]^3 - \\
 & \quad \frac{2}{63} a (19 A b + 9 a B) \operatorname{Csc}[c + d x]^4 - \\
 & \quad \left. \frac{2}{9} a^2 A \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^4 \right) \\
 & \sqrt{\operatorname{Tan}[c + d x]} (a + b \operatorname{Tan}[c + d x])^{5/2} \\
 & (A + \\
 & \quad B \operatorname{Tan}[c + d x])
 \end{aligned}$$

**Problem 450: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x])}{\tan [c + d x]^{13/2}} dx$$

Optimal (type 3, 460 leaves, 13 steps):

$$\frac{(i a - b)^{5/2} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] - (i a + b)^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right]}{d} - \frac{2 a (14 A b + 11 a B) \sqrt{a + b \tan [c + d x]} + 2 (99 a^2 A - 113 A b^2 - 209 a b B) \sqrt{a + b \tan [c + d x]}}{99 d \tan [c + d x]^{9/2}} + \frac{2 (495 a^2 A b - 5 A b^3 + 231 a^3 B - 275 a b^2 B) \sqrt{a + b \tan [c + d x]}}{1155 a d \tan [c + d x]^{5/2}} - \frac{(2 (1155 a^4 A - 1485 a^2 A b^2 - 20 A b^4 - 2541 a^3 b B + 55 a b^3 B) \sqrt{a + b \tan [c + d x]}) / (3465 a^2 d \tan [c + d x]^{3/2}) - (2 (8085 a^4 A b - 495 a^2 A b^3 + 40 A b^5 + 3465 a^5 B - 5313 a^3 b^2 B - 110 a b^4 B) \sqrt{a + b \tan [c + d x]}) / (3465 a^3 d \sqrt{\tan [c + d x]}) - \frac{2 a A (a + b \tan [c + d x])^{3/2}}{11 d \tan [c + d x]^{11/2}}$$

Result (type 4, 5809 leaves):

$$- \left( \left( 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \cos [c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right) \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^3 (A - i B) \right)$$

$$\left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\begin{aligned}
 & \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \left( - \frac{a^3 A \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \right. \\
 & \frac{3 a A b^2 \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \\
 & \frac{3 a^2 b B \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \\
 & \left. \frac{b^3 B \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} \right) \\
 & \left( \frac{a^3 A \cos[2 (c + d x)] \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} + \frac{(3 a A b^2 \cos[2 (c + d x)] \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} + \right. \\
 & \left( \frac{3 a^2 b B \cos[2 (c + d x)] \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} - \frac{(b^3 B \cos[2 (c + d x)] \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} \right) - \\
 & \left( \frac{3 a^2 A b \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sin[2 (c + d x)] \sqrt{\tan[c + d x]}}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} + \right. \\
 & \left( \frac{A b^3 \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sin[2 (c + d x)] \sqrt{\tan[c + d x]}}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} - \right. \\
 & \left( \frac{a^3 B \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sin[2 (c + d x)] \sqrt{\tan[c + d x]}}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} + \right. \\
 & \left. \left. \frac{(3 a b^2 B \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sin[2 (c + d x)] \sqrt{\tan[c + d x]})}{(2 \sqrt{a \cos[c + d x] + b \sin[c + d x]})} \right) \right) (a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x]) \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \cos[c + d x] + b \sin[c + d x])^3 (A \cos[c + d x] + B \sin[c + d x]) \right)
 \end{aligned}$$

$$\left( \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \tan [c+d x]^{3/2}}} \right.$$

$$2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( \left( a^3 A-3 a A b^2-3 a^2 b B+b^3 B \right) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]-\left( a+i b \right)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i\left( b+\sqrt{a^2+b^2} \right)}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]-\left( a-i b \right)^3 (A-i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i\left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\operatorname{Sec} [c+d x]^{5/2} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} + \left( i a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\left( \left( a^3 A-3 a A b^2-3 a^2 b B+b^3 B \right) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]-\left( a+i b \right)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i\left( b+\sqrt{a^2+b^2} \right)}{a}, i \right.$$

$$\begin{aligned}
 & \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-ib)^3 (A-ib) \\
 & \text{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \left. \sqrt{\sec[c+dx]} \right) / \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\tan\left[\frac{1}{2}(c+dx)\right]} \sqrt{\tan[c+dx]} \right) + \\
 & \left( i a \sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right) \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right) \\
 & \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a+ib)^3 (A+ib) \right. \\
 & \left. \text{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & \left. (a-ib)^3 (A-ib) \text{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \right. \right. \\
 & \left. \left. \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec[c+dx]} \right) /
 \end{aligned}$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\ \left. \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]} \sqrt{\operatorname{Tan}[c + dx]} \right) - \\ \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]}} \\ 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\ \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right) \\ \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \\ \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \\ (a - i b)^3 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \right. \\ \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec}[c + dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]} + \\ \left. \left( 1 / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^{3/2} \sqrt{\operatorname{Tan}[c + dx]} \right) \right) \right)$$

$$\begin{aligned}
 & 2 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^3 (A-i B) \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \right) \\
 & \frac{\sqrt{\operatorname{Sec}[c+d x]} (b \operatorname{Cos}[c+d x] - a \operatorname{Sin}[c+d x]) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^{3/2} + 1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}} \\
 & 4 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^3 (A-i B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}} \\
 & 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right) \\
 & \text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \\
 & \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \\
 & (a - i b)^3 (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \sec [c + d x]^{3/2} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \right. \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}} 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Sec}[c + dx]} \\
 & \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \right. \\
 & \quad \left. \left( 4 \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \\
 & \quad \left( i (a + i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \\
 & \quad \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) + \left( i (a - i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \\
 & \quad \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \sqrt{\operatorname{Tan}[c + dx]} \right) + \\
 & \frac{1}{d (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx])} \\
 & \operatorname{Cos}[ \\
 & \quad c + dx]^3 \\
 & \left( \frac{2 (1965 a^4 A - 2050 a^2 A b^2 - 20 A b^4 - 3586 a^3 b B + 55 a b^3 B)}{3465 a^2} \right) - \\
 & \frac{1}{3465 a^3} \\
 & 2 \\
 & \left( 10375 a^4 A b \operatorname{Cos}[c + dx] - 510 a^2 A b^3 \operatorname{Cos}[c + dx] + \right. \\
 & \quad 40 A b^5 \operatorname{Cos}[c + dx] + 4543 a^5 B \operatorname{Cos}[c + dx] - \\
 & \quad \left. 6138 a^3 b^2 B \operatorname{Cos}[c + dx] - 110 a b^4 B \operatorname{Cos}[c + dx] \right) \operatorname{Csc}[c + dx] - \\
 & \frac{1}{3465 a^2} 2 (3090 a^4 A - 2615 a^2 A b^2 - 20 A b^4 - 4631 a^3 b B + 55 a b^3 B)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Csc}[c + d x]^2 + \frac{1}{3465 a} \\
 & 2 \left( 3095 a^2 A b \text{Cos}[c + d x] - 15 A b^3 \text{Cos}[c + d x] + \right. \\
 & \quad \left. 1463 a^3 B \text{Cos}[c + d x] - 825 a b^2 B \text{Cos}[c + d x] \right) \\
 & \text{Csc}[c + d x]^3 + \frac{2}{693} (288 a^2 A - 113 A b^2 - 209 a b B) \\
 & \text{Csc}[c + d x]^4 - \\
 & \frac{2}{99} (23 a A b \text{Cos}[c + d x] + 11 a^2 B \text{Cos}[c + d x]) \\
 & \text{Csc}[c + d x]^5 - \frac{2}{11} \\
 & a^2 \\
 & A \\
 & \left. \text{Csc}[c + d x]^6 \right) \\
 & \sqrt{\text{Tan}[c + d x]} (a + b \text{Tan}[c + d x])^{5/2} \\
 & (A + \\
 & B \\
 & \text{Tan}[c + d x])
 \end{aligned}$$

**Problem 451:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + b \text{Tan}[c + d x])^{5/2} \left( \frac{3bB}{2a} + B \text{Tan}[c + d x] \right)}{\text{Tan}[c + d x]^{5/2}} dx$$

Optimal (type 3, 253 leaves, 14 steps):

$$\begin{aligned}
 & \frac{(i a - b)^{5/2} (2 a - 3 i b) B \text{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right]}{2 a d} + \\
 & \frac{2 b^{5/2} B \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right]}{d} - \frac{(2 a + 3 i b) (i a + b)^{5/2} B \text{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right]}{2 a d} - \\
 & \frac{2 (a^2 + 3 b^2) B \sqrt{a + b \text{Tan}[c + d x]}}{d \sqrt{\text{Tan}[c + d x]}} - \frac{b B (a + b \text{Tan}[c + d x])^{3/2}}{d \text{Tan}[c + d x]^{3/2}}
 \end{aligned}$$

Result (type 4, 76 107 leaves): Display of huge result suppressed!

**Problem 452:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Tan}[c + d x]^{3/2} (A + B \text{Tan}[c + d x])}{\sqrt{a + b \text{Tan}[c + d x]}} dx$$

Optimal (type 3, 206 leaves, 13 steps):

$$\begin{aligned}
 & \frac{(A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{\sqrt{i a - b} d} + \frac{(2 A b - a B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{b^{3/2} d} \\
 & \frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{\sqrt{i a + b} d} + \frac{B \sqrt{\tan[c + d x]} \sqrt{a + b \tan[c + d x]}}{b d}
 \end{aligned}$$

Result (type 4, 10834 leaves):

$$\begin{aligned}
 & \frac{B (a \cos[c + d x] + b \sin[c + d x]) \sqrt{\tan[c + d x]} (A + B \tan[c + d x])}{b d (A \cos[c + d x] + B \sin[c + d x]) \sqrt{a + b \tan[c + d x]}} + \\
 & \left( 2 \sqrt{a^2 + b^2} \left( -B \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] + \right. \\
 & \left. \left( (2 A b - a B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \right. \right. \\
 & \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (-a + b + \sqrt{a^2 + b^2}) - \left( 2 i A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (-i a + b + \sqrt{a^2 + b^2}) +
 \end{aligned}$$

$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( -i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( 2 A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left. \begin{aligned}
 & \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]} \\
 & \sqrt{\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2 + b^2}} \\
 & \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \left( \frac{A \csc[c+dx] \sqrt{\sec[c+dx]} \sqrt{\tan[c+dx]}}{2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} - \frac{a B \csc[c+dx] \sqrt{\sec[c+dx]} \sqrt{\tan[c+dx]}}{2 b \sqrt{a \cos[c+dx] + b \sin[c+dx]}} - \right. \\
 & \frac{A \cos[2(c+dx)] \csc[c+dx] \sqrt{\sec[c+dx]} \sqrt{\tan[c+dx]}}{2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} - \\
 & \left. \frac{B \csc[c+dx] \sqrt{\sec[c+dx]} \sin[2(c+dx)] \sqrt{\tan[c+dx]}}{2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} \right) (A + B \tan[c+dx]) \Big/ \\
 & \left( b d \sqrt{\sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\sec[c+dx]} (A \cos[c+dx] + B \sin[c+dx])} \right. \\
 & \left. \sqrt{\tan[c+dx]} \sqrt{a + b \tan[c+dx]} \right) \\
 & \left( \left( \left( \sqrt{a^2 + b^2} \right) \left( -B \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) + \right. \right.
 \end{aligned} \right)$$

$$\left( (2 A b - a B) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( 2 A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( a + b + \sqrt{a^2 + b^2} \right) + \left( a B \text{EllipticPi} \left[ \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) \left( \text{Sec} [c + d x]^2 \sqrt{\text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \text{Sec} [c + d x]} \right)$$

$$\left( \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{a^2 + b^2}} \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right) /$$

$$\left( b \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \operatorname{Tan}[c+dx]^{3/2}} \right) +$$

$$\left( a \sqrt{a^2 + b^2} \left( -B \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) + \right.$$

$$\left. \left( (2Ab - aB) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / (-a + b + \sqrt{a^2 + b^2}) - \left( 2iAb \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-ia + b + \sqrt{a^2 + b^2}}, \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / (-ia + b + \sqrt{a^2 + b^2}) +$$



$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) - \left( 2 A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( a + b + \sqrt{a^2 + b^2} \right) + a B$$

$$\left. \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/$$

$$\left. \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \text{Sec} [c + d x]}$$

$$\left. \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos} [c + d x] + b \text{Sin} [c + d x])}{a^2 + b^2}} \right/$$

$$\left( 2 b \left( b + \sqrt{a^2 + b^2} \right) \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\frac{a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Tan} [c + d x]} \right) -$$

$$\left( \sqrt{a^2 + b^2} \left( -B \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] + \right.$$

$$\left. \left( 2 A b - a B \right) \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( 2 A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + b + \sqrt{a^2 + b^2} \right) + \left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\sqrt{\operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Sec} [c + d x] (b \operatorname{Cos} [c + d x] - a \operatorname{Sin} [c + d x])}$$

$$\sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2}} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} /$$

$$\left( b \sqrt{\operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])} \sqrt{\operatorname{Tan} [c + d x]} \right) -$$

$$\frac{1}{b \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]} \sqrt{a^2 + b^2} \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]}$$

$$\left( -B \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] + \right.$$

$$\left( (2 A b - a B) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ (-a + b + \sqrt{a^2 + b^2}) - \left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ (-i a + b + \sqrt{a^2 + b^2}) +$$

$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ (-i a + b + \sqrt{a^2 + b^2}) + \left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ (i a + b + \sqrt{a^2 + b^2}) +$$

$$\left( 2 b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) - \left( 2 A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + b + \sqrt{a^2 + b^2} \right) + \right.$$

$$\left. \left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \right. \right.$$

$$\left. \left. \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\sec \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\cos \left[ \frac{1}{2} (c + d x) \right]^2} \sec [c + d x] \right. \right.$$

$$\left. \left. \sin \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{a \sec \left[ \frac{1}{2} (c + d x) \right]^2 (a \cos [c + d x] + b \sin [c + d x])}{a^2 + b^2}} \right. \right.$$

$$\left. \left. \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} + \right. \right.$$

$$\left( \sqrt{a^2 + b^2} \left( -B \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] + \right. \right.$$

$$\left. \left( 2 A b - a B \right) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \right. \right.$$

$$\left. \left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right. \right.$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2+b^2} \right) + \\
 & \left( 2 b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right. \\
 & \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( 2 A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \Big/ \left( a + b + \sqrt{a^2+b^2} \right) + \\
 & \left( a B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right. \\
 & \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( a + b + \sqrt{a^2+b^2} \right) \right) \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]} \\
 & \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \left( \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (b \cos[c+dx] - a \sin[c+dx])}{a^2+b^2} \right) +
 \end{aligned}$$



$$\left. \frac{1}{a^2 + b^2} a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) /$$

$$\left( b \sqrt{\operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} \right.$$

$$\left. \sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])}{a^2 + b^2}} \sqrt{\operatorname{Tan}[c + d x]} \right) +$$

$$\left( 1 / \left( b \sqrt{\operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}} \right) \right)$$

$$2 \sqrt{a^2 + b^2} \sqrt{\operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \operatorname{Sec}[c + d x]}$$

$$\sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])}{a^2 + b^2}}$$

$$\sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( a B \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}} \right)$$

$$\sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{2 \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} -$$

$$\left( a (2 A b - a B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (-a + b + \sqrt{a^2 + b^2}) \right)$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{2 \sqrt{a^2 + b^2}}}$$

$$\begin{aligned}
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-a + b + \sqrt{a^2 + b^2}}\right) \right) + \\
 & \left( i a A b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 2 \sqrt{2} \sqrt{a^2 + b^2} \left( -i a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2 \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \right) - \\
 & \left( a b B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 2 \sqrt{2} \sqrt{a^2 + b^2} \left( -i a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2 \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \right) - \\
 & \left( i a A b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 2 \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2 \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) \right) - \\
 & \left( a b B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 2 \sqrt{2} \sqrt{a^2 + b^2} \left( i a + b + \sqrt{a^2 + b^2} \right) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}}\right) + \\
 & \left(a A b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(2\sqrt{2}\sqrt{a^2 + b^2}(a + b + \sqrt{a^2 + b^2})\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}}\right) - \\
 & \left(a^2 B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4\sqrt{2}\sqrt{a^2 + b^2}(a + b + \sqrt{a^2 + b^2})\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}}\right) + \\
 & \left(\sqrt{a^2 + b^2} \left(-B \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] + \right. \\
 & \left. (2Ab - aB) \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right]\right)\right)
 \end{aligned}$$

$$\left( \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right) / \left( -a+b+\sqrt{a^2+b^2} \right) -$$

$$\left( 2i A b \operatorname{EllipticPi}\left[ \frac{2\sqrt{a^2+b^2}}{-ia+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right) / \left( -ia+b+\sqrt{a^2+b^2} \right) + \left( 2b B \operatorname{EllipticPi}\left[ \frac{2\sqrt{a^2+b^2}}{-ia+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin}\left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right) / \left( -ia+b+\sqrt{a^2+b^2} \right) +$$

$$\left( 2i A b \operatorname{EllipticPi}\left[ \frac{2\sqrt{a^2+b^2}}{ia+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right) / \left( ia+b+\sqrt{a^2+b^2} \right) + \left( 2b B \operatorname{EllipticPi}\left[ \frac{2\sqrt{a^2+b^2}}{ia+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( 2 A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( a + b + \sqrt{a^2+b^2} \right) + \left( a B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( a + b + \sqrt{a^2+b^2} \right) \right)$$

$$\sqrt{\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2+b^2}} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \right.$$

$$\left. \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \tan[c+dx] \right) \Bigg/$$

$$\left( b \sqrt{\sec\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]} \right)$$

$$\int \frac{\sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}} dx$$

Problem 453: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\tan[c+dx]} (A+B \tan[c+dx])}{\sqrt{a+b \tan[c+dx]}} dx$$

Optimal (type 3, 168 leaves, 12 steps):

$$\frac{(i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right]}{\sqrt{i a - b} d} + \frac{2 B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right]}{\sqrt{b} d} - \frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right]}{\sqrt{i a + b} d}$$

Result (type 4, 6384 leaves):

$$\left( \left( 4 a - \left( B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \right) / \left( -a + b + \sqrt{a^2 + b^2} \right) + \left( (A + i B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \dots$$

$$\left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( i B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) \left( a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x] \right)$$

$$\sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( \frac{A \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \right.$$

$$\left. \frac{B \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x] \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} \right) (A + B \operatorname{Tan} [c + d x]) /$$

$$\left( \sqrt{a^2 + b^2} d \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])}{a^2 + b^2}} \right.$$

$$(A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx])$$

$$\left( \frac{1}{\sqrt{a^2 + b^2} \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])}{a^2 + b^2}} \operatorname{Tan}[c + dx]^{3/2}} \right.$$

$$2 a \left( \left( \left( \operatorname{B EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -a + b + \sqrt{a^2 + b^2} \right) \right) +$$

$$\left( (A + i B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) \right) + \left( \operatorname{A EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$



$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( i \text{B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) + \left( \text{B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Bigg/ \left( a + b + \sqrt{a^2+b^2} \right)$$

$$\text{Sec}[c+dx]^{5/2} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} -$$

$$\left( a^2 - \left( \left( \left( \text{B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Bigg/ \left( -a + b + \sqrt{a^2+b^2} \right) + \right.$$

$$\left( (A + i B) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( i B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right/$$

$$\left( \sqrt{a^2 + b^2} \left( b + \sqrt{a^2 + b^2} \right) \sqrt{\frac{a \sec \left[ \frac{1}{2} (c + d x) \right]^2 (a \cos [c + d x] + b \sin [c + d x])}{a^2 + b^2}} \right.$$

$$\left. \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\tan [c + d x]} \right) -$$

$$\left( 2 a \left( - \left( \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right) \right) \right.$$

$$\left. \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/ \left( -a + b + \sqrt{a^2 + b^2} \right) \right) +$$

$$\left( (A + i B) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right) \right),$$

$$\left. \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/ \left( -i a + b + \sqrt{a^2 + b^2} \right) \right) + \left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( i a + b + \sqrt{a^2+b^2} \right) - \\
 & \left( i \text{B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \right. \right. \\
 & \left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( i a + b + \sqrt{a^2+b^2} \right) + \left( \text{B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \right/ \left( a + b + \sqrt{a^2+b^2} \right) \\
 & \left. \sqrt{\text{Sec}[c+dx]} (b \text{Cos}[c+dx] - a \text{Sin}[c+dx]) \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right/ \\
 & \left( \sqrt{a^2+b^2} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right. \\
 & \left. \sqrt{\frac{a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])}{a^2+b^2}} \sqrt{\text{Tan}[c+dx]} \right) -
 \end{aligned}$$

$$\frac{1}{\sqrt{a^2 + b^2} \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{a^2 + b^2}} \sqrt{\operatorname{Tan}[c+dx]}}$$

$$2 a \left( \left( \left( \operatorname{B} \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right. \right. \right.$$

$$\left. \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -a + b + \sqrt{a^2 + b^2} \right) + \right.$$

$$\left. \left( (A + i B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right. \right.$$

$$\left. \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( A \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left. \left( i B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right. \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} +$$

$$\left( 1 / \left( \sqrt{a^2 + b^2} \left( \frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2} \right)^{3/2} \sqrt{\operatorname{Tan} [c + d x]} \right) \right)$$

$$2 a \left( - \left( \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -a + b + \sqrt{a^2 + b^2} \right) \right) +$$

$$\left( (A + i B) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( i B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + b + \sqrt{a^2 + b^2} \right) \right)$$

$$\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( \frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (b \operatorname{Cos}[c + d x] - a \operatorname{Sin}[c + d x])}{a^2 + b^2} + \frac{1}{a^2 + b^2} \right.$$

$$\left. a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) -$$

$$\begin{aligned}
 & \frac{1}{\sqrt{a^2+b^2} \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx])}{a^2+b^2}} \sqrt{\operatorname{Tan}[c+dx]}} \\
 & 4 a \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \\
 & \left( \left( a B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( -a+b+\sqrt{a^2+b^2} \right) \right) \right) \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}} \sqrt{1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2 \sqrt{a^2+b^2}}} \\
 & \sqrt{1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \left( 1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-a+b+\sqrt{a^2+b^2}} \right) \Bigg) - \\
 & \left( a (A+i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( -i a+b+\sqrt{a^2+b^2} \right) \right) \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}} \sqrt{1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2 \sqrt{a^2+b^2}}} \\
 & \sqrt{1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \left( 1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-i a+b+\sqrt{a^2+b^2}} \right) \Bigg) - \\
 & \left( a A \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( i a+b+\sqrt{a^2+b^2} \right) \right) \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}} \sqrt{1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{2 \sqrt{a^2+b^2}}} \\
 & \sqrt{1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \left( 1-\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{i a+b+\sqrt{a^2+b^2}} \right) \Bigg) +
 \end{aligned}$$



$$\begin{aligned}
 & \left( i a B \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( i a + b + \sqrt{a^2+b^2} \right) \right. \\
 & \quad \sqrt{\frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{2 \sqrt{a^2+b^2}}} \\
 & \quad \left. \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2+b^2}}} \left( 1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{i a + b + \sqrt{a^2+b^2}} \right) \right) - \\
 & \left( a B \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( a + b + \sqrt{a^2+b^2} \right) \right. \\
 & \quad \sqrt{\frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{2 \sqrt{a^2+b^2}}} \\
 & \quad \left. \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2+b^2}}} \right) \left( \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{a + b + \sqrt{a^2+b^2}} \right) \right) \left( \sqrt{\operatorname{Tan} [c+d x]} \sqrt{a + b \operatorname{Tan} [c+d x]} \right)
 \end{aligned}$$

**Problem 454: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan} [c+d x]}{\sqrt{\operatorname{Tan} [c+d x]} \sqrt{a + b \operatorname{Tan} [c+d x]}} dx$$

Optimal (type 3, 123 leaves, 7 steps):

$$\frac{(A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan} [c+d x]}}{\sqrt{a + b \operatorname{Tan} [c+d x]}} \right]}{\sqrt{i a - b} d} + \frac{(A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan} [c+d x]}}{\sqrt{a + b \operatorname{Tan} [c+d x]}} \right]}{\sqrt{i a + b} d}$$

Result (type 4, 4376 leaves):

$$\begin{aligned}
 & - \left( \left( 2 \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left( -i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + i (A + i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \\
 & \left. (i A + B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \left( \frac{A \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\tan [c + d x]}}{2 \sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \right. \\
 & \left. \frac{A \cos [2 (c + d x)] \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\tan [c + d x]}}{2 \sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \right. \\
 & \left. \frac{B \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \sin [2 (c + d x)] \sqrt{\tan [c + d x]}}{2 \sqrt{a \cos [c + d x] + b \sin [c + d x]}} \right) (A + B \tan [c + d x]) \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \cos [c + d x] + B \sin [c + d x]) \right) \\
 & \left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \tan [c + d x]^{3/2}} \right) \\
 & \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left( -i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + i (A+i B) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] +$$

$$(i A+B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right],$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \operatorname{Sec} [c+dx]^{5/2} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} +$$

$$\left( \sqrt{2} a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \left( -i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right],$$

$$\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + i (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a},$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (i A+B)$$

$$\operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\left. \sqrt{\operatorname{Sec} [c+dx]} \right) / \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{2 + \frac{2 a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right)$$

$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) + \\
 & \left( a \sqrt{2+\frac{2 a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\left(-i \operatorname{A} \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right],\right. \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+i(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right],\right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(i A+B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a},\right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\sec [c+d x]} \right) / \\
 & \left( \sqrt{2}\left(b-\sqrt{a^2+b^2}\right) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}\sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\right. \\
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) - \\
 & \left( 1 / \left( \sqrt{2} \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}\sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]} \right) \right) \\
 & 3 \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\sqrt{2+\frac{2 a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\left(-i \operatorname{A} \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right],\right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+i(A+i B)
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \\
 & (iA + B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \right) \sqrt{\sec[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos[c + dx] + b \sin[c + dx])^{3/2} \sqrt{\tan[c + dx]}} \\
 & \sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \left( -iA \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + i(A + iB) \right. \\
 & \left. \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \right. \\
 & \left. (iA + B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} +
 \end{aligned}$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}}$$

$$2 \sqrt{2} \cos \left[\frac{1}{2}(c+d x)\right] \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}$$

$$\sqrt{2+\frac{2 a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\left(-i A \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+i(A+i B)\right.$$

$$\operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+$$

$$\left.(i A+B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right],\right.$$

$$\left.\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\sec [c+d x]} \sin \left[\frac{1}{2}(c+d x)\right] \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}-$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}}$$

$$\sqrt{2} \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}$$

$$\sqrt{2+\frac{2 a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\left(-i A \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+i(A+i B)\right.$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \\
 & (iA + B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \right) \operatorname{Sec}[c + dx]^{3/2} \operatorname{Sin}[c + dx] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\tan[c + dx]}} \\
 & 2\sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{\operatorname{Sec}[c + dx]} \left( - \left( \left( A \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \right. \\
 & \left. \left. \left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \right. \\
 & \left. \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + iB) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right) \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) - \\
 & \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (iA + B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right)
 \end{aligned}$$

$$\left( \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \left( \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \sqrt{\operatorname{Tan}[c+dx]} \sqrt{a+b \operatorname{Tan}[c+dx]} \right)$$

**Problem 455: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan}[c + dx]}{\operatorname{Tan}[c + dx]^{3/2} \sqrt{a + b \operatorname{Tan}[c + dx]}} dx$$

Optimal (type 3, 159 leaves, 8 steps):

$$\frac{(i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + dx]}}{\sqrt{a + b \operatorname{Tan}[c + dx]}}\right]}{\sqrt{i a - b} d} + \frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + dx]}}{\sqrt{a + b \operatorname{Tan}[c + dx]}}\right]}{\sqrt{i a + b} d} - \frac{2 A \sqrt{a + b \operatorname{Tan}[c + dx]}}{a d \sqrt{\operatorname{Tan}[c + dx]}}$$

Result (type 4, 4442 leaves):

$$\begin{aligned} & - \left( (2 A (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]) (A + B \operatorname{Tan}[c + dx])) / \right. \\ & \quad \left. (a d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \sqrt{\operatorname{Tan}[c + dx]} \sqrt{a + b \operatorname{Tan}[c + dx]}) \right) - \\ & \left( 2 \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\ & \quad \left. \left( -i B \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \right. \right. \\ & \quad \left. \left. (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) - \end{aligned}$$



$$\left( (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\left( \tan \left[ \frac{1}{2} (c + d x) \right] \right)^{3/2} \left( \frac{B \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\tan [c + d x]}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \right.$$

$$\frac{B \operatorname{Cos} [2 (c + d x)] \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\tan [c + d x]}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} -$$

$$\left. \frac{A \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [2 (c + d x)] \sqrt{\tan [c + d x]}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} \right) (A + B \tan [c + d x]) \left/ \right.$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right)$$

$$\left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \tan [c + d x]^{3/2}} \right)$$

$$\sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( -i B \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A + i B) \operatorname{EllipticPi} \left[ \right. \right.$$

$$\left. \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A - i B) \right)$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec} [c + d x]^{5/2} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \left( \sqrt{2} a \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( -i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A + i B) \text{EllipticPi} \left[ \right. \right. \right. \\
 & \left. \left. \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A - i B) \right. \right. \right. \\
 & \left. \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \left. \sqrt{\text{Sec} [c + d x]} \right) / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{2 + \frac{2 a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\text{Tan} [c + d x]} \right) + \\
 & \left( a \sqrt{2 + \frac{2 a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( -i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A + i B) \text{EllipticPi} \left[ - \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \right.
 \end{aligned}$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (A-iB)$$

$$\operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]$$

$$\left. \sqrt{\operatorname{Sec} [c+dx]} \right/ \left( \sqrt{2} (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\operatorname{Tan} [c+dx]} \right) -$$

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$$\sqrt{2} \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]}$$

$$3 \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{2+\frac{2a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}}$$

$$\left( -iB \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (A+iB) \right.$$

$$\left. \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$\left. (A-iB) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right.$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \sqrt{\sec [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} +$$


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$$\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]}$$

$$\sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( -i B \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A + i B) \operatorname{EllipticPi} \left[ \right. \right.$$

$$\left. \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A - i B) \right.$$

$$\left. \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} +$$


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$$\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]}$$

$$2 \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( -i B \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A + i B) \operatorname{EllipticPi} \left[ \right. \right.$$

$$\begin{aligned}
 & - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} - (A - i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \\
 & \frac{\sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}} \\
 & \sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \\
 & \left( -i B \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A + i B) \operatorname{EllipticPi} \left[ \right. \right. \\
 & \left. \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A - i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}} \\
 & 2 \sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned} & \sqrt{\sec [c+d x]} \left( - \left( \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} B \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \right. \right. \\ & \left. \left( 4 \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) \right) - \\ & \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \left( 1-i \cot \left[ \frac{1}{2} (c+d x) \right] \right) \right. \\ & \left. \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) + \\ & \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A-i B) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \left( 1+i \cot \left[ \frac{1}{2} (c+d x) \right] \right) \right. \\ & \left. \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) \right) \\ & \left. \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \sqrt{\tan [c+d x]} \sqrt{a+b \tan [c+d x]} \right) \end{aligned}$$

Problem 456: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A+B \tan [c+d x]}{\tan [c+d x]^{5/2} \sqrt{a+b \tan [c+d x]}} dx$$

Optimal (type 3, 203 leaves, 9 steps):

$$\begin{aligned} & \frac{(A+i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}} \right] - (A-i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}} \right]}{\sqrt{i a-b} d - \sqrt{i a+b} d} \\ & + \frac{2 A \sqrt{a+b \tan [c+d x]}}{3 a d \tan [c+d x]^{3/2}} + \frac{2 (2 A b-3 a B) \sqrt{a+b \tan [c+d x]}}{3 a^2 d \sqrt{\tan [c+d x]}} \end{aligned}$$

Result (type 4, 4506 leaves):

$$\begin{aligned}
 & - \left( \left( 2 \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left( \begin{aligned}
 & \left( i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (-i A + B) \right. \\
 & \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \\
 & \left. (-i A - B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \left( -\frac{A \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \right. \\
 & \frac{A \cos[2(c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \\
 & \left. \frac{B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sin[2(c + d x)] \sqrt{\tan[c + d x]}}{2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} \right) (A + B \tan[c + d x]) \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \cos[c + d x] + B \sin[c + d x]) \right) \\
 & \left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \tan[c + d x]^{3/2}} \right. \\
 & \left. \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left( \begin{aligned}
 & \left( i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (-i A+B) \operatorname{EllipticPi} \left[ \right. \right. \\
 & \left. \left. -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (-i A-B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \right) \\
 & \operatorname{Sec}[c+dx]^{5/2} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} + \left( \sqrt{2} a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left( i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + \right. \\
 & \left. (-i A+B) \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (-i A-B) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \sqrt{\operatorname{Sec}[c+dx]} \right) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{2 + \frac{2 a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right)
 \end{aligned} \right)$$



$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) + \\
 & \left( a \sqrt{2+\frac{2 a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\right) \left( i A \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(-i A+B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(-i A-B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \right. \\
 & \left. \left. \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(-i A-B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \sqrt{\sec [c+d x]} \Big/ \\
 & \left( \sqrt{2}\left(b-\sqrt{a^2+b^2}\right) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\right) \\
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) - \\
 & \left( 1 / \left( \sqrt{2} \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]} \right) \right) \\
 & 3 \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\sqrt{2+\frac{2 a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\left( \right. \\
 & \left. i A \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(-i A+B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \\
 & (-iA - B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\sec[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} + \\
 & \left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} (a \cos[c + dx] + b \sin[c + dx])^{3/2} \sqrt{\tan[c + dx]}}} \right) \\
 & \sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \left( iA \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (-iA + B) \text{EllipticPi}\left[ \right. \right. \\
 & \left. \left. -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (-iA - B) \right. \\
 & \left. \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]}}}
 \end{aligned}$$

$$\begin{aligned}
 & 2 \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2+b^2}}} \sqrt{2 + \frac{2a \cot\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2+b^2}}} \\
 & \left( i A \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] + (-i A + B) \operatorname{EllipticPi}\left[ \right. \right. \\
 & \quad \left. \left. - \frac{i(b + \sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] + (-i A - B) \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] \right) \\
 & \frac{\sqrt{\sec[c+dx]} \sin\left[\frac{1}{2}(c+dx)\right] \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} - 1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\tan[c+dx]}} \\
 & \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2+b^2}}} \sqrt{2 + \frac{2a \cot\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2+b^2}}} \\
 & \left( i A \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] + (-i A + B) \right. \\
 & \quad \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] + \\
 & \quad \left. (-i A - B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \right. \\
 & \quad \left. \left. \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] \right)
 \end{aligned}$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx] \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} -$$


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$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]} \sqrt{\text{Tan}[c + dx]}}$$

$$2 \sqrt{2} \text{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}$$

$$\sqrt{\text{Sec}[c + dx]} \left( \left( A \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right.$$

$$\left. \left( 4 \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) - \right.$$

$$\left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (-i A + B) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \text{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right. \right.$$

$$\left. \left. \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) - \right.$$

$$\left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (-i A - B) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 + i \text{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right. \right.$$

$$\left. \left. \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right)$$

$$\left. \left. \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \sqrt{\text{Tan}[c + dx]} \sqrt{a + b \text{Tan}[c + dx]} \right) \right) +$$

$$\left( \left( \frac{2 A}{3 a} - \frac{2 (-2 A b \text{Cos}[c + dx] + 3 a B \text{Cos}[c + dx]) \text{Csc}[c + dx]}{3 a^2} - \frac{2 A \text{Csc}[c + dx]^2}{3 a} \right) \right)$$

$$\frac{(a \cos [c+d x]+b \sin [c+d x]) \sqrt{\tan [c+d x]} (A+B \tan [c+d x])}{(d(A \cos [c+d x]+B \sin [c+d x]) \sqrt{a+b \tan [c+d x]})}$$

**Problem 457: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \tan [c+d x]}{\tan [c+d x]^{7/2} \sqrt{a+b \tan [c+d x]}} dx$$

Optimal (type 3, 256 leaves, 10 steps):

$$\frac{(i A-B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{\sqrt{i a-b} d} - \frac{(i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{\sqrt{i a+b} d} - \frac{2 A \sqrt{a+b \tan [c+d x]}}{5 a d \tan [c+d x]^{5/2}} + \frac{2(4 A b-5 a B) \sqrt{a+b \tan [c+d x]}}{15 a^2 d \tan [c+d x]^{3/2}} + \frac{2(15 a^2 A-8 A b^2+10 a b B) \sqrt{a+b \tan [c+d x]}}{15 a^3 d \sqrt{\tan [c+d x]}}$$

Result (type 4, 4549 leaves):

$$-\left(\left(2 \sqrt{2} \cos \left[\frac{1}{2}(c+d x)\right]\right)^2 \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\right) \sqrt{2+\frac{2 a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\right. \\ \left. \left(i B \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right.\right. \\ \left.\left.(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) +$$

$$\left( (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \left( - \frac{B \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} - \right.$$

$$\left. \frac{B \operatorname{Cos} [2 (c + d x)] \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \right.$$

$$\left. \frac{A \operatorname{Csc} [c + d x] \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [2 (c + d x)] \sqrt{\operatorname{Tan} [c + d x]}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} \right) (A + B \operatorname{Tan} [c + d x]) \Big/$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right)$$

$$\left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \operatorname{Tan} [c + d x]^{3/2}} \right)$$

$$\sqrt{2} \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( i B \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \operatorname{EllipticPi} \left[ \right. \right.$$

$$\left. \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \right)$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec}[c + d x]^{5/2} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \left( \sqrt{2} a \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \text{EllipticPi} \left[ \right. \right. \right. \\
 & \left. \left. \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \right. \right. \right. \\
 & \left. \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \left. \sqrt{\text{Sec}[c + d x]} \right) / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{2 + \frac{2 a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\text{Tan}[c + d x]} \right) + \\
 & \left( a \sqrt{2 + \frac{2 a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \text{EllipticPi} \left[ - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \right. \right. \right. \right.
 \end{aligned}$$

$$\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \left. , \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (A-iB) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec[c+dx]} \Bigg/$$

$$\left( \sqrt{2} (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \cos[c+dx]+b \sin[c+dx]} \sqrt{\tan\left[\frac{1}{2}(c+dx)\right]} \sqrt{\tan[c+dx]} \right) -$$

$$\left( 1 / \left( \sqrt{2} \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos[c+dx]+b \sin[c+dx]} \sqrt{\tan[c+dx]} \right) \right)$$

$$3 \sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{2+\frac{2a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\left( i B \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (A+iB) \right.$$

$$\operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] +$$

$$(A-iB) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \right.$$



$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \sqrt{\sec[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} +$$

$$\left( \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos[c + dx] + b \sin[c + dx])^{3/2} \sqrt{\tan[c + dx]}} \right)$$

$$\sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( i B \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \operatorname{EllipticPi}\left[ \right. \right.$$

$$\left. \left. - \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \right.$$

$$\left. \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\frac{\sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]}}$$

$$2 \sqrt{2} \cos\left[\frac{1}{2}(c + dx)\right] \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( i B \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \operatorname{EllipticPi}\left[ \right. \right.$$

$$\begin{aligned}
 & -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (A - iB) \\
 & \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \\
 & \frac{\sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} - 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]}} \\
 & \sqrt{2} \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \left( iB \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (A + iB) \right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \right. \\
 & \left. (A - iB) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \operatorname{Sec}[c + dx]^{3/2} \operatorname{Sin}[c + dx] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} - 1 \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]}}
 \end{aligned}$$

$$\begin{aligned}
 & 2 \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{\sec [c + d x]} \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} B \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \right. \\
 & \left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) - \right. \\
 & \left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \\
 & \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{\tan [c + d x]} \sqrt{a + b \tan [c + d x]} \right) + \\
 & \left( \left( \frac{2 (-4 A b + 5 a B)}{15 a^2} + \frac{1}{15 a^3} 4 (9 a^2 A \cos [c + d x] - 4 A b^2 \cos [c + d x] + 5 a b B \cos [c + d x]) \right. \right. \\
 & \left. \left. \frac{\csc [c + d x] - 2 (-4 A b + 5 a B) \csc [c + d x]^2}{15 a^2} - \frac{2 A \cot [c + d x] \csc [c + d x]^2}{5 a} \right) \right. \\
 & \left. \left( a \cos [c + d x] + b \sin [c + d x] \right) \sqrt{\tan [c + d x]} \right. \\
 & \left. \left( A + B \tan [c + d x] \right) \right) /
 \end{aligned}$$

$$\left( \frac{d (A \cos [c + d x] + B \sin [c + d x])}{\sqrt{a + b \tan [c + d x]}} \right)$$

**Problem 458: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\tan [c + d x]^{3/2} (A + B \tan [c + d x])}{(a + b \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 219 leaves, 13 steps):

$$\begin{aligned} & - \frac{(i A - B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right]}{(i a - b)^{3/2} d} + \frac{2 B \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right]}{b^{3/2} d} \\ & - \frac{(i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right]}{(i a + b)^{3/2} d} + \frac{2 a (A b - a B) \sqrt{\tan [c + d x]}}{b (a^2 + b^2) d \sqrt{a + b \tan [c + d x]}} \end{aligned}$$

Result (type 4, 76 131 leaves): Display of huge result suppressed!

**Problem 459: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\tan [c + d x]} (A + B \tan [c + d x])}{(a + b \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 170 leaves, 8 steps):

$$\begin{aligned} & - \frac{(A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right]}{(i a - b)^{3/2} d} + \\ & - \frac{(A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right]}{(i a + b)^{3/2} d} - \frac{2 (A b - a B) \sqrt{\tan [c + d x]}}{(a^2 + b^2) d \sqrt{a + b \tan [c + d x]}} \end{aligned}$$

Result (type 4, 5177 leaves):

$$- \left( \left( 4 \cos \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right)$$

$$\left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b) (A - i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\operatorname{Sec}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2}$$

$$\left( \frac{A b \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 (a - i b) (a + i b) \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \right.$$

$$\frac{a B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 (a - i b) (a + i b) \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} +$$

$$\left. \frac{(A b \operatorname{Cos}[2 (c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]})}{(2 (a - i b) (a + i b) \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]})} - \right.$$

$$\frac{(a B \operatorname{Cos}[2 (c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]})}{(2 (a - i b) (a + i b) \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]})} +$$

$$\frac{(a A \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[2 (c + d x)] \sqrt{\operatorname{Tan}[c + d x]})}{(2 (a - i b) (a + i b) \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]})} +$$

$$\left. \frac{(b B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[2 (c + d x)] \sqrt{\operatorname{Tan}[c + d x]})}{(2 (a - i b) (a + i b) \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]})} \right) (A + B \operatorname{Tan}[c + d x]) \Big/$$

$$\left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right)$$

$$\left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \tan [c + d x]^{3/2} \right) \right)$$

$$2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b) (A - i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\sec [c + d x]^{5/2} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] + (a + i b) (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \\
 & \left. \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec} [c + d x]} \Big/ \\
 & \left( (a^2 + b^2) (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right. \\
 & \left. \sqrt{\text{Tan} [c + d x]} \right) + \left( a \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( -i (A b - a B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. (a - i b) (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right] \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] + (a + i b) (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \\
 & \left. \left. \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec} [c + d x]} \Big/ \right. \\
 & \left. \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) - \\
 & \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]} \right) \right) \\
 & 3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( -i(A b-a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & (a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a+i b)(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \left. \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} + \right) \\
 & \left( 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left( -i(A b-a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & (a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \right.
 \end{aligned}$$



$$\begin{aligned}
 & \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a+ib)(A-ib) \\
 & \text{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \left. \sqrt{\sec[c+dx]} (b \cos[c+dx] - a \sin[c+dx]) \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \right/ \\
 & \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \cos[c+dx] + b \sin[c+dx])^{3/2} \sqrt{\tan[c+dx]} \right) + \\
 & \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\tan[c+dx]} \right) \right) \\
 & 4 \cos\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{b+\sqrt{a^2+b^2} + a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( -i(Ab - aB) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a-ib)(A+ib) \text{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a+ib)(A-ib) \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\sec [c+d x]} \sin \left[ \frac{1}{2} (c+d x) \right] \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]} \right) \right) \\
 & 2 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( -i (A b-a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b) (A-i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sec [c+d x]^{3/2} \sin [c+d x] \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]} \right) \right) \\
 & 4 \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\sec [c+d x]} \left( - \left( \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A b-a B) \sec \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) - \\
 & \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \\
 & \left. \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{\operatorname{Tan} [c + d x]} (a + b \operatorname{Tan} [c + d x])^{3/2} \right) \right) + \\
 & \left( \operatorname{Sec} [c + d x] (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2 \right. \\
 & \left( \frac{2 (-A b + a B)}{a (a - i b) (a + i b)} - \frac{2 (-A b^2 \operatorname{Sin} [c + d x] + a b B \operatorname{Sin} [c + d x])}{a (a - i b) (a + i b) (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])} \right) \\
 & \left. \sqrt{\operatorname{Tan} [c + d x]} (A + B \operatorname{Tan} [c + d x]) \right) / (d \\
 & (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \\
 & (a + b \operatorname{Tan} [c + d x])^{3/2})
 \end{aligned}$$

**Problem 460: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan} [c + d x]}{\sqrt{\operatorname{Tan} [c + d x]} (a + b \operatorname{Tan} [c + d x])^{3/2}} dx$$

Optimal (type 3, 175 leaves, 8 steps):

$$\frac{(i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{(i a - b)^{3/2} d} + \frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{(i a + b)^{3/2} d} + \frac{2 b (A b - a B) \sqrt{\tan[c + d x]}}{a (a^2 + b^2) d \sqrt{a + b \tan[c + d x]}}$$

Result (type 4, 5177 leaves):

$$\left( 4 i \cos\left[\frac{1}{2}(c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right. \\ \left. \left( (a A + b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right) \\ \operatorname{Sec}[c + d x] (a \cos[c + d x] + b \sin[c + d x]) \tan\left[\frac{1}{2}(c + d x)\right]^{3/2} \\ \left( \frac{a A \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 (a - i b) (a + i b) \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \frac{b B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 (a - i b) (a + i b) \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \frac{a A \cos[2(c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 (a - i b) (a + i b) \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \frac{b B \cos[2(c + d x)] \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 (a - i b) (a + i b) \sqrt{a \cos[c + d x] + b \sin[c + d x]}} \right)$$

$$\begin{aligned}
 & \frac{A b \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2(a-i b)(a+i b) \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} + \\
 & \left. \frac{a B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2(a-i b)(a+i b) \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right. \\
 & \left. - \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \operatorname{Tan}[c+d x]^{3/2} \right) \right) \right) \\
 & 2 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( (a A+b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & (a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+i b)(A-i B) \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)
 \end{aligned}$$

$$\begin{aligned} & \text{Sec}[c + d x]^{5/2} \text{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} - \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\ & \left. \left( (a A + b B) \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\ & \left. (a - i b) (A + i B) \text{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \right. \right. \\ & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A - i B) \text{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\ & \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sqrt{\text{Sec}[c + d x]} \Big/ \left( (a^2 + b^2) \right. \\ & \left. (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \right. \\ & \left. \sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]} \sqrt{\text{Tan}[c + d x]} \right) - \left( i a \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\ & \left. \left( (a A + b B) \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\ & \left. (a - i b) (A + i B) \text{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \right. \right. \\ & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A - i B) \text{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\ & \left. \left. i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sqrt{\text{Sec}[c + d x]} \Big/ \left( (a^2 + b^2) \right. \end{aligned}$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] - (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Big/ \\
 & \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\operatorname{Tan} [c + d x]} \right) + \\
 & \left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]} \right) \right) \\
 & 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a A + b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A + i B) \right. \\
 & \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \\
 & (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} -
 \end{aligned}$$

$$\left( 2 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\right. \right.$$

$$\left. \left( (a A+b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right. \right.$$

$$(a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a},\right.$$

$$i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-(a+i b)(A-i B)$$

$$\left. \left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \right)$$

$$\left. \sqrt{\operatorname{Sec}[c+d x]}(b \operatorname{Cos}[c+d x]-a \operatorname{Sin}[c+d x]) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^{3 / 2}}\right) /$$

$$\left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}(a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^{3 / 2} \sqrt{\operatorname{Tan}[c+d x]}\right)-$$

$$\left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}\right) \right)$$

$$4 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}$$

$$\left( (a A+b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-(a-i b)(A+i B) \right)$$



$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \\
 & (a + ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \sqrt{\sec[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right] \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + \right. \\
 & \left. \left(1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]} \right) \right) \right. \\
 & \left. 2i \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( (aA + bB) \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - ib)(A + iB) \right. \right. \\
 & \left. \left. \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. \left. (a + ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \left. \sec[c + dx]^{3/2} \sin[c + dx] \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) \right) \\
 & 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \sqrt{\sec [c + d x]} \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a A + b B) \sec \left[ \frac{1}{2} (c + d x) \right] \right)^2 / \right. \right. \\
 & \left. \left. \left( 4 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \right) + \\
 & \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \\
 & \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \\
 & \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{\tan [c + d x]} (a + b \tan [c + d x])^{3/2} \right) + \\
 & \left( \sec [c + d x] (a \cos [c + d x] + b \sin [c + d x])^2 \right. \\
 & \left( - \frac{2 b (-A b + a B)}{a^2 (a - i b) (a + i b)} + \right. \\
 & \left. \frac{2 (-A b^3 \sin [c + d x] + a b^2 B \sin [c + d x])}{a^2 (a - i b) (a + i b) (a \cos [c + d x] + b \sin [c + d x])} \right) \\
 & \left. \sqrt{\tan [c + d x]} (A + B \tan [c + d x]) \right) /
 \end{aligned}$$

$$\frac{d (A \cos [c + d x] + B \sin [c + d x])}{(a + b \tan [c + d x])^{3/2}}$$

**Problem 461: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \tan [c + d x]}{\tan [c + d x]^{3/2} (a + b \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 216 leaves, 9 steps):

$$\frac{(A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] - (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right]}{(i a - b)^{3/2} d} - \frac{(i a + b)^{3/2} d}{(i a + b)^{3/2} d}$$

$$\frac{2 A}{a d \sqrt{\tan [c + d x]} \sqrt{a + b \tan [c + d x]}} - \frac{2 b (a^2 A + 2 A b^2 - a b B) \sqrt{\tan [c + d x]}}{a^2 (a^2 + b^2) d \sqrt{a + b \tan [c + d x]}}$$

Result (type 4, 5187 leaves):

$$\left( 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left. - i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A + i B) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b) \right.$$

$$\left. (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\sec [c + d x] (a \cos [c + d x] + b \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2}$$

$$\left( -\frac{A b \csc [c + d x] \sqrt{\sec [c + d x]} \sqrt{\tan [c + d x]}}{2 (a - i b) (a + i b) \sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \right.$$

$$\begin{aligned}
 & \frac{a B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2(a-i b)(a+i b) \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} - \\
 & \frac{A b \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2(a-i b)(a+i b) \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} + \\
 & \frac{a B \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2(a-i b)(a+i b) \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} - \\
 & \frac{a A \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2(a-i b)(a+i b) \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} - \\
 & \left. \frac{b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2(a-i b)(a+i b) \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} \right) (A+B \operatorname{Tan}[c+d x]) \Big/ \\
 & \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right. \\
 & \left. - \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]} \operatorname{Tan}[c+d x]^{3/2} \right) \right) \right) \\
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( -i(A b-a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & (a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a+i b)(A-i B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec}[c + d x]^{5/2} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) \\
 & \left( -i (A b - a B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b) (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b) (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec}[c + d x]} \right) / \left( (a^2 + b^2) \right) \\
 & (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \\
 & \left( \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\tan[c + d x]} \right) - \left( a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( -i (A b - a B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$(a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right]\right],$$

$$\frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a + i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a},$$

$$i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\operatorname{Sec}[c + d x]} \Bigg/$$

$$\left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right.$$

$$\left. \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]} \sqrt{\operatorname{Tan}[c + d x]} \right) +$$

$$\left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} \right) \right)$$

$$3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( -i (A b - a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right]\right],$$

$$\frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a + i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a},$$

$$\begin{aligned}
 & \left( i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} - \\
 & \left( 2 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \right. \right. \\
 & \left. \left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \\
 & \left. (a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a} \right], \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a + i b) (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a} \right], i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \left. \sqrt{\operatorname{Sec} [c+dx]} (b \operatorname{Cos} [c+dx] - a \operatorname{Sin} [c+dx]) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2}} \right) / \\
 & \left( (a^2 + b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx])^{3/2} \sqrt{\operatorname{Tan} [c+dx]} \right) - \\
 & \left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]} \right) \right) \\
 & 4 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b) (A-i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c+d x]} \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} + \\
 & \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]} \right) \right) \\
 & 2 \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b) (A-i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)
 \end{aligned}$$



$$\begin{aligned}
 & \text{Sec}[c+d x]^{3/2} \text{Sin}[c+d x] \text{Tan}\left[\frac{1}{2}(c+d x)\right]^{3/2} + \\
 & \left( \frac{1}{\left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \text{Cos}[c+d x] + b \text{Sin}[c+d x]} \sqrt{\text{Tan}[c+d x]} \right)} \right) \\
 & 4 \text{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\text{Sec}[c+d x]} \left( - \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A b - a B) \text{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \text{Tan}\left[\frac{1}{2}(c+d x)\right]^{3/2} \right) \right) + \\
 & \left( i (a - i b) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A + i B) \text{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \right) / \left( 4 \left( 1 - i \text{Cot}\left[\frac{1}{2}(c+d x)\right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \text{Tan}\left[\frac{1}{2}(c+d x)\right]^{3/2} \right) - \\
 & \left( i (a + i b) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A - i B) \text{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \right) / \left( 4 \left( 1 + i \text{Cot}\left[\frac{1}{2}(c+d x)\right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \text{Tan}\left[\frac{1}{2}(c+d x)\right]^{3/2} \right) \\
 & \left. \text{Tan}\left[\frac{1}{2}(c+d x)\right]^{3/2} \sqrt{\text{Tan}[c+d x]} (a + b \text{Tan}[c+d x])^{3/2} \right) + \\
 & \left( \text{Sec}[c+d x] (a \text{Cos}[c+d x] + b \text{Sin}[c+d x])^2 \right. \\
 & \left( \frac{2 b^2 (-A b + a B)}{a^3 (a^2 + b^2)} - \frac{2 A \text{Cot}[c+d x]}{a^2} - \right. \\
 & \left. \frac{2 (-A b^4 \text{Sin}[c+d x] + a b^3 B \text{Sin}[c+d x])}{a^3 (a - i b) (a + i b) (a \text{Cos}[c+d x] + b \text{Sin}[c+d x])} \right)
 \end{aligned}$$

$$\left( \frac{\sqrt{\tan[c+dx]} (A+B \tan[c+dx])}{d (A \cos[c+dx] + B \sin[c+dx]) (a+b \tan[c+dx])^{3/2}} \right) /$$

**Problem 462: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \tan[c+dx]}{\tan[c+dx]^{5/2} (a+b \tan[c+dx])^{3/2}} dx$$

Optimal (type 3, 276 leaves, 10 steps):

$$\begin{aligned} & - \frac{(i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right]}{(i a - b)^{3/2} d} - \frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right]}{(i a + b)^{3/2} d} - \\ & \frac{2 A}{3 a d \tan[c+dx]^{3/2} \sqrt{a+b \tan[c+dx]}} + \frac{2 (4 A b - 3 a B)}{3 a^2 d \sqrt{\tan[c+dx]} \sqrt{a+b \tan[c+dx]}} + \\ & \frac{2 b (5 a^2 A b + 8 A b^3 - 3 a^3 B - 6 a b^2 B) \sqrt{\tan[c+dx]}}{3 a^3 (a^2 + b^2) d \sqrt{a+b \tan[c+dx]}} \end{aligned}$$

Result (type 4, 5247 leaves):

$$\begin{aligned} & - \left( \left( 4 i \cos\left[\frac{1}{2} (c+dx)\right] \right)^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2} (c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2} (c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\ & \left. \left( (a A + b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b) (A + i B) \right. \right. \\ & \left. \left. \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\ & \left. \left. (a + i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c+dx)\right]}}\right], \right. \right. \end{aligned}$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \text{Sec}[c + dx] (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])$$

$$\text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \left( -\frac{a A \text{Csc}[c + dx] \sqrt{\text{Sec}[c + dx]} \sqrt{\text{Tan}[c + dx]}}{2(a - ib)(a + ib) \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} - \right.$$

$$\frac{b B \text{Csc}[c + dx] \sqrt{\text{Sec}[c + dx]} \sqrt{\text{Tan}[c + dx]}}{2(a - ib)(a + ib) \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} -$$

$$\left. \frac{(a A \text{Cos}[2(c + dx)] \text{Csc}[c + dx] \sqrt{\text{Sec}[c + dx]} \sqrt{\text{Tan}[c + dx]})}{(2(a - ib)(a + ib) \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]})} - \right.$$

$$\left. \frac{(b B \text{Cos}[2(c + dx)] \text{Csc}[c + dx] \sqrt{\text{Sec}[c + dx]} \sqrt{\text{Tan}[c + dx]})}{(2(a - ib)(a + ib) \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]})} + \right.$$

$$\left. \frac{(A b \text{Csc}[c + dx] \sqrt{\text{Sec}[c + dx]} \text{Sin}[2(c + dx)] \sqrt{\text{Tan}[c + dx]})}{(2(a - ib)(a + ib) \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]})} - \right.$$

$$\left. \frac{(a B \text{Csc}[c + dx] \sqrt{\text{Sec}[c + dx]} \text{Sin}[2(c + dx)] \sqrt{\text{Tan}[c + dx]})}{(2(a - ib)(a + ib) \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]})} \right) (A + B \text{Tan}[c + dx]) \Big/$$

$$\left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right.$$

$$\left. \left( 1 \Big/ \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]} \text{Tan}[c + dx]^{3/2} \right) \right) \right)$$

$$2 i \text{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( (a A + b B) \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right.$$

$$\begin{aligned}
 & (a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \quad \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) (A - i B) \\
 & \quad \left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]\right) \\
 & \operatorname{Sec}[c + d x]^{5/2} \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^{3/2} + \left(i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right. \\
 & \quad \left. \left( (a A + b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \quad \left. \left. (a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \right. \right. \right. \\
 & \quad \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \\
 & \quad \left. \left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]\right) \sqrt{\operatorname{Sec}[c + d x]} \Big/ \\
 & \quad \left( (a^2 + b^2) (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right. \\
 & \quad \left. \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{\tan [c+d x]} \right) + \left( i a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( (a A + b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \\
 & \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c+d x]} \right) / \\
 & \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \cos [c+d x] + b \sin [c+d x]} \sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]} \sqrt{\tan [c+d x]} \right) - \\
 & \left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c+d x] + b \sin [c+d x]} \sqrt{\tan [c+d x]} \right) \right) \\
 & 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a A + b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]} + \right. \\
 & \left. \left( 2 i \operatorname{Cos}\left[\frac{1}{2} (c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right) \right. \\
 & \left. \left( (a A + b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & (a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \\
 & \left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \left. \sqrt{\operatorname{Sec}[c + d x]} (b \operatorname{Cos}[c + d x] - a \operatorname{Sin}[c + d x]) \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^{3/2}} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]} \right) + \\
 & \left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) \right) \\
 & 4 i \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a A + b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A - i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) \right) \\
 & 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( (a A + b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a+i b) (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \operatorname{Sec} [c+dx]^{3/2} \operatorname{Sin} [c+dx] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} - \\
 & \left( 1 / \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} [c+dx]} \right) \right) \\
 & 4 i \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\operatorname{Sec} [c+dx]} \left( - \left( \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (aA+bB) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right] \right)^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} \right) \right) + \\
 & \left( i (a-i b) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \left( 4 \left( 1-i \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right] \right) \right) \\
 & \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} \right) + \\
 & \left( i (a+i b) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A-i B) \operatorname{Sec} \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \left( 4 \left( 1+i \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right] \right) \right) \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} \right) \right)
 \end{aligned}$$





$$\int \frac{\text{Tan}[c + d x]^{3/2} (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 244 leaves, 9 steps):

$$\frac{(A + i B) \text{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right]}{(i a - b)^{5/2} d} + \frac{(A - i B) \text{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right]}{(i a + b)^{5/2} d} +$$

$$\frac{2 a (A b - a B) \sqrt{\text{Tan}[c + d x]}}{3 b (a^2 + b^2) d (a + b \text{Tan}[c + d x])^{3/2}} + \frac{2 (2 a^2 A b - 4 A b^3 + a^3 B + 7 a b^2 B) \sqrt{\text{Tan}[c + d x]}}{3 b (a^2 + b^2)^2 d \sqrt{a + b \text{Tan}[c + d x]}}$$

Result (type 4, 5635 leaves):

$$- \left( \left( 4 i \text{Cos}\left[\frac{1}{2} (c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right. \right.$$

$$\left. \left( (a^2 A - A b^2 + 2 a b B) \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \text{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B)$$

$$\left. \left. \text{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right)$$

$$\text{Sec}[c + d x]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2 \text{Tan}\left[\frac{1}{2} (c + d x)\right]^{3/2}$$

$$\left( -\frac{a^2 A \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\text{Tan}[c + d x]}}{2 (a - i b)^2 (a + i b)^2 \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} + \right.$$

$$\left. \frac{A b^2 \text{Csc}[c + d x] \sqrt{\text{Sec}[c + d x]} \sqrt{\text{Tan}[c + d x]}}{2 (a - i b)^2 (a + i b)^2 \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} - \right)$$

$$\begin{aligned}
 & \frac{a b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} - \\
 & \left( \frac{a^2 A \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} + \right. \\
 & \left( \frac{A b^2 \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} - \right. \\
 & \left( \frac{a b B \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left((a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} + \right. \\
 & \left( \frac{a A b \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left((a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} - \right. \\
 & \left( \frac{a^2 B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} + \right. \\
 & \left. \left( \frac{b^2 B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} \right) (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right. \\
 & \left. \left( \left( 2 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \right. \right. \\
 & \left. \left. \left( (a^2 A-A b^2+2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \right. \\
 & \left. \left. (a-i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right]\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \operatorname{Sec} [c + d x]^{5/2} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \operatorname{Tan} [c + d x]^{3/2} \right) + \\
 & \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right] \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sqrt{\operatorname{Sec} [c + d x]} \right) / \\
 & \left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\operatorname{Tan} [c + d x]} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( i a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A + i B) \right. \\
 & \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \\
 & (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \sqrt{\operatorname{Sec}[c+dx]} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \sqrt{\operatorname{Tan}[c+dx]} \right) - \\
 & \left( 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \sqrt{\sec[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]} \right) + \\
 & \left( 2 i \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \\
 & \left. (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \left. \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos[c + dx] + b \sin[c + dx])^{3/2} \sqrt{\tan[c + dx]} \right) + \\
 & \left( 4 i \cos\left[\frac{1}{2}(c + dx)\right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right) \\
 & \left. \sqrt{\sec[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right] \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]} \right) - \\
 & \left( 2 i \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right]}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i\right.$$

$$\left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a + i b)^2 (A - i B) \right.$$

$$\left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)$$

$$\left. \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) /$$

$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} \right) -$$

$$\left( 4 i \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{\operatorname{Sec}[c+dx]} \left( - \left( \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a^2 A - A b^2 + 2 a b B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \right.$$

$$\left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \right) +$$

$$\left( i (a - i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) /$$



$$\begin{aligned}
 & \left( 4 \left( 1 - i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \right. \\
 & \quad \left. \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) / \\
 & \quad \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} \right) \\
 & \quad \left. \sqrt{\operatorname{Tan}[c + d x]} (a + b \operatorname{Tan}[c + d x])^{5/2} \right) + \\
 & \left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right. \\
 & \quad \left( \frac{2 (3 a^2 A - 4 A b^2 + 7 a b B)}{3 a (a - i b)^2 (a + i b)^2} - \right. \\
 & \quad \frac{2 a b (-A b + a B)}{3 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2} + \\
 & \quad \left. \left. (2 (-4 a^2 A b \operatorname{Sin}[c + d x] + 4 A b^3 \operatorname{Sin}[c + d x] + a^3 B \operatorname{Sin}[c + d x] - 7 a b^2 B \operatorname{Sin}[c + d x])) / \right. \right. \\
 & \quad \left. \left. (3 a (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])) \right) \right) \\
 & \quad \left. \sqrt{\operatorname{Tan}[c + d x]} (A + B \operatorname{Tan}[c + d x]) \right) / (d \\
 & \quad (A \operatorname{Cos}[c + d x] + \\
 & \quad B \operatorname{Sin}[c + d x]) \\
 & \quad (a + b \operatorname{Tan}[c + d x])^{5/2})
 \end{aligned}$$

Problem 465: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\tan [c+d x]} (A+B \tan [c+d x])}{(a+b \tan [c+d x])^{5 / 2}} d x$$

Optimal (type 3, 244 leaves, 9 steps):

$$\begin{aligned} & -\frac{(i A-B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{(i a-b)^{5 / 2} d}+\frac{(i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{(i a+b)^{5 / 2} d}- \\ & \frac{2(A b-a B) \sqrt{\tan [c+d x]}}{3\left(a^2+b^2\right) d(a+b \tan [c+d x])^{3 / 2}}-\frac{2\left(5 a^2 A b-A b^3-2 a^3 B+4 a b^2 B\right) \sqrt{\tan [c+d x]}}{3 a\left(a^2+b^2\right)^2 d \sqrt{a+b \tan [c+d x]}} \end{aligned}$$

Result (type 4, 5639 leaves):

$$\begin{aligned} & -\left(\left(4 \cos \left[\frac{1}{2}(c+d x)\right]\right)^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\right. \\ & \left.\left(i\left(-2 a A b+a^2 B-b^2 B\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right. \right. \\ & \left.\left.(a-i b)^2(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a},\right.\right. \right. \\ & \left.\left.\left.i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(a+i b)^2(A-i B) \right. \right. \\ & \left.\left.\left.\operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right)\right) \right) \\ & \operatorname{Sec}[c+d x]^2(a \cos [c+d x]+b \sin [c+d x])^2 \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2} \\ & \left(\frac{a A b \csc [c+d x] \sqrt{\sec [c+d x]} \sqrt{\tan [c+d x]}}{(a-i b)^2(a+i b)^2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}}-\right. \end{aligned}$$

$$\begin{aligned}
 & \frac{a^2 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \frac{b^2 B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \left( \frac{a A b \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{\left( (a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right)} - \right. \\
 & \left( \frac{a^2 B \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{\left( 2(a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right)} + \right. \\
 & \left( \frac{b^2 B \operatorname{Cos}[2(c+dx)] \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}}{\left( 2(a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right)} + \right. \\
 & \left( \frac{a^2 A \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{\left( 2(a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right)} - \right. \\
 & \left( \frac{A b^2 \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{\left( 2(a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right)} + \right. \\
 & \left. \left( \frac{a b B \operatorname{Csc}[c+dx] \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[2(c+dx)] \sqrt{\operatorname{Tan}[c+dx]}}{\left( 2(a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right)} \right) \right) \left( A + B \operatorname{Tan}[c+dx] \right) \Bigg/ \\
 & \left( (a-ib)^2(a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right) \Bigg/ \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right) \\
 & \left( \left( 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right)^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \right. \\
 & \left. \left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \right) \operatorname{Sec}[c + dx]^{5/2} \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} \Big/ \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \tan[c + dx]^{3/2} + \right. \\
 & \left. a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right) \\
 & \left( i(-2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \\
 & \left. \left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \sqrt{\operatorname{Sec}[c + dx]} \Big/ \\
 & \left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) + \\
 & \left( a \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\left(i(-2 a A b+a^2 B-b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-(a-i b)^2(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(a+i b)^2(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \sqrt{\sec [c+d x]} \right) / \\
 & \left( \left(a^2+b^2\right)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}\left(b+\sqrt{a^2+b^2}\right) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\right. \\
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \sqrt{\tan [c+d x]} \right) - \\
 & \left( 3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\right)
 \end{aligned}$$

$$\left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a-i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \left. \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]} \right) /$$

$$\left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]} \right) +$$

$$\left( 2 \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \right)$$

$$\left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a-i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b)^2 (A-i B) \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \left. \sqrt{\text{Sec} [c + d x]} \left( b \text{Cos} [c + d x] - a \text{Sin} [c + d x] \right) \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \left( a \text{Cos} [c + d x] + b \text{Sin} [c + d x] \right)^{3/2} \sqrt{\text{Tan} [c + d x]} \right) + \\
 & \left( 4 \text{Cos} \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{1 + b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( i \left( -2 a A b + a^2 B - b^2 B \right) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a - i b)^2 (A + i B) \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \right. \right. \\
 & \left. \left. \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^2 (A - i B) \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right. \\
 & \left. \sqrt{\text{Sec} [c + d x]} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) /
 \end{aligned}$$

$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) -$$

$$\left( 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right.$$

$$\left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^2 (A - i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\left. \operatorname{Sec} [c + d x]^{3/2} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) /$$

$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) -$$

$$\left( 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left. \sqrt{\operatorname{Sec} [c + d x]} \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (-2 a A b + a^2 B - b^2 B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) /$$



$$\begin{aligned}
 & \left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) + \\
 & \left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
 & \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) - \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \left. \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} \right) \\
 & \left. \left. \sqrt{\operatorname{Tan}[c+dx]} (a + b \operatorname{Tan}[c+dx])^{5/2} \right) \right) + \\
 & \left( \operatorname{Sec}[c+dx]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^3 \right. \\
 & \left. \frac{2(-6a^2Ab + Ab^3 + 3a^3B - 4ab^2B)}{3a^2(a - ib)^2(a + ib)^2} + \frac{2b^2(-Ab + aB)}{3(a - ib)^2(a + ib)^2(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2} \right. \\
 & \left. \left. (2(-7a^2Ab^2 \operatorname{Sin}[c+dx] + Ab^4 \operatorname{Sin}[c+dx] + 4a^3bB \operatorname{Sin}[c+dx] - 4ab^3B \operatorname{Sin}[c+dx])) \right) \right) / \\
 & \left( 3a^2(a - ib)^2(a + ib)^2(a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) \right)
 \end{aligned}$$

$$\left. \sqrt{\tan [c+d x]} (A+B \tan [c+d x]) \right) / \left( d \right. \\ \left. (A \cos [c+d x] + \right. \\ \left. B \sin [c+d x]) \right. \\ \left. (a+b \tan [c+d x])^{5/2} \right)$$

**Problem 466: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \tan [c+d x]}{\sqrt{\tan [c+d x]} (a+b \tan [c+d x])^{5/2}} dx$$

Optimal (type 3, 247 leaves, 9 steps):

$$-\frac{(A+i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{(i a-b)^{5/2} d}-\frac{(A-i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{(i a+b)^{5/2} d}+ \\ \frac{2 b(A b-a B) \sqrt{\tan [c+d x]}}{3 a\left(a^2+b^2\right) d(a+b \tan [c+d x])^{3/2}}+\frac{2 b\left(8 a^2 A b+2 A b^3-5 a^3 B+a b^2 B\right) \sqrt{\tan [c+d x]}}{3 a^2\left(a^2+b^2\right)^2 d \sqrt{a+b \tan [c+d x]}}$$

Result (type 4, 5654 leaves):

$$\left( 4 i \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \right. \\ \left. \left( a^2 A-A b^2+2 a b B \right) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]- \right. \\ \left. (a-i b)^2 (A+i B) \operatorname{EllipticPi}\left[ -\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \right. \\ \left. \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]- (a+i b)^2 (A-i B) \right. \\ \left. \operatorname{EllipticPi}\left[ \frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\begin{aligned} & \text{Sec}[c+dx]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \\ & \left( \frac{a^2 A \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} - \right. \\ & \quad \frac{A b^2 \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} + \\ & \quad \frac{a b B \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}[c+dx]}}{(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} + \\ & \quad \frac{a^2 A \text{Cos}[2(c+dx)] \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} - \\ & \quad \frac{A b^2 \text{Cos}[2(c+dx)] \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} + \\ & \quad \frac{a b B \text{Cos}[2(c+dx)] \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}[c+dx]}}{(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} - \\ & \quad \frac{a A b \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \text{Sin}[2(c+dx)] \sqrt{\text{Tan}[c+dx]}}{(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} + \\ & \quad \frac{a^2 B \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \text{Sin}[2(c+dx)] \sqrt{\text{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} - \\ & \quad \left. \frac{b^2 B \text{Csc}[c+dx] \sqrt{\text{Sec}[c+dx]} \text{Sin}[2(c+dx)] \sqrt{\text{Tan}[c+dx]}}{2(a-ib)^2(a+ib)^2 \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} \right) (A+B \text{Tan}[c+dx]) \Big/ \end{aligned}$$

$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \text{Cos}[c+dx] + B \text{Sin}[c+dx]) \right)$$

$$\left( - \left( \left( 2 i \text{Cos}\left[\frac{1}{2}(c+dx)\right] \right)^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \right)$$

$$\left( (a^2 A - A b^2 + 2 a b B) \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right)$$

$$\begin{aligned}
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\left] \operatorname{Sec}[c + dx]^{5/2} \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \tan[c + dx]^{3/2} \right) - \\
 & \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( a^2 A - A b^2 + 2 a b B \right) \right. \\
 & \left. \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 (A + i B) \right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & \left. (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \sqrt{\operatorname{Sec}[c + dx]} \left) / \left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \\
 & \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} \sqrt{\tan[c + dx]} \left) - \left( i a \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \right. \\
 & \left. \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}} \right] \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec[c + dx]} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} \sqrt{\tan[c + dx]} \right) + \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]} \right) \right) \\
 & 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) -$$

$$(a-ib)^2 (A+ib) \operatorname{EllipticPi}\left[-\frac{ib+\sqrt{a^2+b^2}}{a}, \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right],$$

$$\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^2 (A-ib) \operatorname{EllipticPi}\left[\frac{ib+\sqrt{a^2+b^2}}{a},$$

$$\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} -$$

$$\left( 2ib \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}}\right)$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) -$$

$$(a-ib)^2 (A+ib) \operatorname{EllipticPi}\left[-\frac{ib+\sqrt{a^2+b^2}}{a},$$

$$\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) - (a+ib)^2 (A-ib)$$

$$\operatorname{EllipticPi}\left[\frac{ib+\sqrt{a^2+b^2}}{a}, \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right)$$

$$\begin{aligned}
 & \left. \sqrt{\sec [c+d x]} (b \cos [c+d x]-a \sin [c+d x]) \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}\right\} / \\
 & \left( \left(a^2+b^2\right)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \cos [c+d x]+b \sin [c+d x])^{3 / 2} \sqrt{\tan [c+d x]}\right)- \\
 & \left(1 / \left(\left(a^2+b^2\right)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}\right)\right) \\
 & 4 i \cos \left[\frac{1}{2}(c+d x)\right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \left( \left(a^2 A-A b^2+2 a b B\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- \right. \\
 & \left. (a-i b)^2(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}\right], \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\left(a+i b\right)^2(A-i B) \\
 & \left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}\right], i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \\
 & \sqrt{\sec [c+d x]} \sin \left[\frac{1}{2}(c+d x)\right] \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}+ \\
 & \left(1 / \left(\left(a^2+b^2\right)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan [c+d x]}\right)\right) \\
 & 2 i \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a-i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^2 (A-i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \operatorname{Sec} [c+d x]^{3/2} \operatorname{Sin} [c+d x] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} + \\
 & \left( 1 / \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]} \sqrt{\operatorname{Tan} [c+d x]} \right) \right) \\
 & 4 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\operatorname{Sec} [c+d x]} \left( - \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a^2 A - A b^2 + 2 a b B) \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) \right) + \\
 & \left( i (a-i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \left( 1-i \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right] \right) \right) \\
 & \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} +
 \end{aligned}$$



$$\begin{aligned}
 & \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \sqrt{\operatorname{Tan}[c + d x]} (a + b \operatorname{Tan}[c + d x])^{5/2} \right) + \\
 & \left( \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \right. \\
 & \left( -\frac{2 b (-9 a^2 A b - 2 A b^3 + 6 a^3 B - a b^2 B)}{3 a^3 (a - i b)^2 (a + i b)^2} - \right. \\
 & \left. \frac{2 b^3 (-A b + a B)}{3 a (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2} + \right. \\
 & \left. \left. \frac{2 (-10 a^2 A b^3 \operatorname{Sin}[c + d x] - 2 A b^5 \operatorname{Sin}[c + d x] + 7 a^3 b^2 B \operatorname{Sin}[c + d x] - a b^4 B \operatorname{Sin}[c + d x])}{3 a^3 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])} \right) \right) / \\
 & \left. \sqrt{\operatorname{Tan}[c + d x]} (A + B \operatorname{Tan}[c + d x]) \right) / \\
 & \left( \frac{d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^{5/2}} \right)
 \end{aligned}$$

**Problem 467:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Tan}[c + d x]}{\operatorname{Tan}[c + d x]^{3/2} (a + b \operatorname{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 301 leaves, 10 steps):

$$\frac{(i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{(i a - b)^{5/2} d} - \frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right]}{(i a + b)^{5/2} d} -$$

$$\frac{2 A}{a d \sqrt{\tan[c + d x]} (a + b \tan[c + d x])^{3/2}} - \frac{2 b (3 a^2 A + 4 A b^2 - a b B) \sqrt{\tan[c + d x]}}{3 a^2 (a^2 + b^2) d (a + b \tan[c + d x])^{3/2}} -$$

$$\frac{2 b (3 a^4 A + 17 a^2 A b^2 + 8 A b^4 - 8 a^3 b B - 2 a b^3 B) \sqrt{\tan[c + d x]}}{3 a^3 (a^2 + b^2)^2 d \sqrt{a + b \tan[c + d x]}}$$

Result (type 4, 5666 leaves):

$$\left( 4 \cos\left[\frac{1}{2}(c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}}\right.$$

$$\left. \left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right]}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right.$$

$$\left. (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a + i b)^2 (A - i B) \right.$$

$$\left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right)$$

$$\operatorname{Sec}[c + d x]^2 (a \cos[c + d x] + b \sin[c + d x])^2 \tan\left[\frac{1}{2}(c + d x)\right]^{3/2}$$

$$\left( -\frac{a A b \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{(a - i b)^2 (a + i b)^2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \right.$$

$$\frac{a^2 B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 (a - i b)^2 (a + i b)^2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} -$$

$$\frac{b^2 B \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\tan[c + d x]}}{2 (a - i b)^2 (a + i b)^2 \sqrt{a \cos[c + d x] + b \sin[c + d x]}} -$$

$$\begin{aligned}
 & \frac{a A b \cos [2 (c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{(a-i b)^2 (a+i b)^2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \\
 & \frac{a^2 B \cos [2 (c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2 (a-i b)^2 (a+i b)^2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} - \\
 & \frac{b^2 B \cos [2 (c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{2 (a-i b)^2 (a+i b)^2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} - \\
 & \frac{a^2 A \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sin [2 (c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2 (a-i b)^2 (a+i b)^2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \\
 & \frac{A b^2 \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sin [2 (c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{2 (a-i b)^2 (a+i b)^2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} - \\
 & \left. \frac{a b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sin [2 (c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{(a-i b)^2 (a+i b)^2 \sqrt{a \cos [c+d x]+b \sin [c+d x]}} (A+B \operatorname{Tan}[c+d x]) \right) / \\
 & \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \cos [c+d x]+B \sin [c+d x]) \right. \\
 & \left. - \left( \left( 2 \cos \left[ \frac{1}{2} (c+d x) \right] \right)^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \right. \right. \right. \\
 & \left. \left. \left( i (-2 a A b+a^2 B-b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \right. \\
 & \left. \left. (a-i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \right. \right. \right.
 \end{aligned}$$

$$\left( \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}, \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \sec[c+dx]^{5/2} \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} /$$

$$\left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \tan[c+dx]^{3/2} \right) -$$

$$\left( a \sqrt{\frac{b+\sqrt{a^2+b^2} + a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right) \left( i(-2aAb + a^2B - b^2B) \right.$$

$$\text{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-ib)^2 (A+ib) \right.$$

$$\text{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] +$$

$$(a+ib)^2 (A-ib) \text{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec[c+dx]} / \left( (a^2+b^2)^2 (b-\sqrt{a^2+b^2}) \right.$$

$$\left. \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \right)$$

$$\begin{aligned}
 & \left( \sqrt{\tan\left[\frac{1}{2}(c+dx)\right]} \sqrt{\tan[c+dx]} \right) - \left( a \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( i(-2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - ib)^2 (A + iB) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + ib)^2 (A - iB) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec[c+dx]} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\tan\left[\frac{1}{2}(c+dx)\right]} \sqrt{\tan[c+dx]} \right) + \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\tan[c+dx]} \right) \right) \\
 & 3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( i(-2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\operatorname{Sec}[c + dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]} - \\
 & \left( 2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( i(-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a + i b)^2 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right) \\
 & \left. \sqrt{\operatorname{Sec}[c + dx]} (b \operatorname{Cos}[c + dx] - a \operatorname{Sin}[c + dx]) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2}} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]} \right) - \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) \right) \\
 & 4 \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^2 (A - i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) \right) \\
 & 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.
 \end{aligned}$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a + i b)^2 (A - i B)$$

$$\operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right]$$

$$\operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} +$$

$$\left( 4 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right)$$

$$\sqrt{\operatorname{Sec} [c + d x]} \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (-2 a A b + a^2 B - b^2 B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right)$$

$$\left( 4 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) +$$

$$\left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right)$$

$$\sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} -$$

$$\left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) /$$

$$\left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right)$$

$$\sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} /$$



$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]} \right) \left( \sqrt{\tan[c + dx]} (a + b \tan[c + dx])^{5/2} \right) + \left( \sec[c + dx]^2 (a \cos[c + dx] + b \sin[c + dx])^3 \left( \frac{2b^2(-12a^2Ab - 5Ab^3 + 9a^3B + 2ab^2B)}{3a^4(a - ib)^2(a + ib)^2} - \frac{2A \cot[c + dx]}{a^3} + \frac{2b^4(-Ab + aB)}{3a^2(a - ib)^2(a + ib)^2(a \cos[c + dx] + b \sin[c + dx])^2} - (2(-13a^2Ab^4 \sin[c + dx] - 5Ab^6 \sin[c + dx] + 10a^3b^3B \sin[c + dx] + 2ab^5B \sin[c + dx])) / (3a^4(a - ib)^2(a + ib)^2(a \cos[c + dx] + b \sin[c + dx])) \right) \right) \left( \sqrt{\tan[c + dx]} (A + B \tan[c + dx]) \right) / \left( d (A \cos[c + dx] + B \sin[c + dx]) (a + b \tan[c + dx])^{5/2} \right)$$

**Problem 468: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \tan[c + dx]}{\tan[c + dx]^{5/2} (a + b \tan[c + dx])^{5/2}} dx$$

Optimal (type 3, 359 leaves, 11 steps):

$$\frac{(A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{(i a - b)^{5/2} d} + \frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right]}{(i a + b)^{5/2} d} -$$

$$\frac{2 A}{3 a d \operatorname{Tan}[c + d x]^{3/2} (a + b \operatorname{Tan}[c + d x])^{3/2}} + \frac{2 (2 A b - a B)}{a^2 d \sqrt{\operatorname{Tan}[c + d x]} (a + b \operatorname{Tan}[c + d x])^{3/2}} +$$

$$\frac{2 b (7 a^2 A b + 8 A b^3 - 3 a^3 B - 4 a b^2 B) \sqrt{\operatorname{Tan}[c + d x]}}{3 a^3 (a^2 + b^2) d (a + b \operatorname{Tan}[c + d x])^{3/2}} +$$

$$\frac{(2 b (8 a^4 A b + 30 a^2 A b^3 + 16 A b^5 - 3 a^5 B - 17 a^3 b^2 B - 8 a b^4 B) \sqrt{\operatorname{Tan}[c + d x]})}{(3 a^4 (a^2 + b^2)^2 d \sqrt{a + b \operatorname{Tan}[c + d x]})}$$

Result (type 4, 5723 leaves):

$$- \left( \left( 4 i \operatorname{Cos}\left[\frac{1}{2} (c + d x)\right]\right)^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B)$$

$$\left. \left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right)$$

$$\operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^{3/2}$$

$$\left( -\frac{a^2 A \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 (a - i b)^2 (a + i b)^2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \right.$$

$$\left. \frac{A b^2 \operatorname{Csc}[c + d x] \sqrt{\operatorname{Sec}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{2 (a - i b)^2 (a + i b)^2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \right)$$

$$\begin{aligned}
 & \frac{a b B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}} - \\
 & \left( \frac{a^2 A \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} + \right. \\
 & \left( \frac{A b^2 \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} - \right. \\
 & \left( \frac{a b B \operatorname{Cos}[2(c+d x)] \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{\left((a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} + \right. \\
 & \left( \frac{a A b \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left((a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} - \right. \\
 & \left( \frac{a^2 B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} + \right. \\
 & \left. \left. \left( \frac{b^2 B \operatorname{Csc}[c+d x] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[2(c+d x)] \sqrt{\operatorname{Tan}[c+d x]}}{\left(2(a-i b)^2 (a+i b)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)} \right) (A+B \operatorname{Tan}[c+d x]) \right) \right) / \\
 & \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) \right. \\
 & \left. \left( \left( 2 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \right. \right. \\
 & \left. \left. \left( (a^2 A-A b^2+2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \right. \\
 & \left. \left. (a-i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right]\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \operatorname{Sec} [c + d x]^{5/2} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \Big/ \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \operatorname{Tan} [c + d x]^{3/2} \right) + \\
 & \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sqrt{\operatorname{Sec} [c + d x]} \Big/ \\
 & \left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\operatorname{Tan} [c + d x]} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left( i a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A + i B) \right. \\
 & \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \\
 & (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \sqrt{\operatorname{Sec}[c+dx]} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \sqrt{\operatorname{Tan}[c+dx]} \right) - \\
 & \left( 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \sqrt{\sec[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]} \right) + \\
 & \left( 2 i \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right) \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \\
 & \left. (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \left. \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{\tan [c + d x]} \right) + \\
 & \left( 4 i \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \\
 & \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \left. \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) - \\
 & \left( 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}, \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \right.$$

$$\left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a + i b)^2 (A - i B) \right.$$

$$\left. \left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \right)$$

$$\left. \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx] \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) /$$

$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\tan[c+dx]} \right) -$$

$$\left( 4 i \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right)$$

$$\sqrt{\operatorname{Sec}[c+dx]} \left( - \left( \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a^2 A - A b^2 + 2 a b B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) /$$

$$\left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \right) +$$

$$\left( i (a - i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) /$$



$$\begin{aligned}
 & \left( 4 \left( 1 - i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) / \\
 & \quad \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan [c + d x]} \right) \\
 & \quad \left. \sqrt{\tan [c + d x]} (a + b \tan [c + d x])^{5/2} \right) + \\
 & \left( \sec [c + d x]^2 (a \cos [c + d x] + b \sin [c + d x])^3 \right. \\
 & \quad \left( \frac{2 (a^6 A + 2 a^4 A b^2 + 16 a^2 A b^4 + 8 A b^6 - 12 a^3 b^3 B - 5 a b^5 B)}{3 a^5 (a - i b)^2 (a + i b)^2} - \right. \\
 & \quad \frac{2 (-8 A b \cos [c + d x] + 3 a B \cos [c + d x]) \csc [c + d x]}{3 a^4} - \\
 & \quad \frac{2 A \csc [c + d x]^2}{3 a^3} - \\
 & \quad \left. \frac{2 b^5 (-A b + a B)}{3 a^3 (a - i b)^2 (a + i b)^2 (a \cos [c + d x] + b \sin [c + d x])^2} + \right. \\
 & \quad \left. \frac{2 (-16 a^2 A b^5 \sin [c + d x] - 8 A b^7 \sin [c + d x] + 13 a^3 b^4 B \sin [c + d x] + 5 a b^6 B \sin [c + d x])}{3 a^5 (a - i b)^2 (a + i b)^2 (a \cos [c + d x] + b \sin [c + d x])} \right) \\
 & \quad \left. \sqrt{\tan [c + d x]} (A + B \tan [c + d x]) \right) / (d
 \end{aligned}$$

$$\left( A \cos [c + d x] + B \sin [c + d x] \right) (a + b \tan [c + d x])^{5/2}$$

**Problem 469: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\tan [c + d x]^{3/2} (a B + b B \tan [c + d x])}{(a + b \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 155 leaves, 13 steps):

$$-\frac{B \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{\sqrt{i a-b} d} + \frac{2 B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{\sqrt{b} d} - \frac{B \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right]}{\sqrt{i a+b} d}$$

Result (type 4, 6091 leaves):

$$\left( 4 \sqrt{a^2 + b^2} B \left( \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \right. \right. \\ \left. \left( -a + b + \sqrt{a^2 + b^2} \right) + \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) + \right. \\ \left. \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) - \frac{1}{a + b + \sqrt{a^2 + b^2}} \right. \\ \left. \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right)$$

$$\begin{aligned}
 & \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec^2[c+dx]} \sqrt{\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2 + b^2}} \\
 & \left. \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}} \tan[c+dx]} \right/ \\
 & \left( d \sqrt{\sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{a + b \tan[c+dx]}} \right. \\
 & \left. - \left( 1 / \left( \sqrt{\sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{a \cos[c+dx] + b \sin[c+dx]} \tan[c+dx]^{3/2}} \right) \right) 2 \sqrt{a^2 + b^2} \right) \\
 & \left( \text{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / (-a + \right. \\
 & \left. b + \sqrt{a^2 + b^2}) + \text{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \right. \\
 & \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / (a + i (b + \sqrt{a^2 + b^2})) + \text{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \text{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / (a - i (b + \sqrt{a^2 + b^2})) -
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/ \\
 & \left( a + b + \sqrt{a^2 + b^2} \right) \text{Sec} [c + d x]^2 \sqrt{\text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \text{Sec} [c + d x]} \\
 & \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos} [c + d x] + b \text{Sin} [c + d x])}{a^2 + b^2}} \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} + \\
 & \left( a \sqrt{a^2 + b^2} \left( \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \\
 & \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/ \left( -a + b + \sqrt{a^2 + b^2} \right) + \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/ \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) + \\
 & \left. \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/ \\
 & \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) - \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/ \left( a + b + \sqrt{a^2 + b^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\sec\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]} \\
 & \sqrt{\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2 + b^2}} \Big/ \\
 & \left( (b + \sqrt{a^2 + b^2}) \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\tan[c+dx]} \right) - \\
 & \left( 2\sqrt{a^2 + b^2} \left[ \text{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \right. \right. \\
 & \left. \left. \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ (-a + b + \sqrt{a^2 + b^2}) + \text{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ (a + i (b + \sqrt{a^2 + b^2})) \right) + \\
 & \left( \text{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \right. \\
 & \left. (a - i (b + \sqrt{a^2 + b^2})) \right) - \text{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \left. \text{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ (a + b + \sqrt{a^2 + b^2}) \right) \\
 & \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]} (b \cos[c+dx] - a \sin[c+dx])
 \end{aligned}$$

$$\left. \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{a^2 + b^2}} \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right/$$

$$\left( \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^{3/2} \sqrt{\operatorname{Tan}[c+dx]}} \right) -$$

$$\frac{1}{\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]}} 2 \sqrt{a^2 + b^2} \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]$$

$$\left( \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right/$$

$$\left( -a + b + \sqrt{a^2 + b^2} \right) + \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \left/ \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) \right) +$$

$$\operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \left/$$

$$\left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) - \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \left/ \left( a + b + \sqrt{a^2 + b^2} \right) \right)$$

$$\sqrt{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}$$

$$\begin{aligned}
 & \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{a^2 + b^2}} \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} + \\
 & \left( 2 \sqrt{a^2 + b^2} \left( \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right. \right. \\
 & \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \left( -a + b + \sqrt{a^2 + b^2} \right) + \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) + \\
 & \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \\
 & \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) - \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \\
 & \left( \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx] \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (b \operatorname{Cos}[c+dx] - a \operatorname{Sin}[c+dx])}{a^2 + b^2} + \frac{1}{a^2 + b^2} \right. \\
 & \left. \left. a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{\sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} \right. \\
 & \left. \sqrt{\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2 + b^2}} \sqrt{\tan[c+dx]} \right) + \\
 & \left( 1 / \left( \sqrt{\sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} \sqrt{\tan[c+dx]} \right) \right) \\
 & 4 \sqrt{a^2 + b^2} \sqrt{\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]} \\
 & \sqrt{\frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2 + b^2}} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \left( - \left( \left( a \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (-a + b + \sqrt{a^2 + b^2}) \right) \right. \right. \\
 & \left. \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{2 \sqrt{a^2 + b^2}}} \right. \right. \\
 & \left. \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{-a + b + \sqrt{a^2 + b^2}} \right) \right) \right) - \\
 & \left( a \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (a + i (b + \sqrt{a^2 + b^2})) \right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{2 \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{-i a + b + \sqrt{a^2 + b^2}} \right) \right) - \\
 & \left( a \sec\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (a - i (b + \sqrt{a^2 + b^2})) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(a \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]\right)^2 \Bigg/ \left(4\sqrt{2}\sqrt{a^2 + b^2} \left(a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}}\right) \Bigg) \Bigg) + \\
 & \left(2\sqrt{a^2 + b^2} \left(\operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right]\right), \right. \\
 & \left. \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \Bigg/ \left(-a + b + \sqrt{a^2 + b^2}\right) + \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \Bigg/ \left(a + i \left(b + \sqrt{a^2 + b^2}\right)\right) + \right. \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \Bigg/ \right. \right. \\
 & \left. \left. \left(a - i \left(b + \sqrt{a^2 + b^2}\right)\right) - \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.
 \end{aligned}$$

$$\left. \begin{aligned} & \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + b + \sqrt{a^2 + b^2} \right) \\ & \sqrt{\frac{a \sec\left[\frac{1}{2}(c + dx)\right]^2 (a \cos[c + dx] + b \sin[c + dx])}{a^2 + b^2}} \sqrt{\frac{a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\ & \left( -\cos\left[\frac{1}{2}(c + dx)\right] \sec[c + dx] \sin\left[\frac{1}{2}(c + dx)\right] + \right. \\ & \left. \cos\left[\frac{1}{2}(c + dx)\right]^2 \sec[c + dx] \tan[c + dx] \right) / \\ & \left( \sqrt{\sec\left[\frac{1}{2}(c + dx)\right]^2} \sqrt{\cos\left[\frac{1}{2}(c + dx)\right]^2 \sec[c + dx]} \right. \\ & \left. \left. \sqrt{a \cos[c + dx] + b \sin[c + dx]} \sqrt{\tan[c + dx]} \right) \right) \end{aligned} \right)$$

**Problem 470: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\tan[c + dx]} (a B + b B \tan[c + dx])}{(a + b \tan[c + dx])^{3/2}} dx$$

Optimal (type 3, 117 leaves, 8 steps):

$$\frac{i B \text{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan[c + dx]}}{\sqrt{a + b \tan[c + dx]}} \right]}{\sqrt{i a - b} d} - \frac{i B \text{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan[c + dx]}}{\sqrt{a + b \tan[c + dx]}} \right]}{\sqrt{i a + b} d}$$

Result (type 4, 2767 leaves):

$$\begin{aligned}
 & \left( 2 B \left( \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \quad \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \quad \sqrt{\sec [c + d x]} \sin [c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( d \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]} \right. \\
 & \quad \left. - \left( \left( \left( \left( \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \right) \right) \\
 & \quad \sec [c + d x]^{5/2} \sin [c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \quad \left( \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]} \tan [c + d x]^{3/2} \right) + \\
 & \quad \left( a \left( \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \quad \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \quad \sec \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\sec [c + d x]} \sin [c + d x] \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 \left( -b + \sqrt{a^2 + b^2} \right) \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{-b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Tan}[c + d x]} \right) - \\
 & \left( \left( \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right. \\
 & \left. \sqrt{\operatorname{Sec}[c + d x]} \sin [c + d x] (b \cos [c + d x] - a \sin [c + d x]) \sqrt{1 + \frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{-b + \sqrt{a^2 + b^2}}} \right) / \\
 & \left( (a \cos [c + d x] + b \sin [c + d x])^{3/2} \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}} \sqrt{\operatorname{Tan}[c + d x]} \right) + \\
 & \left( 2 \left( \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{-b + \sqrt{a^2 + b^2}}} \right) / \left( \sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right. \\
 & \left. \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}} \sqrt{\operatorname{Tan}[c + d x]} \right) + \\
 & \left( \left( \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]^2 \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( \sqrt{a \cos[c + d x] + b \sin[c + d x]} \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{\tan[c + d x]} \right) - \\
 & \left( \left( \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \\
 & \left( -\frac{a^2 \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]}{2 (b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right])^2} - \frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 (b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right])} \right) \Big/ \\
 & \left( \sqrt{a \cos[c + d x] + b \sin[c + d x]} \left( -\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]} \right)^{3/2} \sqrt{\tan[c + d x]} \right) + \\
 & \left( 2 \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \right) \\
 & \left( \left( i a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Big/ \left( 4 (b + \sqrt{a^2 + b^2}) \left( 1 - i \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \\
 & \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \Big) -
 \end{aligned}$$

$$\left( i a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( b + \sqrt{a^2 + b^2} \right) \left( 1 + i \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \\ \left. \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right) \right) / \\ \left( \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right. \\ \left. \sqrt{\operatorname{Tan}[c+dx]} \sqrt{a + b \operatorname{Tan}[c+dx]} \right)$$

**Problem 471: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{a B + b B \operatorname{Tan}[c+dx]}{\sqrt{\operatorname{Tan}[c+dx]} (a + b \operatorname{Tan}[c+dx])^{3/2}} dx$$

Optimal (type 3, 111 leaves, 8 steps):

$$\frac{B \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a + b \operatorname{Tan}[c+dx]}}\right]}{\sqrt{i a - b} d} + \frac{B \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a + b \operatorname{Tan}[c+dx]}}\right]}{\sqrt{i a + b} d}$$

Result (type 4, 423 leaves):

$$\left( 2 i \sqrt{2} B \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 \left. \sqrt{2 + \frac{2 a \cot \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 \left. \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right. \\
 \left. \left. \sec [c+d x] \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d \sqrt{\tan [c+d x]} \sqrt{a + b \tan [c+d x]} \right)$$

**Problem 472: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{a B + b B \tan [c+d x]}{\tan [c+d x]^{3/2} (a + b \tan [c+d x])^{3/2}} dx$$

Optimal (type 3, 150 leaves, 10 steps):

$$-\frac{i B \text{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c+d x]}}{\sqrt{a + b \tan [c+d x]}} \right]}{\sqrt{i a - b} d} + \frac{i B \text{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c+d x]}}{\sqrt{a + b \tan [c+d x]}} \right]}{\sqrt{i a + b} d} - \frac{2 B \sqrt{a + b \tan [c+d x]}}{a d \sqrt{\tan [c+d x]}}$$

Result (type 4, 2822 leaves):

$$B \left( \left( 2 \left( \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \right.$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( d \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]} \right) \\
 & \left( \left( \left( \text{EllipticPi} \left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]} \text{Tan}[c + d x]^{3/2} \right) - \\
 & \left( a \left( \text{EllipticPi} \left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \Big/ \\
 & \left( 2 (-b + \sqrt{a^2 + b^2}) \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \sqrt{1 + \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Tan}[c+dx]} \right) + \\
 & \left( \left( \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \quad \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx] (b \operatorname{Cos}[c+dx] - a \operatorname{Sin}[c+dx]) \sqrt{1 + \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \quad \left( (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^{3/2} \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right. \\
 & \quad \left. \sqrt{\operatorname{Tan}[c+dx]} \right) - \\
 & \quad \left( 2 \left( \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right) \\
 & \quad \sqrt{1 + \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \left( \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right) \\
 & \quad \left( \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \sqrt{\operatorname{Tan}[c+dx]} \right) - \\
 & \quad \left( \left( \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]^2 \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{\tan[c + d x]} \right) + \\
 & \left( \left( \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right) \\
 & \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \\
 & \left( -\frac{a^2 \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]}{2 (b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right])^2} - \frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{2 (b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right])} \right) \Big/ \\
 & \left( \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \left( -\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]} \right)^{3/2} \right. \\
 & \left. \sqrt{\tan[c + d x]} \right) - \left( 2 \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( \left( i a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Big/ \left( 4 (b + \sqrt{a^2 + b^2}) \left( 1 - i \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right. \right. \\
 & \left. \left. \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) - \right.
 \end{aligned}$$

$$\left( i a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( b + \sqrt{a^2 + b^2} \right) \left( 1 + i \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] \right) \right. \\ \left. \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right) \right) / \\ \left( \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{-\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \sqrt{\operatorname{Tan}[c+dx]}} \right) \\ \left. \sqrt{a + b \operatorname{Tan}[c+dx]} \right) - \frac{2 \operatorname{Sec}[c+dx] (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{a d \sqrt{\operatorname{Tan}[c+dx]} \sqrt{a + b \operatorname{Tan}[c+dx]}}$$

**Problem 473: Result more than twice size of optimal antiderivative.**

$$\int (a + b \operatorname{Tan}[c + dx])^{2/3} (A + B \operatorname{Tan}[c + dx]) dx$$

Optimal (type 3, 379 leaves, 12 steps):

$$-\frac{1}{4} (a - ib)^{2/3} (A - iB) x - \frac{1}{4} (a + ib)^{2/3} (A + iB) x + \\ \frac{\sqrt{3} (a - ib)^{2/3} (iA + B) \operatorname{ArcTan}\left[\frac{1 + \frac{2(a-b \operatorname{Tan}[c+dx])^{1/3}}{(a-ib)^{1/3}}}{\sqrt{3}}\right]}{2d} - \\ \frac{\sqrt{3} (a + ib)^{2/3} (iA - B) \operatorname{ArcTan}\left[\frac{1 + \frac{2(a-b \operatorname{Tan}[c+dx])^{1/3}}{(a+ib)^{1/3}}}{\sqrt{3}}\right]}{2d} - \\ \frac{(a + ib)^{2/3} (iA - B) \operatorname{Log}[\operatorname{Cos}[c + dx]]}{4d} + \frac{(a - ib)^{2/3} (iA + B) \operatorname{Log}[\operatorname{Cos}[c + dx]]}{4d} + \\ \frac{3 (a - ib)^{2/3} (iA + B) \operatorname{Log}\left[\frac{(a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}}{4d}\right]}{4d} - \\ \frac{3 (a + ib)^{2/3} (iA - B) \operatorname{Log}\left[\frac{(a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}}{4d}\right]}{4d} + \frac{3B (a + b \operatorname{Tan}[c + dx])^{2/3}}{2d}$$

Result (type 3, 6768 leaves):

$$\frac{3B \operatorname{Cos}[c + dx] (a + b \operatorname{Tan}[c + dx])^{2/3} (A + B \operatorname{Tan}[c + dx])}{2d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx])} + \\ \left( \left( 2\sqrt{3} (a + ib)^{1/3} (i a + b) (A - iB) \operatorname{ArcTan}\left[\frac{1 + \frac{2(a+b \operatorname{Tan}[c+dx])^{1/3}}{(a-ib)^{1/3}}}{\sqrt{3}}\right] \right) + \right.$$

$$\begin{aligned}
 & 2\sqrt{3} (a - ib)^{1/3} (-ia + b) (A + iB) \operatorname{ArcTan}\left[\frac{1 + \frac{2(a+b \operatorname{Tan}[c+dx])^{1/3}}{(a+ib)^{1/3}}}{\sqrt{3}}\right] + \\
 & 2iaA (a + ib)^{1/3} \operatorname{Log}\left[(a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] + \\
 & 2A (a + ib)^{1/3} b \operatorname{Log}\left[(a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] + \\
 & 2a (a + ib)^{1/3} B \operatorname{Log}\left[(a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] - \\
 & 2i (a + ib)^{1/3} b B \operatorname{Log}\left[(a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] - \\
 & 2iaA (a - ib)^{1/3} \operatorname{Log}\left[(a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] + \\
 & 2A (a - ib)^{1/3} b \operatorname{Log}\left[(a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] + \\
 & 2a (a - ib)^{1/3} B \operatorname{Log}\left[(a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] + \\
 & 2i (a - ib)^{1/3} b B \operatorname{Log}\left[(a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3}\right] - iaA (a + ib)^{1/3} \\
 & \operatorname{Log}\left[(a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] - \\
 & A (a + ib)^{1/3} b \operatorname{Log}\left[(a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] - \\
 & a (a + ib)^{1/3} B \operatorname{Log}\left[(a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] + \\
 & i (a + ib)^{1/3} b B \\
 & \operatorname{Log}\left[(a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] + iaA \\
 & (a - ib)^{1/3} \operatorname{Log}\left[(a + ib)^{2/3} + (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] - \\
 & A (a - ib)^{1/3} b \operatorname{Log}\left[(a + ib)^{2/3} + (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] - \\
 & a (a - ib)^{1/3} B \operatorname{Log}\left[(a + ib)^{2/3} + (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] - \\
 & i (a - ib)^{1/3} b B \\
 & \left. \operatorname{Log}\left[(a + ib)^{2/3} + (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3}\right] \right) \\
 & (\operatorname{Sec}[c + dx]^2)^{1/3} \left( \frac{aA}{\operatorname{Sec}[c + dx]^{1/3} (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^{1/3}} - \right. \\
 & \frac{bB}{\operatorname{Sec}[c + dx]^{1/3} (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^{1/3}} + \frac{Ab \operatorname{Sec}[c + dx]^{2/3} \operatorname{Sin}[c + dx]}{(a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^{1/3}} + \\
 & \left. \frac{aB \operatorname{Sec}[c + dx]^{2/3} \operatorname{Sin}[c + dx]}{(a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^{1/3}} \right) \left( \frac{a + b \operatorname{Tan}[c + dx]}{\sqrt{\operatorname{Sec}[c + dx]^2}} \right)^{2/3} (A + B \operatorname{Tan}[c + dx]) \Big/ \\
 & \left( 4 (a - ib)^{1/3} (a + ib)^{1/3} d \operatorname{Sec}[c + dx]^{5/3} (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^{2/3} \right. \\
 & (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \\
 & \left. \left( - \frac{1}{6 (a - ib)^{1/3} (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{5/3}} \right) \right. \\
 & \left. b \left( 2\sqrt{3} (a + ib)^{1/3} (ia + b) (A - iB) \operatorname{ArcTan}\left[\frac{1 + \frac{2(a+b \operatorname{Tan}[c+dx])^{1/3}}{(a-ib)^{1/3}}}{\sqrt{3}}\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \sqrt{3} (a - i b)^{1/3} (-i a + b) (A + i B) \operatorname{ArcTan} \left[ \frac{1 + \frac{2(a+b \tan[c+dx])^{1/3}}{(a+i b)^{1/3}}}{\sqrt{3}} \right] + 2 i a A (a + i b)^{1/3} \\
 & \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + 2 A (a + i b)^{1/3} b \operatorname{Log} \left[ (a - i b)^{1/3} - \right. \\
 & \quad \left. (a + b \tan[c+dx])^{1/3} \right] + 2 a (a + i b)^{1/3} B \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] - \\
 & 2 i (a + i b)^{1/3} b B \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] - 2 i a A (a - i b)^{1/3} \\
 & \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + 2 A (a - i b)^{1/3} b \operatorname{Log} \left[ (a + i b)^{1/3} - \right. \\
 & \quad \left. (a + b \tan[c+dx])^{1/3} \right] + 2 a (a - i b)^{1/3} B \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + \\
 & 2 i (a - i b)^{1/3} b B \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] - i a A (a + i b)^{1/3} \\
 & \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] - \\
 & A (a + i b)^{1/3} b \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \tan[c+dx])^{1/3} + \right. \\
 & \quad \left. (a + b \tan[c+dx])^{2/3} \right] - a (a + i b)^{1/3} B \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} \right. \\
 & \quad \left. (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] + i (a + i b)^{1/3} b B \operatorname{Log} \left[ (a - i b)^{2/3} + \right. \\
 & \quad \left. (a - i b)^{1/3} (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] + i a A (a - i b)^{1/3} \\
 & \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] - \\
 & A (a - i b)^{1/3} b \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \tan[c+dx])^{1/3} + \right. \\
 & \quad \left. (a + b \tan[c+dx])^{2/3} \right] - a (a - i b)^{1/3} B \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} \right. \\
 & \quad \left. (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] - i (a - i b)^{1/3} b B \operatorname{Log} \left[ (a + i b)^{2/3} + \right. \\
 & \quad \left. (a + i b)^{1/3} (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] \left. \right) (\operatorname{Sec}[c+dx]^2)^{4/3}
 \end{aligned}$$

$$\left( \frac{a + b \tan[c+dx]}{\sqrt{\operatorname{Sec}[c+dx]^2}} \right)^{2/3} + \frac{1}{6 (a - i b)^{1/3} (a + i b)^{1/3} (a + b \tan[c+dx])^{2/3}}$$

$$\left( 2 \sqrt{3} (a + i b)^{1/3} (i a + b) (A - i B) \operatorname{ArcTan} \left[ \frac{1 + \frac{2(a+b \tan[c+dx])^{1/3}}{(a-i b)^{1/3}}}{\sqrt{3}} \right] + \right.$$

$$\left. 2 \sqrt{3} (a - i b)^{1/3} (-i a + b) (A + i B) \operatorname{ArcTan} \left[ \frac{1 + \frac{2(a+b \tan[c+dx])^{1/3}}{(a+i b)^{1/3}}}{\sqrt{3}} \right] + \right.$$

$$\left. 2 i a A (a + i b)^{1/3} \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + \right.$$

$$\left. 2 A (a + i b)^{1/3} b \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + \right.$$

$$\left. 2 a (a + i b)^{1/3} B \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] - \right.$$

$$\left. 2 i (a + i b)^{1/3} b B \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] - \right.$$

$$\left. 2 i a A (a - i b)^{1/3} \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + \right.$$

$$\left. 2 A (a - i b)^{1/3} b \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + \right.$$

$$\left. 2 a (a - i b)^{1/3} B \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] + \right.$$

$$\left. 2 i (a - i b)^{1/3} b B \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \tan[c+dx])^{1/3} \right] - i a A (a + i b)^{1/3} \right.$$

$$\operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] -$$

$$A (a + i b)^{1/3} b \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \tan[c+dx])^{1/3} + \right.$$

$$\left. (a + b \tan[c+dx])^{2/3} \right] - a (a + i b)^{1/3} B \operatorname{Log} \left[ (a - i b)^{2/3} + \right.$$

$$\left. (a - i b)^{1/3} (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] + i (a + i b)^{1/3} b B$$

$$\operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \tan[c+dx])^{1/3} + (a + b \tan[c+dx])^{2/3} \right] +$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & i a A (a - i b)^{1/3} \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + \right. \\
 & \quad (a + b \operatorname{Tan}[c + d x])^{2/3} - A (a - i b)^{1/3} b \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} \right. \\
 & \quad \quad (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} - a (a - i b)^{1/3} B \operatorname{Log} \left[ (a + i b)^{2/3} + \right. \\
 & \quad \quad \left. (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] - i (a - i b)^{1/3} b B \\
 & \quad \left. \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] \right) \\
 & (\operatorname{Sec}[c + d x]^2)^{1/3} \operatorname{Tan}[c + d x] \left( \frac{a + b \operatorname{Tan}[c + d x]}{\sqrt{\operatorname{Sec}[c + d x]^2}} \right)^{2/3} + \\
 & \left( \frac{1}{6 (a - i b)^{1/3} (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{2/3} \left( \frac{a + b \operatorname{Tan}[c + d x]}{\sqrt{\operatorname{Sec}[c + d x]^2}} \right)^{1/3}} \right) \\
 & \left( 2 \sqrt{3} (a + i b)^{1/3} (i a + b) (A - i B) \operatorname{ArcTan} \left[ \frac{1 + \frac{2 (a + b \operatorname{Tan}[c + d x])^{1/3}}{(a - i b)^{1/3}}}{\sqrt{3}} \right] + \right. \\
 & \quad \left. 2 \sqrt{3} (a - i b)^{1/3} (-i a + b) (A + i B) \operatorname{ArcTan} \left[ \frac{1 + \frac{2 (a + b \operatorname{Tan}[c + d x])^{1/3}}{(a + i b)^{1/3}}}{\sqrt{3}} \right] + \right. \\
 & \quad 2 i a A (a + i b)^{1/3} \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] + \\
 & \quad 2 A (a + i b)^{1/3} b \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] + \\
 & \quad 2 a (a + i b)^{1/3} B \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] - \\
 & \quad 2 i (a + i b)^{1/3} b B \operatorname{Log} \left[ (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] - \\
 & \quad 2 i a A (a - i b)^{1/3} \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] + \\
 & \quad 2 A (a - i b)^{1/3} b \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] + \\
 & \quad 2 a (a - i b)^{1/3} B \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] + \\
 & \quad 2 i (a - i b)^{1/3} b B \operatorname{Log} \left[ (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right] - i a A (a + i b)^{1/3} \\
 & \quad \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] - \\
 & \quad A (a + i b)^{1/3} b \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + \right. \\
 & \quad \quad \left. (a + b \operatorname{Tan}[c + d x])^{2/3} \right] - a (a + i b)^{1/3} B \\
 & \quad \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] + \\
 & \quad i (a + i b)^{1/3} b B \operatorname{Log} \left[ (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + \right. \\
 & \quad \quad \left. (a + b \operatorname{Tan}[c + d x])^{2/3} \right] + i a A (a - i b)^{1/3} \operatorname{Log} \left[ (a + i b)^{2/3} + \right. \\
 & \quad \quad \left. (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] - A (a - i b)^{1/3} b \\
 & \quad \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] - \\
 & \quad a (a - i b)^{1/3} B \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + \right. \\
 & \quad \quad \left. (a + b \operatorname{Tan}[c + d x])^{2/3} \right] - i (a - i b)^{1/3} b B \\
 & \quad \left. \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] \right)
 \end{aligned}
 \end{aligned}$$

$$\begin{aligned}
 & (\text{Sec}[c+dx]^2)^{1/3} \left( b \sqrt{\text{Sec}[c+dx]^2} - \frac{\text{Tan}[c+dx] (a+b \text{Tan}[c+dx])}{\sqrt{\text{Sec}[c+dx]^2}} \right) + \\
 & \frac{1}{4 (a-ib)^{1/3} (a+ib)^{1/3} (a+b \text{Tan}[c+dx])^{2/3}} \\
 & (\text{Sec}[c+dx]^2)^{1/3} \left( \frac{a+b \text{Tan}[c+dx]}{\sqrt{\text{Sec}[c+dx]^2}} \right)^{2/3} \\
 & \left( - \left( (2i a A (a+ib)^{1/3} b \text{Sec}[c+dx]^2) / (3 (a+b \text{Tan}[c+dx])^{2/3} \right. \right. \\
 & \quad \left. \left( (a-ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) - (2 A (a+ib)^{1/3} b^2 \text{Sec}[c+dx]^2) / \\
 & \quad \left( 3 (a+b \text{Tan}[c+dx])^{2/3} \left( (a-ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) - \\
 & \quad \left( 2 a (a+ib)^{1/3} b B \text{Sec}[c+dx]^2 \right) / \left( 3 (a+b \text{Tan}[c+dx])^{2/3} \right. \\
 & \quad \left. \left( (a-ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) + (2i (a+ib)^{1/3} b^2 B \text{Sec}[c+dx]^2) / \\
 & \quad \left( 3 (a+b \text{Tan}[c+dx])^{2/3} \left( (a-ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) + \\
 & \quad \left( 2i a A (a-ib)^{1/3} b \text{Sec}[c+dx]^2 \right) / \left( 3 (a+b \text{Tan}[c+dx])^{2/3} \right. \\
 & \quad \left. \left( (a+ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) - (2 A (a-ib)^{1/3} b^2 \text{Sec}[c+dx]^2) / \\
 & \quad \left( 3 (a+b \text{Tan}[c+dx])^{2/3} \left( (a+ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) - \\
 & \quad \left( 2 a (a-ib)^{1/3} b B \text{Sec}[c+dx]^2 \right) / \left( 3 (a+b \text{Tan}[c+dx])^{2/3} \right. \\
 & \quad \left. \left( (a+ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) - (2i (a-ib)^{1/3} b^2 B \text{Sec}[c+dx]^2) / \\
 & \quad \left( 3 (a+b \text{Tan}[c+dx])^{2/3} \left( (a+ib)^{1/3} - (a+b \text{Tan}[c+dx])^{1/3} \right) \right) - \\
 & \quad \left( i a A (a+ib)^{1/3} \left( \frac{(a-ib)^{1/3} b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{2/3}} + \frac{2 b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{1/3}} \right) \right) / \\
 & \quad \left( (a-ib)^{2/3} + (a-ib)^{1/3} (a+b \text{Tan}[c+dx])^{1/3} + (a+b \text{Tan}[c+dx])^{2/3} \right) - \\
 & \quad \left( A (a+ib)^{1/3} b \left( \frac{(a-ib)^{1/3} b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{2/3}} + \frac{2 b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{1/3}} \right) \right) / \\
 & \quad \left( (a-ib)^{2/3} + (a-ib)^{1/3} (a+b \text{Tan}[c+dx])^{1/3} + (a+b \text{Tan}[c+dx])^{2/3} \right) - \\
 & \quad \left( a (a+ib)^{1/3} B \left( \frac{(a-ib)^{1/3} b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{2/3}} + \frac{2 b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{1/3}} \right) \right) / \\
 & \quad \left( (a-ib)^{2/3} + (a-ib)^{1/3} (a+b \text{Tan}[c+dx])^{1/3} + (a+b \text{Tan}[c+dx])^{2/3} \right) + \\
 & \quad \left( i (a+ib)^{1/3} b B \left( \frac{(a-ib)^{1/3} b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{2/3}} + \frac{2 b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{1/3}} \right) \right) / \\
 & \quad \left( (a-ib)^{2/3} + (a-ib)^{1/3} (a+b \text{Tan}[c+dx])^{1/3} + (a+b \text{Tan}[c+dx])^{2/3} \right) + \\
 & \quad \left( i a A (a-ib)^{1/3} \left( \frac{(a+ib)^{1/3} b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{2/3}} + \frac{2 b \text{Sec}[c+dx]^2}{3 (a+b \text{Tan}[c+dx])^{1/3}} \right) \right) / \\
 & \quad \left( (a+ib)^{2/3} + (a+ib)^{1/3} (a+b \text{Tan}[c+dx])^{1/3} + (a+b \text{Tan}[c+dx])^{2/3} \right) -
 \end{aligned}$$

$$\begin{aligned} & \left( A (a - i b)^{1/3} b \left( \frac{(a + i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{1/3}} \right) \right) / \\ & \left( (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right) - \\ & \left( a (a - i b)^{1/3} B \left( \frac{(a + i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{1/3}} \right) \right) / \\ & \left( (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right) - \\ & \left( i (a - i b)^{1/3} b B \left( \frac{(a + i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{1/3}} \right) \right) / \\ & \left( (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right) + \\ & \left( 4 (a + i b)^{1/3} b (i a + b) (A - i B) \operatorname{Sec}[c + d x]^2 \right) / \\ & \left( 3 (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{2/3} \left( 1 + \frac{1}{3} \left( 1 + \frac{2 (a + b \operatorname{Tan}[c + d x])^{1/3}}{(a - i b)^{1/3}} \right)^2 \right) \right) + \\ & \left( 4 (a - i b)^{1/3} b (-i a + b) (A + i B) \operatorname{Sec}[c + d x]^2 \right) / \\ & \left( 3 (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{2/3} \left( 1 + \frac{1}{3} \left( 1 + \frac{2 (a + b \operatorname{Tan}[c + d x])^{1/3}}{(a + i b)^{1/3}} \right)^2 \right) \right) \end{aligned}$$

**Problem 474: Result more than twice size of optimal antiderivative.**

$$\int (a + b \operatorname{Tan}[c + d x])^{1/3} (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 377 leaves, 12 steps):

$$\begin{aligned} & -\frac{1}{4} (a - i b)^{1/3} (A - i B) x - \frac{1}{4} (a + i b)^{1/3} (A + i B) x - \\ & \frac{\sqrt{3} (a - i b)^{1/3} (i A + B) \operatorname{ArcTan}\left[\frac{1 + \frac{2 (a - b \operatorname{Tan}[c + d x])^{1/3}}{(a - i b)^{1/3}}}{\sqrt{3}}\right]}{2 d} + \\ & \frac{\sqrt{3} (a + i b)^{1/3} (i A - B) \operatorname{ArcTan}\left[\frac{1 + \frac{2 (a - b \operatorname{Tan}[c + d x])^{1/3}}{(a + i b)^{1/3}}}{\sqrt{3}}\right]}{2 d} - \\ & \frac{(a + i b)^{1/3} (i A - B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{4 d} + \frac{(a - i b)^{1/3} (i A + B) \operatorname{Log}[\operatorname{Cos}[c + d x]]}{4 d} + \\ & \frac{3 (a - i b)^{1/3} (i A + B) \operatorname{Log}\left[\frac{(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}}{4 d}\right]}{4 d} - \\ & \frac{3 (a + i b)^{1/3} (i A - B) \operatorname{Log}\left[\frac{(a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}}{4 d}\right]}{4 d} + \frac{3 B (a + b \operatorname{Tan}[c + d x])^{1/3}}{d} \end{aligned}$$

Result (type 3, 6772 leaves):



$$\begin{aligned}
 & \frac{3 B \cos [c+d x] (a+b \tan [c+d x])^{1/3} (A+B \tan [c+d x])}{d (A \cos [c+d x]+B \sin [c+d x])} + \\
 & \left( \left( -2 i \sqrt{3} (a-i b) (a+i b)^{2/3} (A-i B) \operatorname{ArcTan} \left[ \frac{1+\frac{2(a+b \tan [c+d x])^{1/3}}{(a-i b)^{1/3}}}{\sqrt{3}} \right] + \right. \right. \\
 & \quad 2 i \sqrt{3} (a-i b)^{2/3} (a+i b) (A+i B) \operatorname{ArcTan} \left[ \frac{1+\frac{2(a+b \tan [c+d x])^{1/3}}{(a+i b)^{1/3}}}{\sqrt{3}} \right] + \\
 & \quad 2 i a A (a+i b)^{2/3} \operatorname{Log} \left[ (a-i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] + \\
 & \quad 2 A (a+i b)^{2/3} b \operatorname{Log} \left[ (a-i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] + \\
 & \quad 2 a (a+i b)^{2/3} B \operatorname{Log} \left[ (a-i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] - \\
 & \quad 2 i (a+i b)^{2/3} b B \operatorname{Log} \left[ (a-i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] - \\
 & \quad 2 i a A (a-i b)^{2/3} \operatorname{Log} \left[ (a+i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] + \\
 & \quad 2 A (a-i b)^{2/3} b \operatorname{Log} \left[ (a+i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] + \\
 & \quad 2 a (a-i b)^{2/3} B \operatorname{Log} \left[ (a+i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] + \\
 & \quad 2 i (a-i b)^{2/3} b B \operatorname{Log} \left[ (a+i b)^{1/3} - (a+b \tan [c+d x])^{1/3} \right] - i a A (a+i b)^{2/3} \\
 & \quad \operatorname{Log} \left[ (a-i b)^{2/3} + (a-i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] - \\
 & \quad A (a+i b)^{2/3} b \operatorname{Log} \left[ (a-i b)^{2/3} + (a-i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] - \\
 & \quad a (a+i b)^{2/3} B \operatorname{Log} \left[ (a-i b)^{2/3} + (a-i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] + \\
 & \quad i (a+i b)^{2/3} b B \\
 & \quad \operatorname{Log} \left[ (a-i b)^{2/3} + (a-i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] + i a A \\
 & \quad (a-i b)^{2/3} \operatorname{Log} \left[ (a+i b)^{2/3} + (a+i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] - \\
 & \quad A (a-i b)^{2/3} b \operatorname{Log} \left[ (a+i b)^{2/3} + (a+i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] - \\
 & \quad a (a-i b)^{2/3} B \operatorname{Log} \left[ (a+i b)^{2/3} + (a+i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] - \\
 & \quad i (a-i b)^{2/3} b B \\
 & \quad \left. \operatorname{Log} \left[ (a+i b)^{2/3} + (a+i b)^{1/3} (a+b \tan [c+d x])^{1/3} + (a+b \tan [c+d x])^{2/3} \right] \right) \\
 & (\sec [c+d x]^2)^{1/6} \left( \frac{a A}{\sec [c+d x]^{2/3} (a \cos [c+d x]+b \sin [c+d x])^{2/3}} - \right. \\
 & \quad \frac{b B}{\sec [c+d x]^{2/3} (a \cos [c+d x]+b \sin [c+d x])^{2/3}} + \frac{A b \sec [c+d x]^{1/3} \sin [c+d x]}{(a \cos [c+d x]+b \sin [c+d x])^{2/3}} + \\
 & \quad \left. \frac{a B \sec [c+d x]^{1/3} \sin [c+d x]}{(a \cos [c+d x]+b \sin [c+d x])^{2/3}} \right) \left( \frac{a+b \tan [c+d x]}{\sqrt{\sec [c+d x]^2}} \right)^{1/3} (A+B \tan [c+d x]) \Big/ \\
 & \left( 4 (a-i b)^{2/3} (a+i b)^{2/3} d \sec [c+d x]^{4/3} (a \cos [c+d x]+b \sin [c+d x])^{1/3} \right. \\
 & \quad \left. (A \cos [c+d x]+B \sin [c+d x]) \right)
 \end{aligned}$$

$$\left( -\frac{1}{12 (a - i b)^{2/3} (a + i b)^{2/3} (a + b \operatorname{Tan}[c + d x])^{4/3}} \right.$$

$$b \left( -2 i \sqrt{3} (a - i b) (a + i b)^{2/3} (A - i B) \operatorname{ArcTan}\left[\frac{1 + \frac{2 (a+b \operatorname{Tan}[c+d x])^{1/3}}{(a-i b)^{1/3}}}{\sqrt{3}}\right] + \right.$$

$$2 i \sqrt{3} (a - i b)^{2/3} (a + i b) (A + i B) \operatorname{ArcTan}\left[\frac{1 + \frac{2 (a+b \operatorname{Tan}[c+d x])^{1/3}}{(a+i b)^{1/3}}}{\sqrt{3}}\right] +$$

$$2 i a A (a + i b)^{2/3} \operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] +$$

$$2 A (a + i b)^{2/3} b \operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] +$$

$$2 a (a + i b)^{2/3} B \operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] - 2 i (a + i b)^{2/3} b B$$

$$\operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] - 2 i a A (a - i b)^{2/3} \operatorname{Log}\left[(a + i b)^{1/3} - \right.$$

$$(a + b \operatorname{Tan}[c + d x])^{1/3}\right] + 2 A (a - i b)^{2/3} b \operatorname{Log}\left[(a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] +$$

$$2 a (a - i b)^{2/3} B \operatorname{Log}\left[(a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] + 2 i (a - i b)^{2/3}$$

$$b B \operatorname{Log}\left[(a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] - i a A (a + i b)^{2/3} \operatorname{Log}\left[(a - i b)^{2/3} + \right.$$

$$(a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3}\right] - A (a + i b)^{2/3} b$$

$$\operatorname{Log}\left[(a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3}\right] -$$

$$a (a + i b)^{2/3} B \operatorname{Log}\left[(a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + \right.$$

$$(a + b \operatorname{Tan}[c + d x])^{2/3}\right] + i (a + i b)^{2/3} b B \operatorname{Log}\left[(a - i b)^{2/3} + (a - i b)^{1/3} \right.$$

$$(a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3}\right] + i a A (a - i b)^{2/3} \operatorname{Log}\left[(a + i b)^{2/3} + \right.$$

$$(a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3}\right] - A (a - i b)^{2/3} b$$

$$\operatorname{Log}\left[(a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3}\right] -$$

$$a (a - i b)^{2/3} B \operatorname{Log}\left[(a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + \right.$$

$$(a + b \operatorname{Tan}[c + d x])^{2/3}\right] - i (a - i b)^{2/3} b B \operatorname{Log}\left[(a + i b)^{2/3} + \right.$$

$$(a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3}\right] \left. \right) (\operatorname{Sec}[c + d x]^2)^{7/6}$$

$$\left( \frac{(a + b \operatorname{Tan}[c + d x])^{1/3}}{\sqrt{\operatorname{Sec}[c + d x]^2}} \right)^{1/3} + \frac{1}{12 (a - i b)^{2/3} (a + i b)^{2/3} (a + b \operatorname{Tan}[c + d x])^{1/3}}$$

$$\left( -2 i \sqrt{3} (a - i b) (a + i b)^{2/3} (A - i B) \operatorname{ArcTan}\left[\frac{1 + \frac{2 (a+b \operatorname{Tan}[c+d x])^{1/3}}{(a-i b)^{1/3}}}{\sqrt{3}}\right] + \right.$$

$$2 i \sqrt{3} (a - i b)^{2/3} (a + i b) (A + i B) \operatorname{ArcTan}\left[\frac{1 + \frac{2 (a+b \operatorname{Tan}[c+d x])^{1/3}}{(a+i b)^{1/3}}}{\sqrt{3}}\right] +$$

$$2 i a A (a + i b)^{2/3} \operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] +$$

$$2 A (a + i b)^{2/3} b \operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] +$$

$$2 a (a + i b)^{2/3} B \operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] -$$

$$2 i (a + i b)^{2/3} b B \operatorname{Log}\left[(a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] -$$

$$2 i a A (a - i b)^{2/3} \operatorname{Log}\left[(a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3}\right] +$$

$$\begin{aligned}
 & 2A (a - ib)^{2/3} b \operatorname{Log} \left[ (a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] + \\
 & 2a (a - ib)^{2/3} B \operatorname{Log} \left[ (a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] + \\
 & 2i (a - ib)^{2/3} b B \operatorname{Log} \left[ (a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] - ia A (a + ib)^{2/3} \\
 & \operatorname{Log} \left[ (a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - \\
 & A (a + ib)^{2/3} b \operatorname{Log} \left[ (a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + \right. \\
 & \quad \left. (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - a (a + ib)^{2/3} B \operatorname{Log} \left[ (a - ib)^{2/3} + \right. \\
 & \quad \left. (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] + i (a + ib)^{2/3} b B \\
 & \operatorname{Log} \left[ (a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] + \\
 & i a A (a - ib)^{2/3} \operatorname{Log} \left[ (a + ib)^{2/3} + (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + \right. \\
 & \quad \left. (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - A (a - ib)^{2/3} b \operatorname{Log} \left[ (a + ib)^{2/3} + (a + ib)^{1/3} \right. \\
 & \quad \left. (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - a (a - ib)^{2/3} B \operatorname{Log} \left[ (a + ib)^{2/3} + \right. \\
 & \quad \left. (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - i (a - ib)^{2/3} b B \\
 & \left. \operatorname{Log} \left[ (a + ib)^{2/3} + (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] \right) \\
 & (\operatorname{Sec}[c + dx]^2)^{1/6} \operatorname{Tan}[c + dx] \left( \frac{a + b \operatorname{Tan}[c + dx]}{\sqrt{\operatorname{Sec}[c + dx]^2}} \right)^{1/3} + \\
 & \left( 1 / \left( 12 (a - ib)^{2/3} (a + ib)^{2/3} (a + b \operatorname{Tan}[c + dx])^{1/3} \left( \frac{a + b \operatorname{Tan}[c + dx]}{\sqrt{\operatorname{Sec}[c + dx]^2}} \right)^{2/3} \right) \right) \\
 & \left( -2i \sqrt{3} (a - ib) (a + ib)^{2/3} (A - iB) \operatorname{ArcTan} \left[ \frac{1 + \frac{2(a + b \operatorname{Tan}[c + dx])^{1/3}}{(a - ib)^{1/3}}}{\sqrt{3}} \right] + \right. \\
 & \quad \left. 2i \sqrt{3} (a - ib)^{2/3} (a + ib) (A + iB) \operatorname{ArcTan} \left[ \frac{1 + \frac{2(a + b \operatorname{Tan}[c + dx])^{1/3}}{(a + ib)^{1/3}}}{\sqrt{3}} \right] + \right. \\
 & \quad 2i a A (a + ib)^{2/3} \operatorname{Log} \left[ (a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] + \\
 & \quad 2A (a + ib)^{2/3} b \operatorname{Log} \left[ (a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] + \\
 & \quad 2a (a + ib)^{2/3} B \operatorname{Log} \left[ (a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] - \\
 & \quad 2i (a + ib)^{2/3} b B \operatorname{Log} \left[ (a - ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] - \\
 & \quad 2i a A (a - ib)^{2/3} \operatorname{Log} \left[ (a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] + \\
 & \quad 2A (a - ib)^{2/3} b \operatorname{Log} \left[ (a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] + \\
 & \quad 2a (a - ib)^{2/3} B \operatorname{Log} \left[ (a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] + \\
 & \quad 2i (a - ib)^{2/3} b B \operatorname{Log} \left[ (a + ib)^{1/3} - (a + b \operatorname{Tan}[c + dx])^{1/3} \right] - ia A (a + ib)^{2/3} \\
 & \quad \operatorname{Log} \left[ (a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - \\
 & \quad A (a + ib)^{2/3} b \operatorname{Log} \left[ (a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + \right. \\
 & \quad \left. (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - a (a + ib)^{2/3} B \\
 & \quad \operatorname{Log} \left[ (a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] + \\
 & \quad i (a + ib)^{2/3} b B \operatorname{Log} \left[ (a - ib)^{2/3} + (a - ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + \right. \\
 & \quad \left. (a + b \operatorname{Tan}[c + dx])^{2/3} \right] + ia A (a - ib)^{2/3} \operatorname{Log} \left[ (a + ib)^{2/3} + \right. \\
 & \quad \left. (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] - A (a - ib)^{2/3} b \\
 & \quad \operatorname{Log} \left[ (a + ib)^{2/3} + (a + ib)^{1/3} (a + b \operatorname{Tan}[c + dx])^{1/3} + (a + b \operatorname{Tan}[c + dx])^{2/3} \right] -
 \end{aligned}$$

$$\begin{aligned}
 & a (a - i b)^{2/3} B \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + \right. \\
 & \quad \left. (a + b \operatorname{Tan}[c + d x])^{2/3} \right] - i (a - i b)^{2/3} b B \\
 & \quad \left. \operatorname{Log} \left[ (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right] \right) \\
 & (\operatorname{Sec}[c + d x]^2)^{1/6} \left( b \sqrt{\operatorname{Sec}[c + d x]^2} - \frac{\operatorname{Tan}[c + d x] (a + b \operatorname{Tan}[c + d x])}{\sqrt{\operatorname{Sec}[c + d x]^2}} \right) + \\
 & \frac{1}{4 (a - i b)^{2/3} (a + i b)^{2/3} (a + b \operatorname{Tan}[c + d x])^{1/3}} (\operatorname{Sec}[c + d x]^2)^{1/6} \left( \frac{a + b \operatorname{Tan}[c + d x]}{\sqrt{\operatorname{Sec}[c + d x]^2}} \right)^{1/3} \\
 & \left( - \left( (2 i a A (a + i b)^{2/3} b \operatorname{Sec}[c + d x]^2) / (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \right. \right. \\
 & \quad \left. \left. \left( (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right) \right) - (2 A (a + i b)^{2/3} b^2 \operatorname{Sec}[c + d x]^2) / \right. \\
 & \quad \left. (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \left( (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right)) - \right. \\
 & \quad \left. (2 a (a + i b)^{2/3} b B \operatorname{Sec}[c + d x]^2) / (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \right. \\
 & \quad \left. \left( (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right) \right) + (2 i (a + i b)^{2/3} b^2 B \operatorname{Sec}[c + d x]^2) / \\
 & \quad \left. (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \left( (a - i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right)) \right) + \\
 & \quad \left. (2 i a A (a - i b)^{2/3} b \operatorname{Sec}[c + d x]^2) / (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \right. \\
 & \quad \left. \left( (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right) \right) - (2 A (a - i b)^{2/3} b^2 \operatorname{Sec}[c + d x]^2) / \\
 & \quad \left. (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \left( (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right)) - \right. \\
 & \quad \left. (2 a (a - i b)^{2/3} b B \operatorname{Sec}[c + d x]^2) / (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \right. \\
 & \quad \left. \left( (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right) \right) - (2 i (a - i b)^{2/3} b^2 B \operatorname{Sec}[c + d x]^2) / \\
 & \quad \left. (3 (a + b \operatorname{Tan}[c + d x])^{2/3} \left( (a + i b)^{1/3} - (a + b \operatorname{Tan}[c + d x])^{1/3} \right)) - \right. \\
 & \quad \left. \left( i a A (a + i b)^{2/3} \left( \frac{(a - i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{1/3}} \right) \right) / \right. \\
 & \quad \left. \left( (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right) - \right. \\
 & \quad \left. \left( A (a + i b)^{2/3} b \left( \frac{(a - i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{1/3}} \right) \right) / \right. \\
 & \quad \left. \left( (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right) - \right. \\
 & \quad \left. \left( a (a + i b)^{2/3} B \left( \frac{(a - i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{1/3}} \right) \right) / \right. \\
 & \quad \left. \left( (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right) + \right. \\
 & \quad \left. \left( i (a + i b)^{2/3} b B \left( \frac{(a - i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \operatorname{Tan}[c + d x])^{1/3}} \right) \right) / \right. \\
 & \quad \left. \left( (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \operatorname{Tan}[c + d x])^{1/3} + (a + b \operatorname{Tan}[c + d x])^{2/3} \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a - i b)^{2/3} + (a - i b)^{1/3} (a + b \tan [c + d x])^{1/3} + (a + b \tan [c + d x])^{2/3} \right) + \\
 & \left( i a A (a - i b)^{2/3} \left( \frac{(a + i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{1/3}} \right) \right) / \\
 & \left( (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \tan [c + d x])^{1/3} + (a + b \tan [c + d x])^{2/3} \right) - \\
 & \left( A (a - i b)^{2/3} b \left( \frac{(a + i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{1/3}} \right) \right) / \\
 & \left( (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \tan [c + d x])^{1/3} + (a + b \tan [c + d x])^{2/3} \right) - \\
 & \left( a (a - i b)^{2/3} B \left( \frac{(a + i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{1/3}} \right) \right) / \\
 & \left( (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \tan [c + d x])^{1/3} + (a + b \tan [c + d x])^{2/3} \right) - \\
 & \left( i (a - i b)^{2/3} b B \left( \frac{(a + i b)^{1/3} b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{2/3}} + \frac{2 b \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{1/3}} \right) \right) / \\
 & \left( (a + i b)^{2/3} + (a + i b)^{1/3} (a + b \tan [c + d x])^{1/3} + (a + b \tan [c + d x])^{2/3} \right) - \\
 & \frac{4 i (a - i b)^{2/3} (a + i b)^{2/3} b (A - i B) \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{2/3} \left( 1 + \frac{1}{3} \left( 1 + \frac{2 (a + b \tan [c + d x])^{1/3}}{(a - i b)^{1/3}} \right)^2 \right)} + \\
 & \left. \frac{4 i (a - i b)^{2/3} (a + i b)^{2/3} b (A + i B) \operatorname{Sec}[c + d x]^2}{3 (a + b \tan [c + d x])^{2/3} \left( 1 + \frac{1}{3} \left( 1 + \frac{2 (a + b \tan [c + d x])^{1/3}}{(a + i b)^{1/3}} \right)^2 \right)} \right) \right)
 \end{aligned}$$

### Problem 477: Unable to integrate problem.

$$\int \frac{i - \tan [e + f x]}{(c + d \tan [e + f x])^{1/3}} dx$$

Optimal (type 3, 148 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{i x}{2 (c - i d)^{1/3}} - \frac{\sqrt{3} \operatorname{ArcTan} \left[ \frac{1 + \frac{2 (c + d \tan [e + f x])^{1/3}}{(c - i d)^{1/3}}}{\sqrt{3}} \right]}{(c - i d)^{1/3} f} - \\
 & \frac{\operatorname{Log}[\operatorname{Cos}[e + f x]]}{2 (c - i d)^{1/3} f} - \frac{3 \operatorname{Log}[(c - i d)^{1/3} - (c + d \tan [e + f x])^{1/3}]}{2 (c - i d)^{1/3} f}
 \end{aligned}$$

Result (type 8, 29 leaves):

$$\int \frac{i - \tan [e + f x]}{(c + d \tan [e + f x])^{1/3}} dx$$

### Problem 479: Unable to integrate problem.

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) dx$$

Optimal (type 5, 403 leaves, 9 steps):

$$\begin{aligned} & - \left( (b (A b^3 (12 + 7 m + m^2) + 4 a b^2 B (12 + 7 m + m^2) - 2 a^3 B (19 + 8 m + m^2) - a^2 A b (68 + 37 m + 5 m^2)) \right. \\ & \quad \left. \tan [c + d x]^{1+m} / (d (1+m) (3+m) (4+m)) \right) + \frac{1}{d (1+m)} \\ & (a^4 A - 6 a^2 A b^2 + A b^4 - 4 a^3 b B + 4 a b^3 B) \operatorname{Hypergeometric2F1} \left[ 1, \frac{1+m}{2}, \frac{3+m}{2}, -\tan [c + d x]^2 \right] \\ & \tan [c + d x]^{1+m} + \\ & (b^2 (2 a A b (4+m)^2 - b^2 B (12 + 7 m + m^2) + a^2 B (26 + 9 m + m^2)) \tan [c + d x]^{2+m} / \\ & (d (2+m) (3+m) (4+m)) + \frac{1}{d (2+m)} (4 a^3 A b - 4 a A b^3 + a^4 B - 6 a^2 b^2 B + b^4 B) \\ & \operatorname{Hypergeometric2F1} \left[ 1, \frac{2+m}{2}, \frac{4+m}{2}, -\tan [c + d x]^2 \right] \tan [c + d x]^{2+m} + \\ & \frac{b (A b (4+m) + a B (7+m)) \tan [c + d x]^{1+m} (a + b \tan [c + d x])^2}{d (3+m) (4+m)} + \\ & \frac{b B \tan [c + d x]^{1+m} (a + b \tan [c + d x])^3}{d (4+m)} \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^4 (A + B \tan [c + d x]) dx$$

### Problem 480: Unable to integrate problem.

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

Optimal (type 5, 267 leaves, 8 steps):

$$\begin{aligned} & \frac{b (3 a A b (3+m) - b^2 B (3+m) + 2 a^2 B (4+m)) \tan [c + d x]^{1+m}}{d (1+m) (3+m)} + \frac{1}{d (1+m)} \\ & (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{Hypergeometric2F1} \left[ 1, \frac{1+m}{2}, \frac{3+m}{2}, -\tan [c + d x]^2 \right] \tan [c + d x]^{1+m} + \\ & \frac{b^2 (A b (3+m) + a B (5+m)) \tan [c + d x]^{2+m}}{d (2+m) (3+m)} + \frac{1}{d (2+m)} \\ & (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{Hypergeometric2F1} \left[ 1, \frac{2+m}{2}, \frac{4+m}{2}, -\tan [c + d x]^2 \right] \tan [c + d x]^{2+m} + \\ & \frac{b B \tan [c + d x]^{1+m} (a + b \tan [c + d x])^2}{d (3+m)} \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^3 (A + B \tan [c + d x]) dx$$

**Problem 484: Unable to integrate problem.**

$$\int \frac{\tan [c + d x]^m (A + B \tan [c + d x])}{(a + b \tan [c + d x])^2} dx$$

Optimal (type 5, 282 leaves, 9 steps):

$$\begin{aligned} & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, -\tan [c + d x]^2\right] \tan [c + d x]^{1+m} \right) / \\ & \left( (a^2 + b^2)^2 d (1+m) \right) + \left( b (a^2 A b (2-m) - A b^3 m + a b^2 B (1+m) - a^3 (B - B m)) \right. \\ & \left. \operatorname{Hypergeometric2F1}\left[1, 1+m, 2+m, -\frac{b \tan [c + d x]}{a}\right] \tan [c + d x]^{1+m} \right) / \left( a^2 (a^2 + b^2)^2 d (1+m) \right) - \\ & \left( (2 a A b - a^2 B + b^2 B) \operatorname{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, -\tan [c + d x]^2\right] \tan [c + d x]^{2+m} \right) / \\ & \left( (a^2 + b^2)^2 d (2+m) \right) + \frac{b (A b - a B) \tan [c + d x]^{1+m}}{a (a^2 + b^2) d (a + b \tan [c + d x])} \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \frac{\tan [c + d x]^m (A + B \tan [c + d x])}{(a + b \tan [c + d x])^2} dx$$

**Problem 485: Unable to integrate problem.**

$$\int \frac{\tan [c + d x]^m (A + B \tan [c + d x])}{(a + b \tan [c + d x])^3} dx$$

Optimal (type 5, 438 leaves, 10 steps):

$$\begin{aligned} & \left( (a^3 A - 3 a A b^2 + 3 a^2 b B - b^3 B) \right. \\ & \quad \left. \text{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{1+m}\right) / \left( (a^2+b^2)^3 d (1+m) \right) - \\ & \left( b (A b^5 (1-m) m + a b^4 B m (1+m) - 2 a^3 b^2 B (3+m-m^2) + 2 a^2 A b^3 (1+3 m-m^2) - a^4 A b (6-5 m+m^2) + \right. \\ & \quad \left. a^5 B (2-3 m+m^2)) \text{Hypergeometric2F1}\left[1, 1+m, 2+m, -\frac{b \text{Tan}[c+d x]}{a}\right] \text{Tan}[c+d x]^{1+m}\right) / \\ & \left( 2 a^3 (a^2+b^2)^3 d (1+m) \right) - \left( (3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \right. \\ & \quad \left. \text{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{2+m}\right) / \\ & \left( (a^2+b^2)^3 d (2+m) \right) + \frac{b (A b - a B) \text{Tan}[c+d x]^{1+m}}{2 a (a^2+b^2) d (a+b \text{Tan}[c+d x])^2} + \\ & \left( b (A b^3 (1-m) - a^3 B (3-m) + a^2 A b (5-m) + a b^2 B (1+m)) \text{Tan}[c+d x]^{1+m} \right) / \\ & \left( 2 a^2 (a^2+b^2)^2 d (a+b \text{Tan}[c+d x]) \right) \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{(a+b \text{Tan}[c+d x])^3} dx$$

**Problem 486: Unable to integrate problem.**

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{(a+b \text{Tan}[c+d x])^4} dx$$

Optimal (type 5, 659 leaves, 11 steps):



$$\begin{aligned}
 & \left( (a^4 A - 6 a^2 A b^2 + A b^4 + 4 a^3 b B - 4 a b^3 B) \right. \\
 & \quad \left. \text{Hypergeometric2F1}\left[1, \frac{1+m}{2}, \frac{3+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{1+m}\right) / \left( (a^2+b^2)^4 d (1+m) \right) - \\
 & \left( b (a b^6 B m (1-m^2) + 3 a^2 A b^5 m (2-5 m+m^2) + A b^7 m (2-3 m+m^2) + \right. \\
 & \quad 3 a^3 b^4 B (2+5 m+2 m^2-m^3) + a^7 B (6-11 m+6 m^2-m^3) - a^6 A b (24-26 m+9 m^2-m^3) + \\
 & \quad \left. 3 a^4 A b^3 (8+10 m-7 m^2+m^3) - 3 a^5 b^2 B (12-m-4 m^2+m^3) \right) \\
 & \quad \left. \text{Hypergeometric2F1}\left[1, 1+m, 2+m, -\frac{b \text{Tan}[c+d x]}{a}\right] \text{Tan}[c+d x]^{1+m}\right) / \\
 & \left( 6 a^4 (a^2+b^2)^4 d (1+m) \right) - \left( (4 a^3 A b - 4 a A b^3 - a^4 B + 6 a^2 b^2 B - b^4 B) \right. \\
 & \quad \left. \text{Hypergeometric2F1}\left[1, \frac{2+m}{2}, \frac{4+m}{2}, -\text{Tan}[c+d x]^2\right] \text{Tan}[c+d x]^{2+m}\right) / \\
 & \left( (a^2+b^2)^4 d (2+m) \right) + \frac{b (A b - a B) \text{Tan}[c+d x]^{1+m}}{3 a (a^2+b^2) d (a+b \text{Tan}[c+d x])^3} + \\
 & \left( b (A b^3 (2-m) - a^3 B (5-m) + a^2 A b (8-m) + a b^2 B (1+m)) \text{Tan}[c+d x]^{1+m} \right) / \\
 & \left( 6 a^2 (a^2+b^2)^2 d (a+b \text{Tan}[c+d x])^2 \right) + \\
 & \left( b (a b^4 B (1-m^2) + 2 a^3 b^2 B (7+3 m-m^2) + a^4 A b (26-9 m+m^2) + 2 a^2 A b^3 (2-6 m+m^2) - \right. \\
 & \quad \left. a^5 B (11-6 m+m^2) + A b^5 (2-3 m+m^2)) \text{Tan}[c+d x]^{1+m} \right) / \left( 6 a^3 (a^2+b^2)^3 d (a+b \text{Tan}[c+d x]) \right)
 \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \frac{\text{Tan}[c+d x]^m (A+B \text{Tan}[c+d x])}{(a+b \text{Tan}[c+d x])^4} dx$$

**Problem 487: Unable to integrate problem.**

$$\int \text{Tan}[c+d x]^m (a+b \text{Tan}[c+d x])^{5/2} (A+B \text{Tan}[c+d x]) dx$$

Optimal (type 6, 193 leaves, 7 steps):

$$\begin{aligned}
 & \left( a^2 (A+i B) \text{AppellF1}\left[1+m, -\frac{5}{2}, 1, 2+m, -\frac{b \text{Tan}[c+d x]}{a}, -i \text{Tan}[c+d x]\right] \right. \\
 & \quad \left. \text{Tan}[c+d x]^{1+m} \sqrt{a+b \text{Tan}[c+d x]} \right) / \left( 2 d (1+m) \sqrt{1+\frac{b \text{Tan}[c+d x]}{a}} \right) + \\
 & \left( a^2 (A-i B) \text{AppellF1}\left[1+m, -\frac{5}{2}, 1, 2+m, -\frac{b \text{Tan}[c+d x]}{a}, i \text{Tan}[c+d x]\right] \right. \\
 & \quad \left. \text{Tan}[c+d x]^{1+m} \sqrt{a+b \text{Tan}[c+d x]} \right) / \left( 2 d (1+m) \sqrt{1+\frac{b \text{Tan}[c+d x]}{a}} \right)
 \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) dx$$

**Problem 488: Unable to integrate problem.**

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x]) dx$$

Optimal (type 6, 189 leaves, 7 steps):

$$\left( a (A + i B) \operatorname{AppellF1} \left[ 1 + m, -\frac{3}{2}, 1, 2 + m, -\frac{b \tan [c + d x]}{a}, -i \tan [c + d x] \right] \right. \\ \left. \tan [c + d x]^{1+m} \sqrt{a + b \tan [c + d x]} \right) / \left( 2 d (1 + m) \sqrt{1 + \frac{b \tan [c + d x]}{a}} \right) + \\ \left( a (A - i B) \operatorname{AppellF1} \left[ 1 + m, -\frac{3}{2}, 1, 2 + m, -\frac{b \tan [c + d x]}{a}, i \tan [c + d x] \right] \right. \\ \left. \tan [c + d x]^{1+m} \sqrt{a + b \tan [c + d x]} \right) / \left( 2 d (1 + m) \sqrt{1 + \frac{b \tan [c + d x]}{a}} \right)$$

Result (type 8, 35 leaves):

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x]) dx$$

**Problem 489: Unable to integrate problem.**

$$\int \tan [c + d x]^m \sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x]) dx$$

Optimal (type 6, 187 leaves, 7 steps):

$$\left( (A + i B) \operatorname{AppellF1} \left[ 1 + m, -\frac{1}{2}, 1, 2 + m, -\frac{b \tan [c + d x]}{a}, -i \tan [c + d x] \right] \right. \\ \left. \tan [c + d x]^{1+m} \sqrt{a + b \tan [c + d x]} \right) / \left( 2 d (1 + m) \sqrt{1 + \frac{b \tan [c + d x]}{a}} \right) + \\ \left( (A - i B) \operatorname{AppellF1} \left[ 1 + m, -\frac{1}{2}, 1, 2 + m, -\frac{b \tan [c + d x]}{a}, i \tan [c + d x] \right] \right. \\ \left. \tan [c + d x]^{1+m} \sqrt{a + b \tan [c + d x]} \right) / \left( 2 d (1 + m) \sqrt{1 + \frac{b \tan [c + d x]}{a}} \right)$$

Result (type 8, 35 leaves):

$$\int \tan [c + d x]^m \sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x]) dx$$

### Problem 490: Unable to integrate problem.

$$\int \frac{\tan [c+d x]^m (A+B \tan [c+d x])}{\sqrt{a+b \tan [c+d x]}} dx$$

Optimal (type 6, 187 leaves, 7 steps):

$$\left( (A+i B) \operatorname{AppellF1}\left[1+m, \frac{1}{2}, 1, 2+m, -\frac{b \tan [c+d x]}{a}, -i \tan [c+d x]\right] \right. \\ \left. \tan [c+d x]^{1+m} \sqrt{1+\frac{b \tan [c+d x]}{a}} \right) / \left( 2 d (1+m) \sqrt{a+b \tan [c+d x]} \right) + \\ \left( (A-i B) \operatorname{AppellF1}\left[1+m, \frac{1}{2}, 1, 2+m, -\frac{b \tan [c+d x]}{a}, i \tan [c+d x]\right] \right. \\ \left. \tan [c+d x]^{1+m} \sqrt{1+\frac{b \tan [c+d x]}{a}} \right) / \left( 2 d (1+m) \sqrt{a+b \tan [c+d x]} \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\tan [c+d x]^m (A+B \tan [c+d x])}{\sqrt{a+b \tan [c+d x]}} dx$$

### Problem 491: Unable to integrate problem.

$$\int \frac{\tan [c+d x]^m (A+B \tan [c+d x])}{(a+b \tan [c+d x])^{3/2}} dx$$

Optimal (type 6, 193 leaves, 7 steps):

$$\left( (A+i B) \operatorname{AppellF1}\left[1+m, \frac{3}{2}, 1, 2+m, -\frac{b \tan [c+d x]}{a}, -i \tan [c+d x]\right] \right. \\ \left. \tan [c+d x]^{1+m} \sqrt{1+\frac{b \tan [c+d x]}{a}} \right) / \left( 2 a d (1+m) \sqrt{a+b \tan [c+d x]} \right) + \\ \left( (A-i B) \operatorname{AppellF1}\left[1+m, \frac{3}{2}, 1, 2+m, -\frac{b \tan [c+d x]}{a}, i \tan [c+d x]\right] \right. \\ \left. \tan [c+d x]^{1+m} \sqrt{1+\frac{b \tan [c+d x]}{a}} \right) / \left( 2 a d (1+m) \sqrt{a+b \tan [c+d x]} \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\tan [c+d x]^m (A+B \tan [c+d x])}{(a+b \tan [c+d x])^{3/2}} dx$$

**Problem 492: Unable to integrate problem.**

$$\int \frac{\tan [c+d x]^m (A+B \tan [c+d x])}{(a+b \tan [c+d x])^{5/2}} dx$$

Optimal (type 6, 193 leaves, 7 steps):

$$\left( (A+i B) \operatorname{AppellF1}\left[1+m, \frac{5}{2}, 1, 2+m, -\frac{b \tan [c+d x]}{a}, -i \tan [c+d x]\right] \right. \\ \left. \tan [c+d x]^{1+m} \sqrt{1+\frac{b \tan [c+d x]}{a}} \right) / \left( 2 a^2 d (1+m) \sqrt{a+b \tan [c+d x]} \right) + \\ \left( (A-i B) \operatorname{AppellF1}\left[1+m, \frac{5}{2}, 1, 2+m, -\frac{b \tan [c+d x]}{a}, i \tan [c+d x]\right] \right. \\ \left. \tan [c+d x]^{1+m} \sqrt{1+\frac{b \tan [c+d x]}{a}} \right) / \left( 2 a^2 d (1+m) \sqrt{a+b \tan [c+d x]} \right)$$

Result (type 8, 35 leaves):

$$\int \frac{\tan [c+d x]^m (A+B \tan [c+d x])}{(a+b \tan [c+d x])^{5/2}} dx$$

**Problem 493: Unable to integrate problem.**

$$\int \tan [c+d x]^m (a+b \tan [c+d x])^n (A+B \tan [c+d x]) dx$$

Optimal (type 6, 183 leaves, 7 steps):

$$\frac{1}{2 d (1+m)} (A+i B) \operatorname{AppellF1}\left[1+m, -n, 1, 2+m, -\frac{b \tan [c+d x]}{a}, -i \tan [c+d x]\right] \\ \tan [c+d x]^{1+m} (a+b \tan [c+d x])^n \left(1+\frac{b \tan [c+d x]}{a}\right)^{-n} + \frac{1}{2 d (1+m)} \\ (A-i B) \operatorname{AppellF1}\left[1+m, -n, 1, 2+m, -\frac{b \tan [c+d x]}{a}, i \tan [c+d x]\right] \\ \tan [c+d x]^{1+m} (a+b \tan [c+d x])^n \left(1+\frac{b \tan [c+d x]}{a}\right)^{-n}$$

Result (type 8, 33 leaves):

$$\int \tan [c + d x]^m (a + b \tan [c + d x])^n (A + B \tan [c + d x]) dx$$

### Problem 494: Unable to integrate problem.

$$\int \tan [c + d x]^4 (a + b \tan [c + d x])^n (A + B \tan [c + d x]) dx$$

Optimal (type 5, 387 leaves, 9 steps):

$$\begin{aligned} & - \left( \left( (A b^3 (2+n) (3+n) (4+n) - a (b^2 B (3+n) (4+n) - 2 a (3 a B - A b (4+n))) \right) \right. \\ & \quad \left. (a + b \tan [c + d x])^{1+n} \right) / (b^4 d (1+n) (2+n) (3+n) (4+n)) + \\ & \left( (A - i B) \operatorname{Hypergeometric2F1} \left[ 1, 1+n, 2+n, \frac{a + b \tan [c + d x]}{a - i b} \right] (a + b \tan [c + d x])^{1+n} \right) / \\ & \quad (2 (i a + b) d (1+n)) - \\ & \left( (A + i B) \operatorname{Hypergeometric2F1} \left[ 1, 1+n, 2+n, \frac{a + b \tan [c + d x]}{a + i b} \right] (a + b \tan [c + d x])^{1+n} \right) / \\ & \quad (2 (i a - b) d (1+n)) - \\ & \left( (b^2 B (3+n) (4+n) - 2 a (3 a B - A b (4+n))) \tan [c + d x] (a + b \tan [c + d x])^{1+n} \right) / \\ & \quad (b^3 d (2+n) (3+n) (4+n)) - \\ & \frac{(3 a B - A b (4+n)) \tan [c + d x]^2 (a + b \tan [c + d x])^{1+n}}{b^2 d (3+n) (4+n)} + \frac{B \tan [c + d x]^3 (a + b \tan [c + d x])^{1+n}}{b d (4+n)} \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \tan [c + d x]^4 (a + b \tan [c + d x])^n (A + B \tan [c + d x]) dx$$

### Problem 495: Result more than twice size of optimal antiderivative.

$$\int \tan [c + d x]^3 (a + b \tan [c + d x])^n (A + B \tan [c + d x]) dx$$

Optimal (type 5, 291 leaves, 8 steps):

$$\begin{aligned} & \frac{(2 a^2 B - a A b (3+n) - b^2 B (6 + 5 n + n^2)) (a + b \tan [c + d x])^{1+n}}{b^3 d (1+n) (2+n) (3+n)} + \\ & \left( (i A + B) \operatorname{Hypergeometric2F1} \left[ 1, 1+n, 2+n, \frac{a + b \tan [c + d x]}{a - i b} \right] (a + b \tan [c + d x])^{1+n} \right) / \\ & \quad (2 (i a + b) d (1+n)) + \\ & \left( (A + i B) \operatorname{Hypergeometric2F1} \left[ 1, 1+n, 2+n, \frac{a + b \tan [c + d x]}{a + i b} \right] (a + b \tan [c + d x])^{1+n} \right) / \\ & \quad (2 (a + i b) d (1+n)) - \frac{(2 a B - A b (3+n)) \tan [c + d x] (a + b \tan [c + d x])^{1+n}}{b^2 d (2+n) (3+n)} + \\ & \frac{B \tan [c + d x]^2 (a + b \tan [c + d x])^{1+n}}{b d (3+n)} \end{aligned}$$

Result (type 5, 671 leaves):

$$\frac{1}{2 b^3 d n (1+n) (2+n) (3+n) (A \cos [c+d x]+B \sin [c+d x])} \cos [c+d x] (a+b \tan [c+d x])^n$$

$$(A+B \tan [c+d x]) \left( 4 a^3 B n-2 a^2 A b n(3+n)-2 a b^2 B n(2+n)(3+n)-4 a^2 b B n^2 \tan [c+d x]+ \right.$$

$$2 a A b^2 n^2(3+n) \tan [c+d x]-2 b^3 B n(2+n)(3+n) \tan [c+d x]+2 a b^2 B n^2 \tan [c+d x]^2+ \left. \right.$$

$$2 a b^2 B n^3 \tan [c+d x]^2+2 A b^3 n(3+n) \tan [c+d x]^2+2 A b^3 n^2(3+n) \tan [c+d x]^2+ \left. \right.$$

$$4 b^3 B n \tan [c+d x]^3+6 b^3 B n^2 \tan [c+d x]^3+2 b^3 B n^3 \tan [c+d x]^3- \left. \right.$$

$$A b^3(1+n)(2+n)(3+n) \operatorname{Hypergeometric2F1}\left[-n,-n, 1-n, \frac{a+i b}{i b-b \tan [c+d x]}\right] \left. \right.$$

$$\left(\frac{a+b \tan [c+d x]}{b(-i+\tan [c+d x])}\right)^{-n}-i b^3 B(1+n)(2+n)(3+n) \left. \right.$$

$$\operatorname{Hypergeometric2F1}\left[-n,-n, 1-n, \frac{a+i b}{i b-b \tan [c+d x]}\right] \left(\frac{a+b \tan [c+d x]}{b(-i+\tan [c+d x])}\right)^{-n}- \left. \right.$$

$$A b^3(1+n)(2+n)(3+n) \operatorname{Hypergeometric2F1}\left[-n,-n, 1-n, -\frac{a-i b}{i b+b \tan [c+d x]}\right] \left. \right.$$

$$\left(\frac{a+b \tan [c+d x]}{i b+b \tan [c+d x]}\right)^{-n}+i b^3 B(1+n)(2+n)(3+n) \left. \right.$$

$$\operatorname{Hypergeometric2F1}\left[-n,-n, 1-n, -\frac{a-i b}{i b+b \tan [c+d x]}\right] \left(\frac{a+b \tan [c+d x]}{i b+b \tan [c+d x]}\right)^{-n}- \left. \right.$$

$$4 a^3 B n\left(1+\frac{b \tan [c+d x]}{a}\right)^{-n}+2 a^2 A b n(3+n)\left(1+\frac{b \tan [c+d x]}{a}\right)^{-n}$$

**Problem 496: Result more than twice size of optimal antiderivative.**

$$\int \tan [c+d x]^2(a+b \tan [c+d x])^n(A+B \tan [c+d x]) d x$$

Optimal (type 5, 219 leaves, 7 steps):

$$-\frac{(a B-A b(2+n))(a+b \tan [c+d x])^{1+n}}{b^2 d(1+n)(2+n)} +$$

$$\left(\frac{(i A+B) \operatorname{Hypergeometric2F1}\left[1, 1+n, 2+n, \frac{a+b \tan [c+d x]}{a-i b}\right](a+b \tan [c+d x])^{1+n}}{(2(a-i b) d(1+n))} + \right.$$

$$\left.\frac{(A+i B) \operatorname{Hypergeometric2F1}\left[1, 1+n, 2+n, \frac{a+b \tan [c+d x]}{a+i b}\right](a+b \tan [c+d x])^{1+n}}{(2(i a-b) d(1+n))} + \frac{B \tan [c+d x](a+b \tan [c+d x])^{1+n}}{b d(2+n)}\right)$$

Result (type 5, 495 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^2 d n (1+n) (2+n) (A \cos [c+d x] + B \sin [c+d x])} \\
 & \cos [c+d x] (a+b \tan [c+d x])^n (A+B \tan [c+d x]) \\
 & \left( -2 a^2 B n + 2 a A b n (2+n) + 2 a b B n^2 \tan [c+d x] + 2 A b^2 n (2+n) \tan [c+d x] + \right. \\
 & \quad \left. 2 b^2 B n \tan [c+d x]^2 + 2 b^2 B n^2 \tan [c+d x]^2 + i A b^2 (1+n) (2+n) \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -n, -n, 1-n, \frac{a+i b}{i b-b \tan [c+d x]} \right] \left( \frac{a+b \tan [c+d x]}{b(-i+\tan [c+d x])} \right)^{-n} - \right. \\
 & \quad \left. b^2 B (1+n) (2+n) \text{Hypergeometric2F1} \left[ -n, -n, 1-n, \frac{a+i b}{i b-b \tan [c+d x]} \right] \right. \\
 & \quad \left. \left( \frac{a+b \tan [c+d x]}{b(-i+\tan [c+d x])} \right)^{-n} - i A b^2 (1+n) (2+n) \right. \\
 & \quad \left. \text{Hypergeometric2F1} \left[ -n, -n, 1-n, -\frac{a-i b}{i b+b \tan [c+d x]} \right] \left( \frac{a+b \tan [c+d x]}{i b+b \tan [c+d x]} \right)^{-n} - \right. \\
 & \quad \left. b^2 B (1+n) (2+n) \text{Hypergeometric2F1} \left[ -n, -n, 1-n, -\frac{a-i b}{i b+b \tan [c+d x]} \right] \right. \\
 & \quad \left. \left( \frac{a+b \tan [c+d x]}{i b+b \tan [c+d x]} \right)^{-n} + 2 a^2 B n \left( 1 + \frac{b \tan [c+d x]}{a} \right)^{-n} \right)
 \end{aligned}$$

**Problem 507: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \tan [c+d x]) (A+B \tan [c+d x])}{\cot [c+d x]^{3/2}} dx$$

Optimal (type 3, 105 leaves, 6 steps):

$$\begin{aligned}
 & -\frac{2(-1)^{1/4} a (i A+B) \text{ArcTanh} \left[ (-1)^{3/4} \sqrt{\cot [c+d x]} \right]}{d} + \\
 & \frac{2 i a B}{5 d \cot [c+d x]^{5/2}} + \frac{2 a (i A+B)}{3 d \cot [c+d x]^{3/2}} + \frac{2 a (A-i B)}{d \sqrt{\cot [c+d x]}}
 \end{aligned}$$

Result (type 3, 362 leaves):

$$a \left( \frac{1}{d (\cos [d x] + i \sin [d x]) (A \cos [c + d x] + B \sin [c + d x]) \sqrt{\cot [c + d x]} (i + \cot [c + d x]) (B + A \cot [c + d x])} \right. \\ \left( \sec [c] \sec [c + d x]^2 \left( \frac{2 \cos [c]}{15} - \frac{2}{15} i \sin [c] \right) (5 i A \cos [c] + 5 B \cos [c] + 3 i B \sin [c]) + \right. \\ \left. \sec [c] \left( \frac{2 \cos [c]}{15} - \frac{2}{15} i \sin [c] \right) (-5 i A \cos [c] - 5 B \cos [c] + 15 A \sin [c] - 18 i B \sin [c]) + \right. \\ \left. i B \sec [c] \sec [c + d x]^3 \left( \frac{2 \cos [c]}{5} - \frac{2}{5} i \sin [c] \right) \sin [d x] + \right. \\ \left. \sec [c] \sec [c + d x] \left( \frac{2 \cos [c]}{5} - \frac{2}{5} i \sin [c] \right) (5 A \sin [d x] - 6 i B \sin [d x]) \right) \sin [c + d x]^2 + \\ \left( (i A + B) \operatorname{ArcCosh} [e^{2 i (c+d x)}] \sqrt{\cot [c + d x]} (i + \cot [c + d x]) (B + A \cot [c + d x]) \right. \\ \left. (\cos [c] - i \sin [c]) \sin [c + d x]^2 \sqrt{i \tan [c + d x]} \right) / \\ \left. (d (\cos [d x] + i \sin [d x]) (A \cos [c + d x] + B \sin [c + d x])) \right)$$

**Problem 508: Result more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^{7/2} (a + i a \tan [c + d x])^2 (A + B \tan [c + d x]) dx$$

Optimal (type 3, 128 leaves, 6 steps):

$$\frac{4 (-1)^{1/4} a^2 (A - i B) \operatorname{ArcTanh} [(-1)^{3/4} \sqrt{\cot [c + d x]}]}{d} + \frac{4 a^2 (A - i B) \sqrt{\cot [c + d x]}}{d} - \\ \frac{2 a^2 (7 i A + 5 B) \cot [c + d x]^{3/2}}{15 d} - \frac{2 A \cot [c + d x]^{3/2} (i a^2 + a^2 \cot [c + d x])}{5 d}$$

Result (type 3, 330 leaves):

$$a^2 \left( \frac{1}{d (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \sqrt{\cot [c + d x]} (i + \cot [c + d x])^2} \right. \\ (B + A \cot [c + d x]) \left( \csc [c] (-10 i A \cos [c] - 5 B \cos [c] + 33 A \sin [c] - 30 i B \sin [c]) \right. \\ \left( \frac{2}{15} \cos [2 c] - \frac{2}{15} i \sin [2 c] \right) + \csc [c + d x]^2 \left( -\frac{2}{5} A \cos [2 c] + \frac{2}{5} i A \sin [2 c] \right) + \csc [c] \\ \left. \csc [c + d x] \left( \frac{2}{3} \cos [2 c] - \frac{2}{3} i \sin [2 c] \right) (2 i A \sin [d x] + B \sin [d x]) \right) \sin [c + d x]^3 + \\ \left( 2 (A - i B) \operatorname{ArcCosh} [e^{2 i (c+d x)}] (i + \cot [c + d x])^2 (B + A \cot [c + d x]) \right. \\ \left. (\cos [2 c] - i \sin [2 c]) \sin [c + d x]^3 \right) / \\ \left. (d \cot [c + d x]^{3/2} (\cos [d x] + i \sin [d x])^2 (A \cos [c + d x] + B \sin [c + d x]) (i \tan [c + d x])^{3/2} \right)$$



### Problem 513: Result more than twice size of optimal antiderivative.

$$\int \text{Cot}[c + dx]^{9/2} (a + i a \text{Tan}[c + dx])^3 (A + B \text{Tan}[c + dx]) dx$$

Optimal (type 3, 171 leaves, 7 steps):

$$\frac{8 (-1)^{1/4} a^3 (i A + B) \text{ArcTanh}\left[(-1)^{3/4} \sqrt{\text{Cot}[c + dx]}\right]}{d} + \frac{8 a^3 (i A + B) \sqrt{\text{Cot}[c + dx]}}{d} + \frac{8 a^3 (23 A - 21 i B) \text{Cot}[c + dx]^{3/2}}{105 d} - \frac{2 a A \text{Cot}[c + dx]^{3/2} (i a + a \text{Cot}[c + dx])^2}{7 d} - \frac{2 (11 i A + 7 B) \text{Cot}[c + dx]^{3/2} (i a^3 + a^3 \text{Cot}[c + dx])}{35 d}$$

Result (type 3, 384 leaves):

$$a^3 \left( \frac{1}{d (\text{Cos}[dx] + i \text{Sin}[dx])^3 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx])} \sqrt{\text{Cot}[c + dx]} (i + \text{Cot}[c + dx])^3 (B + A \text{Cot}[c + dx]) \left( \text{Csc}[c] (155 A \text{Cos}[c] - 105 i B \text{Cos}[c] + 483 i A \text{Sin}[c] + 441 B \text{Sin}[c]) \left( \frac{2}{105} \text{Cos}[3c] - \frac{2}{105} i \text{Sin}[3c] \right) + \text{Csc}[c] \text{Csc}[c + dx]^2 (5 A \text{Cos}[c] + 21 i A \text{Sin}[c] + 7 B \text{Sin}[c]) \left( -\frac{2}{35} \text{Cos}[3c] + \frac{2}{35} i \text{Sin}[3c] \right) + A \text{Csc}[c] \text{Csc}[c + dx]^3 \left( \frac{2}{7} \text{Cos}[3c] - \frac{2}{7} i \text{Sin}[3c] \right) \text{Sin}[dx] + \text{Csc}[c] \text{Csc}[c + dx] \left( -\frac{2}{21} \text{Cos}[3c] + \frac{2}{21} i \text{Sin}[3c] \right) (31 A \text{Sin}[dx] - 21 i B \text{Sin}[dx]) \right) \text{Sin}[c + dx]^4 + (4 (A - i B) \text{ArcCosh}\left[e^{2i(c+dx)}\right] (i + \text{Cot}[c + dx])^3 (B + A \text{Cot}[c + dx]) (\text{Cos}[3c] - i \text{Sin}[3c]) \text{Sin}[c + dx]^4) / (d \sqrt{\text{Cot}[c + dx]} (\text{Cos}[dx] + i \text{Sin}[dx])^3 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \sqrt{i \text{Tan}[c + dx]}) \right)$$

### Problem 518: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \text{Tan}[c + dx])^3 (A + B \text{Tan}[c + dx])}{\sqrt{\text{Cot}[c + dx]}} dx$$

Optimal (type 3, 173 leaves, 7 steps):

$$\frac{8 (-1)^{1/4} a^3 (A - i B) \text{ArcTanh}\left[(-1)^{3/4} \sqrt{\text{Cot}[c + dx]}\right]}{d} - \frac{8 a^3 (21 A - 23 i B)}{105 d \text{Cot}[c + dx]^{3/2}} + \frac{8 a^3 (i A + B)}{d \sqrt{\text{Cot}[c + dx]}} + \frac{2 i a B (i a + a \text{Cot}[c + dx])^2}{7 d \text{Cot}[c + dx]^{7/2}} - \frac{2 (7 A - 11 i B) (i a^3 + a^3 \text{Cot}[c + dx])}{35 d \text{Cot}[c + dx]^{5/2}}$$

Result (type 3, 433 leaves):

$$a^3 \left( \frac{1}{d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x])} \sqrt{\cot [c + d x]} (i + \cot [c + d x])^3 \right. \\
(B + A \cot [c + d x]) \left( \sec [c] (105 A \cos [c] - 155 i B \cos [c] + 441 i A \sin [c] + 483 B \sin [c]) \right. \\
\left. \left( \frac{2}{105} \cos [3 c] - \frac{2}{105} i \sin [3 c] \right) + \right. \\
\sec [c] \sec [c + d x]^2 (105 A \cos [c] - 170 i B \cos [c] + 21 i A \sin [c] + 63 B \sin [c]) \\
\left. \left( -\frac{2}{105} \cos [3 c] + \frac{2}{105} i \sin [3 c] \right) + \sec [c + d x]^4 \left( -\frac{2}{7} i B \cos [3 c] - \frac{2}{7} B \sin [3 c] \right) + \right. \\
\sec [c] \sec [c + d x]^3 \left( \frac{2}{5} \cos [3 c] - \frac{2}{5} i \sin [3 c] \right) (-i A \sin [d x] - 3 B \sin [d x]) + \sec [c] \\
\left. \sec [c + d x] \left( \frac{2}{5} \cos [3 c] - \frac{2}{5} i \sin [3 c] \right) (21 i A \sin [d x] + 23 B \sin [d x]) \right) \sin [c + d x]^4 - \\
(4 (A - i B) \operatorname{ArcCosh}[e^{2 i (c+d x)}] \sqrt{\cot [c + d x]} (i + \cot [c + d x])^3 (B + A \cot [c + d x]) \\
(\cos [3 c] - i \sin [3 c]) \sin [c + d x]^4 \sqrt{i \tan [c + d x]}) / \\
\left. \left( d (\cos [d x] + i \sin [d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right) \right)$$

### Problem 540: Unable to integrate problem.

$$\int \frac{\sqrt{a + i a \tan [c + d x]} (A + B \tan [c + d x])}{\sqrt{\cot [c + d x]}} dx$$

Optimal (type 3, 192 leaves, 9 steps):

$$-\frac{1}{d} (-1)^{3/4} \sqrt{a} (2A - iB) \operatorname{ArcTan} \left[ \frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan [c + d x]}}{\sqrt{a + i a \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} - \\
\frac{1}{d} (1 + i) \sqrt{a} (A - iB) \operatorname{ArcTanh} \left[ \frac{(1 + i) \sqrt{a} \sqrt{\tan [c + d x]}}{\sqrt{a + i a \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\
\frac{B \sqrt{a + i a \tan [c + d x]}}{d \sqrt{\cot [c + d x]}}$$

Result (type 8, 40 leaves):

$$\int \frac{\sqrt{a + i a \tan [c + d x]} (A + B \tan [c + d x])}{\sqrt{\cot [c + d x]}} dx$$

### Problem 545: Result more than twice size of optimal antiderivative.

$$\int \sqrt{\cot [c + d x]} (a + i a \tan [c + d x])^{3/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 196 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{d} (-1)^{3/4} a^{3/2} (2iA + 3B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \frac{1}{d} \\
 & (2-2i) a^{3/2} (A-iB) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \\
 & \frac{iaB \sqrt{a+ia \tan[c+dx]}}{d \sqrt{\cot[c+dx]}}
 \end{aligned}$$

Result (type 3, 485 leaves):

$$\begin{aligned}
 & \left( e^{-i(2c+dx)} \sqrt{e^{idx}} \sqrt{-1+e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \\
 & \left. \sqrt{\frac{i(1+e^{2i(c+dx)})}{-1+e^{2i(c+dx)}}} \left( -16i(A-iB) \operatorname{Log}\left[ e^{i(c+dx)} + \sqrt{-1+e^{2i(c+dx)}} \right] + \right. \right. \\
 & \left. \left. \sqrt{2} (2iA+3B) \left( \operatorname{Log}\left[ 1-3e^{2i(c+dx)} - 2\sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] - \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Log}\left[ 1-3e^{2i(c+dx)} + 2\sqrt{2} e^{i(c+dx)} \sqrt{-1+e^{2i(c+dx)}} \right] \right) \right) \right) \\
 & \left. (a+ia \tan[c+dx])^{3/2} (A+B \tan[c+dx]) \right) / \left( 4\sqrt{2} d \operatorname{Sec}[c+dx]^{5/2} \right. \\
 & \left. (\cos[dx] + i \sin[dx])^{3/2} (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( \cos[c+dx]^2 \sqrt{\cot[c+dx]} (iB \operatorname{Sec}[c] \operatorname{Sec}[c+dx] (\cos[c] - i \sin[c]) \sin[dx] + \right. \\
 & \left. i(B \cos[c] - iB \sin[c]) \tan[c]) (a+ia \tan[c+dx])^{3/2} (A+B \tan[c+dx]) \right) / \\
 & (d (\cos[dx] + i \sin[dx]) (A \cos[c+dx] + B \sin[c+dx]))
 \end{aligned}$$

**Problem 549: Result more than twice size of optimal antiderivative.**

$$\int \cot[c+dx]^{7/2} (a+ia \tan[c+dx])^{5/2} (A+B \tan[c+dx]) dx$$

Optimal (type 3, 205 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{1}{d} (4+4i) a^{5/2} (A-iB) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+ia \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \\
 & \frac{2a^2 (38A-35iB) \sqrt{\cot[c+dx]} \sqrt{a+ia \tan[c+dx]}}{15d} - \\
 & \frac{2a^2 (8iA+5B) \cot[c+dx]^{3/2} \sqrt{a+ia \tan[c+dx]}}{15d} - \frac{2aA \cot[c+dx]^{5/2} (a+ia \tan[c+dx])^{3/2}}{5d}
 \end{aligned}$$

Result (type 3, 416 leaves):

$$\begin{aligned}
 & - \left( \left( 4 \sqrt{2} (A - i B) e^{-i(3c+dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \sqrt{\frac{i(1 + e^{2i(c+dx)})}{-1 + e^{2i(c+dx)}}} \right. \right. \\
 & \quad \left. \left. \text{Log} \left[ e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}} \right] (a + i a \text{Tan}[c + dx])^{5/2} (A + B \text{Tan}[c + dx]) \right] \right) / \\
 & \quad \left( d \text{Sec}[c + dx]^{7/2} (\text{Cos}[dx] + i \text{Sin}[dx])^{5/2} (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right) \Bigg) + \\
 & \left( \text{Cos}[c + dx]^3 \sqrt{\text{Cot}[c + dx]} \left( (13A - 10iB) \left( \frac{8}{15} \text{Cos}[2c] - \frac{8}{15} i \text{Sin}[2c] \right) + \right. \right. \\
 & \quad \left. \left. \text{Csc}[c + dx]^2 \left( -\frac{2}{5} A \text{Cos}[2c] + \frac{2}{5} i A \text{Sin}[2c] \right) + (11A - 5iB) \text{Csc}[c + dx] \right. \right. \\
 & \quad \left. \left. \left( -\frac{2}{15} i \text{Cos}[3c + dx] - \frac{2}{15} \text{Sin}[3c + dx] \right) \right) (a + i a \text{Tan}[c + dx])^{5/2} (A + B \text{Tan}[c + dx]) \right) / \\
 & \quad \left( d (\text{Cos}[dx] + i \text{Sin}[dx])^2 (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right)
 \end{aligned}$$

**Problem 550: Result more than twice size of optimal antiderivative.**

$$\int \text{Cot}[c + dx]^{5/2} (a + i a \text{Tan}[c + dx])^{5/2} (A + B \text{Tan}[c + dx]) dx$$

Optimal (type 3, 230 leaves, 10 steps):

$$\begin{aligned}
 & \frac{1}{d} 2 (-1)^{3/4} a^{5/2} B \text{ArcTan} \left[ \frac{(-1)^{3/4} \sqrt{a} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a + i a \text{Tan}[c + dx]}} \right] \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Tan}[c + dx]} + \frac{1}{d} \\
 & (4 + 4i) a^{5/2} (iA + B) \text{ArcTanh} \left[ \frac{(1 + i) \sqrt{a} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a + i a \text{Tan}[c + dx]}} \right] \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Tan}[c + dx]} - \\
 & \frac{2 a^2 (2iA + B) \sqrt{\text{Cot}[c + dx]} \sqrt{a + i a \text{Tan}[c + dx]}}{d} - \frac{2 a A \text{Cot}[c + dx]^{3/2} (a + i a \text{Tan}[c + dx])^{3/2}}{3d}
 \end{aligned}$$

Result (type 3, 496 leaves):

$$\begin{aligned}
 & \left( e^{-i(3c+dx)} \sqrt{e^{i dx}} \sqrt{-1+e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \right. \\
 & \sqrt{\frac{i(1+e^{2i(c+dx)})}{-1+e^{2i(c+dx)}}} \left( 16(iA+B) \operatorname{Log}\left[e^{i(c+dx)} + \sqrt{-1+e^{2i(c+dx)}}\right] + \right. \\
 & \left. \sqrt{2} B \left( -\operatorname{Log}\left[1-3e^{2i(c+dx)} - 2\sqrt{2}e^{i(c+dx)}\sqrt{-1+e^{2i(c+dx)}}\right] + \right. \right. \\
 & \left. \left. \operatorname{Log}\left[1-3e^{2i(c+dx)} + 2\sqrt{2}e^{i(c+dx)}\sqrt{-1+e^{2i(c+dx)}}\right]\right) \right) \\
 & \left. (a+i a \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) \right) / \left( 2\sqrt{2} d \operatorname{Sec}[c+dx]^{7/2} \right. \\
 & \left. (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{5/2} (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right) + \\
 & \left( \operatorname{Cos}[c+dx]^3 \sqrt{\operatorname{Cot}[c+dx]} \left( (8A-3iB) \left( -\frac{2}{3}i \operatorname{Cos}[2c] - \frac{2}{3} \operatorname{Sin}[2c] \right) + \right. \right. \\
 & \left. \left. \operatorname{Csc}[c+dx] \left( -\frac{2}{3}A \operatorname{Cos}[3c+dx] + \frac{2}{3}iA \operatorname{Sin}[3c+dx] \right) \right) \right) \\
 & \left. (a+i a \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) \right) / \\
 & \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^2 (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right)
 \end{aligned}$$

### Problem 551: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cot}[c+dx]^{3/2} (a+i a \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) dx$$

Optimal (type 3, 236 leaves, 10 steps):

$$\begin{aligned}
 & \frac{1}{d} (-1)^{3/4} a^{5/2} (2A-5iB) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} + \frac{1}{d} \\
 & (4+4i) a^{5/2} (A-iB) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+i a \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} + \\
 & \frac{a^2 (2iA-B) \sqrt{a+i a \operatorname{Tan}[c+dx]}}{d \sqrt{\operatorname{Cot}[c+dx]}} - \frac{2aA \sqrt{\operatorname{Cot}[c+dx]} (a+i a \operatorname{Tan}[c+dx])^{3/2}}{d}
 \end{aligned}$$

Result (type 3, 496 leaves):

$$\left( e^{-i(3c+dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \right. \\ \left. \sqrt{\frac{i(1 + e^{2i(c+dx)})}{-1 + e^{2i(c+dx)}}} \left( 32(A - iB) \operatorname{Log}[e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}}] - \right. \right. \\ \left. \left. \sqrt{2}(2A - 5iB) \left( \operatorname{Log}[1 - 3e^{2i(c+dx)} - 2\sqrt{2}e^{i(c+dx)}\sqrt{-1 + e^{2i(c+dx)}}] - \right. \right. \right. \\ \left. \left. \left. \operatorname{Log}[1 - 3e^{2i(c+dx)} + 2\sqrt{2}e^{i(c+dx)}\sqrt{-1 + e^{2i(c+dx)}}] \right) \right) \right) \\ \left. \left( a + i a \operatorname{Tan}[c + dx] \right)^{5/2} (A + B \operatorname{Tan}[c + dx]) \right) / \left( 4\sqrt{2} d \operatorname{Sec}[c + dx]^{7/2} \right. \\ \left. (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{5/2} (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right) + \\ \left( \operatorname{Cos}[c + dx]^3 \sqrt{\operatorname{Cot}[c + dx]} (\operatorname{Sec}[c] (2A \operatorname{Cos}[c] + B \operatorname{Sin}[c]) (-\operatorname{Cos}[2c] + i \operatorname{Sin}[2c]) - \right. \\ \left. B \operatorname{Sec}[c] \operatorname{Sec}[c + dx] (\operatorname{Cos}[2c] - i \operatorname{Sin}[2c]) \operatorname{Sin}[dx]) \right. \\ \left. \left( a + i a \operatorname{Tan}[c + dx] \right)^{5/2} (A + B \operatorname{Tan}[c + dx]) \right) / \\ \left( d (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^2 (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right)$$

**Problem 552: Result more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Cot}[c + dx]} (a + i a \operatorname{Tan}[c + dx])^{5/2} (A + B \operatorname{Tan}[c + dx]) dx$$

Optimal (type 3, 246 leaves, 10 steps):

$$-\frac{1}{4d} (-1)^{3/4} a^{5/2} (20iA + 23B) \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c + dx]}}{\sqrt{a + i a \operatorname{Tan}[c + dx]}}\right] \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]} + \\ \frac{1}{d} (4 - 4i) a^{5/2} (A - iB) \operatorname{ArcTanh}\left[\frac{(1 + i) \sqrt{a} \sqrt{\operatorname{Tan}[c + dx]}}{\sqrt{a + i a \operatorname{Tan}[c + dx]}}\right] \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]} - \\ \frac{a^2 (4A - 7iB) \sqrt{a + i a \operatorname{Tan}[c + dx]}}{4d \sqrt{\operatorname{Cot}[c + dx]}} + \frac{i a B (a + i a \operatorname{Tan}[c + dx])^{3/2}}{2d \sqrt{\operatorname{Cot}[c + dx]}}$$

Result (type 3, 606 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^3 \sqrt{\cot [c+d x]} \right. \\
 & \quad \left( \sec [c] (2 B \cos [c] - 4 A \sin [c] + 9 i B \sin [c]) \left( \frac{1}{4} \cos [2 c] - \frac{1}{4} i \sin [2 c] \right) + \right. \\
 & \quad \left. \sec [c+d x]^2 \left( -\frac{1}{2} B \cos [2 c] + \frac{1}{2} i B \sin [2 c] \right) + \right. \\
 & \quad \left. \sec [c] \sec [c+d x] \left( \frac{1}{4} \cos [2 c] - \frac{1}{4} i \sin [2 c] \right) (-4 A \sin [d x] + 9 i B \sin [d x]) \right) \\
 & \quad \left. (a+i a \tan [c+d x])^{5/2} (A+B \tan [c+d x]) \right) / \\
 & \quad \left( d (\cos [d x] + i \sin [d x])^2 (A \cos [c+d x] + B \sin [c+d x]) \right) + \\
 & \quad \frac{1}{8 \sqrt{2} d (\cos [d x] + i \sin [d x])^2 (A \cos [c+d x] + B \sin [c+d x])} \\
 & \quad \left. \cos [c+d x]^3 \sqrt{\cot [c+d x]} \right. \\
 & \quad \left( \sqrt{2} (-20 i A - 23 B) \operatorname{Log} \left[ -\frac{2 e^{\frac{7 i c}{2}} (i \sqrt{2} + \sqrt{2} e^{i(c+d x)} - 2 \sqrt{-1 + e^{2 i(c+d x)}})}{(20 A - 23 i B) (-i + e^{i(c+d x)})} \right] + \right. \\
 & \quad \sqrt{2} (20 i A + 23 B) \operatorname{Log} \left[ -\frac{2 e^{\frac{7 i c}{2}} (-i \sqrt{2} + \sqrt{2} e^{i(c+d x)} + 2 \sqrt{-1 + e^{2 i(c+d x)}})}{(20 A - 23 i B) (i + e^{i(c+d x)})} \right] - \\
 & \quad 64 i (A - i B) \operatorname{Log} [(\cos [c] - i \sin [c])] \\
 & \quad \left. \left( \cos [c+d x] + i \sin [c+d x] + \sqrt{-1 + \cos [2(c+d x)]} + i \sin [2(c+d x)] \right) \right) \\
 & \quad \sqrt{i (i + \cot [c+d x]) \sin [c+d x]^2 (\cos [3 c+d x] - i \sin [3 c+d x])} \\
 & \quad \left. (a+i a \tan [c+d x])^{5/2} (A+B \tan [c+d x]) \right)
 \end{aligned}$$

**Problem 553: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \tan [c+d x])^{5/2} (A+B \tan [c+d x])}{\sqrt{\cot [c+d x]}} dx$$

Optimal (type 3, 292 leaves, 11 steps):

$$\begin{aligned}
 & -\frac{1}{8 d} (-1)^{3/4} a^{5/2} (46 A - 45 i B) \operatorname{ArcTan} \left[ \frac{(-1)^{3/4} \sqrt{a} \sqrt{\tan [c+d x]}}{\sqrt{a+i a \tan [c+d x]}} \right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]} - \\
 & \frac{1}{d} (4+4 i) a^{5/2} (A-i B) \operatorname{ArcTanh} \left[ \frac{(1+i) \sqrt{a} \sqrt{\tan [c+d x]}}{\sqrt{a+i a \tan [c+d x]}} \right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]} - \\
 & \frac{a^2 (2 A - 3 i B) \sqrt{a+i a \tan [c+d x]}}{4 d \cot [c+d x]^{3/2}} + \\
 & \frac{a^2 (18 i A + 19 B) \sqrt{a+i a \tan [c+d x]}}{8 d \sqrt{\cot [c+d x]}} + \frac{i a B (a+i a \tan [c+d x])^{3/2}}{3 d \cot [c+d x]^{3/2}}
 \end{aligned}$$

Result (type 3, 666 leaves):

$$\frac{1}{d \left( \cos [d x] + i \sin [d x] \right)^2 \left( A \cos [c + d x] + B \sin [c + d x] \right)}$$

$$\cos [c + d x]^3 \sqrt{\cot [c + d x]} \left( \sec [c] \left( 12 A \cos [c] - 26 i B \cos [c] + 54 i A \sin [c] + 65 B \sin [c] \right) \right.$$

$$\left. \left( \frac{1}{24} \cos [2 c] - \frac{1}{24} i \sin [2 c] \right) + \right.$$

$$\sec [c] \sec [c + d x]^2 \left( -6 A \cos [c] + 13 i B \cos [c] - 4 B \sin [c] \right) \left( \frac{1}{12} \cos [2 c] - \frac{1}{12} i \sin [2 c] \right) -$$

$$B \sec [c] \sec [c + d x]^3 \left( \frac{1}{3} \cos [2 c] - \frac{1}{3} i \sin [2 c] \right) \sin [d x] +$$

$$\sec [c] \sec [c + d x] \left( \frac{1}{24} \cos [2 c] - \frac{1}{24} i \sin [2 c] \right) \left( 54 i A \sin [d x] + 65 B \sin [d x] \right) \left. \right)$$

$$\left( a + i a \tan [c + d x] \right)^{5/2} \left( A + B \tan [c + d x] \right) -$$


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$$16 \sqrt{2} d \left( \cos [d x] + i \sin [d x] \right)^2 \left( A \cos [c + d x] + B \sin [c + d x] \right)$$

$$\cos [c + d x]^3 \sqrt{\cot [c + d x]}$$

$$\left( \sqrt{2} \left( 46 A - 45 i B \right) \log \left[ \frac{2 e^{\frac{7 i c}{2}} \left( \sqrt{2} - i \sqrt{2} e^{i (c+d x)} + 2 i \sqrt{-1 + e^{2 i (c+d x)}} \right)}{\left( 46 A - 45 i B \right) \left( -i + e^{i (c+d x)} \right)} \right] + \right.$$

$$\sqrt{2} \left( -46 A + 45 i B \right) \log \left[ \frac{2 e^{\frac{7 i c}{2}} \left( -i \sqrt{2} + \sqrt{2} e^{i (c+d x)} + 2 \sqrt{-1 + e^{2 i (c+d x)}} \right)}{\left( 46 i A + 45 B \right) \left( i + e^{i (c+d x)} \right)} \right] +$$

$$128 \left( A - i B \right) \log \left[ \left( \cos [c] - i \sin [c] \right) \right.$$

$$\left. \left. \left( \cos [c + d x] + i \sin [c + d x] + \sqrt{-1 + \cos [2 (c + d x)]} + i \sin [2 (c + d x)] \right) \right] \right)$$

$$\sqrt{i \left( i + \cot [c + d x] \right) \sin [c + d x]^2 \left( \cos [3 c + d x] - i \sin [3 c + d x] \right)}$$

$$\left( a + i a \tan [c + d x] \right)^{5/2} \left( A + B \tan [c + d x] \right)$$

**Problem 562: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cot [c + d x]^{3/2} \left( A + B \tan [c + d x] \right)}{\left( a + i a \tan [c + d x] \right)^{5/2}} dx$$

Optimal (type 3, 260 leaves, 8 steps):



$$\frac{1}{a^{5/2} d} \left( \frac{1}{8} + \frac{i}{8} \right) (A - i B) \operatorname{ArcTanh} \left[ \frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}} \right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} +$$

$$\frac{(A+i B) \sqrt{\cot[c+dx]}}{5 d (a+i a \tan[c+dx])^{5/2}} + \frac{(17 A+7 i B) \sqrt{\cot[c+dx]}}{30 a d (a+i a \tan[c+dx])^{3/2}} +$$

$$\frac{(151 A+41 i B) \sqrt{\cot[c+dx]}}{60 a^2 d \sqrt{a+i a \tan[c+dx]}} - \frac{(317 A+67 i B) \sqrt{\cot[c+dx]} \sqrt{a+i a \tan[c+dx]}}{60 a^3 d}$$

Result (type 3, 529 leaves):

$$\left( (A - i B) e^{-i(-2c+dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \sqrt{\frac{i(1 + e^{2i(c+dx)})}{-1 + e^{2i(c+dx)}}} \operatorname{Log} \left[ \right. \right.$$

$$\left. \left. e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}} \right] \operatorname{Sec}[c+dx]^{3/2} (\cos[dx] + i \sin[dx])^{5/2} (A + B \tan[c+dx]) \right) /$$

$$\frac{(4 \sqrt{2} d (A \cos[c+dx] + B \sin[c+dx]) (a + i a \tan[c+dx])^{5/2}) + 1}{d (A \cos[c+dx] + B \sin[c+dx]) (a + i a \tan[c+dx])^{5/2}}$$

$$\sqrt{\cot[c+dx]} \operatorname{Sec}[c+dx]^2 (\cos[dx] + i \sin[dx])^3$$

$$\left( (13 A + 8 i B) \cos[4 dx] \left( \frac{\cos[c]}{60} - \frac{1}{60} i \sin[c] \right) + (97 A + 32 i B) \cos[2 dx] \right.$$

$$\left. \left( \frac{\cos[c]}{60} + \frac{1}{60} i \sin[c] \right) + (463 A + 83 i B) \left( -\frac{1}{120} \cos[3 c] - \frac{1}{120} i \sin[3 c] \right) + \right.$$

$$(A + i B) \cos[6 dx] \left( \frac{1}{40} \cos[3 c] - \frac{1}{40} i \sin[3 c] \right) + (-97 i A + 32 B)$$

$$\left. \left( \frac{\cos[c]}{60} + \frac{1}{60} i \sin[c] \right) \sin[2 dx] + (-13 i A + 8 B) \left( \frac{\cos[c]}{60} - \frac{1}{60} i \sin[c] \right) \sin[4 dx] + \right.$$

$$\left. (-i A + B) \left( \frac{1}{40} \cos[3 c] - \frac{1}{40} i \sin[3 c] \right) \sin[6 dx] \right) (A + B \tan[c+dx])$$

**Problem 563: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cot[c+dx]} (A + B \tan[c+dx])}{(a + i a \tan[c+dx])^{5/2}} dx$$

Optimal (type 3, 214 leaves, 7 steps):

$$\frac{1}{a^{5/2} d} \left( \frac{1}{8} - \frac{i}{8} \right) (A - i B) \operatorname{ArcTanh} \left[ \frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a+i a \tan[c+dx]}} \right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} +$$

$$\frac{A + i B}{5 d \sqrt{\cot[c+dx]} (a + i a \tan[c+dx])^{5/2}} +$$

$$\frac{13 A + 3 i B}{30 a d \sqrt{\cot[c+dx]} (a + i a \tan[c+dx])^{3/2}} + \frac{67 A - 3 i B}{60 a^2 d \sqrt{\cot[c+dx]} \sqrt{a + i a \tan[c+dx]}}$$

Result (type 3, 531 leaves):

$$\begin{aligned}
 & - \left( \left( i (A - i B) e^{-i(-2c+dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \sqrt{\frac{i(1 + e^{2i(c+dx)})}{-1 + e^{2i(c+dx)}}} \operatorname{Log} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}} \right] \operatorname{Sec}[c + dx]^{3/2} (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^{5/2} (A + B \operatorname{Tan}[c + dx]) \right) \right) / \\
 & \quad \left( 4 \sqrt{2} d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + i a \operatorname{Tan}[c + dx])^{5/2} \right) + \\
 & \quad \frac{1}{d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + i a \operatorname{Tan}[c + dx])^{5/2}} \\
 & \quad \sqrt{\operatorname{Cot}[c + dx]} \operatorname{Sec}[c + dx]^2 (\operatorname{Cos}[dx] + i \operatorname{Sin}[dx])^3 \\
 & \quad \left( (32 i A + 3 B) \operatorname{Cos}[2 dx] \left( \frac{\operatorname{Cos}[c]}{60} + \frac{1}{60} i \operatorname{Sin}[c] \right) + (8 A + 3 i B) \operatorname{Cos}[4 dx] \right. \\
 & \quad \left. \left( \frac{1}{60} i \operatorname{Cos}[c] + \frac{\operatorname{Sin}[c]}{60} \right) + (-83 i A + 3 B) \left( \frac{1}{120} \operatorname{Cos}[3 c] + \frac{1}{120} i \operatorname{Sin}[3 c] \right) + \right. \\
 & \quad \left. (A + i B) \operatorname{Cos}[6 dx] \left( \frac{1}{40} i \operatorname{Cos}[3 c] + \frac{1}{40} \operatorname{Sin}[3 c] \right) + (32 A - 3 i B) \right. \\
 & \quad \left. \left( \frac{\operatorname{Cos}[c]}{60} + \frac{1}{60} i \operatorname{Sin}[c] \right) \operatorname{Sin}[2 dx] + (8 A + 3 i B) \left( \frac{\operatorname{Cos}[c]}{60} - \frac{1}{60} i \operatorname{Sin}[c] \right) \operatorname{Sin}[4 dx] + \right. \\
 & \quad \left. (A + i B) \left( \frac{1}{40} \operatorname{Cos}[3 c] - \frac{1}{40} i \operatorname{Sin}[3 c] \right) \operatorname{Sin}[6 dx] \right) (A + B \operatorname{Tan}[c + dx])
 \end{aligned}$$

**Problem 564: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan}[c + dx]}{\sqrt{\operatorname{Cot}[c + dx]} (a + i a \operatorname{Tan}[c + dx])^{5/2}} dx$$

Optimal (type 3, 216 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{1}{a^{5/2} d} \left( \frac{1}{8} + \frac{i}{8} \right) (A - i B) \operatorname{ArcTanh} \left[ \frac{(1 + i) \sqrt{a} \sqrt{\operatorname{Tan}[c + dx]}}{\sqrt{a + i a \operatorname{Tan}[c + dx]}} \right] \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]} + \\
 & \quad \frac{i A - B}{5 d \sqrt{\operatorname{Cot}[c + dx]} (a + i a \operatorname{Tan}[c + dx])^{5/2}} + \\
 & \quad \frac{3 i A + 7 B}{30 a d \sqrt{\operatorname{Cot}[c + dx]} (a + i a \operatorname{Tan}[c + dx])^{3/2}} - \frac{3 i A - 13 B}{60 a^2 d \sqrt{\operatorname{Cot}[c + dx]} \sqrt{a + i a \operatorname{Tan}[c + dx]}}
 \end{aligned}$$

Result (type 3, 529 leaves):

$$\begin{aligned}
 & - \left( \left( (A - i B) e^{-i(-2c+dx)} \sqrt{e^{i dx}} \sqrt{-1 + e^{2i(c+dx)}} \sqrt{\frac{e^{i(c+dx)}}{1 + e^{2i(c+dx)}}} \sqrt{\frac{i(1 + e^{2i(c+dx)})}{-1 + e^{2i(c+dx)}}} \operatorname{Log} \left[ \right. \right. \right. \\
 & \quad \left. \left. \left. e^{i(c+dx)} + \sqrt{-1 + e^{2i(c+dx)}} \right] \operatorname{Sec}[c+dx]^{3/2} (\cos[dx] + i \sin[dx])^{5/2} (A + B \tan[c+dx]) \right) \right) / \\
 & \quad \left( 4 \sqrt{2} d (A \cos[c+dx] + B \sin[c+dx]) (a + i a \tan[c+dx])^{5/2} \right) + \\
 & \quad \frac{1}{d (A \cos[c+dx] + B \sin[c+dx]) (a + i a \tan[c+dx])^{5/2}} \\
 & \quad \sqrt{\cot[c+dx]} \operatorname{Sec}[c+dx]^2 (\cos[dx] + i \sin[dx])^3 \\
 & \quad \left( (3A - 2iB) \cos[4dx] \left( -\frac{\cos[c]}{60} + \frac{1}{60} i \sin[c] \right) + (3A + 8iB) \cos[2dx] \right. \\
 & \quad \left. \left( \frac{\cos[c]}{60} + \frac{1}{60} i \sin[c] \right) + (3A - 17iB) \left( \frac{1}{120} \cos[3c] + \frac{1}{120} i \sin[3c] \right) \right) + \\
 & \quad (A + iB) \cos[6dx] \left( -\frac{1}{40} \cos[3c] + \frac{1}{40} i \sin[3c] \right) + (-3iA + 8B) \\
 & \quad \left( \frac{\cos[c]}{60} + \frac{1}{60} i \sin[c] \right) \sin[2dx] + (3iA + 2B) \left( \frac{\cos[c]}{60} - \frac{1}{60} i \sin[c] \right) \sin[4dx] + \\
 & \quad (A + iB) \left( \frac{1}{40} i \cos[3c] + \frac{1}{40} \sin[3c] \right) \sin[6dx] \left( A + B \tan[c+dx] \right)
 \end{aligned}$$

**Problem 565: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \tan[c+dx]}{\cot[c+dx]^{3/2} (a + i a \tan[c+dx])^{5/2}} dx$$

Optimal (type 3, 214 leaves, 7 steps):

$$\begin{aligned}
 & \frac{1}{a^{5/2} d} \left( \frac{1}{8} + \frac{i}{8} \right) (iA + B) \operatorname{ArcTanh} \left[ \frac{(1+i) \sqrt{a} \sqrt{\tan[c+dx]}}{\sqrt{a + i a \tan[c+dx]}} \right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \\
 & \quad \frac{iA - B}{5 d \cot[c+dx]^{3/2} (a + i a \tan[c+dx])^{5/2}} + \\
 & \quad \frac{A + 11iB}{30 a d \sqrt{\cot[c+dx]} (a + i a \tan[c+dx])^{3/2}} + \frac{13A - 37iB}{60 a^2 d \sqrt{\cot[c+dx]} \sqrt{a + i a \tan[c+dx]}}
 \end{aligned}$$

Result (type 3, 529 leaves):

$$\left( \left( i A + B \right) e^{-i (-2 c+d x)} \sqrt{e^{i d x}} \sqrt{-1+e^{2 i (c+d x)}} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \sqrt{\frac{i \left(1+e^{2 i (c+d x)}\right)}{-1+e^{2 i (c+d x)}}} \operatorname{Log}\left[ e^{i (c+d x)} + \sqrt{-1+e^{2 i (c+d x)}} \right] \operatorname{Sec}[c+d x]^{3/2} \left(\operatorname{Cos}[d x] + i \operatorname{Sin}[d x]\right)^{5/2} (A+B \operatorname{Tan}[c+d x]) \right) /$$

$$\frac{\left(4 \sqrt{2} d (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) (a+i a \operatorname{Tan}[c+d x])^{5/2}\right)+1}{d (A \operatorname{Cos}[c+d x]+B \operatorname{Sin}[c+d x]) (a+i a \operatorname{Tan}[c+d x])^{5/2}}$$

$$\sqrt{\operatorname{Cot}[c+d x]} \operatorname{Sec}[c+d x]^2 (\operatorname{Cos}[d x]+i \operatorname{Sin}[d x])^3$$

$$\left(\left(8 i A+17 B\right) \operatorname{Cos}[2 d x]\left(\frac{\operatorname{Cos}[c]}{60}+\frac{1}{60} i \operatorname{Sin}[c]\right)+(2 A+7 i B) \operatorname{Cos}[4 d x]\right.$$

$$\left.\left(\frac{1}{60} i \operatorname{Cos}[c]+\frac{\operatorname{Sin}[c]}{60}\right)+(-i A+B) \operatorname{Cos}[6 d x]\left(\frac{1}{40} \operatorname{Cos}[3 c]-\frac{1}{40} i \operatorname{Sin}[3 c]\right)+\right.$$

$$\left.(17 A-23 i B\right)\left(-\frac{1}{120} i \operatorname{Cos}[3 c]+\frac{1}{120} \operatorname{Sin}[3 c]\right)+(8 A-17 i B)\left(\frac{\operatorname{Cos}[c]}{60}+\frac{1}{60} i \operatorname{Sin}[c]\right)$$

$$\operatorname{Sin}[2 d x]+(2 A+7 i B)\left(\frac{\operatorname{Cos}[c]}{60}-\frac{1}{60} i \operatorname{Sin}[c]\right) \operatorname{Sin}[4 d x]+$$

$$(A+i B)\left(-\frac{1}{40} \operatorname{Cos}[3 c]+\frac{1}{40} i \operatorname{Sin}[3 c]\right) \operatorname{Sin}[6 d x]\left.(A+B \operatorname{Tan}[c+d x])\right)$$

**Problem 566: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Tan}[c+d x]}{\operatorname{Cot}[c+d x]^{5/2} (a+i a \operatorname{Tan}[c+d x])^{5/2}} dx$$

Optimal (type 3, 289 leaves, 11 steps):

$$\frac{2(-1)^{1/4} B \operatorname{ArcTan}\left[\frac{(-1)^{3/4} \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}}\right] \sqrt{\operatorname{Cot}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{a^{5/2} d} + \frac{1}{a^{5/2} d}$$

$$\frac{\left(\frac{1}{8}+\frac{i}{8}\right)(A-i B) \operatorname{ArcTanh}\left[\frac{(1+i) \sqrt{a} \sqrt{\operatorname{Tan}[c+d x]}}{\sqrt{a+i a \operatorname{Tan}[c+d x]}}\right] \sqrt{\operatorname{Cot}[c+d x]} \sqrt{\operatorname{Tan}[c+d x]}}{5 d \operatorname{Cot}[c+d x]^{5/2} (a+i a \operatorname{Tan}[c+d x])^{5/2}} +$$

$$\frac{i A-B}{6 a d \operatorname{Cot}[c+d x]^{3/2} (a+i a \operatorname{Tan}[c+d x])^{3/2}} - \frac{i A-7 B}{4 a^2 d \sqrt{\operatorname{Cot}[c+d x]} \sqrt{a+i a \operatorname{Tan}[c+d x]}}$$

Result (type 3, 646 leaves):

$$\begin{aligned}
 & \frac{1}{4 \sqrt{2} d (A \cos [c+d x] + B \sin [c+d x]) (a+i a \tan [c+d x])^{5/2}} \\
 & e^{-i(-2 c+d x)} \sqrt{e^{i d x}} \sqrt{-1+e^{2 i(c+d x)}} \sqrt{\frac{e^{i(c+d x)}}{1+e^{2 i(c+d x)}}} \sqrt{\frac{i(1+e^{2 i(c+d x)})}{-1+e^{2 i(c+d x)}}} \\
 & \left( (A-i B) \operatorname{Log}\left[e^{i(c+d x)} + \sqrt{-1+e^{2 i(c+d x)}}\right] + 2 i \sqrt{2} B \left( \operatorname{Log}\left[1-3 e^{2 i(c+d x)} - 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}}\right] \right. \right. \\
 & \quad \left. \left. - \operatorname{Log}\left[1-3 e^{2 i(c+d x)} + 2 \sqrt{2} e^{i(c+d x)} \sqrt{-1+e^{2 i(c+d x)}}\right] \right) \right) \\
 & \operatorname{Sec}[c+d x]^{3/2} (\cos [d x] + i \sin [d x])^{5/2} (A+B \tan [c+d x]) + \\
 & \frac{1}{d (A \cos [c+d x] + B \sin [c+d x]) (a+i a \tan [c+d x])^{5/2}} \\
 & \sqrt{\cot [c+d x]} \operatorname{Sec}[c+d x]^2 (\cos [d x] + i \sin [d x])^3 \\
 & \left( (7 A+12 i B) \cos [4 d x] \left( -\frac{\cos [c]}{60} + \frac{1}{60} i \sin [c] \right) + (17 A+72 i B) \cos [2 d x] \right. \\
 & \quad \left( \frac{\cos [c]}{60} + \frac{1}{60} i \sin [c] \right) + (23 A+123 i B) \left( -\frac{1}{120} \cos [3 c] - \frac{1}{120} i \sin [3 c] \right) + \\
 & \quad (A+i B) \cos [6 d x] \left( \frac{1}{40} \cos [3 c] - \frac{1}{40} i \sin [3 c] \right) + (-17 i A+72 B) \\
 & \quad \left( \frac{\cos [c]}{60} + \frac{1}{60} i \sin [c] \right) \sin [2 d x] + (7 A+12 i B) \left( \frac{1}{60} i \cos [c] + \frac{\sin [c]}{60} \right) \sin [4 d x] + \\
 & \quad \left. (-i A+B) \left( \frac{1}{40} \cos [3 c] - \frac{1}{40} i \sin [3 c] \right) \sin [6 d x] \right) (A+B \tan [c+d x])
 \end{aligned}$$

**Problem 567: Unable to integrate problem.**

$$\int \cot [c+d x]^m (a+i a \tan [c+d x])^n (A+B \tan [c+d x]) dx$$

Optimal (type 6, 179 leaves, 8 steps):

$$\frac{1}{d(1-m)} (A-i B) \operatorname{AppellF1}[1-m, 1-n, 1, 2-m, -i \tan [c+d x], i \tan [c+d x]]$$

$$\cot [c+d x]^{-1+m} (1+i \tan [c+d x])^{-n} (a+i a \tan [c+d x])^n + \frac{1}{d(1-m)} i B \cot [c+d x]^{-1+m}$$

$$\operatorname{Hypergeometric2F1}[1-m, 1-n, 2-m, -i \tan [c+d x]] (1+i \tan [c+d x])^{-n} (a+i a \tan [c+d x])^n$$

Result (type 8, 36 leaves):

$$\int \cot [c+d x]^m (a+i a \tan [c+d x])^n (A+B \tan [c+d x]) dx$$

**Problem 568: Unable to integrate problem.**

$$\int \cot [c+d x]^{5/2} (a+i a \tan [c+d x])^n (A+B \tan [c+d x]) dx$$

Optimal (type 6, 247 leaves, 11 steps):

$$\frac{2(3B + 2iAn)\sqrt{\cot[c+dx]}(a+ia\tan[c+dx])^n}{3d} - \frac{2A\cot[c+dx]^{3/2}(a+ia\tan[c+dx])^n}{3d} -$$

$$\frac{1}{d\sqrt{\cot[c+dx]}} 2(A-iB) \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, -i\tan[c+dx], i\tan[c+dx]\right]$$

$$(1+i\tan[c+dx])^{-n}(a+ia\tan[c+dx])^n -$$

$$\left(2(1-2n)(3iB-2An) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, -i\tan[c+dx]\right] \right.$$

$$\left. (1+i\tan[c+dx])^{-n}(a+ia\tan[c+dx])^n\right) / (3d\sqrt{\cot[c+dx]})$$

Result (type 8, 38 leaves):

$$\int \cot[c+dx]^{5/2} (a+ia\tan[c+dx])^n (A+B\tan[c+dx]) dx$$

### Problem 569: Unable to integrate problem.

$$\int \cot[c+dx]^{3/2} (a+ia\tan[c+dx])^n (A+B\tan[c+dx]) dx$$

Optimal (type 6, 194 leaves, 10 steps):

$$-\frac{2A\sqrt{\cot[c+dx]}(a+ia\tan[c+dx])^n}{d} + \frac{1}{d\sqrt{\cot[c+dx]}}$$

$$2(iA+B) \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, -i\tan[c+dx], i\tan[c+dx]\right]$$

$$(1+i\tan[c+dx])^{-n}(a+ia\tan[c+dx])^n - \frac{1}{d\sqrt{\cot[c+dx]}} 2iA(1-2n)$$

$$\operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, -i\tan[c+dx]\right] (1+i\tan[c+dx])^{-n}(a+ia\tan[c+dx])^n$$

Result (type 8, 38 leaves):

$$\int \cot[c+dx]^{3/2} (a+ia\tan[c+dx])^n (A+B\tan[c+dx]) dx$$

### Problem 570: Unable to integrate problem.

$$\int \sqrt{\cot[c+dx]} (a+ia\tan[c+dx])^n (A+B\tan[c+dx]) dx$$

Optimal (type 6, 158 leaves, 9 steps):

$$\frac{1}{d\sqrt{\cot[c+dx]}} 2(A-iB) \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, -i\tan[c+dx], i\tan[c+dx]\right]$$

$$(1+i\tan[c+dx])^{-n}(a+ia\tan[c+dx])^n + \frac{1}{d\sqrt{\cot[c+dx]}}$$

$$2iB \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, -i\tan[c+dx]\right] (1+i\tan[c+dx])^{-n}(a+ia\tan[c+dx])^n$$

Result (type 8, 38 leaves):

$$\int \sqrt{\cot [c+d x]} (a+i a \tan [c+d x])^n (A+B \tan [c+d x]) d x$$

Problem 571: Unable to integrate problem.

$$\int \frac{(a+i a \tan [c+d x])^n (A+B \tan [c+d x])}{\sqrt{\cot [c+d x]}} d x$$

Optimal (type 6, 215 leaves, 10 steps):

$$\begin{aligned} & \frac{2 B (a+i a \tan [c+d x])^n}{d (1+2 n) \sqrt{\cot [c+d x]}} - \frac{1}{d \sqrt{\cot [c+d x]}} \\ & 2 (i A+B) \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, -i \tan [c+d x], i \tan [c+d x]\right] \\ & (1+i \tan [c+d x])^{-n} (a+i a \tan [c+d x])^n + \\ & \left(2 (2 B n+i A (1+2 n)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, -i \tan [c+d x]\right] (1+i \tan [c+d x])^{-n} \right. \\ & \left. (a+i a \tan [c+d x])^n\right) / \left(d (1+2 n) \sqrt{\cot [c+d x]}\right) \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \frac{(a+i a \tan [c+d x])^n (A+B \tan [c+d x])}{\sqrt{\cot [c+d x]}} d x$$

Problem 572: Unable to integrate problem.

$$\int \frac{(a+i a \tan [c+d x])^n (A+B \tan [c+d x])}{\cot [c+d x]^{3/2}} d x$$

Optimal (type 6, 291 leaves, 11 steps):

$$\begin{aligned} & \frac{2 B (a+i a \tan [c+d x])^n}{d (3+2 n) \cot [c+d x]^{3/2}} - \frac{2 (2 i B n-A (3+2 n)) (a+i a \tan [c+d x])^n}{d (1+2 n) (3+2 n) \sqrt{\cot [c+d x]}} - \\ & \frac{1}{d \sqrt{\cot [c+d x]}} 2 (A-i B) \operatorname{AppellF1}\left[\frac{1}{2}, 1-n, 1, \frac{3}{2}, -i \tan [c+d x], i \tan [c+d x]\right] \\ & (1+i \tan [c+d x])^{-n} (a+i a \tan [c+d x])^n + \\ & \left(2 (2 A n (3+2 n)-i B (3+6 n+4 n^2)) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1-n, \frac{3}{2}, -i \tan [c+d x]\right] \right. \\ & \left. (1+i \tan [c+d x])^{-n} (a+i a \tan [c+d x])^n\right) / \left(d (1+2 n) (3+2 n) \sqrt{\cot [c+d x]}\right) \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \frac{(a+i a \tan [c+d x])^n (A+B \tan [c+d x])}{\cot [c+d x]^{3/2}} d x$$

### Problem 573: Unable to integrate problem.

$$\int \frac{(a + i a \tan [c + d x])^n (A + B \tan [c + d x])}{\cot [c + d x]^{5/2}} dx$$

Optimal (type 6, 383 leaves, 12 steps):

$$\begin{aligned} & \frac{2 B (a + i a \tan [c + d x])^n}{d (5 + 2 n) \cot [c + d x]^{5/2}} - \frac{2 (2 i B n - A (5 + 2 n)) (a + i a \tan [c + d x])^n}{d (3 + 2 n) (5 + 2 n) \cot [c + d x]^{3/2}} - \\ & \frac{2 (2 i A n (5 + 2 n) + B (15 + 10 n + 4 n^2)) (a + i a \tan [c + d x])^n}{d (1 + 2 n) (3 + 2 n) (5 + 2 n) \sqrt{\cot [c + d x]}} + \frac{1}{d \sqrt{\cot [c + d x]}} \\ & 2 (i A + B) \operatorname{AppellF1}\left[\frac{1}{2}, 1 - n, 1, \frac{3}{2}, -i \tan [c + d x], i \tan [c + d x]\right] (1 + i \tan [c + d x])^{-n} \\ & (a + i a \tan [c + d x])^n - \left(2 (4 B n (9 + 8 n + 2 n^2) + i A (15 + 36 n + 32 n^2 + 8 n^3)) \right. \\ & \quad \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, 1 - n, \frac{3}{2}, -i \tan [c + d x]\right] (1 + i \tan [c + d x])^{-n} \right. \\ & \quad \left. (a + i a \tan [c + d x])^n\right) / \left(d (1 + 2 n) (3 + 2 n) (5 + 2 n) \sqrt{\cot [c + d x]}\right) \end{aligned}$$

Result (type 8, 38 leaves):

$$\int \frac{(a + i a \tan [c + d x])^n (A + B \tan [c + d x])}{\cot [c + d x]^{5/2}} dx$$

### Problem 589: Result more than twice size of optimal antiderivative.

$$\int \frac{\cot [c + d x]^{5/2} (A + B \tan [c + d x])}{a + b \tan [c + d x]} dx$$

Optimal (type 3, 325 leaves, 17 steps):

$$\begin{aligned} & \frac{(b (A - B) - a (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\cot [c + d x]}\right]}{\sqrt{2} (a^2 + b^2) d} - \\ & \frac{(b (A - B) - a (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\cot [c + d x]}\right]}{\sqrt{2} (a^2 + b^2) d} - \\ & \frac{2 b^{5/2} (A b - a B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c + d x]}}{\sqrt{b}}\right]}{a^{5/2} (a^2 + b^2) d} + \frac{2 (A b - a B) \sqrt{\cot [c + d x]}}{a^2 d} - \\ & \frac{2 A \cot [c + d x]^{3/2}}{3 a d} + \frac{(a (A - B) + b (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\cot [c + d x]} + \cot [c + d x]\right]}{2 \sqrt{2} (a^2 + b^2) d} - \\ & \frac{(a (A - B) + b (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\cot [c + d x]} + \cot [c + d x]\right]}{2 \sqrt{2} (a^2 + b^2) d} \end{aligned}$$



Result (type 3, 750 leaves):

$$\begin{aligned} & \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \left( -\frac{2(-A b+a B)}{a^2} - \frac{2 A \cot [c+d x]}{3 a} \right) \right. \\ & \quad \left. (a \cos [c+d x]+b \sin [c+d x]) \right) / \left( d(b+a \cot [c+d x]) (A \cos [c+d x]+B \sin [c+d x]) \right) - \\ & \quad \frac{1}{2 a^2 d(b+a \cot [c+d x]) (A \cos [c+d x]+B \sin [c+d x])} \\ & \quad (B+A \cot [c+d x]) (a \cos [c+d x]+b \sin [c+d x]) \\ & \quad \left( -\left( \left( 2\left( a^2 A-2 A b^2+2 a b B \right) \operatorname{ArcTan}\left[ \frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}} \right] (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \right. \right. \right. \\ & \quad \left. \left. \left. \operatorname{Sec}[c+d x] \right) \right) / \left( \sqrt{a} \sqrt{b} (1+\cot [c+d x])^2 (a+b \tan [c+d x]) \right) \right) - \\ & \quad \left( a^{3 / 2} A \cos [2(c+d x)] (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \left( -4\left( a^2-b^2 \right) \operatorname{ArcTan}\left[ \right. \right. \right. \\ & \quad \left. \left. \left. \frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}} \right] + \sqrt{2} \sqrt{a} \sqrt{b} (-2(a-b) \operatorname{ArcTan}\left[ 1-\sqrt{2} \sqrt{\cot [c+d x]} \right] + \right. \right. \\ & \quad \left. \left. 2(a-b) \operatorname{ArcTan}\left[ 1+\sqrt{2} \sqrt{\cot [c+d x]} \right] + (a+b) \left( \operatorname{Log}\left[ 1-\sqrt{2} \sqrt{\cot [c+d x]} + \right. \right. \right. \\ & \quad \left. \left. \left. \cot [c+d x] \right] - \operatorname{Log}\left[ 1+\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x] \right] \right) \right) \right) \operatorname{Sec}[c+d x] \right) / \\ & \quad \left( 2 \sqrt{b} \left( a^2+b^2 \right) (-1+\cot [c+d x])^2 (1+\cot [c+d x])^2 (a+b \tan [c+d x]) \right) - \\ & \quad \frac{1}{4\left( a^2+b^2 \right) (1+\cot [c+d x])^2 (a+b \tan [c+d x])} \\ & \quad a^2 B(b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[ \frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}} \right] + \sqrt{2} \right. \\ & \quad \left( -2(a+b) \operatorname{ArcTan}\left[ 1-\sqrt{2} \sqrt{\cot [c+d x]} \right] + 2(a+b) \operatorname{ArcTan}\left[ 1+\sqrt{2} \sqrt{\cot [c+d x]} \right] - \right. \\ & \quad \left. (a-b) \left( \operatorname{Log}\left[ 1-\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x] \right] - \operatorname{Log}\left[ \right. \right. \right. \\ & \quad \left. \left. \left. 1+\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x] \right] \right) \right) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \right) \end{aligned}$$

**Problem 594: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \tan [c+d x]}{\cot [c+d x]^{5 / 2} (a+b \tan [c+d x])} d x$$

Optimal (type 3, 325 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{(a(A-B) + b(A+B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c+dx]}\right]}{\sqrt{2} (a^2 + b^2) d} + \\
 & \frac{(a(A-B) + b(A+B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c+dx]}\right]}{\sqrt{2} (a^2 + b^2) d} + \\
 & \frac{2 a^{5/2} (A b - a B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c+dx]}}{\sqrt{b}}\right]}{b^{5/2} (a^2 + b^2) d} + \frac{2 B}{3 b d \operatorname{Cot}[c+dx]^{3/2}} + \frac{2 (A b - a B)}{b^2 d \sqrt{\operatorname{Cot}[c+dx]}} + \\
 & \frac{(b(A-B) - a(A+B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c+dx]} + \operatorname{Cot}[c+dx]\right]}{2 \sqrt{2} (a^2 + b^2) d} - \\
 & \frac{(b(A-B) - a(A+B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c+dx]} + \operatorname{Cot}[c+dx]\right]}{2 \sqrt{2} (a^2 + b^2) d}
 \end{aligned}$$

Result (type 3, 779 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) (a \cos [c+d x]+b \sin [c+d x]) \right. \\
 & \left. \left( -\frac{2 B}{3 b} + \frac{2 B \sec [c+d x]^2}{3 b} + \frac{2 \sec [c+d x] (A b \sin [c+d x]-a B \sin [c+d x])}{b^2} \right) \right) / \\
 & \frac{(d(b+a \cot [c+d x]) (A \cos [c+d x]+B \sin [c+d x])) + 1}{2 b^2 d (b+a \cot [c+d x]) (A \cos [c+d x]+B \sin [c+d x])} \\
 & \frac{(B+A \cot [c+d x]) (a \cos [c+d x]+b \sin [c+d x])}{\left( -\left( \left( 2(-2 a A b+2 a^2 B-b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] (b+a \cot [c+d x]) \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Csc}[c+d x]^3 \sec [c+d x] \right) \right) / \left( \sqrt{a} \sqrt{b} (1+\cot [c+d x])^2 (a+b \tan [c+d x]) \right) \right) -} \\
 & \left( b^{3/2} B \cos [2(c+d x)] (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \left( -4(a^2-b^2) \operatorname{ArcTan}\left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}} \right] + \sqrt{2} \sqrt{a} \sqrt{b} (-2(a-b) \operatorname{ArcTan}[1-\sqrt{2} \sqrt{\cot [c+d x]}] + \right. \right. \\
 & \left. \left. 2(a-b) \operatorname{ArcTan}[1+\sqrt{2} \sqrt{\cot [c+d x]}] + (a+b) (\operatorname{Log}[1-\sqrt{2} \sqrt{\cot [c+d x]} + \right. \right. \\
 & \left. \left. \left. \cot [c+d x]] - \operatorname{Log}[1+\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x]]) \right) \right) \operatorname{Sec}[c+d x] \right) / \\
 & \frac{(2 \sqrt{a} (a^2+b^2) (-1+\cot [c+d x])^2 (1+\cot [c+d x])^2 (a+b \tan [c+d x])) + 1}{4(a^2+b^2) (1+\cot [c+d x])^2 (a+b \tan [c+d x])} \\
 & \frac{A b^2 (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \sqrt{2} \right.}{\left( -2(a+b) \operatorname{ArcTan}[1-\sqrt{2} \sqrt{\cot [c+d x]}] + 2(a+b) \operatorname{ArcTan}[1+\sqrt{2} \sqrt{\cot [c+d x]}] - \right.} \\
 & \left. (a-b) (\operatorname{Log}[1-\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x]] - \operatorname{Log}[1+\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x]]) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \right)
 \end{aligned}$$

**Problem 595: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cot [c+d x]^{3/2} (A+B \tan [c+d x])}{(a+b \tan [c+d x])^2} dx$$

Optimal (type 3, 438 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan} [1 - \sqrt{2} \sqrt{\operatorname{Cot} [c + d x]}] + \\
 & \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan} [1 + \sqrt{2} \sqrt{\operatorname{Cot} [c + d x]}] + \\
 & \frac{b^{3/2} (7 a^2 A b + 3 A b^3 - 5 a^3 B - a b^2 B) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \sqrt{\operatorname{Cot} [c + d x]}}{\sqrt{b}} \right]}{a^{5/2} (a^2 + b^2)^2 d} - \\
 & \frac{(2 a^2 A + 3 A b^2 - a b B) \sqrt{\operatorname{Cot} [c + d x]}}{a^2 (a^2 + b^2) d} + \frac{b (A b - a B) \operatorname{Cot} [c + d x]^{3/2}}{a (a^2 + b^2) d (b + a \operatorname{Cot} [c + d x])} + \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} \\
 & (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log} [1 - \sqrt{2} \sqrt{\operatorname{Cot} [c + d x]} + \operatorname{Cot} [c + d x]] - \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log} [1 + \sqrt{2} \sqrt{\operatorname{Cot} [c + d x]} + \operatorname{Cot} [c + d x]]
 \end{aligned}$$

Result(type 3, 859 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot[c+dx]} (B+A \cot[c+dx]) \csc[c+dx] (a \cos[c+dx] + b \sin[c+dx])^2 \right. \\
 & \left. \left( -\frac{2A}{a^2} + \frac{-Ab^3 \sin[c+dx] + ab^2 B \sin[c+dx]}{a^2 (a-ib)(a+ib)(a \cos[c+dx] + b \sin[c+dx])} \right) \right) / \\
 & \left( d (b+a \cot[c+dx])^2 (A \cos[c+dx] + B \sin[c+dx]) \right) - \\
 & \left( (B+A \cot[c+dx]) \csc[c+dx] (a \cos[c+dx] + b \sin[c+dx])^2 \right. \\
 & \left. \left( -\left( \left( 2(3a^2Ab + 3Ab^3 - a^3B - ab^2B) \operatorname{ArcTan}\left[ \frac{\sqrt{a} \sqrt{\cot[c+dx]}}{\sqrt{b}} \right] (b+a \cot[c+dx]) \right. \right. \right. \right. \\
 & \left. \left. \left. \csc[c+dx]^3 \sec[c+dx] \right) \right) / \left( \sqrt{a} \sqrt{b} (1+\cot[c+dx])^2 (a+b \tan[c+dx]) \right) \right) - \\
 & \left( (a^2Ab - a^3B) \cos[2(c+dx)] (b+a \cot[c+dx]) \csc[c+dx]^3 \left( -4(a^2-b^2) \operatorname{ArcTan}\left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{a} \sqrt{\cot[c+dx]}}{\sqrt{b}} \right] + \sqrt{2} \sqrt{a} \sqrt{b} (-2(a-b) \operatorname{ArcTan}[1-\sqrt{2} \sqrt{\cot[c+dx]}] + \right. \right. \\
 & \left. \left. 2(a-b) \operatorname{ArcTan}[1+\sqrt{2} \sqrt{\cot[c+dx]}] + (a+b) \left( \operatorname{Log}[1-\sqrt{2} \sqrt{\cot[c+dx]} + \right. \right. \right. \\
 & \left. \left. \left. \cot[c+dx]] - \operatorname{Log}[1+\sqrt{2} \sqrt{\cot[c+dx]} + \cot[c+dx]] \right) \right) \right) \sec[c+dx] \right) / \\
 & \left( \frac{2\sqrt{a} \sqrt{b} (a^2+b^2) (-1+\cot[c+dx])^2 (1+\cot[c+dx])^2 (a+b \tan[c+dx])}{1} \right) - \\
 & \frac{4(a^2+b^2) (1+\cot[c+dx])^2 (a+b \tan[c+dx])}{1} \\
 & \left( a^3A + a^2bB \right) (b+a \cot[c+dx]) \csc[c+dx]^2 \left( -8\sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[ \frac{\sqrt{a} \sqrt{\cot[c+dx]}}{\sqrt{b}} \right] + \right. \\
 & \left. \sqrt{2} (-2(a+b) \operatorname{ArcTan}[1-\sqrt{2} \sqrt{\cot[c+dx]}] + 2(a+b) \operatorname{ArcTan}[1+ \right. \\
 & \left. \sqrt{2} \sqrt{\cot[c+dx]}] - (a-b) \left( \operatorname{Log}[1-\sqrt{2} \sqrt{\cot[c+dx]} + \cot[c+dx]] - \right. \right. \\
 & \left. \left. \operatorname{Log}[1+\sqrt{2} \sqrt{\cot[c+dx]} + \cot[c+dx]] \right) \right) \right) \sec[c+dx]^2 \sin[2(c+dx)] \right) / \\
 & \left( 2a^2 (a-ib)(a+ib) d (b+a \cot[c+dx])^2 (A \cos[c+dx] + B \sin[c+dx]) \right)
 \end{aligned}$$

**Problem 596: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cot[c+dx]} (A+B \tan[c+dx])}{(a+b \tan[c+dx])^2} dx$$

Optimal (type 3, 392 leaves, 16 steps):

$$\begin{aligned}
& - \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + \\
& \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] - \\
& \frac{\sqrt{b} (5 a^2 A b + A b^3 - 3 a^3 B + a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right]}{a^{3/2} (a^2 + b^2)^2 d} + \frac{b (A b - a B) \sqrt{\operatorname{Cot}[c + d x]}}{a (a^2 + b^2) d (b + a \operatorname{Cot}[c + d x])} - \\
& \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] + \\
& \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]
\end{aligned}$$

Result (type 3, 808 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot[c+dx]} (B+A \cot[c+dx]) \csc[c+dx] \right. \\
 & \quad \left. (a \cos[c+dx] + b \sin[c+dx]) (A b^2 \sin[c+dx] - a b B \sin[c+dx]) \right) / \\
 & \left( a (a - i b) (a + i b) d (b + a \cot[c+dx])^2 (A \cos[c+dx] + B \sin[c+dx]) \right) + \\
 & \left( (B+A \cot[c+dx]) \csc[c+dx] (a \cos[c+dx] + b \sin[c+dx])^2 \right. \\
 & \quad \left. - \left( \left( 2 (a^2 A + A b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \sqrt{\cot[c+dx]}}{\sqrt{b}} \right] (b + a \cot[c+dx]) \csc[c+dx]^3 \sec[c+dx] \right) \right) / \right. \\
 & \quad \left. \left( \sqrt{a} \sqrt{b} (1 + \cot[c+dx])^2 (a + b \tan[c+dx]) \right) \right) - \\
 & \left( (a^2 A + a b B) \cos[2(c+dx)] (b + a \cot[c+dx]) \csc[c+dx]^3 \left( -4 (a^2 - b^2) \operatorname{ArcTan} \left[ \right. \right. \right. \\
 & \quad \left. \left. \frac{\sqrt{a} \sqrt{\cot[c+dx]}}{\sqrt{b}} \right] + \sqrt{2} \sqrt{a} \sqrt{b} \left( -2 (a - b) \operatorname{ArcTan} [1 - \sqrt{2} \sqrt{\cot[c+dx]}] + \right. \right. \\
 & \quad \left. \left. 2 (a - b) \operatorname{ArcTan} [1 + \sqrt{2} \sqrt{\cot[c+dx]}] + (a + b) \left( \operatorname{Log} [1 - \sqrt{2} \sqrt{\cot[c+dx]} + \right. \right. \right. \\
 & \quad \left. \left. \left. \cot[c+dx] \right] - \operatorname{Log} [1 + \sqrt{2} \sqrt{\cot[c+dx]} + \cot[c+dx]] \right) \right) \right) \sec[c+dx] \Big) / \\
 & \left( \frac{2 \sqrt{a} \sqrt{b} (a^2 + b^2) (-1 + \cot[c+dx])^2 (1 + \cot[c+dx])^2 (a + b \tan[c+dx])}{1} \right) - \\
 & \frac{4 (a^2 + b^2) (1 + \cot[c+dx])^2 (a + b \tan[c+dx])}{1} \\
 & \left( -a A b + a^2 B \right) (b + a \cot[c+dx]) \csc[c+dx]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan} \left[ \frac{\sqrt{a} \sqrt{\cot[c+dx]}}{\sqrt{b}} \right] + \right. \\
 & \quad \sqrt{2} \left( -2 (a + b) \operatorname{ArcTan} [1 - \sqrt{2} \sqrt{\cot[c+dx]}] + 2 (a + b) \operatorname{ArcTan} [1 + \right. \\
 & \quad \left. \sqrt{2} \sqrt{\cot[c+dx]}] - (a - b) \left( \operatorname{Log} [1 - \sqrt{2} \sqrt{\cot[c+dx]} + \cot[c+dx]] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} [1 + \sqrt{2} \sqrt{\cot[c+dx]} + \cot[c+dx]] \right) \right) \right) \sec[c+dx]^2 \sin[2(c+dx)] \Big) / \\
 & \left( 2 a (a - i b) (a + i b) d (b + a \cot[c+dx])^2 (A \cos[c+dx] + B \sin[c+dx]) \right)
 \end{aligned}$$

**Problem 597: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + B \tan[c+dx]}{\sqrt{\cot[c+dx]} (a + b \tan[c+dx])^2} dx$$

Optimal (type 3, 390 leaves, 16 steps):

$$\frac{(a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right]}{\sqrt{2} (a^2 + b^2)^2 d} -$$

$$\frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] +$$

$$\frac{(3 a^2 A b - A b^3 - a^3 B + 3 a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right]}{\sqrt{a} \sqrt{b} (a^2 + b^2)^2 d} - \frac{(A b - a B) \sqrt{\operatorname{Cot}[c + d x]}}{(a^2 + b^2) d (b + a \operatorname{Cot}[c + d x])} -$$

$$\frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] +$$

$$\frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]$$

Result (type 3, 700 leaves):

$$\left(\sqrt{\operatorname{Cot}[c + d x]} (B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] \right. \\ \left. (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (-A b \operatorname{Sin}[c + d x] + a B \operatorname{Sin}[c + d x])\right) / \\ \left((a - i b) (a + i b) d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])\right) + \\ \left((B + A \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x] (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2 \right. \\ \left. - \left(\left(\left((A b - a B) \operatorname{Cos}[2(c + d x)] (b + a \operatorname{Cot}[c + d x]) \operatorname{Csc}[c + d x]\right)^3 \right. \right. \right. \\ \left. \left. \left(-4 (a^2 - b^2) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right] + \sqrt{2} \sqrt{a} \sqrt{b} \right. \right. \right. \\ \left. \left. \left(-2 (a - b) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + 2 (a - b) \operatorname{ArcTan}\left[ \right. \right. \right. \\ \left. \left. \left. 1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + (a + b) \left(\operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] - \right. \right. \right. \\ \left. \left. \left. \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]\right)\right)\right) \operatorname{Sec}[c + d x]\right) / \\ \left.(2 \sqrt{a} \sqrt{b} (a^2 + b^2) (-1 + \operatorname{Cot}[c + d x])^2 (1 + \operatorname{Cot}[c + d x])^2 (a + b \operatorname{Tan}[c + d x])\right) - \\ \frac{1}{4 (a^2 + b^2) (1 + \operatorname{Cot}[c + d x])^2 (a + b \operatorname{Tan}[c + d x])} (a A + b B) (b + a \operatorname{Cot}[c + d x]) \\ \operatorname{Csc}[c + d x]^2 \left(-8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right] + \sqrt{2} \right. \\ \left. (-2 (a + b) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + 2 (a + b) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] - \right. \\ \left. (a - b) \left(\operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] - \right. \right. \\ \left. \left. \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]\right)\right) \operatorname{Sec}[c + d x]^2 \operatorname{Sin}[2(c + d x)] \right) / \\ \left.(2 (a - i b) (a + i b) d (b + a \operatorname{Cot}[c + d x])^2 (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x])\right)$$



Problem 598: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{A + B \tan [c + d x]}{\cot [c + d x]^{3/2} (a + b \tan [c + d x])^2} dx$$

Optimal (type 3, 392 leaves, 16 steps):

$$\frac{(2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\cot [c + d x]}\right]}{\sqrt{2} (a^2 + b^2)^2 d} -$$

$$\frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\cot [c + d x]}\right] -$$

$$\frac{\sqrt{a} (a^2 A b - 3 A b^3 + a^3 B + 5 a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c + d x]}}{\sqrt{b}}\right]}{b^{3/2} (a^2 + b^2)^2 d} + \frac{a (A b - a B) \sqrt{\cot [c + d x]}}{b (a^2 + b^2) d (b + a \cot [c + d x])} +$$

$$\frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\cot [c + d x]} + \cot [c + d x]\right] -$$

$$\frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\cot [c + d x]} + \cot [c + d x]\right]$$

Result (type 3, 810 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x] \right. \\
 & \quad \left. (a \cos [c+d x]+b \sin [c+d x]) (a A b \sin [c+d x]-a^2 B \sin [c+d x]) \right) / \\
 & \left( (a-i b)(a+i b) b d (b+a \cot [c+d x])^2 (A \cos [c+d x]+B \sin [c+d x]) \right) + \\
 & \left( (B+A \cot [c+d x]) \operatorname{Csc}[c+d x] (a \cos [c+d x]+b \sin [c+d x])^2 \right. \\
 & \quad \left. \left( -\left( \left( 2\left(a^2 B+b^2 B\right) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x] \right) \right) / \right. \right. \\
 & \quad \left. \left. \left( \sqrt{a} \sqrt{b} (1+\cot [c+d x])^2 (a+b \tan [c+d x]) \right) \right) \right) - \\
 & \left( (-a A b-b^2 B) \cos [2(c+d x)] (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \left( -4\left(a^2-b^2\right) \operatorname{ArcTan}\left[ \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}} \right] + \sqrt{2} \sqrt{a} \sqrt{b} \left( -2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. 2(a-b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right] + (a+b) \left( \operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]} + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \cot [c+d x]\right] - \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x]\right] \right) \right) \right) \operatorname{Sec}[c+d x] \right) / \\
 & \left( 2 \sqrt{a} \sqrt{b} \left(a^2+b^2\right) (-1+\cot [c+d x])^2 (1+\cot [c+d x])^2 (a+b \tan [c+d x]) \right) - \\
 & \frac{1}{4\left(a^2+b^2\right) (1+\cot [c+d x])^2 (a+b \tan [c+d x])} \\
 & \left( A b^2-a b B\right) (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \right. \\
 & \quad \left. \sqrt{2} \left( -2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right] + 2(a+b) \operatorname{ArcTan}\left[1+ \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{2} \sqrt{\cot [c+d x]}\right] - (a-b) \left( \operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x]\right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]} + \cot [c+d x]\right] \right) \right) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \right) / \\
 & \left( 2(a-i b)(a+i b) b d (b+a \cot [c+d x])^2 (A \cos [c+d x]+B \sin [c+d x]) \right)
 \end{aligned}$$

**Problem 599: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \tan [c+d x]}{\cot [c+d x]^{5 / 2}(a+b \tan [c+d x])^2} d x$$

Optimal (type 3, 437 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}] + \\
 & \frac{1}{\sqrt{2} (a^2 + b^2)^2 d} (a^2 (A - B) - b^2 (A - B) + 2 a b (A + B)) \operatorname{ArcTan}[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}] - \\
 & \frac{a^{3/2} (a^2 A b + 5 A b^3 - 3 a^3 B - 7 a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right]}{b^{5/2} (a^2 + b^2)^2 d} - \frac{a A b - 3 a^2 B - 2 b^2 B}{b^2 (a^2 + b^2) d \sqrt{\operatorname{Cot}[c + d x]}} + \\
 & \frac{a (A b - a B)}{b (a^2 + b^2) d \sqrt{\operatorname{Cot}[c + d x]} (b + a \operatorname{Cot}[c + d x])} + \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} \\
 & (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]] - \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^2 d} (2 a b (A - B) - a^2 (A + B) + b^2 (A + B)) \operatorname{Log}[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]]
 \end{aligned}$$

Result(type 3, 856 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x] (a \cos [c+d x]+b \sin [c+d x])^2 \right. \\
 & \left. \left( \frac{-a^2 A b \sin [c+d x]+a^3 B \sin [c+d x]}{b^2\left(a^2+b^2\right)\left(a \cos [c+d x]+b \sin [c+d x]\right)}+\frac{2 B \tan [c+d x]}{b^2} \right) \right) / \\
 & \left( d(b+a \cot [c+d x])^2(A \cos [c+d x]+B \sin [c+d x]) \right)- \\
 & \left( (B+A \cot [c+d x]) \operatorname{Csc}[c+d x] (a \cos [c+d x]+b \sin [c+d x])^2 \right. \\
 & \left. \left( -\left( \left( 2\left(-a^2 A b-A b^3+3 a^3 B+3 a b^2 B\right) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right](b+a \cot [c+d x]) \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x] \right) \right) / \left( \sqrt{a} \sqrt{b}\left(1+\cot [c+d x]\right)^2(a+b \tan [c+d x]) \right) \right) - \\
 & \left( (A b^3-a b^2 B) \cos [2(c+d x)](b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \left( -4\left(a^2-b^2\right) \operatorname{ArcTan}\left[ \right. \right. \right. \\
 & \left. \left. \left. \frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right]+ \sqrt{2} \sqrt{a} \sqrt{b}\left(-2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+ \right. \right. \\
 & \left. \left. 2(a-b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right]+(a+b)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\right. \right. \right. \\
 & \left. \left. \left. \cot [c+d x]\right]-\operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \right) \operatorname{Sec}[c+d x] \left. \right) / \\
 & \left( \frac{2 \sqrt{a} \sqrt{b}\left(a^2+b^2\right)\left(-1+\cot [c+d x]\right)^2\left(1+\cot [c+d x]\right)^2(a+b \tan [c+d x])}{1} \right)- \\
 & \frac{4\left(a^2+b^2\right)\left(1+\cot [c+d x]\right)^2(a+b \tan [c+d x])}{1} \\
 & \left( a A b^2+b^3 B\right)(b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right]+ \right. \\
 & \left. \sqrt{2}\left(-2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a+b) \operatorname{ArcTan}\left[1+ \right. \right. \right. \\
 & \left. \left. \left. \sqrt{2} \sqrt{\cot [c+d x]}\right]-\left(a-b\right)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \\
 & \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \left. \right) / \\
 & \left( 2(a-i b)(a+i b) b^2 d(b+a \cot [c+d x])^2(A \cos [c+d x]+B \sin [c+d x]) \right)
 \end{aligned}$$

**Problem 600: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cot [c+d x]^{3 / 2}(A+B \tan [c+d x])}{(a+b \tan [c+d x])^3} d x$$

Optimal (type 3, 601 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + \\
 & \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \\
 & \quad \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + \frac{1}{4 a^{7/2} (a^2 + b^2)^3 d} \\
 & b^{3/2} (63 a^4 A b + 46 a^2 A b^3 + 15 A b^5 - 35 a^5 B - 6 a^3 b^2 B - 3 a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right] - \\
 & \frac{(8 a^4 A + 31 a^2 A b^2 + 15 A b^4 - 11 a^3 b B - 3 a b^3 B) \sqrt{\operatorname{Cot}[c + d x]}}{4 a^3 (a^2 + b^2)^2 d} + \\
 & \frac{b (A b - a B) \operatorname{Cot}[c + d x]^{5/2}}{2 a (a^2 + b^2) d (b + a \operatorname{Cot}[c + d x])^2} + \frac{b (13 a^2 A b + 5 A b^3 - 9 a^3 B - a b^2 B) \operatorname{Cot}[c + d x]^{3/2}}{4 a^2 (a^2 + b^2)^2 d (b + a \operatorname{Cot}[c + d x])} + \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \\
 & \quad \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]
 \end{aligned}$$

Result (type 3, 1038 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
 & \left. \left( -\frac{4 a^4 A+8 a^2 A b^2+5 A b^4-a b^3 B}{2 a^3 (a-i b)^2 (a+i b)^2} - \frac{b^3 (-A b+a B)}{2 a (a-i b)^2 (a+i b)^2 (a \cos [c+d x]+b \sin [c+d x])^2} \right. \right. \\
 & \left. \left. (-17 a^2 A b^3 \sin [c+d x]-5 A b^5 \sin [c+d x]+13 a^3 b^2 B \sin [c+d x]+a b^4 B \sin [c+d x]) \right) \right) / \\
 & \left. \left( 4 a^3 (a-i b)^2 (a+i b)^2 (a \cos [c+d x]+b \sin [c+d x]) \right) \right) / \\
 & \left( d (b+a \cot [c+d x])^3 (A \cos [c+d x]+B \sin [c+d x]) \right) - \\
 & \left( (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
 & \left. \left( -\left( \left( 2 (16 a^4 A b+31 a^2 A b^3+15 A b^5-4 a^5 B-7 a^3 b^2 B-3 a b^4 B) \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x] \right) \right) / \right. \\
 & \left. \left( \sqrt{a} \sqrt{b} (1+\cot [c+d x])^2 (a+b \tan [c+d x]) \right) \right) - \left( (8 a^4 A b-4 a^5 B+4 a^3 b^2 B) \cos [ \right. \\
 & \left. 2 (c+d x) \right] (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \left( -4 (a^2-b^2) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \right. \\
 & \left. \sqrt{2} \sqrt{a} \sqrt{b} (-2 (a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2 (a-b) \operatorname{ArcTan}\left[ \right. \right. \\
 & \left. \left. 1+\sqrt{2} \sqrt{\cot [c+d x]}\right] + (a+b) \left( \operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] - \right. \right. \\
 & \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] \right) \right) \right) \operatorname{Sec}[c+d x] \left. \right) / \\
 & \left( 2 \sqrt{a} \sqrt{b} (a^2+b^2) (-1+\cot [c+d x])^2 (1+\cot [c+d x])^2 (a+b \tan [c+d x]) \right) - \\
 & \frac{1}{4 (a^2+b^2) (1+\cot [c+d x])^2 (a+b \tan [c+d x])} (4 a^5 A-4 a^3 A b^2+8 a^4 b B) \\
 & (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \sqrt{2} \right. \\
 & \left. (-2 (a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2 (a+b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right] - \right. \\
 & \left. (a-b) \left( \operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] - \right. \right. \\
 & \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] \right) \right) \operatorname{Sec}[c+d x]^2 \sin [2 (c+d x)] \left. \right) \left. \right) / \\
 & \left( 8 a^3 (a-i b)^2 (a+i b)^2 d (b+a \cot [c+d x])^3 (A \cos [c+d x]+B \sin [c+d x]) \right)
 \end{aligned}$$

**Problem 601: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sqrt{\cot [c+d x]} (A+B \tan [c+d x])}{(a+b \tan [c+d x])^3} dx$$

Optimal (type 3, 534 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + \\
 & \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \\
 & \quad \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] - \frac{1}{4 a^{5/2} (a^2 + b^2)^3 d} \\
 & \sqrt{b} (35 a^4 A b + 6 a^2 A b^3 + 3 A b^5 - 15 a^5 B + 18 a^3 b^2 B + a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right] + \\
 & \frac{b (A b - a B) \operatorname{Cot}[c + d x]^{3/2}}{2 a (a^2 + b^2) d (b + a \operatorname{Cot}[c + d x])^2} + \frac{b (11 a^2 A b + 3 A b^3 - 7 a^3 B + a b^2 B) \sqrt{\operatorname{Cot}[c + d x]}}{4 a^2 (a^2 + b^2)^2 d (b + a \operatorname{Cot}[c + d x])} - \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \\
 & \quad \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] + \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]
 \end{aligned}$$

Result (type 3, 1004 leaves):

$$\begin{aligned}
& \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
& \left. \left( -\frac{b^2(-A b+a B)}{2 a^2(a-i b)^2(a+i b)^2} + \frac{b^2(-A b+a B)}{2(a-i b)^2(a+i b)^2(a \cos [c+d x]+b \sin [c+d x])^2} + \right. \right. \\
& \left. \left. (13 a^2 A b^2 \sin [c+d x]+A b^4 \sin [c+d x]-9 a^3 b B \sin [c+d x]+3 a b^3 B \sin [c+d x]) \right) / \right. \\
& \left. \left. \left( 4 a^2(a-i b)^2(a+i b)^2(a \cos [c+d x]+b \sin [c+d x]) \right) \right) \right) / \\
& \left( d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x]) \right) + \\
& \left( (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2(a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
& \left. \left( -\left( \left( 2\left( 4 a^4 A+7 a^2 A b^2+3 A b^4+a^3 b B+a b^3 B \right) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right](b+a \cot [c+d x]) \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x] \right) / \left( \sqrt{a} \sqrt{b}\left(1+\cot [c+d x]^2\right)^2(a+b \tan [c+d x]) \right) \right) \right) - \\
& \left( \left( 4 a^4 A-4 a^2 A b^2+8 a^3 b B \right) \cos [2(c+d x)](b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \right. \\
& \left. \left( -4\left(a^2-b^2\right) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \right. \right. \\
& \left. \left. \sqrt{2} \sqrt{a} \sqrt{b}\left(-2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a-b) \operatorname{ArcTan}\left[ \right. \right. \right. \right. \\
& \left. \left. \left. 1+\sqrt{2} \sqrt{\cot [c+d x]}\right]+(a+b)\left(\log \left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \right. \\
& \left. \left. \left. \log \left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \right) \operatorname{Sec}[c+d x] \right) / \\
& \left( 2 \sqrt{a} \sqrt{b}\left(a^2+b^2\right)\left(-1+\cot [c+d x]^2\right)\left(1+\cot [c+d x]^2\right)(a+b \tan [c+d x]) \right) - \\
& \frac{1}{4\left(a^2+b^2\right)\left(1+\cot [c+d x]^2\right)(a+b \tan [c+d x])} \left(-8 a^3 A b+4 a^4 B-4 a^2 b^2 B\right) \\
& \left( (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left(-8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right]+\sqrt{2} \right. \right. \\
& \left. \left. (-2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a+b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right]- \right. \right. \\
& \left. \left. (a-b)\left(\log \left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \\
& \left. \left. \log \left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \left. \right) / \\
& \left( 8 a^2(a-i b)^2(a+i b)^2 d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x]) \right)
\end{aligned}$$

**Problem 602: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \tan [c+d x]}{\sqrt{\cot [c+d x]}(a+b \tan [c+d x])^3} d x$$



Optimal (type 3, 534 leaves, 17 steps):

$$\begin{aligned}
 & \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \\
 & \text{ArcTan}\left[1 - \sqrt{2} \sqrt{\text{Cot}[c + d x]}\right] - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} \\
 & (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \text{ArcTan}\left[1 + \sqrt{2} \sqrt{\text{Cot}[c + d x]}\right] + \\
 & \left( (15 a^4 A b - 18 a^2 A b^3 - A b^5 - 3 a^5 B + 26 a^3 b^2 B - 3 a b^4 B) \text{ArcTan}\left[\frac{\sqrt{a} \sqrt{\text{Cot}[c + d x]}}{\sqrt{b}}\right] \right) / \\
 & \left( 4 a^{3/2} \sqrt{b} (a^2 + b^2)^3 d \right) + \frac{b (A b - a B) \sqrt{\text{Cot}[c + d x]}}{2 a (a^2 + b^2) d (b + a \text{Cot}[c + d x])^2} - \\
 & \frac{(9 a^2 A b + A b^3 - 5 a^3 B + 3 a b^2 B) \sqrt{\text{Cot}[c + d x]}}{4 a (a^2 + b^2)^2 d (b + a \text{Cot}[c + d x])} - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \text{Log}\left[1 - \sqrt{2} \sqrt{\text{Cot}[c + d x]} + \text{Cot}[c + d x]\right] + \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \text{Log}\left[1 + \sqrt{2} \sqrt{\text{Cot}[c + d x]} + \text{Cot}[c + d x]\right]
 \end{aligned}$$

Result (type 3, 986 leaves):

$$\begin{aligned}
& \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
& \left. \left( \frac{b(-A b+a B)}{2 a(a-i b)^2(a+i b)^2} - \frac{a b(-A b+a B)}{2(a-i b)^2(a+i b)^2(a \cos [c+d x]+b \sin [c+d x])^2} + \right. \right. \\
& \left. \left. (-9 a^2 A b \sin [c+d x]+3 A b^3 \sin [c+d x]+5 a^3 B \sin [c+d x]-7 a b^2 B \sin [c+d x]) \right) / \right. \\
& \left. \left( 4 a(a-i b)^2(a+i b)^2(a \cos [c+d x]+b \sin [c+d x]) \right) \right) / \\
& \left( d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x]) \right) + \\
& \left( (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2(a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
& \left. \left( - \left( \left( 2(a^2 A b+A b^3-a^3 B-a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right](b+a \cot [c+d x]) \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x] \right) / \left( \sqrt{a} \sqrt{b} (1+\cot [c+d x])^2(a+b \tan [c+d x]) \right) \right) \right) - \\
& \left( (8 a^2 A b-4 a^3 B+4 a b^2 B) \cos [2(c+d x)](b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \right. \\
& \left. \left( -4(a^2-b^2) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \right. \right. \\
& \left. \left. \sqrt{2} \sqrt{a} \sqrt{b} (-2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a-b) \operatorname{ArcTan}\left[ \right. \right. \right. \\
& \left. \left. \left. 1+\sqrt{2} \sqrt{\cot [c+d x]}\right]+(a+b) \left( \log \left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] - \right. \right. \right. \\
& \left. \left. \left. \log \left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] \right) \right) \right) \operatorname{Sec}[c+d x] \right) / \\
& \left( 2 \sqrt{a} \sqrt{b} (a^2+b^2) (-1+\cot [c+d x])^2(1+\cot [c+d x])^2(a+b \tan [c+d x]) \right) - \\
& \frac{1}{4(a^2+b^2)(1+\cot [c+d x])^2(a+b \tan [c+d x])} (4 a^3 A-4 a A b^2+8 a^2 b B) \\
& (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \sqrt{2} \right. \\
& \left. (-2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a+b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right] - \right. \\
& \left. (a-b) \left( \log \left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] - \right. \right. \\
& \left. \left. \log \left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right] \right) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \right) / \\
& \left( 8 a(a-i b)^2(a+i b)^2 d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x]) \right)
\end{aligned}$$

**Problem 603: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \tan [c+d x]}{\cot [c+d x]^{3/2}(a+b \tan [c+d x])^3} d x$$

Optimal (type 3, 530 leaves, 17 steps):

$$\begin{aligned}
 & \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \\
 & \text{ArcTan}\left[1 - \sqrt{2} \sqrt{\text{Cot}[c + d x]}\right] - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} \\
 & (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \text{ArcTan}\left[1 + \sqrt{2} \sqrt{\text{Cot}[c + d x]}\right] - \\
 & \left( (3 a^4 A b - 26 a^2 A b^3 + 3 A b^5 + a^5 B + 18 a^3 b^2 B - 15 a b^4 B) \text{ArcTan}\left[\frac{\sqrt{a} \sqrt{\text{Cot}[c + d x]}}{\sqrt{b}}\right] \right) / \\
 & (4 \sqrt{a} b^{3/2} (a^2 + b^2)^3 d) - \frac{(A b - a B) \sqrt{\text{Cot}[c + d x]}}{2 (a^2 + b^2) d (b + a \text{Cot}[c + d x])^2} + \\
 & \frac{(5 a^2 A b - 3 A b^3 - a^3 B + 7 a b^2 B) \sqrt{\text{Cot}[c + d x]}}{4 b (a^2 + b^2)^2 d (b + a \text{Cot}[c + d x])} + \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \text{Log}\left[1 - \sqrt{2} \sqrt{\text{Cot}[c + d x]} + \text{Cot}[c + d x]\right] - \\
 & \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \text{Log}\left[1 + \sqrt{2} \sqrt{\text{Cot}[c + d x]} + \text{Cot}[c + d x]\right]
 \end{aligned}$$

Result (type 3, 983 leaves):

$$\begin{aligned}
& \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
& \left. \left( -\frac{-A b+a B}{2(a-i b)^2(a+i b)^2} + \frac{a^2(-A b+a B)}{2(a-i b)^2(a+i b)^2(a \cos [c+d x]+b \sin [c+d x])^2} + \right. \right. \\
& \left. \left. (5 a^2 A b \sin [c+d x]-7 A b^3 \sin [c+d x]-a^3 B \sin [c+d x]+11 a b^2 B \sin [c+d x]) / \right. \right. \\
& \left. \left. (4(a-i b)^2(a+i b)^2 b(a \cos [c+d x]+b \sin [c+d x])) \right) \right) / \\
& (d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x])) + \\
& \left( (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2(a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
& \left. \left( -\left( \left( 2(-a^2 A b-A b^3+a^3 B+a b^2 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right](b+a \cot [c+d x]) \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x] \right) / \left( \sqrt{a} \sqrt{b} (1+\cot [c+d x])^2(a+b \tan [c+d x]) \right) \right) \right) - \\
& \left( (-4 a^2 A b+4 A b^3-8 a b^2 B) \cos [2(c+d x)](b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \right. \\
& \left( -4(a^2-b^2) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \right. \\
& \left. \sqrt{2} \sqrt{a} \sqrt{b} (-2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a-b) \operatorname{ArcTan}\left[ \right. \right. \\
& \left. \left. 1+\sqrt{2} \sqrt{\cot [c+d x]}\right]+(a+b)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \\
& \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \right) \operatorname{Sec}[c+d x] \left. \right) / \\
& \left( 2 \sqrt{a} \sqrt{b} (a^2+b^2)(-1+\cot [c+d x])^2(1+\cot [c+d x])^2(a+b \tan [c+d x]) \right) - \\
& \frac{1}{4(a^2+b^2)(1+\cot [c+d x])^2(a+b \tan [c+d x])} (8 a A b^2-4 a^2 b B+4 b^3 B) \\
& (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \sqrt{2} \right. \\
& \left. (-2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a+b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right]- \right. \\
& \left. (a-b)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \\
& \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \left. \right) \left. \right) / \\
& (8(a-i b)^2(a+i b)^2 b d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x]))
\end{aligned}$$

**Problem 604: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \tan [c+d x]}{\cot [c+d x]^{5/2}(a+b \tan [c+d x])^3} dx$$

Optimal (type 3, 534 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + \\
 & \quad \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \\
 & \quad \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] - \frac{1}{4 b^{5/2} (a^2 + b^2)^3 d} \\
 & \quad \sqrt{a} (a^4 A b + 18 a^2 A b^3 - 15 A b^5 + 3 a^5 B + 6 a^3 b^2 B + 35 a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right] + \\
 & \quad \frac{a (A b - a B) \sqrt{\operatorname{Cot}[c + d x]}}{2 b (a^2 + b^2) d (b + a \operatorname{Cot}[c + d x])^2} - \frac{a (a^2 A b - 7 A b^3 + 3 a^3 B + 11 a b^2 B) \sqrt{\operatorname{Cot}[c + d x]}}{4 b^2 (a^2 + b^2)^2 d (b + a \operatorname{Cot}[c + d x])} + \\
 & \quad \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \\
 & \quad \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]
 \end{aligned}$$

Result (type 3, 1006 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
 & \left. \left( \frac{a(-A b+a B)}{2(a-i b)^2(a+i b)^2 b}-\frac{a^3(-A b+a B)}{2(a-i b)^2(a+i b)^2 b(a \cos [c+d x]+b \sin [c+d x])^2} \right. \right. \\
 & \left. \left. \left(-a^3 A b \sin [c+d x]+11 a A b^3 \sin [c+d x]-3 a^4 B \sin [c+d x]-15 a^2 b^2 B \sin [c+d x]\right) / \right. \right. \\
 & \left. \left. \left(4(a-i b)^2(a+i b)^2 b^2(a \cos [c+d x]+b \sin [c+d x])\right)\right)\right) / \\
 & \left(d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x])\right)+ \\
 & \left((B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2(a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
 & \left. \left(-\left(\left(2\left(a^3 A b+a A b^3+3 a^4 B+7 a^2 b^2 B+4 b^4 B\right) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right](b+a \cot [c+d x])\right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x]\right)\right) / \left(\sqrt{a} \sqrt{b}\left(1+\cot [c+d x]^2\right)^2(a+b \tan [c+d x])\right)\right) - \\
 & \left(\left(-8 a A b^3+4 a^2 b^2 B-4 b^4 B\right) \cos [2(c+d x)](b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \right. \\
 & \left. \left(-4\left(a^2-b^2\right) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right]+ \right. \right. \\
 & \left. \left. \sqrt{2} \sqrt{a} \sqrt{b}\left(-2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a-b) \operatorname{ArcTan}\left[ \right. \right. \right. \right. \\
 & \left. \left. \left. 1+\sqrt{2} \sqrt{\cot [c+d x]}\right]+(a+b)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right)\right)\right) \operatorname{Sec}[c+d x]\right) / \\
 & \left(\frac{2 \sqrt{a} \sqrt{b}\left(a^2+b^2\right)\left(-1+\cot [c+d x]^2\right)\left(1+\cot [c+d x]^2\right)(a+b \tan [c+d x])}{1} \right. \\
 & \left. \frac{1}{4\left(a^2+b^2\right)\left(1+\cot [c+d x]^2\right)(a+b \tan [c+d x])}\left(-4 a^2 A b^2+4 A b^4-8 a b^3 B\right) \right. \\
 & \left. (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2\left(-8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right]+\sqrt{2} \right. \right. \\
 & \left. \left. (-2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a+b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right]- \right. \right. \\
 & \left. \left. (a-b)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right)\right)\right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)]\right) / \\
 & \left(8(a-i b)^2(a+i b)^2 b^2 d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x])\right)
 \end{aligned}$$

**Problem 605: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A+B \tan [c+d x]}{\cot [c+d x]^{7 / 2}(a+b \tan [c+d x])^3} d x$$

Optimal (type 3, 600 leaves, 18 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \operatorname{ArcTan}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] + \\
 & \quad \frac{1}{\sqrt{2} (a^2 + b^2)^3 d} (3 a^2 b (A - B) - b^3 (A - B) - a^3 (A + B) + 3 a b^2 (A + B)) \\
 & \quad \operatorname{ArcTan}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]}\right] - \frac{1}{4 b^{7/2} (a^2 + b^2)^3 d} \\
 & a^{3/2} (3 a^4 A b + 6 a^2 A b^3 + 35 A b^5 - 15 a^5 B - 46 a^3 b^2 B - 63 a b^4 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{b}}\right] - \\
 & \quad \frac{3 a^3 A b + 11 a A b^3 - 15 a^4 B - 31 a^2 b^2 B - 8 b^4 B}{4 b^3 (a^2 + b^2)^2 d \sqrt{\operatorname{Cot}[c + d x]}} + \frac{a (A b - a B)}{2 b (a^2 + b^2) d \sqrt{\operatorname{Cot}[c + d x]} (b + a \operatorname{Cot}[c + d x])^2} + \\
 & \quad \frac{a (a^2 A b + 9 A b^3 - 5 a^3 B - 13 a b^2 B)}{4 b^2 (a^2 + b^2)^2 d \sqrt{\operatorname{Cot}[c + d x]} (b + a \operatorname{Cot}[c + d x])} - \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{Log}\left[1 - \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right] + \\
 & \quad \frac{1}{2 \sqrt{2} (a^2 + b^2)^3 d} \\
 & \quad (a^3 (A - B) - 3 a b^2 (A - B) + 3 a^2 b (A + B) - b^3 (A + B)) \operatorname{Log}\left[1 + \sqrt{2} \sqrt{\operatorname{Cot}[c + d x]} + \operatorname{Cot}[c + d x]\right]
 \end{aligned}$$

Result (type 3, 1033 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot [c+d x]} (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2 (a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
 & \left. \left( -\frac{a^2(-A b+a B)}{2(a-i b)^2(a+i b)^2 b^2} + \frac{a^4(-A b+a B)}{2(a-i b)^2(a+i b)^2 b^2(a \cos [c+d x]+b \sin [c+d x])^2} + \right. \right. \\
 & \left. \left. (-3 a^4 A b \sin [c+d x]-15 a^2 A b^3 \sin [c+d x]+7 a^5 B \sin [c+d x]+19 a^3 b^2 B \sin [c+d x]) \right) / \right. \\
 & \left. \left( 4(a-i b)^2(a+i b)^2 b^3(a \cos [c+d x]+b \sin [c+d x]) \right) + \frac{2 B \tan [c+d x]}{b^3} \right) / \\
 & \left( d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x]) \right) - \\
 & \left( (B+A \cot [c+d x]) \operatorname{Csc}[c+d x]^2(a \cos [c+d x]+b \sin [c+d x])^3 \right. \\
 & \left. \left( -\left( \left( 2(-3 a^4 A b-7 a^2 A b^3-4 A b^5+15 a^5 B+31 a^3 b^2 B+16 a b^4 B) \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right](b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \operatorname{Sec}[c+d x] \right) / \right. \right. \\
 & \left. \left. \left( \sqrt{a} \sqrt{b}(1+\cot [c+d x])^2(a+b \tan [c+d x]) \right) \right) - \left( (-4 a^2 A b^3+4 A b^5-8 a b^4 B) \cos [ \right. \right. \\
 & \left. \left. 2(c+d x) \right)(b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^3 \left( -4(a^2-b^2) \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \right. \right. \\
 & \left. \left. \sqrt{2} \sqrt{a} \sqrt{b}(-2(a-b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a-b) \operatorname{ArcTan}\left[ \right. \right. \right. \\
 & \left. \left. \left. 1+\sqrt{2} \sqrt{\cot [c+d x]}\right]+(a+b)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \right) \operatorname{Sec}[c+d x] \right) / \\
 & \left( 2 \sqrt{a} \sqrt{b}(a^2+b^2)(-1+\cot [c+d x])^2(1+\cot [c+d x])^2(a+b \tan [c+d x]) \right) - \\
 & \frac{1}{4(a^2+b^2)(1+\cot [c+d x])^2(a+b \tan [c+d x])} (8 a A b^4-4 a^2 b^3 B+4 b^5 B) \\
 & (b+a \cot [c+d x]) \operatorname{Csc}[c+d x]^2 \left( -8 \sqrt{a} \sqrt{b} \operatorname{ArcTan}\left[\frac{\sqrt{a} \sqrt{\cot [c+d x]}}{\sqrt{b}}\right] + \sqrt{2} \right. \\
 & \left. (-2(a+b) \operatorname{ArcTan}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}\right]+2(a+b) \operatorname{ArcTan}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}\right] - \right. \\
 & \left. (a-b)\left(\operatorname{Log}\left[1-\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]- \right. \right. \\
 & \left. \left. \operatorname{Log}\left[1+\sqrt{2} \sqrt{\cot [c+d x]}+\cot [c+d x]\right]\right) \right) \operatorname{Sec}[c+d x]^2 \sin [2(c+d x)] \left. \right) / \\
 & \left( 8(a-i b)^2(a+i b)^2 b^3 d(b+a \cot [c+d x])^3(A \cos [c+d x]+B \sin [c+d x]) \right)
 \end{aligned}$$

**Problem 612: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c+d x]^{9 / 2} \sqrt{a+b \tan [c+d x]}(A+B \tan [c+d x]) d x$$



Optimal (type 3, 354 leaves, 12 steps):

$$\begin{aligned}
 & -\frac{1}{d} \sqrt{i a - b} \left( i A - B \right) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} - \\
 & \frac{1}{d} \sqrt{i a + b} \left( i A + B \right) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} + \\
 & \frac{1}{105 a^3 d} 2 \left( 35 a^2 A b - 8 A b^3 + 105 a^3 B + 14 a b^2 B \right) \sqrt{\operatorname{Cot}[c + d x]} \sqrt{a + b \operatorname{Tan}[c + d x]} + \\
 & \frac{2 \left( 35 a^2 A + 4 A b^2 - 7 a b B \right) \operatorname{Cot}[c + d x]^{3/2} \sqrt{a + b \operatorname{Tan}[c + d x]}}{105 a^2 d} - \\
 & \frac{2 \left( A b + 7 a B \right) \operatorname{Cot}[c + d x]^{5/2} \sqrt{a + b \operatorname{Tan}[c + d x]}}{35 a d} - \frac{2 A \operatorname{Cot}[c + d x]^{7/2} \sqrt{a + b \operatorname{Tan}[c + d x]}}{7 d}
 \end{aligned}$$

Result (type 4, 4853 leaves):

$$\begin{aligned}
 & \left( \sqrt{\operatorname{Cot}[c + d x]} \left( B + A \operatorname{Cot}[c + d x] \right) \left( \frac{4 \left( 19 a^2 A b - 4 A b^3 + 63 a^3 B + 7 a b^2 B \right)}{105 a^3} + \frac{1}{105 a^2} \right. \right. \\
 & \quad \left. \left. 2 \left( 50 a^2 A \operatorname{Cos}[c + d x] + 4 A b^2 \operatorname{Cos}[c + d x] - 7 a b B \operatorname{Cos}[c + d x] \right) \operatorname{Csc}[c + d x] - \right. \right. \\
 & \quad \left. \left. \frac{2 \left( A b + 7 a B \right) \operatorname{Csc}[c + d x]^2}{35 a} - \frac{2}{7} A \operatorname{Cot}[c + d x] \operatorname{Csc}[c + d x]^2 \right) \right. \\
 & \quad \left. \operatorname{Sin}[c + d x] \sqrt{a + b \operatorname{Tan}[c + d x]} \right) / \left( d \left( A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x] \right) \right) + \\
 & \left( 4 i \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \quad \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + d x]} \left( B + A \operatorname{Cot}[c + d x] \right) \right. \\
 & \quad \left. \left( (a A - b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A + i B) \right. \right. \\
 & \quad \left. \left. \operatorname{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \operatorname{Sin}[c + d x] \left( \frac{a A \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \right. \\
 & \quad \frac{b B \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \\
 & \quad \frac{A b \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \\
 & \quad \left. \frac{a B \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{a + b \operatorname{Tan}[c + d x]} \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right. \\
 & \left. - \left( \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + d x]} \right) \right. \right. \\
 & \left. \left( (a A - b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \Big/ \\
 & \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \right. \\
 & \left. \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) - \left( i a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]} \right. \\
 & \left. (aA - bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & \left. (a+i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \Big/ \right. \\
 & \left. \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \right. \\
 & \left. \left. \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) + \right.
 \end{aligned}$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} \frac{3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}}{\sqrt{\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]}}} \left( (a A-b B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) - (a+i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right] - (a-i b)(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right] \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}\left(a \cos [c+d x]+b \sin [c+d x]\right)^{3 / 2}} \frac{2 i \cos \left[\frac{1}{2}(c+d x)\right]^2}{\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}} \sqrt{\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]}}} \left( (a A-b B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) - (a+i b)(A+i B)$$

$$\begin{aligned}
 & \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \\
 & (a - i b) (A - i B) \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \sqrt{\text{Sec} [c + d x]} (b \text{Cos} [c + d x] - a \text{Sin} [c + d x]) \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Cot} [c + d x]} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} 2 i \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \text{Csc} [c + d x]^2 \right. \\
 & \left. (a A - b B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A + i B) \right. \\
 & \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \\
 & (a - i b) (A - i B) \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \sqrt{\text{Sec} [c + d x]} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \right.
 \end{aligned}$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} 4 i \cos \left[ \frac{1}{2} (c+d x) \right]$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]}$$

$$\left( (a A-b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b) (A+i B) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$(a-i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+d x]} \sin \left[ \frac{1}{2} (c+d x) \right] \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} +$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} 2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]}$$

$$\left( (a A-b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b) (A+i B) \right.$$

$$\text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a - ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right],$$

$$\left.\frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx] \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}}} 4i \cos\left[\frac{1}{2}(c + dx)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]}$$

$$\sqrt{\text{Sec}[c + dx]} \left( - \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (aA - bB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right.$$

$$\left. \left( 4 \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) +$$

$$\left( i(a + ib) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + iB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \cot\left[\frac{1}{2}(c + dx)\right] \right) \right)$$

$$\sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\left( i(a - ib) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - iB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\ \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right)$$

**Problem 613: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^{7/2} \sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 290 leaves, 11 steps):

$$\frac{1}{d} \sqrt{i a - b} (A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} - \frac{1}{d} \\ \sqrt{i a + b} (A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ \frac{2 (15 a^2 A + 2 A b^2 - 5 a b B) \sqrt{\cot [c + d x]} \sqrt{a + b \tan [c + d x]}}{15 a^2 d} - \\ \frac{2 (A b + 5 a B) \cot [c + d x]^{3/2} \sqrt{a + b \tan [c + d x]}}{15 a d} - \frac{2 A \cot [c + d x]^{5/2} \sqrt{a + b \tan [c + d x]}}{5 d}$$

Result (type 4, 4786 leaves):

$$\left( \sqrt{\cot [c + d x]} (B + A \cot [c + d x]) \left( \frac{2 (18 a^2 A + 2 A b^2 - 5 a b B)}{15 a^2} - \frac{2 (A b \cos [c + d x] + 5 a B \cos [c + d x]) \operatorname{Csc} [c + d x]}{15 a} - \frac{2}{5} A \operatorname{Csc} [c + d x]^2 \right) \right. \\ \left. \sin [c + d x] \sqrt{a + b \tan [c + d x]} \right) / (d (A \cos [c + d x] + B \sin [c + d x])) - \\ \left( 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\ \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} (B + A \cot [c + d x]) \right)$$



$$\left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A + i B) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)$$

$$\left. (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\operatorname{Sin}[c + d x] \left( -\frac{A b \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \frac{a B \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \frac{a A \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \frac{b B \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} \right) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{a + b \tan[c + d x]} \Big/$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right.$$

$$\left. \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + d x]} \right) \right)$$

$$\left( i (A b + a B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)(A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)(A-i B) \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec}[c+dx]} \Bigg) /$$

$$\left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \right.$$

$$\left. \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) + \left( a \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \right.$$

$$\left( i (A b + a B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)(A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)(A-i B) \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\begin{aligned}
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \Bigg/ \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]}} \frac{3}{\sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}}} \\
 & \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]} \\
 & \left( i (A+b) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & \left. (a+i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx])^{3/2}} 2 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( i (A b + a B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B) \\
 & \left. \operatorname{EllipticPi}\left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\sqrt{\operatorname{Sec}[c + dx]} (b \operatorname{Cos}[c + dx] - a \operatorname{Sin}[c + dx]) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + 1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} \\
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \\
 & \operatorname{Csc}[c + dx]^2 \left( i (A b + a B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} \\
 & 4 \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \sqrt{\cot [c + d x]} \left( i (A b + a B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b) (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B) \\
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( i (A b + a B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.
 \end{aligned}$$

$$(a + i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a},\right.$$

$$\left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a - i b) (A - i B)$$

$$\left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]\right)$$

$$\operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x] \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}}} 4 \operatorname{Cos}\left[\frac{1}{2} (c + d x)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + d x]}$$

$$\sqrt{\operatorname{Sec}[c + d x]} \left( \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A b + a B) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2}{4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^{3/2}} \right) +$$

$$\left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right] \right) \right)$$

$$\left( \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^{3/2} \right) -$$

$$\left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2} (c + d x)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right] \right) \right) \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}}$$

$$\left( \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right)$$

**Problem 614: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c+dx]^{5/2} \sqrt{a+b \operatorname{Tan}[c+dx]} (A+B \operatorname{Tan}[c+dx]) dx$$

Optimal (type 3, 239 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{d} \sqrt{i a - b} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} + \frac{1}{d} \\ & \sqrt{i a + b} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a+b \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} - \\ & \frac{2(A b + 3 a B) \sqrt{\operatorname{Cot}[c+dx]} \sqrt{a+b \operatorname{Tan}[c+dx]}}{3 a d} - \frac{2 A \operatorname{Cot}[c+dx]^{3/2} \sqrt{a+b \operatorname{Tan}[c+dx]}}{3 d} \end{aligned}$$

Result (type 4, 4756 leaves):

$$\begin{aligned} & \left( \sqrt{\operatorname{Cot}[c+dx]} \left( -\frac{2(A b + 3 a B)}{3 a} - \frac{2}{3} A \operatorname{Cot}[c+dx] \right) (B + A \operatorname{Cot}[c+dx]) \right. \\ & \left. \operatorname{Sin}[c+dx] \sqrt{a+b \operatorname{Tan}[c+dx]} \right) / (d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx])) - \\ & \left( 4 i \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\ & \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}} \sqrt{\operatorname{Cot}[c+dx]} (B + A \operatorname{Cot}[c+dx])} \right) \\ & \left( (a A - b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) (A + i B) \right) \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b) \\
 & \left. (A - i B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \sin[c + dx] \left( -\frac{a A \sqrt{\cot[c + dx]}}{\sqrt{\sec[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} + \right. \\
 & \quad \left. \frac{b B \sqrt{\cot[c + dx]}}{\sqrt{\sec[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} - \right. \\
 & \quad \left. \frac{A b \sqrt{\cot[c + dx]} \sqrt{\sec[c + dx]} \sin[c + dx]}{\sqrt{a \cos[c + dx] + b \sin[c + dx]}} - \right. \\
 & \quad \left. \frac{a B \sqrt{\cot[c + dx]} \sqrt{\sec[c + dx]} \sin[c + dx]}{\sqrt{a \cos[c + dx] + b \sin[c + dx]}} \right) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} \sqrt{a + b \tan[c + dx]} \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \cos[c + dx] + b \sin[c + dx]) (A \cos[c + dx] + B \sin[c + dx]) \right. \\
 & \left. \left( \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \right. \right. \right. \\
 & \left. \left( (a A - b B) \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. \left. (a + i b) (A + i B) \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] - (a - i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Big/ \\
 & \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right. \\
 & \left. \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) + \left( i a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \right. \\
 & \left. (a A - b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) -
 \end{aligned}$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} \frac{3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}}{\sqrt{\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]}}} \left( (a A-b B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) - (a+i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right] - (a-i b)(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right] \right) \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} + \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} (a \cos [c+d x]+b \sin [c+d x])^{3/2}}} \frac{2 i \cos \left[\frac{1}{2}(c+d x)\right]^2}{\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}} \sqrt{\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]}}} \left( (a A-b B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right) - (a+i b)(A+i B)$$

$$\text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a - ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 2i \cos\left[\frac{1}{2}(c + dx)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \csc[c + dx]^2$$

$$\left( (aA - bB) \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + ib)(A + iB)$$

$$\text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a - ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\sec[c + dx]} \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} 4 i \cos \left[ \frac{1}{2} (c+d x) \right]$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]}$$

$$\left( (a A-b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b) (A+i B) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$(a-i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+d x]} \sin \left[ \frac{1}{2} (c+d x) \right] \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} 2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]}$$

$$\left( (a A-b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b) (A+i B) \right.$$

$$\text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a - ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right],$$

$$\left.\frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx] \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}}} 4i \cos\left[\frac{1}{2}(c + dx)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]}$$

$$\sqrt{\text{Sec}[c + dx]} \left( - \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (aA - bB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) /$$

$$\left( 4 \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) +$$

$$\left( i(a + ib) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + iB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \cot\left[\frac{1}{2}(c + dx)\right] \right) \right)$$

$$\sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\left( i(a - ib) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - iB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\ \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right)$$

**Problem 615: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^{3/2} \sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 194 leaves, 9 steps):

$$-\frac{1}{d} \sqrt{i a - b} (A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ \frac{1}{d} \sqrt{i a + b} (A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} - \\ \frac{2 A \sqrt{\cot [c + d x]} \sqrt{a + b \tan [c + d x]}}{d}$$

Result (type 4, 4716 leaves):

$$-\left( \frac{2 A \sqrt{\cot [c + d x]} (B + A \cot [c + d x]) \sin [c + d x] \sqrt{a + b \tan [c + d x]}}{(d (A \cos [c + d x] + B \sin [c + d x]))} \right) + \\ \left( 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\ \left. \sqrt{\cot [c + d x]} (B + A \cot [c + d x]) \right) \\ \left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A + i B) \right. \\ \left. \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) \right)$$

$$\begin{aligned}
 & \left( (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \operatorname{Sin}[c + d x] \left( \frac{A b \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \right. \\
 & \quad \frac{a B \sqrt{\operatorname{Cot}[c + d x]}}{\sqrt{\operatorname{Sec}[c + d x]} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \\
 & \quad \frac{a A \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} + \\
 & \quad \left. \frac{b B \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{a + b \operatorname{Tan}[c + d x]} \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]) (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \right) \\
 & \left( - \left( \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + d x]} \right) \right. \right. \\
 & \quad \left( i (A b + a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \quad \left. (a + i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \quad \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \Big/ \\
 & \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \right. \\
 & \left. \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) - \left( a \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]} \right. \\
 & \left. \left( i (A+b+a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \\
 & \left. \left. (a+i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \right) \Big/ \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) +
 \end{aligned}$$



$$\begin{aligned}
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} \sqrt[3]{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \\
 & \sqrt[3]{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( i(A b+a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right. \\
 & (a+i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(a-i b)(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}- \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}(a \cos [c+d x]+b \sin [c+d x])^{3/2}}} 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( i(A b+a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right. \\
 & (a+i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a-i b) (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \sqrt{\operatorname{Sec} [c+d x]} (b \operatorname{Cos} [c+d x] - a \operatorname{Sin} [c+d x]) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+d x]} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} \\
 & 2 \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \operatorname{Csc} [c+d x]^2 \left( i (A b+a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & \left. (a+i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b) (A-i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c+d x]} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}}
 \end{aligned}$$

$$\begin{aligned}
 & 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\operatorname{Cot}[c+dx]} \left( i (A+b) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+i b)(A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)(A-i B) \\
 & \left. \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}}} 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \\
 & \left( i (A+b) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+i b)(A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)(A-i B)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec} [c + d x]^{3/2} \text{Sin} [c + d x] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} 4 \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\text{Cot} [c + d x]} \\
 & \sqrt{\text{Sec} [c + d x]} \left( \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A b + a B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{4 \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2}} \right) + \\
 & \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) - \\
 & \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 + i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left. \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right)
 \end{aligned}$$

Problem 616: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \sqrt{\cot [c+d x]} \sqrt{a+b \tan [c+d x]} (A+B \tan [c+d x]) d x$$

Optimal (type 3, 229 leaves, 13 steps):

$$-\frac{1}{d} \sqrt{i a-b} (i A-B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]} +$$

$$\frac{2 \sqrt{b} B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}}{d} - \frac{1}{d}$$

$$\sqrt{i a+b} (i A+B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}$$

Result (type 4, 12351 leaves):

$$\left(4 a \cos [c+d x] \sqrt{\cot [c+d x]}\right) \left(A \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right]+$$

$$\left(b B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right]\right) /$$

$$\left(-a+b+\sqrt{a^2+b^2}\right) -$$

$$\left(A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right]\right) /$$

$$\left(-i a+b+\sqrt{a^2+b^2}\right) -$$

$$\left( a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) -$$

$$\left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( -i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( i B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( -i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( i A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( A B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}, \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) - \frac{1}{a + b + \sqrt{a^2 + b^2}}$$

$$b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right]$$

$$\left( A \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} + \right.$$

$$\left. B \sqrt{\operatorname{Cot} [c + d x]} \operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right)$$

$$\sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{a + b \operatorname{Tan} [c + d x]} (A + B \operatorname{Tan} [c + d x])$$

$$\left( \sqrt{a^2 + b^2} d \sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2}} \right)$$

$$(A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x])$$

$$\left( \left( a^2 \sqrt{\cot[c+dx]} \left( A \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) + \right.$$

$$\left. \left( b B \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \right) \right.$$

$$\left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( -a+b+\sqrt{a^2+b^2} \right) - \left( A b \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( -i a+b+\sqrt{a^2+b^2} \right) -$$

$$\left( a A \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \right)$$

$$\left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( a+i \left( b+\sqrt{a^2+b^2} \right) \right) - \left( a B \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right.$$



$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( -i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( i b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( -i a + b + \sqrt{a^2+b^2} \right) - \left( i a A \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( a B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( i a + b + \sqrt{a^2+b^2} \right) +$$

$$\left( i b \text{B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \left/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( b \text{B EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \left/ \left( a + b + \sqrt{a^2+b^2} \right) \right)$$

$$\left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \sqrt{\text{Sec}[c+dx]} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right/$$

$$\left( \sqrt{a^2+b^2} \left( b + \sqrt{a^2+b^2} \right) \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \left( a \text{Cos}[c+dx] + b \text{Sin}[c+dx] \right)}{a^2+b^2}} \right.$$

$$\left. \sqrt{\frac{a \tan \left[ \frac{1}{2}(c+dx) \right]}{b + \sqrt{a^2+b^2}}} \right) +$$

$$\left( 2 a \sqrt{\cot [c+d x]} \left( A \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}, \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] + \right. \right.$$

$$\left. \left. b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}, \right. \right. \right.$$

$$\left. \left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( -a+b+\sqrt{a^2+b^2} \right) - A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right. \right. \right.$$

$$\left. \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}, \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( -i a+b+\sqrt{a^2+b^2} \right) - \right. \right.$$

$$\left. \left. \left. a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}, \right. \right. \right.$$

$$\left. \left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( a+i \left( b+\sqrt{a^2+b^2} \right) \right) - a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Bigg/ \left( -i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Bigg/ \left( -i a + b + \sqrt{a^2 + b^2} \right) - \left( i a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right] \Bigg/ \left( i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left( A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2 + b^2} \right) - \left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) +$$

$$\left( i b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \Bigg/ \left( a + b + \sqrt{a^2+b^2} \right)$$

$$\left. \sqrt{\text{Sec}[c+dx]} (b \text{Cos}[c+dx] - a \text{Sin}[c+dx]) \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right] \Bigg/$$

$$\left( \sqrt{a^2+b^2} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]} \right.$$

$$\left. \left. \sqrt{\frac{a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \text{Cos}[c+dx] + b \text{Sin}[c+dx])}{a^2+b^2}} \right) \right) -$$

$$\frac{1}{\sqrt{a^2 + b^2} \sqrt{\cot [c + d x]} \sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \cos [c + d x] + b \sin [c + d x])}{a^2 + b^2}}}$$

$$2 a \operatorname{Csc} [c + d x]^2 \left( A \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] + \right.$$

$$\left. \left( b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right.$$

$$\left. \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left. \left( a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) - \left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( i b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2+b^2} \right) - \left( i a A \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Big/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Big/$$

$$\left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( a B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Big/$$

$$\begin{aligned}
 & \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( i b \operatorname{B EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) - \\
 & \left( b \operatorname{B EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( a + b + \sqrt{a^2 + b^2} \right) \\
 & \frac{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}}{1} \\
 & \frac{\sqrt{a^2 + b^2} \sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2}}}{\sqrt{a^2 + b^2}} \\
 & 2 a \sqrt{\operatorname{Cot} [c + d x]} \left( \operatorname{A EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) +
 \end{aligned}$$



$$\left( b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$(-a + b + \sqrt{a^2 + b^2}) - \left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (-i a + b + \sqrt{a^2 + b^2}) -$$

$$\left( a A \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (a + i (b + \sqrt{a^2 + b^2})) - \left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (-i a + b + \sqrt{a^2 + b^2}) -$$

$$\left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2 + b^2} \right) - \left( i a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) + \left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \Bigg/$$

$$\left( a + b + \sqrt{a^2+b^2} \right) \text{Sec}[c+dx]^{3/2}$$

$$\frac{\sin[c+dx] \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}}{1}$$

$$\frac{1}{\sqrt{a^2+b^2} \left( \frac{a \sec\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2+b^2} \right)^{3/2}}$$

$$2 a \sqrt{\text{Cot}[c+dx]}$$

$$\left( A \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) +$$

$$\left( b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \Bigg/$$

$$\begin{aligned}
 & \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) - \\
 & \left( a A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \\
 & \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) - \left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) - \\
 & \left( i b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.
 \end{aligned}$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( -i a + b + \sqrt{a^2 + b^2} \right) - \left( i a A \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) + \left( i b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\sqrt{\text{Sec}[c + d x]} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\frac{a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( \frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (b \text{Cos}[c + d x] - a \text{Sin}[c + d x])}{a^2 + b^2} + \frac{1}{a^2 + b^2} \right.$$

$$\left. a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x]) \text{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) +$$

$$\frac{1}{\sqrt{a^2 + b^2} \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])}{a^2 + b^2}}} - 4 a \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Sec}[c + d x]}$$

$$\sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\frac{a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( - \left( a A \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}} \right.$$

$$\left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{2 \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) -$$

$$\left( a b B \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (-a + b + \sqrt{a^2 + b^2}) \right)$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(a A b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4 \sqrt{2} \sqrt{a^2 + b^2} \left(-i a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(a^2 A \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4 \sqrt{2} \sqrt{a^2 + b^2} \left(a + i \left(b + \sqrt{a^2 + b^2}\right)\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(a^2 B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4 \sqrt{2} \sqrt{a^2 + b^2} \left(-i a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) +
 \end{aligned}$$

$$\left( i a b B \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( -i a + b + \sqrt{a^2+b^2} \right) \right. \\ \left. \sqrt{\frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{2 \sqrt{a^2+b^2}}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2+b^2}}} \left( 1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{-i a + b + \sqrt{a^2+b^2}} \right) \right) \right) +$$

$$\left( i a^2 A \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( i a + b + \sqrt{a^2+b^2} \right) \right. \\ \left. \sqrt{\frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{2 \sqrt{a^2+b^2}}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2+b^2}}} \left( 1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{i a + b + \sqrt{a^2+b^2}} \right) \right) \right) +$$

$$\left( a A b \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( i a + b + \sqrt{a^2+b^2} \right) \right. \\ \left. \sqrt{\frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{2 \sqrt{a^2+b^2}}} \right. \right. \\ \left. \left. \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2+b^2}}} \left( 1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{i a + b + \sqrt{a^2+b^2}} \right) \right) \right) +$$

$$\left( a^2 B \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2+b^2} \left( i a + b + \sqrt{a^2+b^2} \right) \right. \\ \left. \sqrt{\frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2+b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{2 \sqrt{a^2+b^2}}} \right)$$



$$\begin{aligned}
 & \left( \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}} \right) \right) - \\
 & \left( a b B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \left( a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2 \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}} \right) \right) + \\
 & \left( a b B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \left( a + b + \sqrt{a^2 + b^2} \right) \right. \\
 & \left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2 \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}} \right) \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

**Problem 617: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a + b \tan[c + dx]} (A + B \tan[c + dx])}{\sqrt{\cot[c + dx]}} dx$$

Optimal (type 3, 261 leaves, 14 steps):

$$\frac{1}{d} \sqrt{i a - b} (A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} +$$

$$\frac{(2 A b + a B) \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} - \frac{1}{d}}{\sqrt{b} d}$$

$$\sqrt{i a + b} (A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} +$$

$$\frac{B \sqrt{a + b \tan [c + d x]}}{d \sqrt{\cot [c + d x]}}$$

Result (type 4, 59809 leaves): Display of huge result suppressed!

**Problem 618: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{a + b \tan [c + d x]} (A + B \tan [c + d x])}{\cot [c + d x]^{3/2}} dx$$

Optimal (type 3, 324 leaves, 15 steps):

$$\frac{1}{d} \sqrt{i a - b} (i A - B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \frac{1}{4 b^{3/2} d}$$

$$(4 a A b - a^2 B - 8 b^2 B) \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \frac{1}{d}$$

$$\sqrt{i a + b} (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} +$$

$$\frac{(4 A b - a B) \sqrt{a + b \tan [c + d x]}}{4 b d \sqrt{\cot [c + d x]}} + \frac{B (a + b \tan [c + d x])^{3/2}}{2 b d \sqrt{\cot [c + d x]}}$$

Result (type 4, 73529 leaves): Display of huge result suppressed!

**Problem 619: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^{11/2} (a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 422 leaves, 13 steps):

$$\begin{aligned} & \frac{1}{d} (i a - b)^{3/2} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} - \frac{1}{d} \\ & (i a + b)^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} - \frac{1}{315 a^3 d} \\ & 2 (315 a^4 A - 63 a^2 A b^2 + 8 A b^4 - 420 a^3 b B - 18 a b^3 B) \sqrt{\cot[c + d x]} \sqrt{a + b \tan[c + d x]} + \\ & \frac{1}{315 a^2 d} 2 (126 a^2 A b + 4 A b^3 + 105 a^3 B - 9 a b^2 B) \cot[c + d x]^{3/2} \sqrt{a + b \tan[c + d x]} + \\ & \frac{2 (21 a^2 A - A b^2 - 24 a b B) \cot[c + d x]^{5/2} \sqrt{a + b \tan[c + d x]}}{105 a d} - \\ & \frac{2 (10 A b + 9 a B) \cot[c + d x]^{7/2} \sqrt{a + b \tan[c + d x]}}{63 d} - \frac{2 a A \cot[c + d x]^{9/2} \sqrt{a + b \tan[c + d x]}}{9 d} \end{aligned}$$

Result (type 4, 5158 leaves):

$$\begin{aligned} & \frac{1}{d (a \cos[c + d x] + b \sin[c + d x]) (A \cos[c + d x] + B \sin[c + d x])} \\ & \cos[c + d x]^2 \sqrt{\cot[c + d x]} \left( -\frac{2 (413 a^4 A - 66 a^2 A b^2 + 8 A b^4 - 492 a^3 b B - 18 a b^3 B)}{315 a^3} + \frac{1}{315 a^2} \right. \\ & \quad 2 (176 a^2 A b \cos[c + d x] + 4 A b^3 \cos[c + d x] + 150 a^3 B \cos[c + d x] - 9 a b^2 B \cos[c + d x]) \\ & \quad \left. \operatorname{Csc}[c + d x] + \frac{2 (133 a^2 A - 3 A b^2 - 72 a b B) \operatorname{Csc}[c + d x]^2}{315 a} - \right. \\ & \quad \left. \frac{2}{63} (10 A b \cos[c + d x] + 9 a B \cos[c + d x]) \operatorname{Csc}[c + d x]^3 - \frac{2}{9} a A \operatorname{Csc}[c + d x]^4 \right) \\ & (a + b \tan[c + d x])^{3/2} (A + B \tan[c + d x]) + \\ & \left( 4 \cos\left[\frac{1}{2} (c + d x)\right]^2 \cos[c + d x]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\ & \quad \left. \sqrt{1 + \frac{a \cot\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + d x]} \right) \\ & \left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 \right. \\ & \quad \left. (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \right) \end{aligned}$$

$$\begin{aligned}
 & (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left( \frac{2 a A b \sqrt{\cot [c + d x]}}{\sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \right. \\
 & \frac{a^2 B \sqrt{\cot [c + d x]}}{\sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} - \\
 & \frac{b^2 B \sqrt{\cot [c + d x]}}{\sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} - \\
 & \frac{a^2 A \sqrt{\cot [c + d x]} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \\
 & \frac{A b^2 \sqrt{\cot [c + d x]} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \\
 & \left. \frac{2 a b B \sqrt{\cot [c + d x]} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{a \cos [c + d x] + b \sin [c + d x]}} \right) \\
 & \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} (a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x]) \right) / \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right) \\
 & \left( - \left( \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right) \right) \right)
 \end{aligned}$$

$$\left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a-i b)^2 (A-i B) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\operatorname{Sec}[c+dx]}\right) /$$

$$\left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \right.$$

$$\left. \left. \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}\right) - \left( a \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \right)$$

$$\left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a-i b)^2 (A-i B) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\begin{aligned}
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \Big/ \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]}} \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \\
 & \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]} \\
 & \left( i (2 a A b+a^2 B-b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & \left. (a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx])^{3/2}} 2 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^2 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec}[c + dx]} (b \operatorname{Cos}[c + dx] - a \operatorname{Sin}[c + dx]) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \operatorname{Csc}[c + dx]^2 \\
 & \left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^2 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \sqrt{\operatorname{Sec} [c+dx]} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}}} 4 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right] \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]} \\
 & \left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-i b)^2 (A-i B) \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c+dx]} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}}} 2 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]} \\
 & \left( i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.
 \end{aligned}$$



$$\begin{aligned}
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \quad \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^2 (A - i B) \\
 & \quad \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}}} 4 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \\
 & \sqrt{\operatorname{Sec} [c + d x]} \left( \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (2 a A b + a^2 B - b^2 B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2}{4 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2}} \right) + \\
 & \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \\
 & \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left. \left. \left. \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}} \tan\left[\frac{1}{2}(c+dx)\right]^{3/2}} \right) \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \right)$$

**Problem 620: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c+d x]^{9 / 2}(a+b \tan [c+d x])^{3 / 2}(A+B \tan [c+d x]) d x$$

Optimal (type 3, 351 leaves, 12 steps):

$$\begin{aligned} & -\frac{1}{d}(i a-b)^{3 / 2}(A+i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}-\frac{1}{d} \\ & (i a+b)^{3 / 2}(A-i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}+ \\ & \frac{1}{105 a^2 d} 2\left(140 a^2 A b+6 A b^3+105 a^3 B-21 a b^2 B\right) \sqrt{\cot [c+d x]} \sqrt{a+b \tan [c+d x]}+ \\ & \frac{2\left(35 a^2 A-3 A b^2-42 a b B\right) \cot [c+d x]^{3 / 2} \sqrt{a+b \tan [c+d x]}}{105 a d}- \\ & \frac{2(8 A b+7 a B) \cot [c+d x]^{5 / 2} \sqrt{a+b \tan [c+d x]}}{35 d}-\frac{2 a A \cot [c+d x]^{7 / 2} \sqrt{a+b \tan [c+d x]}}{7 d} \end{aligned}$$

Result (type 4, 5099 leaves):

$$\begin{aligned} & \left(\cos [c+d x]^2 \sqrt{\cot [c+d x]}\left(\frac{2\left(164 a^2 A b+6 A b^3+126 a^3 B-21 a b^2 B\right)}{105 a^2}+\frac{1}{105 a}\right.\right. \\ & \left.2\left(50 a^2 A \cos [c+d x]-3 A b^2 \cos [c+d x]-42 a b B \cos [c+d x]\right) \operatorname{Csc}[c+d x]-\right. \\ & \left.\frac{2}{35}(8 A b+7 a B) \operatorname{Csc}[c+d x]^2-\frac{2}{7} a A \cot [c+d x] \operatorname{Csc}[c+d x]^2\right) \\ & (a+b \tan [c+d x])^{3 / 2}(A+B \tan [c+d x])\left. \right) / \\ & (d(a \cos [c+d x]+b \sin [c+d x])(A \cos [c+d x]+B \sin [c+d x]))+ \\ & \left(4 i \cos \left[\frac{1}{2}(c+d x)\right]^2 \cos [c+d x]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\right. \\ & \left.\sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]}}\right) \end{aligned}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^2 \right.$$

$$(A+ib) \operatorname{EllipticPi}\left[-\frac{ib+\sqrt{a^2+b^2}}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] -$$

$$(a-ib)^2 (A-ib) \operatorname{EllipticPi}\left[\frac{ib+\sqrt{a^2+b^2}}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right],$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \left( \frac{a^2 A \sqrt{\cot[c+dx]}}{\sqrt{\sec[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]}} - \right.$$

$$\frac{A b^2 \sqrt{\cot[c+dx]}}{\sqrt{\sec[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]}} -$$

$$\frac{2 a b B \sqrt{\cot[c+dx]}}{\sqrt{\sec[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]}} +$$

$$\frac{2 a A b \sqrt{\cot[c+dx]} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{a \cos[c+dx] + b \sin[c+dx]}} +$$

$$\frac{a^2 B \sqrt{\cot[c+dx]} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{a \cos[c+dx] + b \sin[c+dx]}} -$$

$$\left. \frac{b^2 B \sqrt{\cot[c+dx]} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{a \cos[c+dx] + b \sin[c+dx]}} \right)$$

$$\left. \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} (a+b \tan[c+dx])^{3/2} (A+B \tan[c+dx]) \right) /$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \cos[c+dx] + b \sin[c+dx])^2 (A \cos[c+dx] + B \sin[c+dx]) \right)$$

$$\left( - \left( \left( \left( \frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}} \sqrt{\operatorname{Cot} [c + d x]} \right. \right. \right. \right.$$

$$\left. \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$\left. (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\left. \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \right) \right) /$$

$$\left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right.$$

$$\left. \left. \left. \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) \right) - \left( i a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \right.$$

$$\left. \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$\left. (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] - (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Big) / \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \\
 & \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} -
 \end{aligned}$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} (a \cos [c+d x] + b \sin [c+d x])^{3/2}}} 2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^2 (A-i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\sqrt{\sec [c+d x]} (b \cos [c+d x] - a \sin [c+d x]) \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]} \sqrt{a \cos [c+d x] + b \sin [c+d x]}}} 2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \operatorname{Csc} [c+d x]^2$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$\begin{aligned}
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\sec[c + dx]} \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 4 i \cos\left[\frac{1}{2}(c + dx)\right] \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \\
 & \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & \left. (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \sqrt{\sec[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right] \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 2 i \cos\left[\frac{1}{2}(c + dx)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \operatorname{Sec}[c + dx]^{3/2} \operatorname{Sin}[c + dx] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 4 i \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \sqrt{\operatorname{Sec}[c + dx]} \left( - \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^2 A - A b^2 - 2 a b B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \\
 & \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right)
 \end{aligned}$$



$$\left( \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) +$$

$$\left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right)$$

**Problem 621: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c+dx]^{7/2} (a+b \operatorname{Tan}[c+dx])^{3/2} (A+B \operatorname{Tan}[c+dx]) dx$$

Optimal (type 3, 299 leaves, 11 steps):

$$\frac{1}{\sqrt{i a - b} d} (a + i b)^2 (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a + b \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} +$$

$$\frac{1}{d} (i a + b)^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a + b \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} +$$

$$\frac{2 (15 a^2 A - 3 A b^2 - 20 a b B) \sqrt{\operatorname{Cot}[c+dx]} \sqrt{a + b \operatorname{Tan}[c+dx]}}{15 a d} -$$

$$\frac{2 (6 A b + 5 a B) \operatorname{Cot}[c+dx]^{3/2} \sqrt{a + b \operatorname{Tan}[c+dx]}}{15 d} - \frac{2 a A \operatorname{Cot}[c+dx]^{5/2} \sqrt{a + b \operatorname{Tan}[c+dx]}}{5 d}$$

Result (type 4, 5041 leaves):

$$\left( \operatorname{Cos}[c+dx]^2 \sqrt{\operatorname{Cot}[c+dx]} \right.$$

$$\left( \frac{2 (18 a^2 A - 3 A b^2 - 20 a b B)}{15 a} - \frac{2}{15} (6 A b \operatorname{Cos}[c+dx] + 5 a B \operatorname{Cos}[c+dx]) \operatorname{Csc}[c+dx] -$$

$$\frac{2}{5} a A \operatorname{Csc}[c+dx]^2 \right) (a + b \operatorname{Tan}[c+dx])^{3/2} (A + B \operatorname{Tan}[c+dx]) \Big/$$

$$(d (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]) (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx])) +$$

$$\left( 4 \cos\left[\frac{1}{2}(c+dx)\right]^2 \cos[c+dx]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot[c+dx]}$$

$$\left. -i(2aAb+a^2B-b^2B) \operatorname{EllipticF}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a+ib)^2$$

$$(A+ib) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$(a-ib)^2 (A-ib) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right],$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \left( -\frac{2aAb\sqrt{\cot[c+dx]}}{\sqrt{\sec[c+dx]}\sqrt{a\cos[c+dx]+b\sin[c+dx]}} - \right.$$

$$\frac{a^2B\sqrt{\cot[c+dx]}}{\sqrt{\sec[c+dx]}\sqrt{a\cos[c+dx]+b\sin[c+dx]}} +$$

$$\frac{b^2B\sqrt{\cot[c+dx]}}{\sqrt{\sec[c+dx]}\sqrt{a\cos[c+dx]+b\sin[c+dx]}} +$$

$$\frac{a^2A\sqrt{\cot[c+dx]}\sqrt{\sec[c+dx]}\sin[c+dx]}{\sqrt{a\cos[c+dx]+b\sin[c+dx]}} -$$

$$\frac{Ab^2\sqrt{\cot[c+dx]}\sqrt{\sec[c+dx]}\sin[c+dx]}{\sqrt{a\cos[c+dx]+b\sin[c+dx]}} -$$

$$\left. \frac{2aBB\sqrt{\cot[c+dx]}\sqrt{\sec[c+dx]}\sin[c+dx]}{\sqrt{a\cos[c+dx]+b\sin[c+dx]}} \right)$$

$$\left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} (a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x]) \right/$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \cos [c + d x] + b \sin [c + d x])^2 (A \cos [c + d x] + B \sin [c + d x]) \right.$$

$$\left. - \left( \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right. \right. \right.$$

$$\left. \left. \left. - i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right], \right. \right. \right.$$

$$\left. \left. \left. (a + i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \right. \right. \right.$$

$$\left. \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \right) /$$

$$\left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right.$$

$$\left. \left. \left. \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right) - \left( a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right)$$

$$\left( -i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + \right.$$

$$\left. (a+i b)^2 (A+i B) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^2 (A-i B) \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec}[c+dx]} \Bigg) /$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) +$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}} \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]}$$

$$\left( -i (2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + \right.$$

$$\begin{aligned}
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\sec[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos[c + dx] + b \sin[c + dx])^{3/2}} 2 \cos\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \\
 & \left( -i(2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \right. \\
 & (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 (A - i B) \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 2 \cos\left[\frac{1}{2}(c + dx)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \operatorname{Csc}[c + dx]^2 \\
 & \left( -i(2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \\
 & (a + ib)^2 (A + iB) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - ib)^2 (A - iB) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 4 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( -i(2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \\
 & (a + ib)^2 (A + iB) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - ib)^2 (A - iB)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( -i \left( 2 a A b + a^2 B - b^2 B \right) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \\
 & \left. (a + i b)^2 (A + i B) \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sec [c + d x]^{3/2} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]}
 \end{aligned}$$

$$\begin{aligned} & \sqrt{\sec [c+d x]} \left( - \left( \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (2 a A b+a^2 B-b^2 B) \sec \left[ \frac{1}{2}(c+d x) \right]^2 \right) / \right. \right. \\ & \left. \left( 4 \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \right) \right) - \\ & \left( i(a+i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \sec \left[ \frac{1}{2}(c+d x) \right]^2 \right) / \left( 4 \left( 1-i \cot \left[ \frac{1}{2}(c+d x) \right] \right) \right) \\ & \left. \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \right) + \\ & \left( i(a-i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A-i B) \sec \left[ \frac{1}{2}(c+d x) \right]^2 \right) / \\ & \left( 4 \left( 1+i \cot \left[ \frac{1}{2}(c+d x) \right] \right) \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \right. \\ & \left. \left. \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \right) \right) \tan \left[ \frac{1}{2}(c+d x) \right]^{3 / 2} \right) \end{aligned}$$

**Problem 622: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c+d x]^{5 / 2}(a+b \tan [c+d x])^{3 / 2}(A+B \tan [c+d x]) d x$$

Optimal (type 3, 236 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{d}(i a-b)^{3 / 2}(A+i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}+\frac{1}{d} \\ & (i a+b)^{3 / 2}(A-i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}- \\ & \frac{2(4 A b+3 a B) \sqrt{\cot [c+d x]} \sqrt{a+b \tan [c+d x]}}{3 d}-\frac{2 a A \cot [c+d x]^{3 / 2} \sqrt{a+b \tan [c+d x]}}{3 d} \end{aligned}$$

Result (type 4, 5000 leaves):



$$\begin{aligned}
 & \left( \cos [c+d x]^2 \sqrt{\cot [c+d x]} \left( -\frac{2}{3} (4 A b+3 a B)-\frac{2}{3} a A \cot [c+d x] \right) (a+b \tan [c+d x])^{3 / 2} \right. \\
 & \quad \left. (A+B \tan [c+d x]) \right) / \left( d (a \cos [c+d x]+b \sin [c+d x]) (A \cos [c+d x]+B \sin [c+d x]) \right) - \\
 & \left( 4 i \cos \left[ \frac{1}{2} (c+d x) \right]^2 \cos [c+d x]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \quad \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \quad \left( a^2 A-A b^2-2 a b B \right) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\left( a+i b \right)^2 \\
 & \quad \left( A+i B \right) \operatorname{EllipticPi}\left[ -\frac{i\left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- \\
 & \quad \left( a-i b \right)^2 \left( A-i B \right) \operatorname{EllipticPi}\left[ \frac{i\left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \\
 & \quad \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \left( -\frac{a^2 A \sqrt{\cot [c+d x]}}{\sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \right. \\
 & \quad \frac{A b^2 \sqrt{\cot [c+d x]}}{\sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \\
 & \quad \frac{2 a b B \sqrt{\cot [c+d x]}}{\sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} - \\
 & \quad \frac{2 a A b \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{a \cos [c+d x]+b \sin [c+d x]}} - \\
 & \quad \left. \frac{a^2 B \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \right)
 \end{aligned}$$

$$\left. \frac{b^2 B \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{a \cos [c+d x]+b \sin [c+d x]}} \right)$$

$$\left. \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} (a+b \tan [c+d x])^{3/2} (A+B \tan [c+d x]) \right/$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \cos [c+d x]+b \sin [c+d x])^2 (A \cos [c+d x]+B \sin [c+d x]) \right.$$

$$\left. \left( \left( i a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \right. \right. \right.$$

$$\left. \left( (a^2 A-A b^2-2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$\left. (a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+d x]} \right/$$

$$\left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right.$$

$$\begin{aligned}
 & \sqrt{\tan\left[\frac{1}{2}(c+dx)\right]} + \left( i a \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c+dx]} \right. \\
 & \left. \left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. (a + i b)^2 (A + i B) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec[c+dx]} \right) / \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \cos[c+dx] + b \sin[c+dx]} \sqrt{\tan\left[\frac{1}{2}(c+dx)\right]} \right) - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c+dx] + b \sin[c+dx]}} 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c+dx]}
 \end{aligned}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec}[c+d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]} +$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} (a \operatorname{Cos}[c+d x] + b \operatorname{Sin}[c+d x])^{3/2}}} - 2 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+d x]}$$

$$\left( (a^2 A - A b^2 - 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^2 (A-i B)$$

$$\operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\begin{aligned}
 & \sqrt{\sec [c+d x]} (b \cos [c+d x]-a \sin [c+d x]) \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}+ \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} 2 i \cos \left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \operatorname{Csc}[c+d x]^2 \\
 & \left( \left(a^2 A-A b^2-2 a b B\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- \right. \\
 & \left. (a+i b)^2(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\left(a-i b\right)^2(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right) \sqrt{\sec [c+d x]} \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}+ \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} 4 i \cos \left[\frac{1}{2}(c+d x)\right] \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( \left(a^2 A-A b^2-2 a b B\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- \right. \\
 & \left. (a+i b)^2(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \right.
 \end{aligned}$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-i b)^2 (A-i B)$$

$$\operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]$$

$$\sqrt{\operatorname{Sec} [c+d x]} \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}}} 2 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+d x]}$$

$$\left( a^2 A - A b^2 - 2 a b B \right) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$(a+i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-i b)^2 (A-i B)$$

$$\operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]$$

$$\operatorname{Sec} [c+d x]^{3/2} \operatorname{Sin} [c+d x] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}}} 4 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \sqrt{\operatorname{Sec}[c + dx]} \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^2 A - A b^2 - 2 a b B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \right. \\
 & \left. \left( 4 \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \\
 & \left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right) \\
 & \left. \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) + \\
 & \left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \\
 & \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left. \left. \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right)
 \end{aligned}$$

**Problem 623: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + dx]^{3/2} (a + b \operatorname{Tan}[c + dx])^{3/2} (A + B \operatorname{Tan}[c + dx]) dx$$

Optimal (type 3, 269 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{1}{\sqrt{i a - b} d} (a + i b)^2 (i A - B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} + \\
 & \frac{2 b^{3/2} B \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{d} - \frac{1}{d} \\
 & (i a + b)^{3/2} (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} - \\
 & \frac{2 a A \sqrt{\operatorname{Cot}[c + d x]} \sqrt{a + b \operatorname{Tan}[c + d x]}}{d}
 \end{aligned}$$

Result (type 4, 74 118 leaves): Display of huge result suppressed!

**Problem 624: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Cot}[c + d x]} (a + b \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x]) dx$$

Optimal (type 3, 264 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{1}{d} (i a - b)^{3/2} (A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} + \\
 & \frac{1}{d} \sqrt{b} (2 A b + 3 a B) \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} - \frac{1}{d} \\
 & (i a + b)^{3/2} (A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}} \right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]} + \\
 & \frac{b B \sqrt{a + b \operatorname{Tan}[c + d x]}}{d \sqrt{\operatorname{Cot}[c + d x]}}
 \end{aligned}$$

Result (type 4, 82 770 leaves): Display of huge result suppressed!

**Problem 625: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \operatorname{Tan}[c + d x])^{3/2} (A + B \operatorname{Tan}[c + d x])}{\sqrt{\operatorname{Cot}[c + d x]}} dx$$

Optimal (type 3, 328 leaves, 15 steps):



$$\begin{aligned} & \frac{1}{\sqrt{i a - b} d} (a + i b)^2 (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ & \frac{1}{4 \sqrt{b} d} (12 a A b + 3 a^2 B - 8 b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ & \frac{1}{d} (i a + b)^{3/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ & \frac{b B \sqrt{a + b \tan [c + d x]}}{2 d \cot [c + d x]^{3/2}} + \frac{(4 A b + 5 a B) \sqrt{a + b \tan [c + d x]}}{4 d \sqrt{\cot [c + d x]}} \end{aligned}$$

Result (type 4, 91499 leaves): Display of huge result suppressed!

**Problem 626: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan [c + d x])^{3/2} (A + B \tan [c + d x])}{\cot [c + d x]^{3/2}} dx$$

Optimal (type 3, 383 leaves, 16 steps):

$$\begin{aligned} & \frac{1}{d} (i a - b)^{3/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \frac{1}{8 b^{3/2} d} \\ & (6 a^2 A b - 16 A b^3 - a^3 B - 24 a b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ & \frac{1}{d} (i a + b)^{3/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ & \frac{(6 a A b - a^2 B - 8 b^2 B) \sqrt{a + b \tan [c + d x]}}{8 b d \sqrt{\cot [c + d x]}} + \\ & \frac{(6 A b - a B) (a + b \tan [c + d x])^{3/2}}{12 b d \sqrt{\cot [c + d x]}} + \frac{B (a + b \tan [c + d x])^{5/2}}{3 b d \sqrt{\cot [c + d x]}} \end{aligned}$$

Result (type 4, 105230 leaves): Display of huge result suppressed!

**Problem 627: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^{13/2} (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 500 leaves, 14 steps):

$$\begin{aligned}
 & -\frac{1}{d} (i a - b)^{5/2} (i A - B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}} \right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} - \frac{1}{d} \\
 & (i a + b)^{5/2} (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}} \right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} - \\
 & \frac{1}{3465 a^3 d} 2 (8085 a^4 A b - 495 a^2 A b^3 + 40 A b^5 + 3465 a^5 B - 5313 a^3 b^2 B - 110 a b^4 B) \\
 & \sqrt{\cot[c + d x]} \sqrt{a + b \tan[c + d x]} - \frac{1}{3465 a^2 d} \\
 & 2 (1155 a^4 A - 1485 a^2 A b^2 - 20 A b^4 - 2541 a^3 b B + 55 a b^3 B) \cot[c + d x]^{3/2} \sqrt{a + b \tan[c + d x]} + \\
 & \frac{1}{1155 a d} 2 (495 a^2 A b - 5 A b^3 + 231 a^3 B - 275 a b^2 B) \cot[c + d x]^{5/2} \sqrt{a + b \tan[c + d x]} + \\
 & \frac{2 (99 a^2 A - 113 A b^2 - 209 a b B) \cot[c + d x]^{7/2} \sqrt{a + b \tan[c + d x]}}{693 d} - \\
 & \frac{2 a (14 A b + 11 a B) \cot[c + d x]^{9/2} \sqrt{a + b \tan[c + d x]}}{99 d} - \frac{2 a A \cot[c + d x]^{11/2} (a + b \tan[c + d x])^{3/2}}{11 d}
 \end{aligned}$$

Result (type 4, 5419 leaves):

$$\begin{aligned}
 & \frac{1}{d (a \cos[c + d x] + b \sin[c + d x])^2 (A \cos[c + d x] + B \sin[c + d x])} \cos[c + d x]^3 \sqrt{\cot[c + d x]} \\
 & \left( -\frac{1}{3465 a^3} 2 (10375 a^4 A b - 510 a^2 A b^3 + 40 A b^5 + 4543 a^5 B - 6138 a^3 b^2 B - 110 a b^4 B) - \right. \\
 & \frac{1}{3465 a^2} 2 (1965 a^4 A \cos[c + d x] - 2050 a^2 A b^2 \cos[c + d x] - 20 A b^4 \cos[c + d x] - \\
 & \quad \left. 3586 a^3 b B \cos[c + d x] + 55 a b^3 B \cos[c + d x]) \operatorname{Csc}[c + d x] + \right. \\
 & \left. \frac{2 (3095 a^2 A b - 15 A b^3 + 1463 a^3 B - 825 a b^2 B) \operatorname{Csc}[c + d x]^2}{3465 a} + \right. \\
 & \frac{2}{693} (225 a^2 A \cos[c + d x] - 113 A b^2 \cos[c + d x] - 209 a b B \cos[c + d x]) \operatorname{Csc}[c + d x]^3 - \\
 & \left. \frac{2}{99} a (23 A b + 11 a B) \operatorname{Csc}[c + d x]^4 - \frac{2}{11} a^2 A \cot[c + d x] \operatorname{Csc}[c + d x]^4 \right) \\
 & (a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x]) - \\
 & \left( 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \cos[c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + d x]} \right)
 \end{aligned}$$

$$\left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right]}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a+ib)^3 (A+ib) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}\right],$$

$$i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-ib)^3 (A-ib)$$

$$\left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}\right], i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)$$

$$\left( -\frac{a^3 A \sqrt{\operatorname{Cot}[c+dx]}}{\sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \right.$$

$$\frac{3 a A b^2 \sqrt{\operatorname{Cot}[c+dx]}}{\sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} +$$

$$\frac{3 a^2 b B \sqrt{\operatorname{Cot}[c+dx]}}{\sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} -$$

$$\frac{b^3 B \sqrt{\operatorname{Cot}[c+dx]}}{\sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} -$$

$$\frac{3 a^2 A b \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} +$$

$$\frac{A b^3 \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} -$$

$$\frac{a^3 B \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} +$$

$$\left. \frac{3 a b^2 B \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right)$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} (a+b \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) \right) /$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \cos [c + d x] + b \sin [c + d x])^3 (A \cos [c + d x] + B \sin [c + d x]) \right.$$

$$\left. \left( \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right) (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \right. \right.$$

$$\text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B)$$

$$\text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] -$$

$$(a - i b)^3 (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \Big/ \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \right.$$

$$\left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \right) +$$

$$\left( i a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right) (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B)$$

$$\text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+\text{i}b)^3 (A+\text{i}B)$$

$$\text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] -$$

$$(a-\text{i}b)^3 (A-\text{i}B) \text{EllipticPi}\left[\frac{\text{i}(b+\sqrt{a^2+b^2})}{a},$$

$$\left. \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\text{Sec}[c+dx]} \right) /$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\sqrt{a \text{Cos}[c+dx]+b \text{Sin}[c+dx]} \sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \text{Cos}[c+dx]+b \text{Sin}[c+dx]}} 3 \text{i} \sqrt{\frac{b+\sqrt{a^2+b^2}+a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\sqrt{1+\frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\text{Cot}[c+dx]} \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \right)$$

$$\text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+\text{i}b)^3 (A+\text{i}B)$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \\
 & (a-ib)^3 (A-ib) \text{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \left. \sqrt{\sec[c+dx]} \sqrt{\tan\left[\frac{1}{2}(c+dx)\right]} + \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}} (a \cos[c+dx] + b \sin[c+dx])^{3/2} 2i \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
 & \left. \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot[c+dx]} \right. \\
 & \left. \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right) \text{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^3 (A+ib) \text{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-ib)^3 (A-ib) \right. \\
 & \left. \text{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right) \\
 & \sqrt{\sec[c+dx]} (b \cos[c+dx] - a \sin[c+dx]) \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \\
 & 2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \operatorname{Csc}[c+d x]^2 \left( \left( a^3 A-3 a A b^2-3 a^2 b B+b^3 B \right) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^3 (A-i B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\sec [c+d x]} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} + \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \\
 & 4 i \cos \left[ \frac{1}{2} (c+d x) \right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\cot [c+d x]} \left( \left( a^3 A-3 a A b^2-3 a^2 b B+b^3 B \right) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i \left( b+\sqrt{a^2+b^2} \right)}{a}, \right. \right.
 \end{aligned}$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-i b)^3 (A-i B)$$

$$\operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]$$

$$\sqrt{\operatorname{Sec} [c+dx]} \operatorname{Sin} \left[ \frac{1}{2} (c+dx) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}} 2 i \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]}$$

$$\left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a+i b)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-i b)^3 (A-i B) \right.$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\operatorname{Sec} [c+dx]^{3/2} \operatorname{Sin} [c+dx] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}} 4 i \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2$$



$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \sqrt{\operatorname{Sec}[c + dx]} \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \right. \\
 & \left. \left( 4 \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \\
 & \left( i (a + i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right) \\
 & \left. \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) + \\
 & \left( i (a - i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \\
 & \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left. \left. \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right)
 \end{aligned}$$

**Problem 628: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + dx]^{11/2} (a + b \operatorname{Tan}[c + dx])^{5/2} (A + B \operatorname{Tan}[c + dx]) \, dx$$

Optimal (type 3, 418 leaves, 13 steps):

$$\frac{1}{d} (i a - b)^{5/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} - \frac{1}{d}$$

$$(i a + b)^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} - \frac{1}{315 a^2 d}$$

$$2 (315 a^4 A - 483 a^2 A b^2 - 10 A b^4 - 735 a^3 b B + 45 a b^3 B) \sqrt{\cot[c + d x]} \sqrt{a + b \tan[c + d x]} +$$

$$\frac{1}{315 a d} 2 (231 a^2 A b - 5 A b^3 + 105 a^3 B - 135 a b^2 B) \cot[c + d x]^{3/2} \sqrt{a + b \tan[c + d x]} +$$

$$\frac{2 (21 a^2 A - 25 A b^2 - 45 a b B) \cot[c + d x]^{5/2} \sqrt{a + b \tan[c + d x]}}{105 d} -$$

$$\frac{2 a (4 A b + 3 a B) \cot[c + d x]^{7/2} \sqrt{a + b \tan[c + d x]}}{21 d} - \frac{2 a A \cot[c + d x]^{9/2} (a + b \tan[c + d x])^{3/2}}{9 d}$$

Result (type 4, 5348 leaves):

$$\frac{1}{d (a \cos[c + d x] + b \sin[c + d x])^2 (A \cos[c + d x] + B \sin[c + d x])}$$

$$\cos[c + d x]^3 \sqrt{\cot[c + d x]} \left( -\frac{2 (413 a^4 A - 558 a^2 A b^2 - 10 A b^4 - 870 a^3 b B + 45 a b^3 B)}{315 a^2} + \frac{1}{315 a} \right.$$

$$2 (326 a^2 A b \cos[c + d x] - 5 A b^3 \cos[c + d x] + 150 a^3 B \cos[c + d x] - 135 a b^2 B \cos[c + d x])$$

$$\operatorname{Csc}[c + d x] + \frac{2}{315} (133 a^2 A - 75 A b^2 - 135 a b B) \operatorname{Csc}[c + d x]^2 -$$

$$\frac{2}{63} (19 a A b \cos[c + d x] + 9 a^2 B \cos[c + d x]) \operatorname{Csc}[c + d x]^3 - \frac{2}{9} a^2 A \operatorname{Csc}[c + d x]^4 \left. \right)$$

$$(a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x]) +$$

$$\left( 4 \cos\left[\frac{1}{2} (c + d x)\right]^2 \cos[c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}}\right.$$

$$\left. \sqrt{1 + \frac{a \cot\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + d x]} \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \right. \right.$$

$$\left. \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \right.$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a - ib)^3 \\
 & \left. (A - ib) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \left( \frac{3a^2Ab\sqrt{\cot[c + dx]}}{\sqrt{\sec[c + dx]}\sqrt{a\cos[c + dx] + b\sin[c + dx]}} - \right. \\
 & \frac{Ab^3\sqrt{\cot[c + dx]}}{\sqrt{\sec[c + dx]}\sqrt{a\cos[c + dx] + b\sin[c + dx]}} + \\
 & \frac{a^3B\sqrt{\cot[c + dx]}}{\sqrt{\sec[c + dx]}\sqrt{a\cos[c + dx] + b\sin[c + dx]}} - \\
 & \frac{3ab^2B\sqrt{\cot[c + dx]}}{\sqrt{\sec[c + dx]}\sqrt{a\cos[c + dx] + b\sin[c + dx]}} - \\
 & \frac{a^3A\sqrt{\cot[c + dx]}\sqrt{\sec[c + dx]}\sin[c + dx]}{\sqrt{a\cos[c + dx] + b\sin[c + dx]}} + \\
 & \frac{3aAb^2\sqrt{\cot[c + dx]}\sqrt{\sec[c + dx]}\sin[c + dx]}{\sqrt{a\cos[c + dx] + b\sin[c + dx]}} + \\
 & \frac{3a^2bB\sqrt{\cot[c + dx]}\sqrt{\sec[c + dx]}\sin[c + dx]}{\sqrt{a\cos[c + dx] + b\sin[c + dx]}} - \\
 & \left. \frac{b^3B\sqrt{\cot[c + dx]}\sqrt{\sec[c + dx]}\sin[c + dx]}{\sqrt{a\cos[c + dx] + b\sin[c + dx]}} \right) \\
 & \left. \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} (a + b \tan[c + dx])^{5/2} (A + B \tan[c + dx]) \right) / \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \cos[c + dx] + b \sin[c + dx])^3 (A \cos[c + dx] + B \sin[c + dx]) \right)
 \end{aligned}$$

$$\left( \left( \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \right) \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \right. \right. \right.$$

$$\operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B)$$

$$\operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] +$$

$$(a - i b)^3 (A - i B) \operatorname{EllipticPi}\left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right],$$

$$\left. \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec}[c + dx]} \right) / \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \right. \right.$$

$$\left. \left. \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]} \right) \right) -$$

$$\left( a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \right) \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \right.$$

$$\operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B)$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \\
 & (a - ib)^3 (A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\operatorname{Sec}[c + dx]}\right] / \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \left( i(3a^2Ab - Ab^3 + a^3B - 3ab^2B) \right. \\
 & \left. \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + ib)^3 (A + iB) \right. \\
 & \left. \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & (a - i b)^3 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\operatorname{Sec}[c + dx]} \sqrt{\tan\left[\frac{1}{2}(c + dx)\right]} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos[c + dx] + b \sin[c + dx])^{3/2}} 2 \cos\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \\
 & \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a - i b)^3 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \sqrt{\operatorname{Sec}[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]}}
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \operatorname{Csc}[c+dx]^2 \left( i(3a^2Ab - Ab^3 + a^3B - 3ab^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+ib)^3 (A+iB) \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a-ib)^3 (A-ib) \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \\
 & 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\operatorname{Cot}[c+dx]} \left( i(3a^2Ab - Ab^3 + a^3B - 3ab^2B) \right. \\
 & \left. \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+ib)^3 (A+iB) \right. \\
 & \left. \operatorname{EllipticPi}\left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & (a - i b)^3 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x] \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} +} \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} 2 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2} \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \\
 & \left( i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a - i b)^3 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} 4 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2}
 \end{aligned}$$



$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \sqrt{\operatorname{Sec}[c + dx]} \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (3a^2Ab - Ab^3 + a^3B - 3a^2B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \\
 & \left( 4 \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) + \\
 & \left( i(a + ib)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + iB) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right) \\
 & \left. \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) - \\
 & \left( i(a - ib)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - iB) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \\
 & \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left. \left. \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right)
 \end{aligned}$$

**Problem 629: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c + dx]^{9/2} (a + b \operatorname{Tan}[c + dx])^{5/2} (A + B \operatorname{Tan}[c + dx]) dx$$

Optimal (type 3, 349 leaves, 12 steps):

$$\frac{1}{d} (i a - b)^{5/2} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} + \frac{1}{d} (i a + b)^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} + \frac{1}{105 a d} 2 (245 a^2 A b - 15 A b^3 + 105 a^3 B - 161 a b^2 B) \sqrt{\cot[c + d x]} \sqrt{a + b \tan[c + d x]} + \frac{2 (35 a^2 A - 45 A b^2 - 77 a b B) \cot[c + d x]^{3/2} \sqrt{a + b \tan[c + d x]}}{105 d} - \frac{2 a (10 A b + 7 a B) \cot[c + d x]^{5/2} \sqrt{a + b \tan[c + d x]}}{35 d} - \frac{2 a A \cot[c + d x]^{7/2} (a + b \tan[c + d x])^{3/2}}{7 d}$$

Result (type 4, 5276 leaves):

$$\left( \cos[c + d x]^3 \sqrt{\cot[c + d x]} \left( \frac{2 (290 a^2 A b - 15 A b^3 + 126 a^3 B - 161 a b^2 B)}{105 a} + \frac{2}{105} (50 a^2 A \cos[c + d x] - 45 A b^2 \cos[c + d x] - 77 a b B \cos[c + d x]) \operatorname{Csc}[c + d x] - \frac{2}{35} a (15 A b + 7 a B) \operatorname{Csc}[c + d x]^2 - \frac{2}{7} a^2 A \cot[c + d x] \operatorname{Csc}[c + d x]^2 \right) (a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x]) \right) / \left( d (a \cos[c + d x] + b \sin[c + d x])^2 (A \cos[c + d x] + B \sin[c + d x]) \right) + \left( 4 i \cos\left[\frac{1}{2} (c + d x)\right]^2 \cos[c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + d x]} \left( a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B \right) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2} (c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^3 \right)$$

$$\left( (A - i B) \operatorname{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\left( \frac{a^3 A \sqrt{\operatorname{Cot} [c + d x]}}{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} - \frac{3 a A b^2 \sqrt{\operatorname{Cot} [c + d x]}}{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} - \frac{3 a^2 b B \sqrt{\operatorname{Cot} [c + d x]}}{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \frac{b^3 B \sqrt{\operatorname{Cot} [c + d x]}}{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \frac{3 a^2 A b \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{\sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} - \frac{A b^3 \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{\sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \frac{a^3 B \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{\sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} - \frac{3 a b^2 B \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{\sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} \right)$$

$$\left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} (a + b \operatorname{Tan} [c + d x])^{5/2} (A + B \operatorname{Tan} [c + d x]) \right/$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^3 (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right)$$

$$\left( - \left( \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \right) (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \right) \right)$$

$$\text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+\text{i}b)^3 (A+\text{i}B)$$

$$\text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] -$$

$$(a-\text{i}b)^3 (A-\text{i}B) \text{EllipticPi}\left[\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right],$$

$$\left.\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\text{Sec}[c+dx]} \Big/ \left(\left(b-\sqrt{a^2+b^2}\right) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}\right)$$

$$\left.\sqrt{1+\frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}}\sqrt{a \text{Cos}[c+dx]+b \text{Sin}[c+dx]}\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}\right] -$$

$$\left(\text{i}a \sqrt{1+\frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}}\sqrt{\text{Cot}[c+dx]}\left(a^3A-3aAb^2-3a^2bB+b^3B\right)\right)$$

$$\text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+\text{i}b)^3 (A+\text{i}B)$$

$$\text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] -$$

$$(a-\text{i}b)^3 (A-\text{i}B) \text{EllipticPi}\left[\frac{\text{i}(b+\sqrt{a^2+b^2})}{a},$$

$$\begin{aligned}
 & \left. \left( \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+dx]} \right) / \\
 & \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \cos [c+dx]+b \sin [c+dx]} \sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]} \right) + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+dx]+b \sin [c+dx]}} \operatorname{EllipticF} \left[ \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+ib)^3 (A+ib) \\
 & \left. \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+dx]} \right) (a^3 A-3 a A b^2-3 a^2 b B+b^3 B) \\
 & \operatorname{EllipticF} \left[ \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+ib)^3 (A+ib) \\
 & \operatorname{EllipticPi} \left[ -\frac{ib+\sqrt{a^2+b^2}}{a}, \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \\
 & (a-ib)^3 (A-ib) \operatorname{EllipticPi} \left[ \frac{ib+\sqrt{a^2+b^2}}{a}, \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+dx]} \sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]} -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} (a \cos [c+d x] + b \sin [c+d x])^{3/2}}} 2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^3 (A-i B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \sqrt{\sec [c+d x]} (b \cos [c+d x] - a \sin [c+d x]) \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{\cot [c+d x]} \sqrt{a \cos [c+d x] + b \sin [c+d x]}}} \\
 & 2 i \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \operatorname{Csc} [c+d x]^2 \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a-i b)^3 (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \frac{\sqrt{\operatorname{Sec} [c+d x]} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}}}{4 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}}} \\
 & \sqrt{\operatorname{Cot} [c+d x]} \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^3 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a-i b)^3 (A-i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
 & \frac{\sqrt{\operatorname{Sec} [c+d x]} \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} + \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}}}{2 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^3 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^3 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \operatorname{Sec}[c + dx]^{3/2} \operatorname{Sin}[c + dx] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 4 i \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \sqrt{\operatorname{Sec}[c + dx]} \left( - \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^3 A - 3 a A b^2 - 3 a^2 b B + b^3 B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \\
 & \left( i (a + i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right)
 \end{aligned}$$



$$\left( \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) +$$

$$\left( i (a - i b)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right)$$

**Problem 630: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cot}[c+dx]^{7/2} (a+b \operatorname{Tan}[c+dx])^{5/2} (A+B \operatorname{Tan}[c+dx]) dx$$

Optimal (type 3, 287 leaves, 11 steps):

$$-\frac{1}{d} (i a - b)^{5/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a + b \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} + \frac{1}{d}$$

$$(i a + b)^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c+dx]}}{\sqrt{a + b \operatorname{Tan}[c+dx]}}\right] \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Tan}[c+dx]} +$$

$$\frac{2 (15 a^2 A - 23 A b^2 - 35 a b B) \sqrt{\operatorname{Cot}[c+dx]} \sqrt{a + b \operatorname{Tan}[c+dx]}}{15 d} -$$

$$\frac{2 a (8 A b + 5 a B) \operatorname{Cot}[c+dx]^{3/2} \sqrt{a + b \operatorname{Tan}[c+dx]}}{15 d} - \frac{2 a A \operatorname{Cot}[c+dx]^{5/2} (a + b \operatorname{Tan}[c+dx])^{3/2}}{5 d}$$

Result (type 4, 5229 leaves):

$$\left( \operatorname{Cos}[c+dx]^3 \sqrt{\operatorname{Cot}[c+dx]} \right.$$

$$\left( \frac{2}{15} (18 a^2 A - 23 A b^2 - 35 a b B) - \frac{2}{15} (11 a A b \operatorname{Cos}[c+dx] + 5 a^2 B \operatorname{Cos}[c+dx]) \operatorname{Csc}[c+dx] - \right.$$

$$\left. \left. \frac{2}{5} a^2 A \operatorname{Csc}[c+dx]^2 \right) (a + b \operatorname{Tan}[c+dx])^{5/2} (A + B \operatorname{Tan}[c+dx]) \right) /$$

$$\left( d (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2 (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right) +$$

$$\left( 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \cos [c + d x]^3 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right.$$

$$\left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right) - i (3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B)$$

$$\text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^3 (A + i B)$$

$$\text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^3$$

$$\left. (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\left( -\frac{3 a^2 A b \sqrt{\cot [c + d x]}}{\sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} + \right.$$

$$\frac{A b^3 \sqrt{\cot [c + d x]}}{\sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} -$$

$$\frac{a^3 B \sqrt{\cot [c + d x]}}{\sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} +$$

$$\frac{3 a b^2 B \sqrt{\cot [c + d x]}}{\sqrt{\sec [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} +$$

$$\frac{a^3 A \sqrt{\cot [c + d x]} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{a \cos [c + d x] + b \sin [c + d x]}} -$$

$$\frac{3 a A b^2 \sqrt{\cot [c + d x]} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{a \cos [c + d x] + b \sin [c + d x]}} -$$

$$\left. \frac{3 a^2 b B \sqrt{\cot [c + d x]} \sqrt{\sec [c + d x]} \sin [c + d x]}{\sqrt{a \cos [c + d x] + b \sin [c + d x]}} \right) +$$

$$\left. \frac{b^3 B \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{a \cos [c+d x]+b \sin [c+d x]}} \right)$$

$$\left. \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} (a+b \tan [c+d x])^{5/2} (A+B \tan [c+d x]) \right) /$$

$$\left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (a \cos [c+d x]+b \sin [c+d x])^3 (A \cos [c+d x]+B \sin [c+d x]) \right)$$

$$\left( - \left( \left( a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \right) \left( -i (3 a^2 A b-A b^3+a^3 B-3 a b^2 B) \right. \right. \right)$$

$$\text{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b)^3 (A+i B)$$

$$\text{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$(a-i b)^3 (A-i B) \text{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+d x]} / \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \right)$$

$$\left. \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}}{b-\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right) -$$

$$\left( a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \right) \left( -i (3a^2Ab - Ab^3 + a^3B - 3ab^2B) \right.$$

$$\operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] + (a+ib)^3 (A+ib)$$

$$\operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] -$$

$$(a-ib)^3 (A-ib) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2+b^2}}{b - \sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec}[c+dx]} \right) /$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2+b^2}}} (b + \sqrt{a^2+b^2}) \sqrt{\frac{b + \sqrt{a^2+b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) +$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \frac{3}{\sqrt{\frac{b + \sqrt{a^2+b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2+b^2}}}}$$

$$\left( \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \right) \left( -i (3a^2Ab - Ab^3 + a^3B - 3ab^2B) \right)$$

$$\text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a+\text{i}b)^3 (A+\text{i}B)$$

$$\text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] -$$

$$(a-\text{i}b)^3 (A-\text{i}B) \text{EllipticPi}\left[\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right],$$

$$\left.\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\text{Sec}[c+dx]} \sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]} -$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} (a \cos[c+dx] + b \sin[c+dx])^{3/2}}} 2 \cos\left[\frac{1}{2}(c+dx)\right]^2$$

$$\sqrt{\frac{b+\sqrt{a^2+b^2} + a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot[c+dx]}$$

$$\left(-\text{i}(3a^2Ab - Ab^3 + a^3B - 3a^2B) \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right],$$

$$\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a+\text{i}b)^3 (A+\text{i}B) \text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a},$$

$$\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-\text{i}b)^3 (A-\text{i}B)$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \csc [c + d x]^2 \\
 & \left( -i \left( 3 a^2 A b - A b^3 + a^3 B - 3 a b^2 B \right) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^3 (A + i B) \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^3 (A - i B) \right) \\
 & \left( \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} \\
 & 4 \cos \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\text{Cot}[c+dx]} \left( -i (3a^2Ab - Ab^3 + a^3B - 3ab^2B) \right. \\
 & \quad \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+ib)^3 (A+iB) \\
 & \quad \text{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \\
 & \quad (a-ib)^3 (A-ib) \text{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \\
 & \quad \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \left. \sqrt{\text{Sec}[c+dx]} \text{Sin} \left[ \frac{1}{2} (c+dx) \right] \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} + \right. \\
 & \quad \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}} 2 \text{Cos} \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \quad \sqrt{\frac{b+\sqrt{a^2+b^2} + a \text{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \left. \sqrt{\text{Cot}[c+dx]} \left( -i (3a^2Ab - Ab^3 + a^3B - 3ab^2B) \right) \right. \\
 & \quad \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+ib)^3 (A+iB)
 \end{aligned}$$

$$\text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a - ib)^3 (A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right.$$

$$\left.\frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx] \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} 4 \text{Cos}\left[\frac{1}{2}(c + dx)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\text{Cot}[c + dx]}$$

$$\sqrt{\text{Sec}[c + dx]} \left( - \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (3a^2A - Ab^3 + a^3B - 3ab^2B) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) /$$

$$\left( 4 \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) -$$

$$\left( i(a + ib)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + iB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \text{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right)$$

$$\sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\left( i(a - ib)^3 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - iB) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) /$$



$$\left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\ \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right)$$

**Problem 631: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^{5/2} (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 300 leaves, 15 steps):

$$-\frac{1}{d} (i a - b)^{5/2} (i A - B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} + \\ \frac{2 b^{5/2} B \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]}}{d} - \frac{1}{d} \\ (i a + b)^{5/2} (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}} \right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} - \\ \frac{2 a (2 A b + a B) \sqrt{\cot [c + d x]} \sqrt{a + b \tan [c + d x]}}{d} - \frac{2 a A \cot [c + d x]^{3/2} (a + b \tan [c + d x])^{3/2}}{3 d}$$

Result (type 4, 97068 leaves): Display of huge result suppressed!

**Problem 632: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cot [c + d x]^{3/2} (a + b \tan [c + d x])^{5/2} (A + B \tan [c + d x]) dx$$

Optimal (type 3, 301 leaves, 15 steps):

$$\frac{1}{d} (i a - b)^{5/2} (A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} +$$

$$\frac{1}{d} b^{3/2} (2 A b + 5 a B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} - \frac{1}{d}$$

$$(i a + b)^{5/2} (A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} +$$

$$\frac{b (2 a A + b B) \sqrt{a + b \tan[c + d x]}}{d \sqrt{\cot[c + d x]}} - \frac{2 a A \sqrt{\cot[c + d x]} (a + b \tan[c + d x])^{3/2}}{d}$$

Result (type 4, 105692 leaves): Display of huge result suppressed!

**Problem 633: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cot[c + d x]} (a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x]) dx$$

Optimal (type 3, 320 leaves, 15 steps):

$$\frac{1}{d} (i a - b)^{5/2} (i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} + \frac{1}{4 d}$$

$$\sqrt{b} (20 a A b + 15 a^2 B - 8 b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} +$$

$$\frac{1}{d} (i a + b)^{5/2} (i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]} +$$

$$\frac{b (4 A b + 7 a B) \sqrt{a + b \tan[c + d x]}}{4 d \sqrt{\cot[c + d x]}} + \frac{b B (a + b \tan[c + d x])^{3/2}}{2 d \sqrt{\cot[c + d x]}}$$

Result (type 4, 114434 leaves): Display of huge result suppressed!

**Problem 634: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \tan[c + d x])^{5/2} (A + B \tan[c + d x])}{\sqrt{\cot[c + d x]}} dx$$

Optimal (type 3, 376 leaves, 16 steps):

$$\begin{aligned}
 & -\frac{1}{d} (\sqrt{a-b})^{5/2} (A + \sqrt{a-b} B) \operatorname{ArcTan}\left[\frac{\sqrt{a-b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \frac{1}{8 \sqrt{b} d} \\
 & (30 a^2 A b - 16 A b^3 + 5 a^3 B - 40 a b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \\
 & \frac{1}{d} (\sqrt{a+b})^{5/2} (A - \sqrt{a+b} B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \\
 & \frac{(14 a A b + 5 a^2 B - 8 b^2 B) \sqrt{a+b \tan[c+dx]}}{8 d \sqrt{\cot[c+dx]}} + \\
 & \frac{b B (a+b \tan[c+dx])^{3/2}}{3 d \cot[c+dx]^{3/2}} + \frac{(2 A b + 3 a B) (a+b \tan[c+dx])^{3/2}}{4 d \sqrt{\cot[c+dx]}}
 \end{aligned}$$

Result (type 4, 123 145 leaves): Display of huge result suppressed!

**Problem 635: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a+b \tan[c+dx])^{5/2} (A+B \tan[c+dx])}{\cot[c+dx]^{3/2}} dx$$

Optimal (type 3, 457 leaves, 17 steps):

$$\begin{aligned}
 & -\frac{1}{d} (\sqrt{a-b})^{5/2} (\sqrt{a-b} A - B) \operatorname{ArcTan}\left[\frac{\sqrt{a-b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \\
 & \frac{1}{64 b^{3/2} d} (40 a^3 A b - 320 a A b^3 - 5 a^4 B - 240 a^2 b^2 B + 128 b^4 B) \\
 & \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} - \frac{1}{d} \\
 & (\sqrt{a+b})^{5/2} (\sqrt{a+b} A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]} + \\
 & \frac{(40 a^2 A b - 64 A b^3 - 5 a^3 B - 112 a b^2 B) \sqrt{a+b \tan[c+dx]}}{64 b d \sqrt{\cot[c+dx]}} + \\
 & \frac{(40 a A b - 5 a^2 B - 48 b^2 B) (a+b \tan[c+dx])^{3/2}}{96 b d \sqrt{\cot[c+dx]}} + \\
 & \frac{(8 A b - a B) (a+b \tan[c+dx])^{5/2}}{24 b d \sqrt{\cot[c+dx]}} + \frac{B (a+b \tan[c+dx])^{7/2}}{4 b d \sqrt{\cot[c+dx]}}
 \end{aligned}$$

Result (type 4, 136 892 leaves): Display of huge result suppressed!

Problem 636: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + dx]^{7/2} (A + B \text{Tan}[c + dx])}{\sqrt{a + b \text{Tan}[c + dx]}} dx$$

Optimal (type 3, 296 leaves, 11 steps):

$$\frac{(i A - B) \text{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a + b \text{Tan}[c + dx]}}\right] \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Tan}[c + dx]}}{\sqrt{i a - b} d} -$$

$$\frac{(i A + B) \text{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\text{Tan}[c + dx]}}{\sqrt{a + b \text{Tan}[c + dx]}}\right] \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Tan}[c + dx]}}{\sqrt{i a + b} d} +$$

$$\frac{2 (15 a^2 A - 8 A b^2 + 10 a b B) \sqrt{\text{Cot}[c + dx]} \sqrt{a + b \text{Tan}[c + dx]}}{15 a^3 d} +$$

$$\frac{2 (4 A b - 5 a B) \text{Cot}[c + dx]^{3/2} \sqrt{a + b \text{Tan}[c + dx]}}{15 a^2 d} - \frac{2 A \text{Cot}[c + dx]^{5/2} \sqrt{a + b \text{Tan}[c + dx]}}{5 a d}$$

Result (type 4, 4516 leaves):

$$\left( (B + A \text{Cot}[c + dx]) \right.$$

$$\left( \frac{4 (9 a^2 A - 4 A b^2 + 5 a b B)}{15 a^3} - \frac{2 (-4 A b \text{Cos}[c + dx] + 5 a B \text{Cos}[c + dx]) \text{Csc}[c + dx]}{15 a^2} - \right.$$

$$\left. \frac{2 A \text{Csc}[c + dx]^2}{5 a} \right) (a \text{Cos}[c + dx] + b \text{Sin}[c + dx]) \Big/$$

$$\left( d \sqrt{\text{Cot}[c + dx]} (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \sqrt{a + b \text{Tan}[c + dx]} \right) -$$

$$\left( 4 \text{Cos}\left[\frac{1}{2} (c + dx)\right]^2 \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2} (c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2} (c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right.$$

$$(B + A \text{Cot}[c + dx]) \left( i B \text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(A + i B) \text{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] +$$

$$\left( (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\left( - \frac{B \sqrt{\operatorname{Cot} [c + d x]}}{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \frac{A \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{\sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} /$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d \sqrt{\operatorname{Cot} [c + d x]} (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right)$$

$$\left( a \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \right)$$

$$\left( i B \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\begin{aligned}
 & \left. \sqrt{\sec [c+d x]} \right) / \left( \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \right) + \\
 & \left( a \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \right. \\
 & \left. \left( i B \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (A+i B) \operatorname{EllipticPi}\left[\right. \right. \right. \\
 & \left. \left. \left. -\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (A-i B) \right. \right. \\
 & \left. \left. \left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right) \right) \right) \\
 & \left. \sqrt{\sec [c+d x]} \right) / \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \right) - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \\
 & \left( i B \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \operatorname{EllipticPi}\left[ \right. \right. \\
 & \quad \left. \left. - \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \right. \\
 & \quad \left. \left. \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} + \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^{3/2}} \\
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \\
 & \left( i B \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \operatorname{EllipticPi}\left[ \right. \right. \\
 & \quad \left. \left. - \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\text{Sec} [c + d x]} (b \text{Cos} [c + d x] - a \text{Sin} [c + d x]) \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Cot} [c + d x]} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} 2 \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Csc} [c + d x]^2 \\
 & \left( i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \text{EllipticPi} \left[ \right. \right. \\
 & \quad \left. \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \right. \\
 & \quad \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\text{Sec} [c + d x]} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} \\
 & 4 \text{Cos} \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{\text{Cot} [c + d x]} \left( i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \text{EllipticPi} \left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \\
 & (A - iB) \text{EllipticPi} \left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left[ \sqrt{\text{Sec} [c + dx]} \text{Sin} \left[ \frac{1}{2} (c + dx) \right] \text{Tan} \left[ \frac{1}{2} (c + dx) \right]^{3/2} - \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + dx] + b \text{Sin} [c + dx]}} 2 \text{Cos} \left[ \frac{1}{2} (c + dx) \right]^2 \right. \\
 & \left. \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + dx) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + dx) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Cot} [c + dx]} \right. \\
 & \left. \left( iB \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + iB) \text{EllipticPi} \left[ \right. \right. \\
 & \left. \left. -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - iB) \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \right. \\
 & \left. \text{Sec} [c + dx]^{3/2} \text{Sin} [c + dx] \text{Tan} \left[ \frac{1}{2} (c + dx) \right]^{3/2} - \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + dx] + b \text{Sin} [c + dx]}} 4 \text{Cos} \left[ \frac{1}{2} (c + dx) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \sqrt{\operatorname{Sec}[c + dx]} \left( \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2}{4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2}} + \right. \\
 & \left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) - \right. \\
 & \left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) \\
 & \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \sqrt{a + b \operatorname{Tan}[c + dx]} \right)
 \end{aligned}$$

**Problem 637: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + dx]^{5/2} (A + B \operatorname{Tan}[c + dx])}{\sqrt{a + b \operatorname{Tan}[c + dx]}} dx$$

Optimal (type 3, 243 leaves, 10 steps):

$$\begin{aligned}
 & \frac{(A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]}}{\sqrt{i a - b} d} \\
 & - \frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]}}{\sqrt{i a + b} d} + \\
 & \frac{2(2 A b - 3 a B) \sqrt{\cot[c + d x]} \sqrt{a + b \tan[c + d x]}}{3 a^2 d} - \frac{2 A \cot[c + d x]^{3/2} \sqrt{a + b \tan[c + d x]}}{3 a d}
 \end{aligned}$$

Result (type 4, 4488 leaves):

$$\begin{aligned}
 & \left( (B + A \cot[c + d x]) \left( -\frac{2(-2 A b + 3 a B)}{3 a^2} - \frac{2 A \cot[c + d x]}{3 a} \right) (a \cos[c + d x] + b \sin[c + d x]) \right) / \\
 & \left( d \sqrt{\cot[c + d x]} (A \cos[c + d x] + B \sin[c + d x]) \sqrt{a + b \tan[c + d x]} \right) + \\
 & \left( 4 \cos\left[\frac{1}{2}(c + d x)\right]^2 \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & (B + A \cot[c + d x]) \left( -i A \operatorname{EllipticF}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) + \\
 & i (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) + \\
 & \left. (i A + B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \left( -\frac{A \sqrt{\cot[c + d x]}}{\sqrt{\sec[c + d x]} \sqrt{a \cos[c + d x] + b \sin[c + d x]}} - \right. \\
 & \left. \frac{B \sqrt{\cot[c + d x]} \sqrt{\sec[c + d x]} \sin[c + d x]}{\sqrt{a \cos[c + d x] + b \sin[c + d x]}} \right) \tan\left[\frac{1}{2}(c + d x)\right]^{3/2} /
 \end{aligned}$$

$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d \sqrt{\cot [c + d x]} (A \cos [c + d x] + B \sin [c + d x]) \right.$$

$$\left. - \left( \left( a \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right. \right. \right.$$

$$\left. \left. \left. - i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + i (A + i B) \right. \right. \right.$$

$$\left. \left. \left. \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \right. \right.$$

$$\left. \left. \left. (i A + B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \right) / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \right. \right.$$

$$\left. \left. \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \right) \right) -$$

$$\left( a \sqrt{\frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \left( -i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + i (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \Big] + (i A + B)$$

$$\operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right]$$

$$\sqrt{\sec [c+dx]} \Big/ \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}}} \right)$$

$$\sqrt{a \cos [c+dx] + b \sin [c+dx]} \sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]} \Big]$$

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+dx] + b \sin [c+dx]}} \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}}$$

$$\sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+dx]}$$

$$\left( -i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + i (A + i B) \operatorname{EllipticPi} \left[ \right. \right.$$

$$\left. - \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (i A + B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\begin{aligned}
 & \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} - \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}\left(a \cos [c+d x]+b \sin [c+d x]\right)^{3 / 2}} \\
 & 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\sqrt{\cot [c+d x]} \\
 & \left(-i A \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+i(A+i B) \operatorname{EllipticPi}\left[\right.\right. \\
 & \quad \left.\left.-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+(i A+B) \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \\
 & \sqrt{\sec [c+d x]}\left(b \cos [c+d x]-a \sin [c+d x]\right) \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}- \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}\sqrt{\cot [c+d x]}\sqrt{a \cos [c+d x]+b \sin [c+d x]}} 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\operatorname{Csc}[c+d x]^2 \\
 & \left(-i A \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+i(A+i B) \operatorname{EllipticPi}\left[\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (iA + B) \\
 & \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \\
 & \sqrt{\sec[c + dx]} \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} - \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} \\
 & 4 \cos\left[\frac{1}{2}(c + dx)\right] \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \\
 & \left(-iA \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + i(A + iB) \operatorname{EllipticPi}\left[\right. \right. \\
 & \left. \left. -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (iA + B) \right. \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]\right) \\
 & \sqrt{\sec[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right] \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 2 \cos\left[\frac{1}{2}(c + dx)\right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( -i A \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right]}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + i (A + i B) \operatorname{EllipticPi}\left[\right. \\
 & \quad \left. - \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (i A + B) \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]\right) \\
 & \operatorname{Sec}[c + dx]^{3/2} \operatorname{Sin}[c + dx] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 4 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Sec}[c + dx]} \left( - \left( \left( A \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right] \right)^2 \right) / \right. \\
 & \quad \left. \left( 4 \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right] \right)^2 / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right) \\
 & \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) -
 \end{aligned}$$



$$\left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (i A + B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\ \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \\ \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \sqrt{a + b \operatorname{Tan} [c + d x]} \right)$$

**Problem 638: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot} [c + d x]^{3/2} (A + B \operatorname{Tan} [c + d x])}{\sqrt{a + b \operatorname{Tan} [c + d x]}} dx$$

Optimal (type 3, 199 leaves, 9 steps):

$$\frac{(i A - B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]} + (i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{i a - b} d} - \frac{\sqrt{i a + b} d}{2 A \sqrt{\operatorname{Cot} [c + d x]} \sqrt{a + b \operatorname{Tan} [c + d x]}} \frac{1}{a d}$$

Result (type 4, 4447 leaves):

$$- \left( (2 A (B + A \operatorname{Cot} [c + d x]) (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])) / (a d \sqrt{\operatorname{Cot} [c + d x]} (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \sqrt{a + b \operatorname{Tan} [c + d x]}) \right) + \left( 4 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) (B + A \operatorname{Cot} [c + d x]) \left( i B \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right)$$

$$\begin{aligned}
 & (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \\
 & \left. (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \left( \frac{B \sqrt{\operatorname{Cot}[c + dx]}}{\sqrt{\operatorname{Sec}[c + dx]} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} - \right. \\
 & \left. \frac{A \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{\sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} \right) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \Big/ \\
 & \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d \sqrt{\operatorname{Cot}[c + dx]} (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right. \\
 & \left. - \left( \left( a \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \right) \right. \right. \\
 & \left. \left( i B \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (A + i B) \operatorname{EllipticPi}\left[ \right. \right. \right. \\
 & \left. \left. \left. -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (A - i B) \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right. \\
 & \left. \sqrt{\text{Sec} [c + d x]} \right) / \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) - \left( a \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{\text{Cot} [c + d x]} \left( i \text{B EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec} [c + d x]} \right) / \\
 & \left( (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} \sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}}} \sqrt[3]{\frac{b-\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt[3]{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( i B \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\left(A+i B\right) \operatorname{EllipticPi}\left[\right. \right. \\
 & \quad \left. \left. -\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]+\left(A-i B\right) \right. \\
 & \quad \left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \\
 & \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}-\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}\left(a \cos [c+d x]+b \sin [c+d x]\right)^{3 / 2}}} \\
 & 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt[3]{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( i B \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\left(A+i B\right) \operatorname{EllipticPi}\left[\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (A - iB) \\
 & \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \\
 & \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 2 \cos\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Csc}[c + dx]^2 \\
 & \left( iB \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (A + iB) \operatorname{EllipticPi}\left[ \right. \right. \\
 & \left. \left. -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (A - iB) \right. \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \sqrt{\sec[c + dx]} \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} - \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} \\
 & 4 \cos\left[\frac{1}{2}(c + dx)\right] \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\text{Cot}[c + d x]} \left( i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \right. \\
 & \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \\
 & (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \sqrt{\text{Sec}[c + d x]} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \right. \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}}} 2 \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Cot}[c + d x]} \\
 & \left( i B \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (A + i B) \text{EllipticPi} \left[ \right. \right. \\
 & \left. \left. -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (A - i B) \right. \\
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}[c+dx]^{3/2} \text{Sin}[c+dx] \text{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} \sqrt{a \text{Cos}[c+dx] + b \text{Sin}[c+dx]}}} 4 \text{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{\frac{b - \sqrt{a^2+b^2} + a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2+b^2}}} \sqrt{\text{Cot}[c+dx]} \\
 & \sqrt{\text{Sec}[c+dx]} \left( \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} B \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{4 \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \text{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2}} + \right. \\
 & \left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2+b^2}}} (A + i B) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( 1 - i \text{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2+b^2}}} \text{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) - \right. \\
 & \left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2+b^2}}} (A - i B) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4 \left( 1 + i \text{Cot}\left[\frac{1}{2}(c+dx)\right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2+b^2}}} \text{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \right) \right) \\
 & \left. \text{Tan}\left[\frac{1}{2}(c+dx)\right]^{3/2} \sqrt{a + b \text{Tan}[c+dx]} \right)
 \end{aligned}$$

Problem 639: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\text{Cot}[c + d x]} (A + B \text{Tan}[c + d x])}{\sqrt{a + b \text{Tan}[c + d x]}} dx$$

Optimal (type 3, 163 leaves, 8 steps):

$$\frac{(A + i B) \text{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right] \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Tan}[c + d x]} + (A - i B) \text{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right] \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Tan}[c + d x]}}{\sqrt{i a - b} d + \sqrt{i a + b} d}$$

Result (type 4, 4378 leaves):

$$\begin{aligned} & - \left( \left( 4 \text{Cos}\left[\frac{1}{2}(c + d x)\right] \right)^2 \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Cot}[c + d x]} \right. \\ & \left. \left( -i A \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + i (A + i B) \right. \right. \\ & \left. \left. \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \right. \right. \\ & \left. \left. (i A + B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \right) \\ & \left( \frac{A \sqrt{\text{Cot}[c + d x]}}{\sqrt{\text{Sec}[c + d x]} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} + \frac{B \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{\sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} \text{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} (A + B \text{Tan}[c + d x]) \right) / \end{aligned}$$



$$\left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \cos [c + d x] + B \sin [c + d x]) \right.$$

$$\left( \left( a \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right. \right.$$

$$\left. \left. - i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + i (A + i B) \right. \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] +$$

$$(i A + B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \left/ \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \right. \right.$$

$$\left. \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \right) + \right.$$

$$\left. \left( a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right) \left( -i A \operatorname{EllipticF} \left[ \right. \right.$$

$$\begin{aligned}
 & i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + i(A+iB) \operatorname{EllipticPi}\left[ \right. \\
 & \left. -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (iA+B) \right. \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right) \\
 & \left. \sqrt{\operatorname{Sec}[c+dx]} \right) / \left( (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{\frac{b-\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) - \\
 & \frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}} \sqrt{\frac{b-\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \\
 & \left( -iA \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + i(A+iB) \right. \\
 & \left. \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & (i A + B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^{3/2}} 2 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \\
 & \left( -i A \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + i (A + i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \\
 & (i A + B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} (b \operatorname{Cos} [c + d x] - a \operatorname{Sin} [c + d x]) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} 2 \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Csc}[c + dx]^2 \\
 & \left( -i A \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + i(A + iB) \right. \\
 & \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + \\
 & (iA + B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 4 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] \right. \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( -i A \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + i(A + iB) \right. \\
 & \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] +
 \end{aligned}$$

$$\begin{aligned}
 & (\text{i A} + \text{B}) \text{EllipticPi} \left[ \frac{\text{i} (b + \sqrt{a^2 + b^2})}{a}, \text{i ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\text{Sec} [c + d x]} \text{Sin} \left[ \frac{1}{2} (c + d x) \right] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} 2 \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Cot} [c + d x]} \\
 & \left( -\text{i A EllipticF} \left[ \text{i ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \text{i} (A + \text{i B}) \right. \\
 & \left. \text{EllipticPi} \left[ -\frac{\text{i} (b + \sqrt{a^2 + b^2})}{a}, \text{i ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \\
 & \left. (\text{i A} + \text{B}) \text{EllipticPi} \left[ \frac{\text{i} (b + \sqrt{a^2 + b^2})}{a}, \text{i ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \text{Sec} [c + d x]^{3/2} \text{Sin} [c + d x] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \right. \\
 & \left. \frac{1}{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} 4 \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \right.
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b - \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}} \\
 & \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Sec}[c + dx]} \left( - \left( \left( A \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right. \right. \\
 & \left. \left. \left( 4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) + \right. \\
 & \left. \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) - \right. \\
 & \left. \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (i A + B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right. \right. \\
 & \left. \left. \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \sqrt{a + b \operatorname{Tan}[c + dx]} \right) \right)
 \end{aligned}$$

**Problem 640: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan}[c + dx]}{\sqrt{\operatorname{Cot}[c + dx]} \sqrt{a + b \operatorname{Tan}[c + dx]}} dx$$

Optimal (type 3, 228 leaves, 13 steps):

$$\frac{(\sqrt{-1} A - B) \operatorname{ArcTan}\left[\frac{\sqrt{-1} a - b \sqrt{\tan[c+d x]}}{\sqrt{a+b \tan[c+d x]}}\right] \sqrt{\cot[c+d x]} \sqrt{\tan[c+d x]}}{\sqrt{-1} a - b d} +$$

$$\frac{2 B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c+d x]}}{\sqrt{a+b \tan[c+d x]}}\right] \sqrt{\cot[c+d x]} \sqrt{\tan[c+d x]}}{\sqrt{b} d} -$$

$$\frac{(\sqrt{-1} A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{-1} a + b \sqrt{\tan[c+d x]}}{\sqrt{a+b \tan[c+d x]}}\right] \sqrt{\cot[c+d x]} \sqrt{\tan[c+d x]}}{\sqrt{-1} a + b d}$$

Result (type 4, 6452 leaves):

$$\left( 4 a (B + A \cot[c+d x]) \right.$$

$$\left. \left( \left( B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right) / \right.$$

$$\left. \left( -a+b+\sqrt{a^2+b^2} \right) - \left( (A + \sqrt{-1} B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-\sqrt{-1} a+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right) / \left( -\sqrt{-1} a+b+\sqrt{a^2+b^2} \right) -$$

$$\left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) - \frac{1}{a + b + \sqrt{a^2 + b^2}}$$

$$\left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right)$$

$$(a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]) \left( \frac{B \sqrt{\operatorname{Cot} [c + d x]} \operatorname{Sec} [c + d x]^{3/2}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} - \right.$$

$$\left. \frac{B \operatorname{Cos} [2 (c + d x)] \sqrt{\operatorname{Cot} [c + d x]} \operatorname{Sec} [c + d x]^{3/2}}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \right.$$

$$\left. \frac{A \sqrt{\operatorname{Cot} [c + d x]} \operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [2 (c + d x)]}{2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} \right) \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} /$$

$$\left( \sqrt{a^2 + b^2} d \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2}} \right)$$

$$(A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x])$$



$$\left( \left( a^2 \sqrt{\cot[c+dx]} \left( \left( B \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right. \right. \right.$$

$$\left. \left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( -a+b+\sqrt{a^2+b^2} \right) - \left( A+iB \right) \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-ia+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( -ia+b+\sqrt{a^2+b^2} \right) - \right.$$

$$\left. \left( A \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{ia+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \right.$$

$$\left. \left( ia+b+\sqrt{a^2+b^2} \right) + \left( B \operatorname{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{ia+b+\sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / \left( a-i \left( b+\sqrt{a^2+b^2} \right) \right) -$$

$$\left( \text{B EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\text{Sec} [c + d x]} \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]} /$$

$$\left( \sqrt{a^2 + b^2} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos} [c + d x] + b \text{Sin} [c + d x])}{a^2 + b^2}} \right)$$

$$\sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} + 2 a \sqrt{\text{Cot} [c + d x]}$$

$$\left( \left( \text{B EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$(-a + b + \sqrt{a^2 + b^2}) - \left( (A + i B) \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / (-i a + b + \sqrt{a^2 + b^2}) -$$

$$\left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) + \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) -$$

$$\left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\operatorname{Sec} [c + d x]} (b \operatorname{Cos} [c + d x] - a \operatorname{Sin} [c + d x])$$

$$\left. \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) / \left( \sqrt{a^2 + b^2} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right)$$

$$\sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2}} -$$

$$\frac{1}{\sqrt{a^2 + b^2} \sqrt{\cot [c + d x]} \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 (a \cos [c+d x]+b \sin [c+d x])}{a^2+b^2}}} 2 a \operatorname{Csc}[c+d x]^2$$

$$\left( \left( B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right) / \right.$$

$$\left. \left(-a+b+\sqrt{a^2+b^2}\right) - \left( (A+i B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right) / \left(-i a+b+\sqrt{a^2+b^2}\right) - \right.$$

$$\left. \left( A \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right) / \right.$$

$$\left. \left( i a+b+\sqrt{a^2+b^2}\right) + \left( B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] \right) / \right.$$

$$\begin{aligned}
 & \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) - \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right) \\
 & \frac{\sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} +}{\sqrt{a^2 + b^2} \sqrt{\frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2}}} - 2 a \sqrt{\operatorname{Cot} [c + d x]} \\
 & \left( \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right. \\
 & \left. \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( (A + i B) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \right. \\
 & \left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) -
 \end{aligned}$$

$$\left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) + \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) -$$

$$\left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) \operatorname{Sec} [c + d x]^{3/2}$$

$$\frac{\operatorname{Sin} [c + d x] \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}}{\sqrt{a^2 + b^2} \left( \frac{a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{a^2 + b^2} \right)^{3/2}} - \frac{2 a \sqrt{\operatorname{Cot} [c + d x]}}{1}$$

$$\left( \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \right) /$$

$$\left( -a + b + \sqrt{a^2 + b^2} \right) - \left( (A + i B) \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( A \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( i a + b + \sqrt{a^2 + b^2} \right) + \left( B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a - i \left( b + \sqrt{a^2 + b^2} \right) \right) -$$

$$\left( \text{B EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) /$$

$$\left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\text{Sec}[c + d x]} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}$$

$$\sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( \frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (b \text{Cos}[c + d x] - a \text{Sin}[c + d x])}{a^2 + b^2} + \right.$$

$$\left. \frac{1}{a^2 + b^2} a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right] \right) +$$

$$\frac{1}{\sqrt{a^2 + b^2} \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])}{a^2 + b^2}}} 4 a \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Sec}[c + d x]}$$

$$\sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( - \left( a \text{B Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (-a + b + \sqrt{a^2 + b^2}) \right) \right.$$

$$\left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{2 \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{-a + b + \sqrt{a^2 + b^2}} \right) \right) \right) +$$

$$\left( a (A + i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (-i a + b + \sqrt{a^2 + b^2}) \right)$$



$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{-i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(a A \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4\sqrt{2}\sqrt{a^2 + b^2}\left(i a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) - \\
 & \left(a B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4\sqrt{2}\sqrt{a^2 + b^2}\left(a - i\left(b + \sqrt{a^2 + b^2}\right)\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) \Bigg) + \\
 & \left(a B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4\sqrt{2}\sqrt{a^2 + b^2}\left(a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left( \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{a + b + \sqrt{a^2 + b^2}} \right) \right) \left( \sqrt{a + b \operatorname{Tan} [c + d x]} \right)$$

**Problem 641:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Tan} [c + d x]}{\operatorname{Cot} [c + d x]^{3/2} \sqrt{a + b \operatorname{Tan} [c + d x]}} dx$$

Optimal (type 3, 266 leaves, 14 steps):

$$\begin{aligned} & \frac{(A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{i a - b} d} + \\ & \frac{(2 A b - a B) \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{b^{3/2} d} - \\ & \frac{(A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{i a + b} d} + \frac{B \sqrt{a + b \operatorname{Tan} [c + d x]}}{b d \sqrt{\operatorname{Cot} [c + d x]}} \end{aligned}$$

Result (type 4, 11682 leaves):

$$\begin{aligned} & \frac{B (B + A \operatorname{Cot} [c + d x]) (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])}{b d \operatorname{Cot} [c + d x]^{3/2} (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \sqrt{a + b \operatorname{Tan} [c + d x]}} - \\ & \left( \sqrt{2} \sqrt{a^2 + b^2} (B + A \operatorname{Cot} [c + d x]) \right) \\ & \left( -B \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) + \end{aligned}$$

$$\left( (2 A b - a B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / (-a + b + \sqrt{a^2 + b^2}) - \left( 2 i A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / (-i a + b + \sqrt{a^2 + b^2}) + \left( 2 b B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / (-i a + b + \sqrt{a^2 + b^2}) + \left( 2 i A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / (i a + b + \sqrt{a^2 + b^2}) + \left( 2 b B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / (i a + b + \sqrt{a^2 + b^2})$$

$$\begin{aligned}
 & \left( i a + b + \sqrt{a^2 + b^2} \right) - \\
 & \left( 2 A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( a + b + \sqrt{a^2 + b^2} \right) + \\
 & \left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( a + b + \sqrt{a^2 + b^2} \right) \\
 & \sqrt{\operatorname{Sec}[c + d x] \operatorname{Sin}[c + d x] \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} \\
 & \left( \frac{A \sqrt{\operatorname{Cot}[c + d x]} \operatorname{Sec}[c + d x]^{3/2}}{2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \frac{a B \sqrt{\operatorname{Cot}[c + d x]} \operatorname{Sec}[c + d x]^{3/2}}{2 b \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \right. \\
 & \frac{A \operatorname{Cos}[2(c + d x)] \sqrt{\operatorname{Cot}[c + d x]} \operatorname{Sec}[c + d x]^{3/2}}{2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} - \\
 & \left. \frac{B \sqrt{\operatorname{Cot}[c + d x]} \operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[2(c + d x)]}{2 \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} \right) \\
 & \sqrt{\operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{\frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}} \\
 & \sqrt{\frac{a \left( a + 2 b \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)^2}{a^2 + b^2}}
 \end{aligned}$$

$$\sqrt{\frac{a + 2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \Bigg/$$

$$\left( b d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) \left( -2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right) \right)$$

$$\left( \frac{1}{b \left( -2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right)^2} \right)$$

$$\sqrt{2} \sqrt{a^2 + b^2} \left( -B \operatorname{EllipticF}\left[ \operatorname{ArcSin}\left[ \frac{\sqrt{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] + \right)$$

$$\left( (2 A b - a B) \operatorname{EllipticPi}\left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[ \frac{\sqrt{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}}{\sqrt{a^2 + b^2}} \right] \right], \right)$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Bigg/ \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( 2 i A b \operatorname{EllipticPi}\left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right)$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( -i a + b + \sqrt{a^2+b^2} \right) + \right.$$

$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-i a + b + \sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( -i a + b + \sqrt{a^2+b^2} \right) + 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) + \right.$$

$$\left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \Bigg/ \left( i a + b + \sqrt{a^2+b^2} \right) - 2 A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( a+b+\sqrt{a^2+b^2} \right) +$$

$$\left( a B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \right/$$

$$\left( a+b+\sqrt{a^2+b^2} \right) \sqrt{\text{Cot} \left[ \frac{1}{2}(c+dx) \right] - \text{Tan} \left[ \frac{1}{2}(c+dx) \right]}$$

$$\sqrt{\frac{a \text{Tan} \left[ \frac{1}{2}(c+dx) \right]}{b+\sqrt{a^2+b^2}} \left( -b \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 + a \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \text{Tan} \left[ \frac{1}{2}(c+dx) \right] \right)}$$

$$\sqrt{\frac{1+\text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{1-\text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}} \sqrt{\frac{a \left( a+2b \text{Tan} \left[ \frac{1}{2}(c+dx) \right] - a \text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right)}{a^2+b^2}}$$

$$\sqrt{\frac{a+2b \text{Tan} \left[ \frac{1}{2}(c+dx) \right] - a \text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{1+\text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}} -$$

$$\left( a \left( -B \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) + \right.$$

$$\left( (2Ab - aB) \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \right] \right),$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( 2 i A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 i A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$



$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) - \left( 2 A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\text{Cot} \left[ \frac{1}{2} (c + d x) \right] - \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}$$

$$\sqrt{\frac{a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \left( b \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 - a \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \text{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)$$

$$\left. \sqrt{\frac{1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}} \sqrt{\frac{a + 2 b \text{Tan} \left[ \frac{1}{2} (c + d x) \right] - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}} \right) /$$

$$\left( \sqrt{2} b \sqrt{a^2 + b^2} \sqrt{\frac{a \left( a + 2 b \text{Tan} \left[ \frac{1}{2} (c + d x) \right] - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right)}{a^2 + b^2}} \right)$$

$$\left( -2 b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \right) \right) -$$

$$\left( a \sqrt{a^2+b^2} \left( -B \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}}\right] + \right.$$

$$\left. \left( (2 A b - a B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / (-a+b+\sqrt{a^2+b^2}) - \left( 2 i A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right.$$

$$\left. \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / (-i a+b+\sqrt{a^2+b^2}) +$$

$$\left( 2 b B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}}\right], \right.$$

$$\left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) / (-i a+b+\sqrt{a^2+b^2}) + \left( 2 i A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2+b^2}}{i a+b+\sqrt{a^2+b^2}}, \right.$$

$$\begin{aligned}
 & \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( i a + b + \sqrt{a^2+b^2} \right) + \\
 & \left( 2 b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right. \\
 & \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( i a + b + \sqrt{a^2+b^2} \right) - \left( 2 A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) \right/ \left( a + b + \sqrt{a^2+b^2} \right) + a B \\
 & \left. \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \right/ \\
 & \left( a + b + \sqrt{a^2+b^2} \right) \right) \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \sqrt{\text{Cot} \left[ \frac{1}{2}(c+dx) \right] - \text{Tan} \left[ \frac{1}{2}(c+dx) \right]} \\
 & \sqrt{\frac{1 + \text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}{1 - \text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2}} \sqrt{\frac{a \left( a + 2 b \text{Tan} \left[ \frac{1}{2}(c+dx) \right] - a \text{Tan} \left[ \frac{1}{2}(c+dx) \right]^2 \right)}{a^2 + b^2}}
 \end{aligned}$$

$$\left( \sqrt{\frac{a + 2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2}} \right) / \left( 2 \sqrt{2} b \left( b + \sqrt{a^2 + b^2} \right) \right.$$

$$\left. \sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}} \left( -2 b \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right] + a \left( -1 + \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^2 \right) \right)} \right) -$$

$$\left( \sqrt{a^2 + b^2} \left( -B \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] + \right. \right.$$

$$\left. \left( (2 A b - a B) \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / \left( -a + b + \sqrt{a^2 + b^2} \right) - \right.$$

$$\left. \left( 2 i A b \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 b B \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( -i a + b + \sqrt{a^2+b^2} \right) +$$

$$\left( 2 i A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( i a + b + \sqrt{a^2+b^2} \right) + \left( 2 b B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{i a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right] \right/ \left( i a + b + \sqrt{a^2+b^2} \right) -$$

$$\left( 2 A b \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( a + b + \sqrt{a^2+b^2} \right) + \left( a B \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{a + b + \sqrt{a^2+b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right/ \left( a+b+\sqrt{a^2+b^2} \right)$$

$$\left( -\frac{1}{2} \text{Csc} \left[ \frac{1}{2}(c+dx) \right]^2 - \frac{1}{2} \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \right) \sqrt{\frac{a \tan\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}$$

$$\sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a\left(a+2b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2\right)}{a^2+b^2}}$$

$$\left. \sqrt{\frac{a+2b \tan\left[\frac{1}{2}(c+dx)\right]-a \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right/$$

$$\left( \sqrt{2} b \sqrt{\text{Cot} \left[ \frac{1}{2}(c+dx) \right] - \tan \left[ \frac{1}{2}(c+dx) \right]} \right.$$

$$\left. \left( -2b \tan \left[ \frac{1}{2}(c+dx) \right] + a \left( -1 + \tan \left[ \frac{1}{2}(c+dx) \right]^2 \right) \right) \right) -$$

$$\left( \sqrt{a^2+b^2} \left( -B \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] \right) + \right.$$

$$\left( (2Ab - aB) \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right] \right), \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -a + b + \sqrt{a^2 + b^2} \right) - \left( 2 i A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( -i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 i A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 b B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) - \left( 2 A b \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( a B \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right.$$

$$\left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + b + \sqrt{a^2 + b^2} \right) \sqrt{\text{Cot} \left[ \frac{1}{2} (c + d x) \right] - \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}$$

$$\sqrt{\frac{a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \left( a + 2 b \text{Tan} \left[ \frac{1}{2} (c + d x) \right] - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)^2}{a^2 + b^2}}$$

$$\sqrt{\frac{a + 2 b \text{Tan} \left[ \frac{1}{2} (c + d x) \right] - a \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}}$$

$$\left( \frac{\text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \text{Tan} \left[ \frac{1}{2} (c + d x) \right]}{1 - \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2} + \left( \text{Sec} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \text{Tan} \left[ \frac{1}{2} (c + d x) \right] \right.$$

$$\left. \left. \left( 1 + \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) / \left( 1 - \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) /$$



$$\left( \sqrt{2} b \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \left( -2b \tan\left[\frac{1}{2}(c+dx)\right] + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) -$$

$$\left( \sqrt{a^2 + b^2} \left( -B \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] + \right.$$

$$\left. \left( 2Ab - aB \right) \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / \left( -a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( 2iAb \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-ia + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / \left( -ia + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2bB \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2 + b^2}}{-ia + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / \left( -ia + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2\sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}}\right] \right) / \left( -ia + b + \sqrt{a^2 + b^2} \right) +$$

$$\left( 2 i A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) + \left( 2 b B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( i a + b + \sqrt{a^2 + b^2} \right) -$$

$$\left( 2 A b \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right.$$

$$\left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( a + b + \sqrt{a^2 + b^2} \right) + \left( a B \operatorname{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right.$$

$$\left. \left. \operatorname{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \Big/ \left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\sqrt{\operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \sqrt{\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{1 + \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^2}}$$

$$\begin{aligned}
 & \sqrt{\frac{a \left( a + 2 b \tan \left[ \frac{1}{2} (c + d x) \right] - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)}{a^2 + b^2}} \\
 & \left( \frac{b \sec \left[ \frac{1}{2} (c + d x) \right]^2 - a \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2} - \right. \\
 & \left. \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \left( a + 2 b \tan \left[ \frac{1}{2} (c + d x) \right] - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) / \\
 & \left. \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) / \\
 & \left( \sqrt{2} b \sqrt{\frac{a + 2 b \tan \left[ \frac{1}{2} (c + d x) \right] - a \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
 & \left. \left( -2 b \tan \left[ \frac{1}{2} (c + d x) \right] + a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) \right) - \\
 & \frac{1}{b \left( -2 b \tan \left[ \frac{1}{2} (c + d x) \right] + a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right)} \\
 & \sqrt{2} \sqrt{a^2 + b^2} \sqrt{\cot \left[ \frac{1}{2} (c + d x) \right] - \tan \left[ \frac{1}{2} (c + d x) \right]} \\
 & \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \\
 & \sqrt{\frac{a \left( a + 2 b \tan \left[ \frac{1}{2} (c + d x) \right] - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)}{a^2 + b^2}} \\
 & \sqrt{\frac{a + 2 b \tan \left[ \frac{1}{2} (c + d x) \right] - a \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \\
 & \left( a B \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{2\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \right) - \\
& \left( a(2Ab - aB) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 4\sqrt{2}\sqrt{a^2 + b^2}(-a + b + \sqrt{a^2 + b^2}) \right) \\
& \left( \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{2\sqrt{a^2 + b^2}}} \right) \\
& \left( \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{-a + b + \sqrt{a^2 + b^2}} \right) \right) + \\
& \left( i a A B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 2\sqrt{2}\sqrt{a^2 + b^2}(-i a + b + \sqrt{a^2 + b^2}) \right) \\
& \left( \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{2\sqrt{a^2 + b^2}}} \right) \\
& \left( \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{-i a + b + \sqrt{a^2 + b^2}} \right) \right) - \\
& \left( a b B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 2\sqrt{2}\sqrt{a^2 + b^2}(-i a + b + \sqrt{a^2 + b^2}) \right) \\
& \left( \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{2\sqrt{a^2 + b^2}}} \right) \\
& \left( \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c+dx)\right]}{-i a + b + \sqrt{a^2 + b^2}} \right) \right) - \\
& \left( i a A B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 2\sqrt{2}\sqrt{a^2 + b^2}(i a + b + \sqrt{a^2 + b^2}) \right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) - \\
 & \left(a b B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(2\sqrt{2}\sqrt{a^2 + b^2} \left(i a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{i a + b + \sqrt{a^2 + b^2}}\right) + \\
 & \left(a A b \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(2\sqrt{2}\sqrt{a^2 + b^2} \left(a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left(1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}}\right) - \\
 & \left(a^2 B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2\right) / \left(4\sqrt{2}\sqrt{a^2 + b^2} \left(a + b + \sqrt{a^2 + b^2}\right)\right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2\sqrt{a^2 + b^2}}} \\
 & \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\left( \left( \left( \left( \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{a + b + \sqrt{a^2 + b^2}} \right) \right) \right) \right) \right) \sqrt{a + b \operatorname{Tan}[c + dx]} \right)$$

**Problem 642: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + dx]^{5/2} (A + B \operatorname{Tan}[c + dx])}{(a + b \operatorname{Tan}[c + dx])^{3/2}} dx$$

Optimal (type 3, 316 leaves, 11 steps):

$$\begin{aligned} & \frac{(\operatorname{I} A - B) \operatorname{ArcTan}\left[\frac{\sqrt{\operatorname{I} a - b} \sqrt{\operatorname{Tan}[c + dx]}}{\sqrt{a + b \operatorname{Tan}[c + dx]}}\right] \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]}}{(\operatorname{I} a - b)^{3/2} d} - \\ & \frac{(\operatorname{I} A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{\operatorname{I} a + b} \sqrt{\operatorname{Tan}[c + dx]}}{\sqrt{a + b \operatorname{Tan}[c + dx]}}\right] \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Tan}[c + dx]}}{(\operatorname{I} a + b)^{3/2} d} + \\ & \frac{2 b (5 a^2 A b + 8 A b^3 - 3 a^3 B - 6 a b^2 B)}{3 a^3 (a^2 + b^2) d \sqrt{\operatorname{Cot}[c + dx]} \sqrt{a + b \operatorname{Tan}[c + dx]}} + \\ & \frac{2 (4 A b - 3 a B) \sqrt{\operatorname{Cot}[c + dx]}}{3 a^2 d \sqrt{a + b \operatorname{Tan}[c + dx]}} - \frac{2 A \operatorname{Cot}[c + dx]^{3/2}}{3 a d \sqrt{a + b \operatorname{Tan}[c + dx]}} \end{aligned}$$

Result (type 4, 4988 leaves):

$$\begin{aligned} & \left( \sqrt{\operatorname{Cot}[c + dx]} \operatorname{Sec}[c + dx] (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])^2 \right. \\ & \left( -\frac{2(-5 A b + 3 a B)}{3 a^3} - \frac{2 A \operatorname{Cot}[c + dx]}{3 a^2} - \frac{2(-A b^4 \operatorname{Sin}[c + dx] + a b^3 B \operatorname{Sin}[c + dx])}{a^3 (a - \operatorname{I} b) (a + \operatorname{I} b) (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])} \right) \\ & \left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) (a + b \operatorname{Tan}[c + dx])^{3/2} \right) - \\ & \left( 4 \operatorname{I} \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \right) \end{aligned}$$

$$\left( (aA + bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - ib) (A + ib) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + ib)$$

$$\left. (A - ib) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\operatorname{Sec}[c + dx] (a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx])$$

$$\left( - \left( (aA \sqrt{\operatorname{Cot}[c + dx]}) / \left( (a - ib) (a + ib) \sqrt{\operatorname{Sec}[c + dx]} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \right) \right) - \right.$$

$$\left( bB \sqrt{\operatorname{Cot}[c + dx]} \right) / \left( (a - ib) (a + ib) \sqrt{\operatorname{Sec}[c + dx]} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \right) +$$

$$\frac{aB \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{(a - ib) (a + ib) \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} -$$

$$\left. \frac{aB \sqrt{\operatorname{Cot}[c + dx]} \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{(a - ib) (a + ib) \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} \right) \operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]^{3/2}$$

$$\left. (A + B \operatorname{Tan}[c + dx]) \right) / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \operatorname{Cos}[c + dx] + B \operatorname{Sin}[c + dx]) \right)$$

$$\left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + dx) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \right)$$

$$\left( (aA + bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$\begin{aligned}
 & (a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\operatorname{Sec}[c + d x]} \Big/ \\
 & \left( (a^2 + b^2) (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]} \sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]} \right) + \left( i a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{\operatorname{Cot}[c + d x]} \left( (a A + b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \\
 & \left. (a - i b) (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b) (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \sqrt{\operatorname{Sec}[c + d x]} \Big/ \\
 & \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \right) - \\
 & \frac{1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \\
 & 3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( (a A+B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-(a-i b)(A+i B) \right. \\
 & \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- \\
 & \left. (a+i b)(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} + \\
 & \frac{1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \cos [c+d x]+b \sin [c+d x])^{3 / 2}} 2 i \cos \left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( (a A+B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-(a-i b)(A+i B) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \\
 & (a + ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \sqrt{\sec[c + dx]} (b \cos[c + dx] - a \sin[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + \right. \\
 & \left. \left(1 / \left((a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]}\right)\right) \right. \\
 & \left. 2i \cos\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}}\right. \right. \\
 & \left. \left. \csc[c + dx]^2 \left( (aA + bB) \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \right. \right. \\
 & \left. \left. (a - ib)(A + iB) \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + ib)(A - iB) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \sqrt{\sec[c + dx]} \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 4i \cos\left[\frac{1}{2}(c + dx)\right]
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( (aA + bB) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - ib)(A + iB) \right. \\
 & \quad \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \\
 & \quad (a + ib)(A - iB) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \quad \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \left. \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} - \right. \\
 & \quad \left. \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 2i \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \right) \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( (aA + bB) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - ib)(A + iB) \right. \\
 & \quad \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \operatorname{Sec} [c + d x]^{3/2} \operatorname{Sin} [c + d x] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} 4 i \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \\
 & \sqrt{\operatorname{Sec} [c + d x]} \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a A + b B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) / \right. \\
 & \left. \left( 4 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) + \\
 & \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \\
 & \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a + i b) \\
 & \left. (A - i B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \text{Sec}[c + dx] (a \cos[c + dx] + b \sin[c + dx]) \\
 & \left( - \left( \frac{A b \sqrt{\cot[c + dx]}}{\left( (a - i b) (a + i b) \sqrt{\sec[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \right)} \right) + \right. \\
 & \left. \frac{a B \sqrt{\cot[c + dx]}}{\left( (a - i b) (a + i b) \sqrt{\sec[c + dx]} \sqrt{a \cos[c + dx] + b \sin[c + dx]} \right)} - \right. \\
 & \left. \frac{a A \sqrt{\cot[c + dx]} \sqrt{\sec[c + dx]} \sin[c + dx]}{(a - i b) (a + i b) \sqrt{a \cos[c + dx] + b \sin[c + dx]}} - \right. \\
 & \left. \frac{b B \sqrt{\cot[c + dx]} \sqrt{\sec[c + dx]} \sin[c + dx]}{(a - i b) (a + i b) \sqrt{a \cos[c + dx] + b \sin[c + dx]}} \right) \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} \\
 & \left. (A + B \tan[c + dx]) \right) \left/ \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \cos[c + dx] + B \sin[c + dx]) \right) \right. \\
 & \left. \left( - \left( \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]} \right) - i (A b - a B) \right) \right) \right. \\
 & \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b) (A + i B) \\
 & \text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] +
 \end{aligned}$$

$$\begin{aligned}
 & (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Bigg/ \left( (a^2 + b^2) (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) - \\
 & \left( a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \left( -i (A b - a B) \operatorname{EllipticF} \left[ \right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A + i B) \right. \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + \right. \right. \\
 & \left. \left. (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \right. \\
 & \left. \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sqrt{\operatorname{Sec} [c + d x]} \Bigg/ \\
 & \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \right) + \\
 & \frac{1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \\
 & 3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( -i(A b-a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & (a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a+i b)(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} - \\
 & \frac{1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \cos [c+d x]+b \sin [c+d x])^{3 / 2}} 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( -i(A b-a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & (a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right.
 \end{aligned}$$



$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a+i b) (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \sqrt{\operatorname{Sec} [c+d x]} (b \operatorname{Cos} [c+d x] - a \operatorname{Sin} [c+d x]) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \left( \frac{1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+d x]} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} \right) \\
 & 2 \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
 & \operatorname{Csc} [c+d x]^2 \left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+d x]} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \frac{1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} 4 \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+d x]}
 \end{aligned}$$

$$\begin{aligned}
& \left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
& (a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
& \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b) (A-i B) \right. \\
& \left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \\
& \frac{\sqrt{\operatorname{Sec} [c+d x]} \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} + 1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} \\
& 2 \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \\
& \sqrt{\operatorname{Cot} [c+d x]} \left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
& (a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
& \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b) (A-i B) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \frac{\text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x] \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + 1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]}} \\
 & 4 \text{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \\
 & \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Sec}[c + d x]} \left( - \left( \left( \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A b - a B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right. \right. \\
 & \left. \left. \left( 4 \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) + \right. \\
 & \left. \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \right. \\
 & \left. \left. \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) - \right. \\
 & \left. \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right. \\
 & \left. \left( 4 \left( 1 + i \text{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\frac{a \text{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \right. \\
 & \left. \left. \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) \text{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} (a + b \text{Tan}[c + d x])^{3/2}
 \end{aligned}$$

Problem 644: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\cot [c+d x]} (A+B \tan [c+d x])}{(a+b \tan [c+d x])^{3/2}} dx$$

Optimal (type 3, 215 leaves, 9 steps):

$$\frac{(i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}}{(i a - b)^{3/2} d} +$$

$$\frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}}\right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]}}{(i a + b)^{3/2} d} +$$

$$\frac{2 b (A b - a B)}{a (a^2 + b^2) d \sqrt{\cot [c+d x]} \sqrt{a+b \tan [c+d x]}}$$

Result (type 4, 4931 leaves):

$$- \left( \left( 2 \sqrt{\cot [c+d x]} \operatorname{Sec}[c+d x] (a \cos [c+d x] + b \sin [c+d x]) \right. \right.$$

$$\left. \left. (-A b^2 \sin [c+d x] + a b B \sin [c+d x]) (A+B \tan [c+d x]) \right) / \right.$$

$$\left. (a (a - i b) (a + i b) d (A \cos [c+d x] + B \sin [c+d x]) (a+b \tan [c+d x])^{3/2} \right) +$$

$$\left( 4 i \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c+d x]} \right.$$

$$\left( (a A + b B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A + i B) \right.$$

$$\operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)$$

$$\left. (A - i B) \operatorname{EllipticPi}\left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\operatorname{Sec}[c+d x] (a \cos [c+d x] + b \sin [c+d x])$$

$$\begin{aligned}
 & \left( \left( \frac{a A \sqrt{\cot [c+d x]}}{(a-i b)(a+i b) \sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \right) + \right. \\
 & \left( \frac{b B \sqrt{\cot [c+d x]}}{(a-i b)(a+i b) \sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \right) - \\
 & \frac{A b \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \sin [c+d x]}{(a-i b)(a+i b) \sqrt{a \cos [c+d x]+b \sin [c+d x]}} + \\
 & \left. \frac{a B \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \sin [c+d x]}{(a-i b)(a+i b) \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \right) \\
 & \left. \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} (A+B \tan [c+d x]) \right) / \\
 & \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \cos [c+d x]+B \sin [c+d x]) \right. \\
 & \left. - \left( \left( i a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \right. \right. \right. \\
 & \left. \left( (a A+b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \\
 & \left. \left. (a-i b)(A+i B) \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \right. \\
 & \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)(A-i B) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \right. \right. \\
 & \left. \left. \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+d x]} \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( (a^2 + b^2) \left( b - \sqrt{a^2 + b^2} \right) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]} \right) - \left( i a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{\operatorname{Cot}[c + dx]} \left( (aA + bB) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right. \\
 & \left. \left. (a - i b) (A + i B) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \right. \right. \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec}[c + dx]} \right) / \\
 & \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]} \right) + \\
 & \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} \\
 & 3 i \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]}
 \end{aligned}$$

$$\left( (aA + bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - ib) (A + iB) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] -$$

$$(a + ib) (A - iB) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]} -$$

$$\frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \operatorname{Cos} [c + dx] + b \operatorname{Sin} [c + dx])^{3/2}} 2 i \operatorname{Cos} \left[ \frac{1}{2} (c + dx) \right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + dx) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + dx) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + dx]}$$

$$\left( (aA + bB) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - ib) (A + iB) \right.$$

$$\operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] -$$

$$(a + ib) (A - iB) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} -$$

$$\left( \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} \right)$$

$$2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}$$

$$\operatorname{Csc}[c + d x]^2 \left( (a A + b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] -$$

$$(a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right],$$

$$\frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a},$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right) \sqrt{\sec [c + d x]} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} -$$

$$\frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 4 i \cos \left[ \frac{1}{2} (c + d x) \right]$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]}$$

$$\left( (a A + b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b) (A + i B)$$



$$\text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a + i b) (A - i B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right] \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos[c + dx] + b \sin[c + dx]}} 2 i \cos\left[\frac{1}{2}(c + dx)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + dx]}$$

$$\left( (aA + bB) \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b) (A + i B)$$

$$\text{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] -$$

$$(a + i b) (A - i B) \text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right],$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sec[c + dx]^{3/2} \sin[c + dx] \tan\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\begin{aligned}
& \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}}} 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
& \sqrt{\sec [c + d x]} \left( - \left( \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a A + b B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \right. \right. \\
& \left. \left( 4 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \right) + \\
& \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
& \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) + \\
& \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
& \left( 4 \left( 1 + i \cot \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
& \left. \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left( \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left( a + b \tan [c + d x] \right)^{3/2}
\end{aligned}$$

**Problem 645: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \tan [c + d x]}{\sqrt{\cot [c + d x]} (a + b \tan [c + d x])^{3/2}} dx$$

Optimal (type 3, 210 leaves, 9 steps):

$$\frac{(A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]}}{(i a - b)^{3/2} d} +$$

$$\frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]}}{(i a + b)^{3/2} d} -$$

$$\frac{2 (A b - a B)}{(a^2 + b^2) d \sqrt{\cot[c + d x]} \sqrt{a + b \tan[c + d x]}}$$

Result (type 4, 4928 leaves):

$$\left( 2 \sqrt{\cot[c + d x]} \operatorname{Sec}[c + d x] (a \cos[c + d x] + b \sin[c + d x]) \right. \\ \left. (-A b \sin[c + d x] + a B \sin[c + d x]) (A + B \tan[c + d x]) \right) / \\ \left( (a - i b) (a + i b) d (A \cos[c + d x] + B \sin[c + d x]) (a + b \tan[c + d x])^{3/2} \right) -$$

$$\left( 4 \cos\left[\frac{1}{2}(c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + d x]} \right. \\ \left. - i (A b - a B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b) (A + i B) \right. \\ \left. \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] + (a + i b) \right. \\ \left. (A - i B) \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right)$$

$$\operatorname{Sec}[c + d x] (a \cos[c + d x] + b \sin[c + d x]) \\ \left( (A b \sqrt{\cot[c + d x]}) / \left( (a - i b) (a + i b) \sqrt{\sec[c + d x]} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \right) - \right. \\ \left. (a B \sqrt{\cot[c + d x]}) / \left( (a - i b) (a + i b) \sqrt{\sec[c + d x]} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \right) + \right. \\ \left. \frac{a A \sqrt{\cot[c + d x]} \sqrt{\sec[c + d x]} \sin[c + d x]}{(a - i b) (a + i b) \sqrt{a \cos[c + d x] + b \sin[c + d x]}} + \right.$$

$$\frac{b B \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \sin [c+d x]}{(a-i b)(a+i b) \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \tan \left[ \frac{1}{2}(c+d x) \right]^{3/2}$$

$$(A+B \tan [c+d x]) \left/ \left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \cos [c+d x]+B \sin [c+d x]) \right. \right.$$

$$\left. \left. \left( a \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2}(c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \right. \right. \right.$$

$$\left. \left. \left( -i(A b-a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2}(c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \right. \right.$$

$$\left. \left. (a-i b)(A+i B) \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2}(c+d x) \right]}} \right], \right. \right. \right.$$

$$\left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b)(A-i B) \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right.$$

$$\left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2}(c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\sec [c+d x]} \right/ \left( (a^2+b^2) \right.$$

$$\left. (b-\sqrt{a^2+b^2}) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right.$$

$$\left. \sqrt{\tan \left[ \frac{1}{2}(c+d x) \right]} \right) + \left( a \sqrt{1+\frac{a \cot \left[ \frac{1}{2}(c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \right.$$

$$\left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b) (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+d x]} \Bigg) /$$

$$\left( (a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]} \right) -$$


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$$\frac{1}{(a^2+b^2) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}}$$

$$3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+d x]}$$

$$\left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a-i b) (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right.$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a + i b) (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} + \\
 & \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2}} 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( -i (A b - a B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a - i b) (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b) (A - i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \left( 1 / \left( (a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right) \right) \\
 & 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \text{Csc}[c + dx]^2 \left( -i (Ab - aB) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - ib) (A + iB) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + ib) (A - iB) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \left. \sqrt{\text{Sec}[c + dx]} \text{Tan} \left[ \frac{1}{2} (c + dx) \right]^{3/2} + \right. \\
 & \frac{1}{(a^2 + b^2) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} 4 \text{Cos} \left[ \frac{1}{2} (c + dx) \right] \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot} \left[ \frac{1}{2} (c + dx) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot} \left[ \frac{1}{2} (c + dx) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\text{Cot}[c + dx]} \\
 & \left( -i (Ab - aB) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - ib) (A + iB) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + ib) (A - iB) \\
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan} \left[ \frac{1}{2} (c + dx) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \frac{\sqrt{\sec [c+d x]} \sin \left[\frac{1}{2}(c+d x)\right] \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}-1}{\left(a^2+b^2\right) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \\
 & 2 \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\cot [c+d x]} \left(-i(A b-a B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right)-\right. \\
 & \left.(a-i b)(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right]\right],\right. \\
 & \left.\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right)+\left.(a+i b)(A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a},\right.\right. \\
 & \left.\left.i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \sec [c+d x]^{3 / 2} \sin [c+d x] \\
 & \tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}-\frac{1}{\left(a^2+b^2\right) \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \\
 & 4 \cos \left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \\
 & \sqrt{\cot [c+d x]} \sqrt{\sec [c+d x]} \left(-\left(\left(\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}(A b-a B) \sec \left[\frac{1}{2}(c+d x)\right]\right)^2\right) / \right. \\
 & \left.\left(4 \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}\tan \left[\frac{1}{2}(c+d x)\right]^{3 / 2}\right)\right)+
 \end{aligned}$$



$$\begin{aligned}
 & \left( i (a - i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) - \\
 & \left( i (a + i b) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
 & \left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) (a + b \operatorname{Tan} [c + d x])^{3/2}
 \end{aligned}$$

Problem 646: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Tan} [c + d x]}{\operatorname{Cot} [c + d x]^{3/2} (a + b \operatorname{Tan} [c + d x])^{3/2}} dx$$

Optimal (type 3, 279 leaves, 14 steps):

$$\begin{aligned}
 & \frac{(i A - B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{(i a - b)^{3/2} d} + \\
 & \frac{2 B \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{b^{3/2} d} - \\
 & \frac{(i A + B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{(i a + b)^{3/2} d} + \\
 & \frac{2 a (A b - a B)}{b (a^2 + b^2) d \sqrt{\operatorname{Cot} [c + d x]} \sqrt{a + b \operatorname{Tan} [c + d x]}}
 \end{aligned}$$

Result (type 4, 65204 leaves): Display of huge result suppressed!

Problem 647: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\text{Cot}[c + d x]^{5/2} (A + B \text{Tan}[c + d x])}{(a + b \text{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 399 leaves, 12 steps):

$$\frac{(A + i B) \text{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right] \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Tan}[c + d x]} + (i a - b)^{5/2} d}{(i a + b)^{5/2} d} + \frac{(A - i B) \text{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\text{Tan}[c + d x]}}{\sqrt{a + b \text{Tan}[c + d x]}}\right] \sqrt{\text{Cot}[c + d x]} \sqrt{\text{Tan}[c + d x]} + (i a + b)^{5/2} d}{(i a + b)^{5/2} d} + \frac{2 b (7 a^2 A b + 8 A b^3 - 3 a^3 B - 4 a b^2 B)}{3 a^3 (a^2 + b^2) d \sqrt{\text{Cot}[c + d x]} (a + b \text{Tan}[c + d x])^{3/2}} + \frac{2 (2 A b - a B) \sqrt{\text{Cot}[c + d x]}}{a^2 d (a + b \text{Tan}[c + d x])^{3/2}} - \frac{2 A \text{Cot}[c + d x]^{3/2}}{3 a d (a + b \text{Tan}[c + d x])^{3/2}} + \frac{2 b (8 a^4 A b + 30 a^2 A b^3 + 16 A b^5 - 3 a^5 B - 17 a^3 b^2 B - 8 a b^4 B)}{3 a^4 (a^2 + b^2)^2 d \sqrt{\text{Cot}[c + d x]} \sqrt{a + b \text{Tan}[c + d x]}}$$

Result (type 4, 5403 leaves):

$$\left( \sqrt{\text{Cot}[c + d x]} \text{Sec}[c + d x]^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^3 - \left( - \frac{2 (-8 a^4 A b - 16 a^2 A b^3 - 9 A b^5 + 3 a^5 B + 6 a^3 b^2 B + 4 a b^4 B)}{3 a^4 (a - i b)^2 (a + i b)^2} - \frac{2 A \text{Cot}[c + d x]}{3 a^3} + \frac{2 b^4 (-A b + a B)}{3 a^2 (a - i b)^2 (a + i b)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])^2} - (2 (-15 a^2 A b^4 \text{Sin}[c + d x] - 7 A b^6 \text{Sin}[c + d x] + 12 a^3 b^3 B \text{Sin}[c + d x] + 4 a b^5 B \text{Sin}[c + d x])) / (3 a^4 (a - i b)^2 (a + i b)^2 (a \text{Cos}[c + d x] + b \text{Sin}[c + d x])) \right) / \left( (A + B \text{Tan}[c + d x]) / (d (A \text{Cos}[c + d x] + B \text{Sin}[c + d x]) (a + b \text{Tan}[c + d x])^{5/2}) - \left( 4 i \text{Cos}\left[\frac{1}{2} (c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2} (c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2} (c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\text{Cot}[c + d x]} \right) - \left( (a^2 A - A b^2 + 2 a b B) \text{EllipticF}\left[i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2} (c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right.$$

$$\begin{aligned}
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \quad \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \\
 & \quad \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \operatorname{Sec} [c + d x]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2 \left( - \left( (a^2 A \sqrt{\operatorname{Cot} [c + d x]}) / \right. \right. \\
 & \quad \left( (a - i b)^2 (a + i b)^2 \sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right) \left. \right) + \\
 & \quad \left( (a b^2 \sqrt{\operatorname{Cot} [c + d x]}) / \left( (a - i b)^2 (a + i b)^2 \sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right) \right) - \\
 & \quad \left( 2 a b B \sqrt{\operatorname{Cot} [c + d x]} \right) / \\
 & \quad \left( (a - i b)^2 (a + i b)^2 \sqrt{\operatorname{Sec} [c + d x]} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right) + \\
 & \quad \frac{2 a A b \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{(a - i b)^2 (a + i b)^2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} - \\
 & \quad \frac{a^2 B \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{(a - i b)^2 (a + i b)^2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} + \\
 & \quad \left. \frac{b^2 B \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} [c + d x]}{(a - i b)^2 (a + i b)^2 \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} \right) \\
 & \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} (A + B \operatorname{Tan} [c + d x]) \right) / \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) \right) \\
 & \left( \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \right) \right)
 \end{aligned}$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\operatorname{Sec}[c+dx]} \Bigg) /$$

$$\left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}}\right.$$

$$\left. \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) +$$

$$\left( i a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \right.$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\begin{aligned}
 & \left( i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \Big/ \\
 & \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) - \\
 & \frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx]}} \\
 & 3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} + \\
 & \frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \operatorname{Cos} [c+dx]+b \operatorname{Sin} [c+dx])^{3/2}} 2 i \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \sqrt{\operatorname{Sec}[c + dx]} (b \operatorname{Cos}[c + dx] - a \operatorname{Sin}[c + dx]) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \right) \right) \\
 & 2 i \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \operatorname{Csc}[c + dx]^2 \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right),
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} 4 i \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \right. \\
 & \left. \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec} [c + d x]} \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]}} 2 i \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]}
 \end{aligned}$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a + i b)^2 (A - i B)$$

$$\left. \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\frac{\operatorname{Sec} [c+d x]^{3/2} \operatorname{Sin} [c+d x] \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} 4 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2}{\sqrt{\operatorname{Sec} [c+d x]} \left( - \left( \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a^2 A - A b^2 + 2 a b B) \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) / \left( 4 \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b - \sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2+b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) \right) + \left( i (a - i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A + i B) \operatorname{Sec} \left[ \frac{1}{2} (c+d x) \right] \right)^2 / \left( 4 \left( 1 - i \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right] \right) \right) + \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b - \sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b + \sqrt{a^2+b^2}}} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) +$$



$$\left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left. \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} \right) \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} (a + b \operatorname{Tan}[c + d x])^{5/2} \right)$$

**Problem 648: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Cot}[c + d x]^{3/2} (A + B \operatorname{Tan}[c + d x])}{(a + b \operatorname{Tan}[c + d x])^{5/2}} dx$$

Optimal (type 3, 341 leaves, 11 steps):

$$\frac{(i A - B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{(i a - b)^{5/2} d} -$$

$$\frac{(i A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\operatorname{Tan}[c + d x]}}{\sqrt{a + b \operatorname{Tan}[c + d x]}}\right] \sqrt{\operatorname{Cot}[c + d x]} \sqrt{\operatorname{Tan}[c + d x]}}{(i a + b)^{5/2} d} -$$

$$\frac{2 b (3 a^2 A + 4 A b^2 - a b B)}{3 a^2 (a^2 + b^2) d \sqrt{\operatorname{Cot}[c + d x]} (a + b \operatorname{Tan}[c + d x])^{3/2}} -$$

$$\frac{2 A \sqrt{\operatorname{Cot}[c + d x]}}{a d (a + b \operatorname{Tan}[c + d x])^{3/2}} - \frac{2 b (3 a^4 A + 17 a^2 A b^2 + 8 A b^4 - 8 a^3 b B - 2 a b^3 B)}{3 a^3 (a^2 + b^2)^2 d \sqrt{\operatorname{Cot}[c + d x]} \sqrt{a + b \operatorname{Tan}[c + d x]}}$$

Result (type 4, 5368 leaves):

$$\left( \sqrt{\operatorname{Cot}[c + d x]} \operatorname{Sec}[c + d x]^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^3 \left( -\frac{2 (3 a^4 A + 6 a^2 A b^2 + 4 A b^4 - a b^3 B)}{3 a^3 (a - i b)^2 (a + i b)^2} - \right. \right.$$

$$\left. \frac{2 b^3 (-A b + a B)}{3 a (a - i b)^2 (a + i b)^2 (a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x])^2} + \right.$$

$$\left. \left. (2 (-12 a^2 A b^3 \operatorname{Sin}[c + d x] - 4 A b^5 \operatorname{Sin}[c + d x] + 9 a^3 b^2 B \operatorname{Sin}[c + d x] + a b^4 B \operatorname{Sin}[c + d x])) \right) \right) (A + B \operatorname{Tan}[c + d x]) \Big/$$

$$\left( d (A \operatorname{Cos}[c + d x] + B \operatorname{Sin}[c + d x]) (a + b \operatorname{Tan}[c + d x])^{5/2} \right) +$$

$$\left( 4 \cos\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot[c+dx]} \right.$$

$$\left. \left( i(-2aAb+a^2B-b^2B) \operatorname{EllipticF}\left[\frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right]}{\frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a-ib)^2(A+ib) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. \frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a+ib)^2(A-ib) \right.$$

$$\left. \operatorname{EllipticPi}\left[\frac{i(b+\sqrt{a^2+b^2})}{a}, \frac{i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \right)$$

$$\operatorname{Sec}[c+dx]^2 (a \cos[c+dx] + b \sin[c+dx])^2 \left( - \left( (2aAb \sqrt{\cot[c+dx]}) / \right.$$

$$\left. \left( (a-ib)^2(a+ib)^2 \sqrt{\sec[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \right) \right) +$$

$$\left( \frac{a^2 B \sqrt{\cot[c+dx]}}{(a-ib)^2(a+ib)^2 \sqrt{\sec[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]}} \right) -$$

$$\left( \frac{b^2 B \sqrt{\cot[c+dx]}}{(a-ib)^2(a+ib)^2 \sqrt{\sec[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]}} \right) -$$

$$\frac{a^2 A \sqrt{\cot[c+dx]} \sqrt{\sec[c+dx]} \sin[c+dx]}{(a-ib)^2(a+ib)^2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} +$$

$$\frac{Ab^2 \sqrt{\cot[c+dx]} \sqrt{\sec[c+dx]} \sin[c+dx]}{(a-ib)^2(a+ib)^2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} -$$

$$\left. \frac{2aBb \sqrt{\cot[c+dx]} \sqrt{\sec[c+dx]} \sin[c+dx]}{(a-ib)^2(a+ib)^2 \sqrt{a \cos[c+dx] + b \sin[c+dx]}} \right)$$

$$\left. \tan\left[\frac{1}{2}(c+dx)\right]^{3/2} (A+B \tan[c+dx]) \right) /$$

$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \cos [c + d x] + B \sin [c + d x]) \right)$$

$$\left( - \left( \left( a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right) \left( i (-2 a A b + a^2 B - b^2 B) \right) \right) \right)$$

$$\text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A + i B)$$

$$\text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] +$$

$$(a + i b)^2 (A - i B) \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \Big/ \left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \right)$$

$$\left( \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \right) -$$

$$\left( a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \left( i (-2 a A b + a^2 B - b^2 B) \right) \right)$$

$$\begin{aligned}
 & \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a-\text{i}b)^2 (A+\text{i}B) \\
 & \text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + \\
 & (a+\text{i}b)^2 (A-\text{i}B) \text{EllipticPi}\left[\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\text{Sec}[c+dx]} \Big/ \\
 & \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right. \\
 & \left. \sqrt{a \text{Cos}[c+dx]+b \text{Sin}[c+dx]} \sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) + \\
 & \frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \text{Cos}[c+dx]+b \text{Sin}[c+dx]}} \\
 & 3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \text{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\text{Cot}[c+dx]} \\
 & \left( \text{i}(-2aAb+a^2B-b^2B) \text{EllipticF}\left[\text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right. \\
 & \left. (a-\text{i}b)^2 (A+\text{i}B) \text{EllipticPi}\left[-\frac{\text{i}(b+\sqrt{a^2+b^2})}{a}, \text{i ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} - \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2}} 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^2 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right) \right) \\
 & 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}} \operatorname{Csc}[c+dx]^2} \\
 & \left( i(-2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - ib)^2 (A + iB) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + ib)^2 (A - iB) \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sqrt{\operatorname{Sec}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}^{3/2} - \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}}} 4 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}} \operatorname{Cot}[c+dx]} \\
 & \left( i(-2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - ib)^2 (A + iB) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + ib)^2 (A - iB) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( i (-2 a A b + a^2 B - b^2 B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a - i b)^2 (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^2 (A - i B) \right. \\
 & \left. \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sec [c + d x]^{3/2} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]}
 \end{aligned}$$

$$\begin{aligned} & \sqrt{\sec [c+d x]} \left( \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (-2 a A b+a^2 B-b^2 B) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2}{4 \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^{3 / 2}} \right. \\ & \left. \left( i(a-i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \right) / \left( 4\left(1-i \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]\right) \right. \right. \\ & \left. \left. \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^{3 / 2} \right) - \right. \\ & \left. \left( i(a+i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A-i B) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^2 \right) / \right. \\ & \left. \left( 4\left(1+i \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]\right) \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right. \right. \\ & \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^{3 / 2} \right) \right) \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^{3 / 2} (a+b \operatorname{Tan}[c+d x])^{5 / 2} \end{aligned}$$

Problem 649: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\operatorname{Cot}[c+d x]} (A+B \operatorname{Tan}[c+d x])}{(a+b \operatorname{Tan}[c+d x])^{5 / 2}} d x$$

Optimal (type 3, 287 leaves, 10 steps):



$$\begin{aligned}
 & \frac{(A + i B) \operatorname{ArcTan}\left[\frac{\sqrt{i a - b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]}}{(i a - b)^{5/2} d} - \\
 & \frac{(A - i B) \operatorname{ArcTanh}\left[\frac{\sqrt{i a + b} \sqrt{\tan[c + d x]}}{\sqrt{a + b \tan[c + d x]}}\right] \sqrt{\cot[c + d x]} \sqrt{\tan[c + d x]}}{(i a + b)^{5/2} d} + \\
 & \frac{2 b (A b - a B)}{3 a (a^2 + b^2) d \sqrt{\cot[c + d x]} (a + b \tan[c + d x])^{3/2}} + \\
 & \frac{2 b (8 a^2 A b + 2 A b^3 - 5 a^3 B + a b^2 B)}{3 a^2 (a^2 + b^2)^2 d \sqrt{\cot[c + d x]} \sqrt{a + b \tan[c + d x]}}
 \end{aligned}$$

Result (type 4, 5350 leaves):

$$\begin{aligned}
 & \left( \sqrt{\cot[c + d x]} \operatorname{Sec}[c + d x]^2 (a \cos[c + d x] + b \sin[c + d x])^3 \right. \\
 & \left( - \frac{2 b^2 (-A b + a B)}{3 a^2 (a - i b)^2 (a + i b)^2} + \frac{2 b^2 (-A b + a B)}{3 (a - i b)^2 (a + i b)^2 (a \cos[c + d x] + b \sin[c + d x])^2} - \right. \\
 & \left. \left. (2 (-9 a^2 A b^2 \sin[c + d x] - A b^4 \sin[c + d x] + 6 a^3 b B \sin[c + d x] - 2 a b^3 B \sin[c + d x])) \right) / \right. \\
 & \left. \left. (3 a^2 (a - i b)^2 (a + i b)^2 (a \cos[c + d x] + b \sin[c + d x])) \right) (A + B \tan[c + d x]) \right) / \\
 & (d (A \cos[c + d x] + B \sin[c + d x]) (a + b \tan[c + d x])^{5/2}) + \\
 & \left( 4 i \cos\left[\frac{1}{2}(c + d x)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot[c + d x]} \right. \right. \\
 & \left. \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - i b)^2 \right. \right. \\
 & \left. (A + i B) \operatorname{EllipticPi}\left[-\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & \left. (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + d x)\right]}}\right], \right.
 \end{aligned}$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \text{Sec}[c + dx]^2 (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])^2$$

$$\left( \left( a^2 A \sqrt{\text{Cot}[c + dx]} \right) / \left( (a - ib)^2 (a + ib)^2 \sqrt{\text{Sec}[c + dx]} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]} \right) - \right.$$

$$\left( A b^2 \sqrt{\text{Cot}[c + dx]} \right) / \left( (a - ib)^2 (a + ib)^2 \sqrt{\text{Sec}[c + dx]} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]} \right) +$$

$$\left( 2 a b B \sqrt{\text{Cot}[c + dx]} \right) / \left( (a - ib)^2 (a + ib)^2 \sqrt{\text{Sec}[c + dx]} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]} \right) -$$

$$\frac{2 a A b \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Sec}[c + dx]} \text{Sin}[c + dx]}{(a - ib)^2 (a + ib)^2 \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} +$$

$$\frac{a^2 B \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Sec}[c + dx]} \text{Sin}[c + dx]}{(a - ib)^2 (a + ib)^2 \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} -$$

$$\frac{b^2 B \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Sec}[c + dx]} \text{Sin}[c + dx]}{(a - ib)^2 (a + ib)^2 \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} \left. \right)$$

$$\text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} (A + B \text{Tan}[c + dx]) \left. \right)$$

$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \text{Cos}[c + dx] + B \text{Sin}[c + dx]) \right)$$

$$\left( - \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\text{Cot}[c + dx]} \left( a^2 A - A b^2 + 2 a b B \right) \right. \right)$$

$$\text{EllipticF}\left[ i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - ib)^2 (A + ib B)$$

$$\text{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\text{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] -$$

$$\begin{aligned}
 & (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \Bigg/ \left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]} \right) - \\
 & \left( i a \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot} [c + d x]} \left( a^2 A - A b^2 + 2 a b B \right) \right. \\
 & \left. \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a - i b)^2 (A + i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\operatorname{Sec} [c + d x]} \right) \Bigg/ \\
 & \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (b + \sqrt{a^2 + b^2}) \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} \right) + \\
 & \frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \cos [c+d x]+b \sin [c+d x]}} \\
 & 3 i \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( (a^2 A-A b^2+2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- \right. \\
 & (a-i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- (a+i b)^2 (A-i B) \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\sec [c+d x]} \sqrt{\tan \left[\frac{1}{2}(c+d x)\right]} - \\
 & \frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \cos [c+d x]+b \sin [c+d x])^{3/2}} 2 i \cos \left[\frac{1}{2}(c+d x)\right]^2 \\
 & \sqrt{\frac{b+\sqrt{a^2+b^2}+a \cot \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\cot [c+d x]} \\
 & \left( (a^2 A-A b^2+2 a b B) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]- \right. \\
 & (a-i b)^2 (A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, \right.
 \end{aligned}$$

$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} - (a+i b)^2 (A-i B) \\
 & \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \sqrt{\operatorname{Sec} [c+d x]} (b \operatorname{Cos} [c+d x] - a \operatorname{Sin} [c+d x]) \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \left( 1 / \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+d x]} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]} \right) \right) \\
 & 2 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \\
 & \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \operatorname{Csc} [c+d x]^2 \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right. \\
 & (a-i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \right. \\
 & \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - (a+i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \sqrt{\operatorname{Sec} [c+d x]} \operatorname{Tan} \left[ \frac{1}{2} (c+d x) \right]^{3/2} - \\
 & \frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+d x] + b \operatorname{Sin} [c+d x]}} 4 i \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right]
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}\right], \\
 & i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B) \\
 & \left. \operatorname{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \\
 & \frac{\sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + 1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]}} 2 i \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b + \sqrt{a^2 + b^2})}{a}\right], \\
 & i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + i b)^2 (A - i B)
 \end{aligned}$$

$$\text{EllipticPi}\left[\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan\left[\frac{1}{2}(c + dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right]$$

$$\text{Sec}[c + dx]^{3/2} \text{Sin}[c + dx] \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} +$$

$$\frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]}} 4 i \text{Cos}\left[\frac{1}{2}(c + dx)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\text{Cot}[c + dx]}$$

$$\sqrt{\text{Sec}[c + dx]} \left( - \left( i \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a^2 A - A b^2 + 2 a b B) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \right.$$

$$\left. \left( 4 \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) +$$

$$\left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \left( 1 - i \text{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \right)$$

$$\left. \left( \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) +$$

$$\left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \text{Cot}\left[\frac{1}{2}(c + dx)\right] \right) \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \text{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \right.$$

$$\left. \left. \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} \right) \right) \text{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} (a + b \text{Tan}[c + dx])^{5/2}$$

Problem 650: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{A + B \tan [c + d x]}{\sqrt{\cot [c + d x]} (a + b \tan [c + d x])^{5/2}} dx$$

Optimal (type 3, 284 leaves, 10 steps):

$$\frac{(\text{i} A - B) \operatorname{ArcTan}\left[\frac{\sqrt{\text{i} a - b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} - (\text{i} a - b)^{5/2} d}{(\text{i} a - b)^{5/2} d} + \frac{(\text{i} A + B) \operatorname{ArcTanh}\left[\frac{\sqrt{\text{i} a + b} \sqrt{\tan [c + d x]}}{\sqrt{a + b \tan [c + d x]}}\right] \sqrt{\cot [c + d x]} \sqrt{\tan [c + d x]} - 2 (A b - a B)}{(\text{i} a + b)^{5/2} d} - \frac{2 (A b - a B)}{3 (a^2 + b^2) d \sqrt{\cot [c + d x]} (a + b \tan [c + d x])^{3/2}} - \frac{2 (5 a^2 A b - A b^3 - 2 a^3 B + 4 a b^2 B)}{3 a (a^2 + b^2)^2 d \sqrt{\cot [c + d x]} \sqrt{a + b \tan [c + d x]}}$$

Result (type 4, 5338 leaves):

$$\left( \sqrt{\cot [c + d x]} \operatorname{Sec}[c + d x]^2 (a \cos [c + d x] + b \sin [c + d x])^3 \left( \frac{2 b (-A b + a B)}{3 a (a - \text{i} b)^2 (a + \text{i} b)^2} - \frac{2 a b (-A b + a B)}{3 (a - \text{i} b)^2 (a + \text{i} b)^2 (a \cos [c + d x] + b \sin [c + d x])^2} + (2 (-6 a^2 A b \sin [c + d x] + 2 A b^3 \sin [c + d x] + 3 a^3 B \sin [c + d x] - 5 a b^2 B \sin [c + d x])) / (3 a (a - \text{i} b)^2 (a + \text{i} b)^2 (a \cos [c + d x] + b \sin [c + d x])) \right) (A + B \tan [c + d x]) \right) / (d (A \cos [c + d x] + B \sin [c + d x]) (a + b \tan [c + d x])^{5/2}) - \left( 4 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right) \left( \text{i} (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[\text{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a - \text{i} b)^2 (A + \text{i} B) \operatorname{EllipticPi}\left[-\frac{\text{i} (b + \sqrt{a^2 + b^2})}{a}\right], \right)$$



$$\begin{aligned}
 & i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} + (a+ib)^2 (A-ib) \\
 & \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \\
 & \operatorname{Sec}[c+dx]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])^2 \left( (2aAb \sqrt{\operatorname{Cot}[c+dx]}) / \right. \\
 & \quad \left( (a-ib)^2 (a+ib)^2 \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right) - \\
 & \quad \left( a^2 B \sqrt{\operatorname{Cot}[c+dx]} \right) / \left( (a-ib)^2 (a+ib)^2 \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right) + \\
 & \quad \left( b^2 B \sqrt{\operatorname{Cot}[c+dx]} \right) / \left( (a-ib)^2 (a+ib)^2 \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right) + \\
 & \quad \frac{a^2 A \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{(a-ib)^2 (a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} - \\
 & \quad \frac{A b^2 \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{(a-ib)^2 (a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} + \\
 & \quad \left. \frac{2aAb \sqrt{\operatorname{Cot}[c+dx]} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{(a-ib)^2 (a+ib)^2 \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}} \right) \\
 & \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^{3/2} (A+B \operatorname{Tan}[c+dx]) \left. \right) / \\
 & \left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} d (A \operatorname{Cos}[c+dx] + B \operatorname{Sin}[c+dx]) \right) \\
 & \left( a \sqrt{\frac{b+\sqrt{a^2+b^2} + a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \right)
 \end{aligned}$$

$$\left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\operatorname{Sec}[c+dx]} \Bigg) / \left( (a^2 + b^2)^2 \right.$$

$$\left. (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]} \right.$$

$$\left. \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) + \left( a \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c+dx]} \right.$$

$$\left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[-\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] + (a + i b)^2 (A - i B) \operatorname{EllipticPi}\left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left( i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right) \sqrt{\operatorname{Sec} [c+dx]} \Big/$$

$$\left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} \right) -$$

1

$$\frac{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx]}}{1}$$

$$3 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b+\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c+dx) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot} [c+dx]}$$

$$\left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$\left. (a-i b)^2 (A+i B) \operatorname{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] + (a+i b)^2 (A-i B) \operatorname{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \sqrt{\operatorname{Sec} [c+dx]} \sqrt{\operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]} +$$

1

$$\frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a \operatorname{Cos} [c+dx] + b \operatorname{Sin} [c+dx])^{3/2}} 2 \operatorname{Cos} \left[ \frac{1}{2} (c+dx) \right]^2$$

$$\begin{aligned}
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \\
 & \left( i(-2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - ib)^2 (A + iB) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + ib)^2 (A - iB) \right. \\
 & \left. \operatorname{EllipticPi}\left[ \frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\operatorname{Sec}[c + dx]} (b \operatorname{Cos}[c + dx] - a \operatorname{Sin}[c + dx]) \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]^{3/2} + \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + dx]} \sqrt{a \operatorname{Cos}[c + dx] + b \operatorname{Sin}[c + dx]} \right) \right) \\
 & 2 \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \\
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + dx)\right]}{b - \sqrt{a^2 + b^2}}} \operatorname{Csc}[c + dx]^2 \\
 & \left( i(-2aAb + a^2B - b^2B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - ib)^2 (A + iB) \operatorname{EllipticPi}\left[ -\frac{i(b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}} \right], \right. \\
 & \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right),
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} + (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 4 \cos \left[ \frac{1}{2} (c + d x) \right] \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^2 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 2 \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]}
 \end{aligned}$$

$$\left( i (-2 a A b + a^2 B - b^2 B) \operatorname{EllipticF}\left[ i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi}\left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] + (a + i b)^2 (A - i B)$$

$$\left. \operatorname{EllipticPi}\left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh}\left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)$$

$$\operatorname{Sec}[c + d x]^{3/2} \operatorname{Sin}[c + d x] \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} -$$

$$\frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \operatorname{Cos}[c + d x] + b \operatorname{Sin}[c + d x]}} 4 \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right]^2$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\operatorname{Cot}[c + d x]}$$

$$\sqrt{\operatorname{Sec}[c + d x]} \left( \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (-2 a A b + a^2 B - b^2 B) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2}{4 \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2}} \right) +$$

$$\left( i (a - i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A + i B) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) / \left( 4 \left( 1 - i \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right] \right) \right)$$

$$\sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c + d x)\right]}{b + \sqrt{a^2 + b^2}}} \operatorname{Tan}\left[\frac{1}{2}(c + d x)\right]^{3/2} -$$

$$\left( i (a + i b)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (A - i B) \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^2 \right) /$$

$$\left( 4 \left( 1 + i \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right] \right) \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right. \\ \left. \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} \right) \left( \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]^{3/2} (a + b \operatorname{Tan} [c + d x])^{5/2} \right)$$

**Problem 651: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Tan} [c + d x]}{\operatorname{Cot} [c + d x]^{3/2} (a + b \operatorname{Tan} [c + d x])^{5/2}} dx$$

Optimal (type 3, 284 leaves, 10 steps):

$$\frac{(A + i B) \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]} + (i a - b)^{5/2} d}{(A - i B) \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]} + (i a + b)^{5/2} d} + \frac{2 a (A b - a B)}{3 b (a^2 + b^2) d \sqrt{\operatorname{Cot} [c + d x]} (a + b \operatorname{Tan} [c + d x])^{3/2}} + \frac{2 (2 a^2 A b - 4 A b^3 + a^3 B + 7 a b^2 B)}{3 b (a^2 + b^2)^2 d \sqrt{\operatorname{Cot} [c + d x]} \sqrt{a + b \operatorname{Tan} [c + d x]}}$$

Result (type 4, 5323 leaves):

$$\left( \sqrt{\operatorname{Cot} [c + d x]} \operatorname{Sec} [c + d x]^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^3 \right. \\ \left( - \frac{2 (-A b + a B)}{3 (a - i b)^2 (a + i b)^2} + \frac{2 a^2 (-A b + a B)}{3 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])^2} + \frac{2 (3 a^2 A \operatorname{Sin} [c + d x] - 5 A b^2 \operatorname{Sin} [c + d x] + 8 a b B \operatorname{Sin} [c + d x])}{3 (a - i b)^2 (a + i b)^2 (a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x])} \right) (A + B \operatorname{Tan} [c + d x]) \Big/ \\ (d (A \operatorname{Cos} [c + d x] + B \operatorname{Sin} [c + d x]) (a + b \operatorname{Tan} [c + d x])^{5/2}) -$$

$$\left( 4 i \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^2 \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+d x)\right]}{b-\sqrt{a^2+b^2}}}\sqrt{\operatorname{Cot}[c+d x]} \right.$$

$$\left. \left( a^2 A-A b^2+2 a b B\right) \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\right.$$

$$\left. (a-i b)^2(A+i B) \operatorname{EllipticPi}\left[-\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a},\right. \right.$$

$$\left. \left. i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]-\left(a+i b\right)^2(A-i B) \right.$$

$$\left. \left. \operatorname{EllipticPi}\left[\frac{i\left(b+\sqrt{a^2+b^2}\right)}{a}, i \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right]\right) \right)$$

$$\operatorname{Sec}[c+d x]^2(a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x])^2\left(-\left(\left(a^2 A \sqrt{\operatorname{Cot}[c+d x]}\right) / \right. \right.$$

$$\left. \left. \left(\left(a-i b\right)^2\left(a+i b\right)^2 \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}\right)\right)+\right.$$

$$\left. \left. \left(\frac{A b^2 \sqrt{\operatorname{Cot}[c+d x]}}{\left(a-i b\right)^2\left(a+i b\right)^2 \sqrt{\operatorname{Sec}[c+d x]} \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}}\right)-\right. \right.$$

$$\left. \left. \left(\frac{2 a b B \sqrt{\operatorname{Cot}[c+d x]}}{\left(a-i b\right)^2\left(a+i b\right)^2 \sqrt{\operatorname{Sec}[c+d x]}}\right.\right.$$

$$\left. \left. \left.\frac{\sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}}{\left(a-i b\right)^2\left(a+i b\right)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}}-\right. \right.$$

$$\left. \left. \frac{a^2 B \sqrt{\operatorname{Cot}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\left(a-i b\right)^2\left(a+i b\right)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}}+\right. \right.$$

$$\left. \left. \frac{b^2 B \sqrt{\operatorname{Cot}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\left(a-i b\right)^2\left(a+i b\right)^2 \sqrt{a \operatorname{Cos}[c+d x]+b \operatorname{Sin}[c+d x]}}\right) \right)$$

$$\left. \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^{3 / 2}(A+B \operatorname{Tan}[c+d x])\right) /$$



$$\left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} d (A \cos [c + d x] + B \sin [c + d x]) \right.$$

$$\left. \left( \left( i a \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right. \right. \right.$$

$$\left. \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \right.$$

$$(a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \right.$$

$$\left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right.$$

$$\left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \Big/$$

$$\left( (a^2 + b^2)^2 (b - \sqrt{a^2 + b^2}) \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \right.$$

$$\left. \sqrt{a \cos [c + d x] + b \sin [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} \right) +$$

$$\left( i a \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \right.$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a-ib)^2 (A+ib) \operatorname{EllipticPi}\left[-\frac{ib+\sqrt{a^2+b^2}}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - (a+ib)^2 (A-ib) \operatorname{EllipticPi}\left[\frac{ib+\sqrt{a^2+b^2}}{a}, \right.$$

$$\left. \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] \sqrt{\operatorname{Sec}[c+dx]} \Bigg) /$$

$$\left( (a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (b+\sqrt{a^2+b^2}) \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \right.$$

$$\left. \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]} \sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right) -$$

$$\frac{1}{(a^2+b^2)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} \sqrt{a \operatorname{Cos}[c+dx]+b \operatorname{Sin}[c+dx]}}$$

$$3ib \sqrt{\frac{b+\sqrt{a^2+b^2}+a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b-\sqrt{a^2+b^2}}} \sqrt{\operatorname{Cot}[c+dx]}$$

$$\left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}}\right] - \right.$$

$$(a-ib)^2 (A+ib) \operatorname{EllipticPi}\left[-\frac{ib+\sqrt{a^2+b^2}}{a}, \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right.$$

$$\begin{aligned}
 & \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \Big] - (a + i b)^2 (A - i B) \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \sqrt{\sec [c + d x]} \sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]} + \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} (a \cos [c + d x] + b \sin [c + d x])^{3/2}} 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. (a - i b)^2 (A + i B) \operatorname{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \right. \\
 & \left. \left. i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \right. \\
 & \left. \operatorname{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \operatorname{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} + \\
 & \left( 1 / \left( (a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \right) \right) \\
 & 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}} \operatorname{Csc}[c+dx]^2} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - \operatorname{i} b)^2 (A + \operatorname{i} B) \operatorname{EllipticPi}\left[-\frac{\operatorname{i}(b + \sqrt{a^2 + b^2})}{a}, \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \right. \\
 & \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + \operatorname{i} b)^2 (A - \operatorname{i} B) \operatorname{EllipticPi}\left[\frac{\operatorname{i}(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] \right) \sqrt{\operatorname{Sec}[c+dx] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}^{3/2} + \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}} \sqrt{a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx]}}} 4 \operatorname{i} \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \operatorname{Cot}\left[\frac{1}{2}(c+dx)\right]}{b - \sqrt{a^2 + b^2}} \operatorname{Cot}[c+dx]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \operatorname{EllipticF}\left[\operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - \right. \\
 & (a - \operatorname{i} b)^2 (A + \operatorname{i} B) \operatorname{EllipticPi}\left[-\frac{\operatorname{i}(b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. \operatorname{i} \operatorname{ArcSinh}\left[\frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}\right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}}\right] - (a + \operatorname{i} b)^2 (A - \operatorname{i} B) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\sec [c + d x]} \sin \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 2 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]} \\
 & \left( (a^2 A - A b^2 + 2 a b B) \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & (a - i b)^2 (A + i B) \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, \right. \\
 & \left. i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - (a + i b)^2 (A - i B) \\
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c + d x) \right]}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sec [c + d x]^{3/2} \sin [c + d x] \tan \left[ \frac{1}{2} (c + d x) \right]^{3/2} - \\
 & \frac{1}{(a^2 + b^2)^2 \sqrt{\frac{a}{b + \sqrt{a^2 + b^2}}} \sqrt{a \cos [c + d x] + b \sin [c + d x]}} 4 i \cos \left[ \frac{1}{2} (c + d x) \right]^2 \\
 & \sqrt{\frac{b + \sqrt{a^2 + b^2} + a \cot \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{\cot [c + d x]}
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{\sec [c+d x]} \left( - \left( \left( i \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (a^2 A - A b^2 + 2 a b B) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \right. \right. \\
& \left. \left( 4 \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) \right) + \\
& \left( i (a-i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A+i B) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \left( 4 \left( 1-i \cot \left[ \frac{1}{2} (c+d x) \right] \right) \right) \\
& \left. \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) + \\
& \left( i (a+i b)^2 \sqrt{\frac{a}{b+\sqrt{a^2+b^2}}} (A-i B) \sec \left[ \frac{1}{2} (c+d x) \right]^2 \right) / \\
& \left( 4 \left( 1+i \cot \left[ \frac{1}{2} (c+d x) \right] \right) \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1 + \frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}} \right. \\
& \left. \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} \right) \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2} (a+b \tan [c+d x])^{5/2} \right)
\end{aligned}$$

**Problem 652: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \tan [c+d x]}{\cot [c+d x]^{5/2} (a+b \tan [c+d x])^{5/2}} dx$$

Optimal (type 3, 342 leaves, 15 steps):

$$\begin{aligned}
 & \frac{(\sqrt{a-b} - B) \operatorname{ArcTan}\left[\frac{\sqrt{a-b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]}}{(\sqrt{a-b})^{5/2} d} + \\
 & \frac{2 B \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]}}{b^{5/2} d} - \\
 & \frac{(\sqrt{a+b} + B) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]}}{(\sqrt{a+b})^{5/2} d} + \\
 & \frac{2 a (A b - a B)}{3 b (a^2 + b^2) d \cot[c+dx]^{3/2} (a + b \tan[c+dx])^{3/2}} + \\
 & \frac{2 a (2 A b^3 - a (a^2 + 3 b^2) B)}{b^2 (a^2 + b^2)^2 d \sqrt{\cot[c+dx]} \sqrt{a + b \tan[c+dx]}}
 \end{aligned}$$

Result (type 4, 97 014 leaves): Display of huge result suppressed!

**Problem 653: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cot[c+dx]} (a B + b B \tan[c+dx])}{(a + b \tan[c+dx])^{3/2}} dx$$

Optimal (type 3, 151 leaves, 9 steps):

$$\begin{aligned}
 & \frac{B \operatorname{ArcTan}\left[\frac{\sqrt{a-b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]}}{\sqrt{a-b} d} + \\
 & \frac{B \operatorname{ArcTanh}\left[\frac{\sqrt{a+b} \sqrt{\tan[c+dx]}}{\sqrt{a+b \tan[c+dx]}}\right] \sqrt{\cot[c+dx]} \sqrt{\tan[c+dx]}}{\sqrt{a+b} d}
 \end{aligned}$$

Result (type 4, 431 leaves):

$$\frac{1}{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}} d \sqrt{a+b \tan [c+d x]}}}$$

$$4 i B \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sqrt{\frac{b-\sqrt{a^2+b^2}+a \cot \left[ \frac{1}{2} (c+d x) \right]}{b-\sqrt{a^2+b^2}}} \sqrt{1+\frac{a \cot \left[ \frac{1}{2} (c+d x) \right]}{b+\sqrt{a^2+b^2}}}$$

$$\sqrt{\cot [c+d x]} \left( \text{EllipticF} \left[ i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.$$

$$\text{EllipticPi} \left[ -\frac{i (b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] -$$

$$\left. \text{EllipticPi} \left[ \frac{i (b+\sqrt{a^2+b^2})}{a}, i \text{ArcSinh} \left[ \frac{\sqrt{\frac{a}{b+\sqrt{a^2+b^2}}}}{\sqrt{\tan \left[ \frac{1}{2} (c+d x) \right]}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right)$$

$$\sec [c+d x] \tan \left[ \frac{1}{2} (c+d x) \right]^{3/2}$$

**Problem 654:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{a B + b B \tan [c+d x]}{\sqrt{\cot [c+d x]} (a+b \tan [c+d x])^{3/2}} dx$$

Optimal (type 3, 157 leaves, 9 steps):

$$\frac{i B \text{ArcTan} \left[ \frac{\sqrt{i a-b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}} \right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]} - \sqrt{i a-b} d}{\sqrt{i a+b} d}$$

$$\frac{i B \text{ArcTanh} \left[ \frac{\sqrt{i a+b} \sqrt{\tan [c+d x]}}{\sqrt{a+b \tan [c+d x]}} \right] \sqrt{\cot [c+d x]} \sqrt{\tan [c+d x]} - \sqrt{i a+b} d}{\sqrt{i a+b} d}$$

Result (type 4, 2641 leaves):



$$\begin{aligned}
 & \left( 2 B \left( \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \quad \left. \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \quad \sqrt{\text{Sec}[c + d x]} \sin[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( d \sqrt{\frac{a}{a - \left( b + \sqrt{a^2 + b^2} \right) \cot \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \right. \\
 & \quad \left( \left( a \sqrt{\cot[c + d x]} \left( \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \right. \right. \right. \\
 & \quad \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \right. \right. \\
 & \quad \left. \left. \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \sqrt{\text{Sec}[c + d x]} \sin[c + d x] \Big/ \\
 & \left( 2 \left( -b + \sqrt{a^2 + b^2} \right) \sqrt{\frac{a}{a - \left( b + \sqrt{a^2 + b^2} \right) \cot \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \right. \\
 & \quad \left. \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \right) - \left( \sqrt{\cot[c + d x]} \right. \\
 & \quad \left( \text{EllipticPi} \left[ -\frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \quad \left. \text{EllipticPi} \left[ \frac{i \left( b + \sqrt{a^2 + b^2} \right)}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{\sec [c+d x]} \sin [c+d x] (b \cos [c+d x]-a \sin [c+d x]) \sqrt{1+\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{-b+\sqrt{a^2+b^2}}} \Big/ \\
& \left( \sqrt{\frac{a}{a-(b+\sqrt{a^2+b^2}) \cot \left[\frac{1}{2}(c+d x)\right]}} (a \cos [c+d x]+b \sin [c+d x])^{3/2} \right) + \\
& \left( 2 \sqrt{\cot [c+d x]} \left( \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right], \right. \right. \right. \\
& \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, \right. \right. \\
& \left. \left. i \operatorname{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \sqrt{1+\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{-b+\sqrt{a^2+b^2}}} \Big/ \\
& \left( \sqrt{\frac{a}{a-(b+\sqrt{a^2+b^2}) \cot \left[\frac{1}{2}(c+d x)\right]}} \sqrt{\sec [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right) - \\
& \left( \csc [c+d x] \left( \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right], \right. \right. \right. \\
& \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \operatorname{EllipticPi} \left[ \frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right], \right. \right. \\
& \left. \left. \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] \right) \sqrt{\sec [c+d x]} \sqrt{1+\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{-b+\sqrt{a^2+b^2}}} \Big/ \\
& \left( \sqrt{\frac{a}{a-(b+\sqrt{a^2+b^2}) \cot \left[\frac{1}{2}(c+d x)\right]}} \sqrt{\cot [c+d x]} \sqrt{a \cos [c+d x]+b \sin [c+d x]} \right) + \\
& \left( a(b+\sqrt{a^2+b^2}) \sqrt{\cot [c+d x]} \csc \left[\frac{1}{2}(c+d x)\right]^2 \right) \\
& \left( \operatorname{EllipticPi} \left[ -\frac{i(b+\sqrt{a^2+b^2})}{a}, i \operatorname{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}} \right], \frac{b+\sqrt{a^2+b^2}}{b-\sqrt{a^2+b^2}} \right] - \right.
\end{aligned}$$

$$\begin{aligned}
 & \left( \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \sqrt{\text{Sec}[c + d x]} \sin[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( 2 \left( \frac{a}{a - (b + \sqrt{a^2 + b^2}) \cot \left[ \frac{1}{2} (c + d x) \right]} \right)^{3/2} \left( a - (b + \sqrt{a^2 + b^2}) \cot \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right. \\
 & \left. \sqrt{a \cos[c + d x] + b \sin[c + d x]} \right) + \left( \sqrt{\cot[c + d x]} \right. \\
 & \left( \text{EllipticPi} \left[ -\frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] - \right. \\
 & \left. \text{EllipticPi} \left[ \frac{i (b + \sqrt{a^2 + b^2})}{a}, i \text{ArcSinh} \left[ \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right], \frac{b + \sqrt{a^2 + b^2}}{b - \sqrt{a^2 + b^2}} \right] \right) \\
 & \text{Sec}[c + d x]^{3/2} \sin[c + d x]^2 \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \Big/ \\
 & \left( \sqrt{\frac{a}{a - (b + \sqrt{a^2 + b^2}) \cot \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{a \cos[c + d x] + b \sin[c + d x]} \right) + \\
 & \left( 2 \sqrt{\cot[c + d x]} \sqrt{\text{Sec}[c + d x]} \sin[c + d x] \sqrt{1 + \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{-b + \sqrt{a^2 + b^2}}} \right. \\
 & \left. \left( i a \sec \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \Big/ \left( 4 (b + \sqrt{a^2 + b^2}) \left( 1 - i \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \\
 & \sqrt{-\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) -
 \end{aligned}$$

$$\left( i a \operatorname{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 4 (b + \sqrt{a^2 + b^2}) \left( 1 + i \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\ \left. \sqrt{-\frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b - \sqrt{a^2 + b^2}}} \sqrt{1 - \frac{a \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) \right) / \\ \left( \sqrt{\frac{a}{a - (b + \sqrt{a^2 + b^2}) \operatorname{Cot} \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{a \operatorname{Cos} [c + d x] + b \operatorname{Sin} [c + d x]} \right) \\ \left. \sqrt{a + b \operatorname{Tan} [c + d x]} \right)$$

**Problem 655: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{a B + b B \operatorname{Tan} [c + d x]}{\operatorname{Cot} [c + d x]^{3/2} (a + b \operatorname{Tan} [c + d x])^{3/2}} dx$$

Optimal (type 3, 215 leaves, 14 steps):

$$\frac{B \operatorname{ArcTan} \left[ \frac{\sqrt{i a - b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{i a - b} d} + \\ \frac{2 B \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{b} d} - \\ \frac{B \operatorname{ArcTanh} \left[ \frac{\sqrt{i a + b} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{a + b \operatorname{Tan} [c + d x]}} \right] \sqrt{\operatorname{Cot} [c + d x]} \sqrt{\operatorname{Tan} [c + d x]}}{\sqrt{i a + b} d}$$

Result (type 4, 5277 leaves):

$$- \left( \left( 4 a B \sqrt{\operatorname{Cot} [c + d x]} \right) \right)$$

$$\begin{aligned}
 & \left( - \left( \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) \right. \\
 & \left. (-a + b + \sqrt{a^2 + b^2}) \right) - \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \\
 & \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \left( a + i (b + \sqrt{a^2 + b^2}) \right) - \\
 & \left( i \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \\
 & \left( i a + b + \sqrt{a^2 + b^2} \right) + \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \\
 & \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + b + \sqrt{a^2 + b^2} \right) \right) \text{Sec} [c + d x] (a \text{Cos} [c + d x] + b \text{Sin} [c + d x]) \\
 & \left( \frac{\sqrt{\text{Cot} [c + d x]} \text{Sec} [c + d x]^{3/2}}{2 \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} - \frac{\text{Cos} [2 (c + d x)] \sqrt{\text{Cot} [c + d x]} \text{Sec} [c + d x]^{3/2}}{2 \sqrt{a \text{Cos} [c + d x] + b \text{Sin} [c + d x]}} \right)
 \end{aligned}$$

$$\left( \frac{\sqrt{\frac{a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{b+\sqrt{a^2+b^2}}}}{\right) /$$

$$\left( \sqrt{a^2+b^2} d \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \operatorname{Cos}[c+dx] + b \operatorname{Sin}[c+dx])}{a^2+b^2}} \right)$$

$$\left( - \left( \left( a^2 \sqrt{\operatorname{Cot}[c+dx]} \right) - \left( \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right] \right) \right), \right)$$

$$\left( \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right) / \left( -a+b+\sqrt{a^2+b^2} \right) - \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right)$$

$$\operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right], \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right) / \left( a+i \left( b+\sqrt{a^2+b^2} \right) \right) -$$

$$\left( i \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{i a+b+\sqrt{a^2+b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}\right] \right), \right)$$

$$\left( \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right) / \left( i a+b+\sqrt{a^2+b^2} \right) + \operatorname{EllipticPi}\left[\frac{2\sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \right)$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( a+b+\sqrt{a^2+b^2} \right) \right.$$

$$\left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 \sqrt{\text{Sec}[c+dx]} \sqrt{a \cos[c+dx] + b \sin[c+dx]} \right. /$$

$$\left( \sqrt{a^2+b^2} (b+\sqrt{a^2+b^2}) \sqrt{\frac{a \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2+b^2}} \right.$$

$$\left. \left. \sqrt{\frac{a \tan \left[ \frac{1}{2}(c+dx) \right]}{b+\sqrt{a^2+b^2}}} \right) \right. -$$

$$\left( 2a \sqrt{\text{Cot}[c+dx]} \left( \left( \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \right. \right. \right.$$

$$\left. \left. \left. \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( -a+b+\sqrt{a^2+b^2} \right) - \text{EllipticPi} \left[ \frac{2\sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right. \right. \right.$$

$$\left. \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}}, \frac{2\sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \left( a+i (b+\sqrt{a^2+b^2}) \right) \right) - \right.$$

$$\left( \begin{aligned} & \left( \begin{aligned} & \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right] \right], \right. \\ & \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( a + b + \sqrt{a^2 + b^2} \right) + \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \\ & \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \Big/ \left( a + b + \sqrt{a^2 + b^2} \right) \right) \\ & \left. \sqrt{\sec [c + d x]} (b \cos [c + d x] - a \sin [c + d x]) \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} \right) \Big/ \end{aligned} \right) \\
 \left( \begin{aligned} & \sqrt{a^2 + b^2} \sqrt{a \cos [c + d x] + b \sin [c + d x]} \\ & \sqrt{\frac{a \sec \left[ \frac{1}{2} (c + d x) \right]^2 (a \cos [c + d x] + b \sin [c + d x])}{a^2 + b^2}} \right) + \\ & \frac{1}{\sqrt{a^2 + b^2} \sqrt{\cot [c + d x]} \sqrt{\frac{a \sec \left[ \frac{1}{2} (c + d x) \right]^2 (a \cos [c + d x] + b \sin [c + d x])}{a^2 + b^2}}} - 2 a \csc [c + d x]^2 \end{aligned} \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( - \left( \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] \right) / \right. \\
 & \left. \left( -a + b + \sqrt{a^2 + b^2} \right) - \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) - \right. \\
 & \left. \left( i \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \right. \right. \right. \\
 & \left. \left. \left. \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( i a + b + \sqrt{a^2 + b^2} \right) + \text{EllipticPi} \left[ \frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \right. \right. \right. \\
 & \left. \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + b + \sqrt{a^2 + b^2} \right) \right) \right) \\
 & \sqrt{\text{Sec}[c + d x]} \sqrt{a \text{Cos}[c + d x] + b \text{Sin}[c + d x]} \sqrt{\frac{a \tan \left[ \frac{1}{2} (c + d x) \right]}{b + \sqrt{a^2 + b^2}}} -
 \end{aligned}$$

$$\frac{1}{\sqrt{a^2 + b^2} \sqrt{\frac{a \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a \cos[c+dx] + b \sin[c+dx])}{a^2 + b^2}}} - 2 a \sqrt{\operatorname{Cot}[c+dx]}$$

$$\left( \left( \left( \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \right. \right.$$

$$\left. \left. \left( -a + b + \sqrt{a^2 + b^2} \right) \right) - \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{-i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + i \left( b + \sqrt{a^2 + b^2} \right) \right) -$$

$$\left( i \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{i a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \left( i a + b + \sqrt{a^2 + b^2} \right) + \operatorname{EllipticPi}\left[\frac{2 \sqrt{a^2 + b^2}}{a + b + \sqrt{a^2 + b^2}}, \operatorname{ArcSin}\left[\frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}}}\right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right) / \left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\begin{aligned}
 & \frac{\sec [c+d x]^{3/2} \sin [c+d x] \sqrt{a \cos [c+d x]+b \sin [c+d x]} \sqrt{\frac{a \tan \left[\frac{1}{2}(c+d x)\right]}{b+\sqrt{a^2+b^2}}}}{\sqrt{a^2+b^2} \left(\frac{a \sec \left[\frac{1}{2}(c+d x)\right]^2 (a \cos [c+d x]+b \sin [c+d x])}{a^2+b^2}\right)^{3/2} 2 a \sqrt{\cot [c+d x]}} \\
 & \left( - \left( \text{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / \right. \right. \\
 & \left. \left. (-a+b+\sqrt{a^2+b^2}) - \text{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{-i a+b+\sqrt{a^2+b^2}}, \right. \right. \right. \\
 & \left. \left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / (a+i(b+\sqrt{a^2+b^2})) - \right. \\
 & \left. \left( i \text{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{i a+b+\sqrt{a^2+b^2}}, \text{ArcSin} \left[ \frac{\sqrt{\frac{b+\sqrt{a^2+b^2}-a \tan \left[\frac{1}{2}(c+d x)\right]}}{\sqrt{a^2+b^2}}}}{\sqrt{2}} \right], \right. \right. \right. \\
 & \left. \left. \frac{2 \sqrt{a^2+b^2}}{b+\sqrt{a^2+b^2}} \right] / (i a+b+\sqrt{a^2+b^2}) + \text{EllipticPi} \left[ \frac{2 \sqrt{a^2+b^2}}{a+b+\sqrt{a^2+b^2}}, \right. \right. \right.
 \end{aligned}$$

$$\left. \text{ArcSin} \left[ \frac{\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}}{\sqrt{a^2 + b^2}}}}{\sqrt{2}} \right], \frac{2 \sqrt{a^2 + b^2}}{b + \sqrt{a^2 + b^2}} \right] / \left( a + b + \sqrt{a^2 + b^2} \right)$$

$$\sqrt{\text{Sec}[c + dx]} \sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( \frac{a \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 (b \text{Cos}[c + dx] - a \text{Sin}[c + dx])}{a^2 + b^2} + \frac{1}{a^2 + b^2} \right.$$

$$\left. a \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 (a \text{Cos}[c + dx] + b \text{Sin}[c + dx]) \tan\left[\frac{1}{2}(c + dx)\right] \right) -$$

$$\frac{1}{\sqrt{a^2 + b^2} \sqrt{\frac{a \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 (a \text{Cos}[c + dx] + b \text{Sin}[c + dx])}{a^2 + b^2}}} 4 a \sqrt{\text{Cot}[c + dx]} \sqrt{\text{Sec}[c + dx]}$$

$$\sqrt{a \text{Cos}[c + dx] + b \text{Sin}[c + dx]} \sqrt{\frac{a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}}$$

$$\left( \left( a \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (-a + b + \sqrt{a^2 + b^2}) \right) \right.$$

$$\left. \sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2 \sqrt{a^2 + b^2}}} \right.$$

$$\left. \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{b + \sqrt{a^2 + b^2}}} \left( 1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{-a + b + \sqrt{a^2 + b^2}} \right) \right) +$$

$$\left( a \text{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \right) / \left( 4 \sqrt{2} \sqrt{a^2 + b^2} (a + b + \sqrt{a^2 + b^2}) \right)$$

$$\sqrt{\frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{\sqrt{a^2 + b^2}}} \sqrt{1 - \frac{b + \sqrt{a^2 + b^2} - a \tan\left[\frac{1}{2}(c + dx)\right]}{2 \sqrt{a^2 + b^2}}}$$



$$\frac{1}{2d(1-m)} (A + iB) \text{AppellF1}\left[1-m, -n, 1, 2-m, -\frac{b \tan[c+dx]}{a}, -i \tan[c+dx]\right]$$

$$\cot[c+dx]^{-1+m} (a+b \tan[c+dx])^n \left(1 + \frac{b \tan[c+dx]}{a}\right)^{-n} + \frac{1}{2d(1-m)}$$

$$(A - iB) \text{AppellF1}\left[1-m, -n, 1, 2-m, -\frac{b \tan[c+dx]}{a}, i \tan[c+dx]\right]$$

$$\cot[c+dx]^{-1+m} (a+b \tan[c+dx])^n \left(1 + \frac{b \tan[c+dx]}{a}\right)^{-n}$$

Result (type 8, 33 leaves):

$$\int \cot[c+dx]^m (a+b \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

**Problem 657: Unable to integrate problem.**

$$\int \cot[c+dx]^{3/2} (a+b \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

Optimal (type 6, 169 leaves, 10 steps):

$$-\frac{1}{d} (A + iB) \text{AppellF1}\left[-\frac{1}{2}, 1, -n, \frac{1}{2}, -i \tan[c+dx], -\frac{b \tan[c+dx]}{a}\right]$$

$$\sqrt{\cot[c+dx]} (a+b \tan[c+dx])^n \left(1 + \frac{b \tan[c+dx]}{a}\right)^{-n} - \frac{1}{d}$$

$$(A - iB) \text{AppellF1}\left[-\frac{1}{2}, 1, -n, \frac{1}{2}, i \tan[c+dx], -\frac{b \tan[c+dx]}{a}\right]$$

$$\sqrt{\cot[c+dx]} (a+b \tan[c+dx])^n \left(1 + \frac{b \tan[c+dx]}{a}\right)^{-n}$$

Result (type 8, 35 leaves):

$$\int \cot[c+dx]^{3/2} (a+b \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

**Problem 658: Unable to integrate problem.**

$$\int \sqrt{\cot[c+dx]} (a+b \tan[c+dx])^n (A+B \tan[c+dx]) dx$$

Optimal (type 6, 167 leaves, 10 steps):

$$\frac{1}{d\sqrt{\cot[c+dx]}} (A + iB) \text{AppellF1}\left[\frac{1}{2}, 1, -n, \frac{3}{2}, -i \tan[c+dx], -\frac{b \tan[c+dx]}{a}\right]$$

$$(a+b \tan[c+dx])^n \left(1 + \frac{b \tan[c+dx]}{a}\right)^{-n} + \frac{1}{d\sqrt{\cot[c+dx]}}$$

$$(A - iB) \text{AppellF1}\left[\frac{1}{2}, 1, -n, \frac{3}{2}, i \tan[c+dx], -\frac{b \tan[c+dx]}{a}\right]$$

$$(a+b \tan[c+dx])^n \left(1 + \frac{b \tan[c+dx]}{a}\right)^{-n}$$

Result (type 8, 35 leaves):

$$\int \sqrt{\cot [c+d x]} (a+b \tan [c+d x])^n (A+B \tan [c+d x]) d x$$

**Problem 659: Unable to integrate problem.**

$$\int \frac{(a+b \tan [c+d x])^n (A+B \tan [c+d x])}{\sqrt{\cot [c+d x]}} d x$$

Optimal (type 6, 173 leaves, 10 steps):

$$\begin{aligned} & \left( (A+i B) \operatorname{AppellF1}\left[\frac{3}{2}, 1, -n, \frac{5}{2}, -i \tan [c+d x], -\frac{b \tan [c+d x]}{a}\right] \right. \\ & \quad \left. (a+b \tan [c+d x])^n \left(1+\frac{b \tan [c+d x]}{a}\right)^{-n}\right) / (3 d \cot [c+d x]^{3/2}) + \\ & \left( (A-i B) \operatorname{AppellF1}\left[\frac{3}{2}, 1, -n, \frac{5}{2}, i \tan [c+d x], -\frac{b \tan [c+d x]}{a}\right] \right. \\ & \quad \left. (a+b \tan [c+d x])^n \left(1+\frac{b \tan [c+d x]}{a}\right)^{-n}\right) / (3 d \cot [c+d x]^{3/2}) \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(a+b \tan [c+d x])^n (A+B \tan [c+d x])}{\sqrt{\cot [c+d x]}} d x$$

**Problem 660: Unable to integrate problem.**

$$\int \frac{(a+b \tan [c+d x])^n (A+B \tan [c+d x])}{\cot [c+d x]^{3/2}} d x$$

Optimal (type 6, 173 leaves, 10 steps):

$$\begin{aligned} & \left( (A+i B) \operatorname{AppellF1}\left[\frac{5}{2}, 1, -n, \frac{7}{2}, -i \tan [c+d x], -\frac{b \tan [c+d x]}{a}\right] \right. \\ & \quad \left. (a+b \tan [c+d x])^n \left(1+\frac{b \tan [c+d x]}{a}\right)^{-n}\right) / (5 d \cot [c+d x]^{5/2}) + \\ & \left( (A-i B) \operatorname{AppellF1}\left[\frac{5}{2}, 1, -n, \frac{7}{2}, i \tan [c+d x], -\frac{b \tan [c+d x]}{a}\right] \right. \\ & \quad \left. (a+b \tan [c+d x])^n \left(1+\frac{b \tan [c+d x]}{a}\right)^{-n}\right) / (5 d \cot [c+d x]^{5/2}) \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(a+b \tan [c+d x])^n (A+B \tan [c+d x])}{\cot [c+d x]^{3/2}} d x$$

**Problem 661: Unable to integrate problem.**

$$\int \tan [c+d x]^{3/2} (a+b \tan [c+d x])^n (A+B \tan [c+d x]) d x$$

Optimal (type 6, 173 leaves, 9 steps):

$$\frac{1}{5d} (A + iB) \operatorname{AppellF1}\left[\frac{5}{2}, 1, -n, \frac{7}{2}, -i \operatorname{Tan}[c + dx], -\frac{b \operatorname{Tan}[c + dx]}{a}\right]$$

$$\operatorname{Tan}[c + dx]^{5/2} (a + b \operatorname{Tan}[c + dx])^n \left(1 + \frac{b \operatorname{Tan}[c + dx]}{a}\right)^{-n} + \frac{1}{5d}$$

$$(A - iB) \operatorname{AppellF1}\left[\frac{5}{2}, 1, -n, \frac{7}{2}, i \operatorname{Tan}[c + dx], -\frac{b \operatorname{Tan}[c + dx]}{a}\right]$$

$$\operatorname{Tan}[c + dx]^{5/2} (a + b \operatorname{Tan}[c + dx])^n \left(1 + \frac{b \operatorname{Tan}[c + dx]}{a}\right)^{-n}$$

Result (type 8, 35 leaves):

$$\int \operatorname{Tan}[c + dx]^{3/2} (a + b \operatorname{Tan}[c + dx])^n (A + B \operatorname{Tan}[c + dx]) dx$$

**Problem 662: Unable to integrate problem.**

$$\int \sqrt{\operatorname{Tan}[c + dx]} (a + b \operatorname{Tan}[c + dx])^n (A + B \operatorname{Tan}[c + dx]) dx$$

Optimal (type 6, 173 leaves, 9 steps):

$$\frac{1}{3d} (A + iB) \operatorname{AppellF1}\left[\frac{3}{2}, 1, -n, \frac{5}{2}, -i \operatorname{Tan}[c + dx], -\frac{b \operatorname{Tan}[c + dx]}{a}\right]$$

$$\operatorname{Tan}[c + dx]^{3/2} (a + b \operatorname{Tan}[c + dx])^n \left(1 + \frac{b \operatorname{Tan}[c + dx]}{a}\right)^{-n} + \frac{1}{3d}$$

$$(A - iB) \operatorname{AppellF1}\left[\frac{3}{2}, 1, -n, \frac{5}{2}, i \operatorname{Tan}[c + dx], -\frac{b \operatorname{Tan}[c + dx]}{a}\right]$$

$$\operatorname{Tan}[c + dx]^{3/2} (a + b \operatorname{Tan}[c + dx])^n \left(1 + \frac{b \operatorname{Tan}[c + dx]}{a}\right)^{-n}$$

Result (type 8, 35 leaves):

$$\int \sqrt{\operatorname{Tan}[c + dx]} (a + b \operatorname{Tan}[c + dx])^n (A + B \operatorname{Tan}[c + dx]) dx$$

**Problem 663: Unable to integrate problem.**

$$\int \frac{(a + b \operatorname{Tan}[c + dx])^n (A + B \operatorname{Tan}[c + dx])}{\sqrt{\operatorname{Tan}[c + dx]}} dx$$

Optimal (type 6, 167 leaves, 9 steps):

$$\frac{1}{d} (A + iB) \operatorname{AppellF1}\left[\frac{1}{2}, 1, -n, \frac{3}{2}, -i \operatorname{Tan}[c + dx], -\frac{b \operatorname{Tan}[c + dx]}{a}\right]$$

$$\sqrt{\operatorname{Tan}[c + dx]} (a + b \operatorname{Tan}[c + dx])^n \left(1 + \frac{b \operatorname{Tan}[c + dx]}{a}\right)^{-n} + \frac{1}{d}$$

$$(A - iB) \operatorname{AppellF1}\left[\frac{1}{2}, 1, -n, \frac{3}{2}, i \operatorname{Tan}[c + dx], -\frac{b \operatorname{Tan}[c + dx]}{a}\right]$$

$$\sqrt{\operatorname{Tan}[c + dx]} (a + b \operatorname{Tan}[c + dx])^n \left(1 + \frac{b \operatorname{Tan}[c + dx]}{a}\right)^{-n}$$



Result (type 8, 35 leaves):

$$\int \frac{(a + b \tan[c + d x])^n (A + B \tan[c + d x])}{\sqrt{\tan[c + d x]}} dx$$

Problem 664: Unable to integrate problem.

$$\int \frac{(a + b \tan[c + d x])^n (A + B \tan[c + d x])}{\tan[c + d x]^{3/2}} dx$$

Optimal (type 6, 169 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{d \sqrt{\tan[c + d x]}} (A + i B) \operatorname{AppellF1}\left[-\frac{1}{2}, 1, -n, \frac{1}{2}, -i \tan[c + d x], -\frac{b \tan[c + d x]}{a}\right] \\ & (a + b \tan[c + d x])^n \left(1 + \frac{b \tan[c + d x]}{a}\right)^{-n} - \frac{1}{d \sqrt{\tan[c + d x]}} \\ & (A - i B) \operatorname{AppellF1}\left[-\frac{1}{2}, 1, -n, \frac{1}{2}, i \tan[c + d x], -\frac{b \tan[c + d x]}{a}\right] \\ & (a + b \tan[c + d x])^n \left(1 + \frac{b \tan[c + d x]}{a}\right)^{-n} \end{aligned}$$

Result (type 8, 35 leaves):

$$\int \frac{(a + b \tan[c + d x])^n (A + B \tan[c + d x])}{\tan[c + d x]^{3/2}} dx$$

Problem 666: Result more than twice size of optimal antiderivative.

$$\int (a + i a \tan[e + f x]) (A + B \tan[e + f x]) (c - i c \tan[e + f x])^4 dx$$

Optimal (type 3, 59 leaves, 3 steps):

$$\frac{a (i A + B) c^4 (1 - i \tan[e + f x])^4}{4 f} - \frac{a B c^4 (1 - i \tan[e + f x])^5}{5 f}$$

Result (type 3, 226 leaves):

$$\begin{aligned} & \frac{1}{40 f} a c^4 \operatorname{Sec}[e] \operatorname{Sec}[e + f x]^5 \\ & (5 (-5 i A + 3 B) \cos[f x] + 5 (-5 i A + 3 B) \cos[2 e + f x] - 10 i A \cos[2 e + 3 f x] + \\ & 10 B \cos[2 e + 3 f x] - 10 i A \cos[4 e + 3 f x] + 10 B \cos[4 e + 3 f x] + 25 A \sin[f x] + \\ & 15 i B \sin[f x] - 25 A \sin[2 e + f x] - 15 i B \sin[2 e + f x] + \\ & 15 A \sin[2 e + 3 f x] + 5 i B \sin[2 e + 3 f x] - 10 A \sin[4 e + 3 f x] - \\ & 10 i B \sin[4 e + 3 f x] + 5 A \sin[4 e + 5 f x] + 3 i B \sin[4 e + 5 f x]) \end{aligned}$$

Problem 667: Result more than twice size of optimal antiderivative.

$$\int (a + i a \tan[e + f x]) (A + B \tan[e + f x]) (c - i c \tan[e + f x])^3 dx$$

Optimal (type 3, 59 leaves, 3 steps):

$$\frac{a (i A + B) c^3 (1 - i \tan[e + f x])^3}{3 f} - \frac{a B c^3 (1 - i \tan[e + f x])^4}{4 f}$$

Result (type 3, 161 leaves):

$$\frac{1}{12 f} a c^3 \sec[e] \sec[e + f x]^4 \\ (3 (-2 i A + B) \cos[e] + 3 (-i A + B) \cos[e + 2 f x] - 3 i A \cos[3 e + 2 f x] + \\ 3 B \cos[3 e + 2 f x] - 6 A \sin[e] - 3 i B \sin[e] + 5 A \sin[e + 2 f x] + i B \sin[e + 2 f x] - \\ 3 A \sin[3 e + 2 f x] - 3 i B \sin[3 e + 2 f x] + 2 A \sin[3 e + 4 f x] + i B \sin[3 e + 4 f x])$$

**Problem 671: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan[e + f x]) (A + B \tan[e + f x])}{c - i c \tan[e + f x]} dx$$

Optimal (type 3, 54 leaves, 3 steps):

$$\frac{i a B x}{c} + \frac{a B \log[\cos[e + f x]]}{c f} + \frac{a (A - i B)}{c f (i + \tan[e + f x])}$$

Result (type 3, 123 leaves):

$$\frac{1}{2 c f} a (-i \cos[e + f x] + \sin[e + f x]) \\ (\cos[e + f x] (A - i B - 4 B f x + i B \log[\cos[e + f x]^2]) + 2 B \operatorname{ArcTan}[\tan[2 e + f x]] \\ (\cos[e + f x] - i \sin[e + f x]) + (i A + B + 4 i B f x + B \log[\cos[e + f x]^2]) \sin[e + f x])$$

**Problem 675: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan[e + f x]) (A + B \tan[e + f x])}{(c - i c \tan[e + f x])^5} dx$$

Optimal (type 3, 55 leaves, 3 steps):

$$\frac{a (A - i B)}{5 c^5 f (i + \tan[e + f x])^5} + \frac{a B}{4 c^5 f (i + \tan[e + f x])^4}$$

Result (type 3, 124 leaves):

$$-\frac{1}{320 c^5 f} \\ i a (20 A + 5 (6 A + i B) \cos[2 (e + f x)] + 4 (3 A + 2 i B) \cos[4 (e + f x)] - 10 i A \sin[2 (e + f x)] + \\ 15 B \sin[2 (e + f x)] - 8 i A \sin[4 (e + f x)] + 12 B \sin[4 (e + f x)]) \\ (\cos[6 (e + f x)] + i \sin[6 (e + f x)])$$

**Problem 677: Result more than twice size of optimal antiderivative.**

$$\int (a + i a \tan[e + f x])^2 (A + B \tan[e + f x]) (c - i c \tan[e + f x])^5 dx$$

Optimal (type 3, 99 leaves, 3 steps):

$$\frac{2 a^2 (i A + B) c^5 (1 - i \tan[e + f x])^5}{5 f} - \frac{a^2 (i A + 3 B) c^5 (1 - i \tan[e + f x])^6}{6 f} + \frac{a^2 B c^5 (1 - i \tan[e + f x])^7}{7 f}$$

Result (type 3, 254 leaves):

$$\frac{1}{840 f} a^2 c^5 \sec[e] \sec[e + f x]^7 (35 (-7 i A + 3 B) \cos[f x] + 35 (-7 i A + 3 B) \cos[2 e + f x] - 105 i A \cos[2 e + 3 f x] + 105 B \cos[2 e + 3 f x] - 105 i A \cos[4 e + 3 f x] + 105 B \cos[4 e + 3 f x] + 245 A \sin[f x] + 105 i B \sin[f x] - 245 A \sin[2 e + f x] - 105 i B \sin[2 e + f x] + 189 A \sin[2 e + 3 f x] + 21 i B \sin[2 e + 3 f x] - 105 A \sin[4 e + 3 f x] - 105 i B \sin[4 e + 3 f x] + 98 A \sin[4 e + 5 f x] + 42 i B \sin[4 e + 5 f x] + 14 A \sin[6 e + 7 f x] + 6 i B \sin[6 e + 7 f x])$$

**Problem 682: Result more than twice size of optimal antiderivative.**

$$\int (a + i a \tan[e + f x])^2 (A + B \tan[e + f x]) dx$$

Optimal (type 3, 80 leaves, 3 steps):

$$2 a^2 (A - i B) x - \frac{2 a^2 (i A + B) \log[\cos[e + f x]]}{f} - \frac{a^2 (A - i B) \tan[e + f x]}{f} + \frac{B (a + i a \tan[e + f x])^2}{2 f}$$

Result (type 3, 263 leaves):

$$\frac{1}{4 f (\cos[f x] + i \sin[f x])^2} a^2 \sec[e] \sec[e + f x]^2 ((\cos[2 f x] + i \sin[2 f x]) (-8 (A - i B) \operatorname{ArcTan}[\tan[3 e + f x]] \cos[e] \cos[e + f x]^2 - i (4 i A f x \cos[3 e + 2 f x] + 4 B f x \cos[3 e + 2 f x] + (i A + B) \cos[e + 2 f x] (4 f x - i \log[\cos[e + f x]^2]) + A \cos[3 e + 2 f x] \log[\cos[e + f x]^2] - i B \cos[3 e + 2 f x] \log[\cos[e + f x]^2] + 2 \cos[e] (-i B + 4 i A f x + 4 B f x + (A - i B) \log[\cos[e + f x]^2]) + 2 i A \sin[e] + 4 B \sin[e] - 2 i A \sin[e + 2 f x] - 4 B \sin[e + 2 f x]))$$

**Problem 683: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan[e + f x])^2 (A + B \tan[e + f x])}{c - i c \tan[e + f x]} dx$$

Optimal (type 3, 93 leaves, 3 steps):

$$-\frac{a^2 (A - 3iB)x}{c} + \frac{a^2 (iA + 3B) \operatorname{Log}[\operatorname{Cos}[e + fx]]}{cf} - \frac{ia^2 B \operatorname{Tan}[e + fx]}{cf} + \frac{2a^2 (A - iB)}{cf (i + \operatorname{Tan}[e + fx])}$$

Result (type 3, 418 leaves):

$$\frac{1}{2cf (\operatorname{Cos}[fx] + i \operatorname{Sin}[fx])^2 (A \operatorname{Cos}[e + fx] + B \operatorname{Sin}[e + fx])} \\ a^2 \operatorname{Sec}[e] (2 (A - 3iB) fx \operatorname{Cos}[e]^3 \operatorname{Cos}[e + fx] + A fx \operatorname{Cos}[3e] \operatorname{Cos}[e + fx] + \\ 2iA fx \operatorname{Cos}[2e] \operatorname{Cos}[e + fx] \operatorname{Sin}[e] + 6B fx \operatorname{Cos}[2e] \operatorname{Cos}[e + fx] \operatorname{Sin}[e] - \\ 2i \operatorname{Cos}[e]^2 \operatorname{Cos}[e + fx] ((5A - 9iB) fx + (-iA - 3B) \operatorname{Log}[\operatorname{Cos}[e + fx]^2])) \operatorname{Sin}[e] + \\ 2iA fx \operatorname{Cos}[e + fx] \operatorname{Sin}[e]^3 + 6B fx \operatorname{Cos}[e + fx] \operatorname{Sin}[e]^3 - 2 (A - 3iB) \operatorname{ArcTan}[\operatorname{Tan}[3e + fx]] \\ \operatorname{Cos}[e] \operatorname{Cos}[e + fx] (\operatorname{Cos}[2e] - i \operatorname{Sin}[2e]) - 6iB fx \operatorname{Cos}[e + fx] \operatorname{Sin}[e] \operatorname{Sin}[2e] + \\ 2iB \operatorname{Cos}[2e] \operatorname{Sin}[fx] + 2B \operatorname{Sin}[2e] \operatorname{Sin}[fx] + \operatorname{Cos}[e] \operatorname{Cos}[e + fx] \\ (A fx + 2 (iA + B) \operatorname{Cos}[2fx] - i \operatorname{Cos}[2e] (6B fx + (A - 3iB) \operatorname{Log}[\operatorname{Cos}[e + fx]^2])) - \\ 2A fx \operatorname{Sin}[e]^2 + 18iB fx \operatorname{Sin}[e]^2 - 6B fx \operatorname{Sin}[2e] - 2A \operatorname{Sin}[2fx] + 2iB \operatorname{Sin}[2fx])) \\ (-i \operatorname{Cos}[e + fx] + \operatorname{Sin}[e + fx])^2 (A + B \operatorname{Tan}[e + fx])$$

**Problem 684: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + ia \operatorname{Tan}[e + fx])^2 (A + B \operatorname{Tan}[e + fx])}{(c - ic \operatorname{Tan}[e + fx])^2} dx$$

Optimal (type 3, 91 leaves, 3 steps):

$$-\frac{ia^2 Bx}{c^2} - \frac{a^2 B \operatorname{Log}[\operatorname{Cos}[e + fx]]}{c^2 f} + \frac{a^2 (iA + B)}{c^2 f (i + \operatorname{Tan}[e + fx])^2} - \frac{a^2 (A - 3iB)}{c^2 f (i + \operatorname{Tan}[e + fx])}$$

Result (type 3, 184 leaves):

$$\frac{1}{4c^2 f (\operatorname{Cos}[fx] + i \operatorname{Sin}[fx])^2} \\ a^2 (4B - i \operatorname{Cos}[2(e + fx)] (A - iB + 8Bfx - 2iB \operatorname{Log}[\operatorname{Cos}[e + fx]^2]) + A \operatorname{Sin}[2(e + fx)] - \\ iB \operatorname{Sin}[2(e + fx)] - 8Bfx \operatorname{Sin}[2(e + fx)] + 2iB \operatorname{Log}[\operatorname{Cos}[e + fx]^2] \operatorname{Sin}[2(e + fx)] + \\ 4B \operatorname{ArcTan}[\operatorname{Tan}[3e + fx]] (i \operatorname{Cos}[2(e + fx)] + \operatorname{Sin}[2(e + fx)])) \\ (\operatorname{Cos}[2(e + 2fx)] + i \operatorname{Sin}[2(e + 2fx)])$$

**Problem 689: Result more than twice size of optimal antiderivative.**

$$\int (a + ia \operatorname{Tan}[e + fx])^3 (A + B \operatorname{Tan}[e + fx]) (c - ic \operatorname{Tan}[e + fx])^n dx$$

Optimal (type 3, 151 leaves, 3 steps):

$$\frac{4a^3 (iA + B) (c - ic \operatorname{Tan}[e + fx])^n}{fn} - \frac{4a^3 (iA + 2B) (c - ic \operatorname{Tan}[e + fx])^{1+n}}{cf (1+n)} + \\ \frac{a^3 (iA + 5B) (c - ic \operatorname{Tan}[e + fx])^{2+n}}{c^2 f (2+n)} - \frac{a^3 B (c - ic \operatorname{Tan}[e + fx])^{3+n}}{c^3 f (3+n)}$$

Result (type 3, 822 leaves):

$$\begin{aligned}
 & \frac{1}{f (\cos [f x] + i \sin [f x])^3 (A \cos [e + f x] + B \sin [e + f x])} \\
 & \cos [e + f x]^4 \left( \frac{1}{(2+n)(3+n)} \operatorname{Sec}[e] \operatorname{Sec}[e + f x]^2 \right. \\
 & \quad \left. (3 A \cos [e] - 9 i B \cos [e] + A n \cos [e] - 2 i B n \cos [e] + 2 B \sin [e] + B n \sin [e]) \right. \\
 & \quad \left. (-i e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \cos [3 e] - \right. \\
 & \quad \left. e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \sin [3 e]) + \right. \\
 & \quad \left. \frac{1}{(1+n)(2+n)(3+n)} \operatorname{Sec}[e] (12 i A \cos [e] + 12 B \cos [e] + 13 i A n \cos [e] + \right. \\
 & \quad \left. 9 B n \cos [e] + 6 i A n^2 \cos [e] + 6 B n^2 \cos [e] + i A n^3 \cos [e] + B n^3 \cos [e] - 9 A n \sin [e] + \right. \\
 & \quad \left. 13 i B n \sin [e] - 6 A n^2 \sin [e] + 6 i B n^2 \sin [e] - A n^3 \sin [e] + i B n^3 \sin [e]) \right. \\
 & \quad \left. \left( \frac{2 e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \cos [3 e]}{n} - \right. \right. \\
 & \quad \left. \left. \frac{2 i e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \sin [3 e]}{n} \right) \right) + \\
 & \quad \left( (9 A - 13 i B + 6 A n - 6 i B n + A n^2 - i B n^2) \operatorname{Sec}[e] \operatorname{Sec}[e + f x] \right. \\
 & \quad \left. (-2 e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \cos [3 e] + \right. \\
 & \quad \left. 2 i e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \sin [3 e]) \sin [f x] \right) / \\
 & \quad \left( (1+n)(2+n)(3+n) - \frac{1}{3+n} i \operatorname{Sec}[e] \operatorname{Sec}[e + f x]^3 \right. \\
 & \quad \left. (B e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \cos [3 e] - \right. \\
 & \quad \left. i B e^{-i f n x + n (i f x - \log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])} \sin [3 e]) \sin [f x] \right) \\
 & (a + i a \tan [e + f x])^3 (A + B \tan [e + f x]) (c - i c \tan [e + f x])^{n - \frac{n(-\log [c \operatorname{Sec}[e + f x] + \log [c - i c \tan [e + f x]])}{\log [c - i c \tan [e + f x]}}}
 \end{aligned}$$

### Problem 695: Result more than twice size of optimal antiderivative.

$$\int (a + i a \tan [e + f x])^3 (A + B \tan [e + f x]) (c - i c \tan [e + f x]) dx$$

Optimal (type 3, 61 leaves, 3 steps):

$$\frac{a^3 (i A - B) c (1 + i \tan [e + f x])^3}{3 f} - \frac{a^3 B c (1 + i \tan [e + f x])^4}{4 f}$$

Result (type 3, 161 leaves):

$$\begin{aligned}
 & \frac{1}{12 f} a^3 c \operatorname{Sec}[e] \operatorname{Sec}[e + f x]^4 \\
 & (3 (2 i A + B) \cos [e] + 3 (i A + B) \cos [e + 2 f x] + 3 i A \cos [3 e + 2 f x] + 3 B \cos [3 e + 2 f x] - \\
 & \quad 6 A \sin [e] + 3 i B \sin [e] + 5 A \sin [e + 2 f x] - i B \sin [e + 2 f x] - \\
 & \quad 3 A \sin [3 e + 2 f x] + 3 i B \sin [3 e + 2 f x] + 2 A \sin [3 e + 4 f x] - i B \sin [3 e + 4 f x])
 \end{aligned}$$

### Problem 696: Result more than twice size of optimal antiderivative.

$$\int (a + i a \tan[e + f x])^3 (A + B \tan[e + f x]) dx$$

Optimal (type 3, 110 leaves, 4 steps):

$$4 a^3 (A - i B) x - \frac{4 a^3 (i A + B) \operatorname{Log}[\operatorname{Cos}[e + f x]]}{f} - \frac{2 a^3 (A - i B) \operatorname{Tan}[e + f x]}{f} + \frac{a (i A + B) (a + i a \operatorname{Tan}[e + f x])^2}{2 f} + \frac{B (a + i a \operatorname{Tan}[e + f x])^3}{3 f}$$

Result (type 3, 883 leaves):

$$\begin{aligned} & \left( \operatorname{Cos}[e + f x]^4 \left( A \operatorname{Cos}\left[\frac{3 e}{2}\right] - i B \operatorname{Cos}\left[\frac{3 e}{2}\right] - i A \operatorname{Sin}\left[\frac{3 e}{2}\right] - B \operatorname{Sin}\left[\frac{3 e}{2}\right] \right) \right. \\ & \quad \left( -2 i \operatorname{Cos}\left[\frac{3 e}{2}\right] \operatorname{Log}[\operatorname{Cos}[e + f x]^2] - 2 \operatorname{Log}[\operatorname{Cos}[e + f x]^2] \operatorname{Sin}\left[\frac{3 e}{2}\right] \right) \\ & \quad \left. (a + i a \operatorname{Tan}[e + f x])^3 (A + B \operatorname{Tan}[e + f x]) \right) / \\ & \left( f (\operatorname{Cos}[f x] + i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e + f x] + B \operatorname{Sin}[e + f x]) \right) + \\ & \left( \operatorname{Cos}[e + f x]^2 (3 A \operatorname{Cos}[e] - 9 i B \operatorname{Cos}[e] + 2 B \operatorname{Sin}[e]) \left( -\frac{1}{6} i \operatorname{Cos}[3 e] - \frac{1}{6} \operatorname{Sin}[3 e] \right) \right. \\ & \quad \left. (a + i a \operatorname{Tan}[e + f x])^3 (A + B \operatorname{Tan}[e + f x]) \right) / \left( f \left( \operatorname{Cos}\left[\frac{e}{2}\right] - \operatorname{Sin}\left[\frac{e}{2}\right] \right) \right) \\ & \left( \operatorname{Cos}\left[\frac{e}{2}\right] + \operatorname{Sin}\left[\frac{e}{2}\right] \right) (\operatorname{Cos}[f x] + i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e + f x] + B \operatorname{Sin}[e + f x]) \right) + \\ & \left( (A - i B) \operatorname{Cos}[e + f x]^4 (4 f x \operatorname{Cos}[3 e] - 4 i f x \operatorname{Sin}[3 e]) (a + i a \operatorname{Tan}[e + f x])^3 \right. \\ & \quad \left. (A + B \operatorname{Tan}[e + f x]) \right) / \left( f (\operatorname{Cos}[f x] + i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e + f x] + B \operatorname{Sin}[e + f x]) \right) - \\ & \left( i B \operatorname{Cos}[e + f x] \left( \frac{1}{3} \operatorname{Cos}[3 e] - \frac{1}{3} i \operatorname{Sin}[3 e] \right) \operatorname{Sin}[f x] (a + i a \operatorname{Tan}[e + f x])^3 (A + B \operatorname{Tan}[e + f x]) \right) / \\ & \left( f \left( \operatorname{Cos}\left[\frac{e}{2}\right] - \operatorname{Sin}\left[\frac{e}{2}\right] \right) \left( \operatorname{Cos}\left[\frac{e}{2}\right] + \operatorname{Sin}\left[\frac{e}{2}\right] \right) \right. \\ & \quad \left. (\operatorname{Cos}[f x] + i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e + f x] + B \operatorname{Sin}[e + f x]) \right) + \\ & \left( \operatorname{Cos}[e + f x]^3 \left( \frac{1}{3} \operatorname{Cos}[3 e] - \frac{1}{3} i \operatorname{Sin}[3 e] \right) (-9 A \operatorname{Sin}[f x] + 13 i B \operatorname{Sin}[f x]) \right. \\ & \quad \left. (a + i a \operatorname{Tan}[e + f x])^3 (A + B \operatorname{Tan}[e + f x]) \right) / \left( f \left( \operatorname{Cos}\left[\frac{e}{2}\right] - \operatorname{Sin}\left[\frac{e}{2}\right] \right) \right. \\ & \quad \left. \left( \operatorname{Cos}\left[\frac{e}{2}\right] + \operatorname{Sin}\left[\frac{e}{2}\right] \right) (\operatorname{Cos}[f x] + i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e + f x] + B \operatorname{Sin}[e + f x]) \right) + \\ & \quad \frac{1}{(\operatorname{Cos}[f x] + i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e + f x] + B \operatorname{Sin}[e + f x])} \\ & x \operatorname{Cos}[e + f x]^4 (-2 A \operatorname{Cos}[e] + 2 i B \operatorname{Cos}[e] + 2 A \operatorname{Cos}[e]^3 - 2 i B \operatorname{Cos}[e]^3 + 4 i A \operatorname{Sin}[e] + \\ & \quad 4 B \operatorname{Sin}[e] - 8 i A \operatorname{Cos}[e]^2 \operatorname{Sin}[e] - 8 B \operatorname{Cos}[e]^2 \operatorname{Sin}[e] - 12 A \operatorname{Cos}[e] \operatorname{Sin}[e]^2 + \\ & \quad 12 i B \operatorname{Cos}[e] \operatorname{Sin}[e]^2 + 8 i A \operatorname{Sin}[e]^3 + 8 B \operatorname{Sin}[e]^3 + 2 A \operatorname{Sin}[e] \operatorname{Tan}[e] - 2 i B \operatorname{Sin}[e] \operatorname{Tan}[e] + \\ & \quad 2 A \operatorname{Sin}[e]^3 \operatorname{Tan}[e] - 2 i B \operatorname{Sin}[e]^3 \operatorname{Tan}[e] + i (A - i B) (4 \operatorname{Cos}[3 e] - 4 i \operatorname{Sin}[3 e]) \operatorname{Tan}[e]) \\ & \quad (a + i a \operatorname{Tan}[e + f x])^3 (A + B \operatorname{Tan}[e + f x]) \end{aligned}$$

### Problem 697: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan[e + f x])^3 (A + B \tan[e + f x])}{c - i c \tan[e + f x]} dx$$

Optimal (type 3, 119 leaves, 3 steps):

$$-\frac{4 a^3 (A - 2 i B) x}{c} + \frac{4 a^3 (i A + 2 B) \operatorname{Log}[\operatorname{Cos}[e + f x]]}{c f} + \frac{a^3 (A - 4 i B) \tan[e + f x]}{c f} + \frac{a^3 B \tan[e + f x]^2}{2 c f} + \frac{4 a^3 (A - i B)}{c f (i + \tan[e + f x])}$$

Result (type 3, 944 leaves):

$$\begin{aligned}
& \left( (A - i B) \cos[2fx] \cos[e + fx]^4 \left( -\frac{2i \cos[e]}{c} - \frac{2 \sin[e]}{c} \right) (a + ia \tan[e + fx])^3 \right. \\
& \quad \left. (A + B \tan[e + fx]) \right) / \left( f (\cos[fx] + i \sin[fx])^3 (A \cos[e + fx] + B \sin[e + fx]) \right) + \\
& \left( \cos[e + fx]^2 \left( \frac{B \cos[3e]}{2c} - \frac{i B \sin[3e]}{2c} \right) (a + ia \tan[e + fx])^3 (A + B \tan[e + fx]) \right) / \\
& \quad \left( f (\cos[fx] + i \sin[fx])^3 (A \cos[e + fx] + B \sin[e + fx]) \right) + \\
& \left( (A - 2i B) \cos[e + fx]^4 \left( -\frac{4fx \cos[3e]}{c} + \frac{4i fx \sin[3e]}{c} \right) (a + ia \tan[e + fx])^3 \right. \\
& \quad \left. (A + B \tan[e + fx]) \right) / \left( f (\cos[fx] + i \sin[fx])^3 (A \cos[e + fx] + B \sin[e + fx]) \right) + \\
& \left( (i A + 2 B) \cos[e + fx]^4 \left( \frac{2 \cos[3e] \log[\cos[e + fx]^2]}{c} - \frac{2i \log[\cos[e + fx]^2] \sin[3e]}{c} \right) \right. \\
& \quad \left. (a + ia \tan[e + fx])^3 (A + B \tan[e + fx]) \right) / \\
& \quad \left( f (\cos[fx] + i \sin[fx])^3 (A \cos[e + fx] + B \sin[e + fx]) \right) + \\
& \left( \cos[e + fx]^3 \left( \frac{\cos[3e]}{c} - \frac{i \sin[3e]}{c} \right) (A \sin[fx] - 4i B \sin[fx]) \right. \\
& \quad \left. (a + ia \tan[e + fx])^3 (A + B \tan[e + fx]) \right) / \left( f \left( \cos\left[\frac{e}{2}\right] - \sin\left[\frac{e}{2}\right] \right) \right. \\
& \quad \left. \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) (\cos[fx] + i \sin[fx])^3 (A \cos[e + fx] + B \sin[e + fx]) \right) + \\
& \left( (A - i B) \cos[e + fx]^4 \left( \frac{2 \cos[e]}{c} - \frac{2i \sin[e]}{c} \right) \sin[2fx] (a + ia \tan[e + fx])^3 \right. \\
& \quad \left. (A + B \tan[e + fx]) \right) / \left( f (\cos[fx] + i \sin[fx])^3 (A \cos[e + fx] + B \sin[e + fx]) \right) + \\
& \quad 1 \\
& \left( \cos[fx] + i \sin[fx] \right)^3 (A \cos[e + fx] + B \sin[e + fx]) \\
& x \cos[e + fx]^4 \left( \frac{2A \cos[e]}{c} - \frac{4i B \cos[e]}{c} - \frac{2A \cos[e]^3}{c} + \frac{4i B \cos[e]^3}{c} - \right. \\
& \quad \frac{4i A \sin[e]}{c} - \frac{8B \sin[e]}{c} + \frac{8i A \cos[e]^2 \sin[e]}{c} + \frac{16B \cos[e]^2 \sin[e]}{c} + \\
& \quad \frac{12A \cos[e] \sin[e]^2}{c} - \frac{24i B \cos[e] \sin[e]^2}{c} - \frac{8i A \sin[e]^3}{c} - \frac{16B \sin[e]^3}{c} - \\
& \quad \frac{2A \sin[e] \tan[e]}{c} + \frac{4i B \sin[e] \tan[e]}{c} - \frac{2A \sin[e]^3 \tan[e]}{c} + \frac{4i B \sin[e]^3 \tan[e]}{c} - \\
& \quad \left. i (A - 2i B) \left( \frac{4 \cos[3e]}{c} - \frac{4i \sin[3e]}{c} \right) \tan[e] \right) (a + ia \tan[e + fx])^3 (A + B \tan[e + fx])
\end{aligned}$$

**Problem 698: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + ia \tan[e + fx])^3 (A + B \tan[e + fx])}{(c - ic \tan[e + fx])^2} dx$$



Optimal (type 3, 123 leaves, 3 steps):

$$\frac{a^3 (A - 5 i B) x}{c^2} - \frac{a^3 (i A + 5 B) \operatorname{Log}[\operatorname{Cos}[e + f x]]}{c^2 f} +$$

$$\frac{i a^3 B \operatorname{Tan}[e + f x]}{c^2 f} + \frac{2 a^3 (i A + B)}{c^2 f (i + \operatorname{Tan}[e + f x])^2} - \frac{4 a^3 (A - 2 i B)}{c^2 f (i + \operatorname{Tan}[e + f x])}$$

Result (type 3, 1063 leaves):

$$\begin{aligned}
 & \left( (i A + 3 B) \cos[2 f x] \cos[e + f x]^4 \left( \frac{\cos[e]}{c^2} - \frac{i \sin[e]}{c^2} \right) (a + i a \tan[e + f x])^3 \right. \\
 & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (A - i B) \cos[4 f x] \cos[e + f x]^4 \left( -\frac{i \cos[e]}{2 c^2} + \frac{\sin[e]}{2 c^2} \right) (a + i a \tan[e + f x])^3 \right. \\
 & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (A - 5 i B) \cos[e + f x]^4 \left( \frac{f x \cos[3 e]}{c^2} - \frac{i f x \sin[3 e]}{c^2} \right) (a + i a \tan[e + f x])^3 \right. \\
 & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (A - 5 i B) \cos[e + f x]^4 \left( -\frac{i \cos[3 e] \log[\cos[e + f x]^2]}{2 c^2} - \frac{\log[\cos[e + f x]^2] \sin[3 e]}{2 c^2} \right) \right. \\
 & \quad \left. (a + i a \tan[e + f x])^3 (A + B \tan[e + f x]) \right) / \\
 & \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( i B \cos[e + f x]^3 \left( \frac{\cos[3 e]}{c^2} - \frac{i \sin[3 e]}{c^2} \right) \sin[f x] (a + i a \tan[e + f x])^3 (A + B \tan[e + f x]) \right) / \\
 & \left( f \left( \cos\left[\frac{e}{2}\right] - \sin\left[\frac{e}{2}\right] \right) \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) \right. \\
 & \quad \left. (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (A - 3 i B) \cos[e + f x]^4 \left( -\frac{\cos[e]}{c^2} + \frac{i \sin[e]}{c^2} \right) \sin[2 f x] (a + i a \tan[e + f x])^3 \right. \\
 & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (A - i B) \cos[e + f x]^4 \left( \frac{\cos[e]}{2 c^2} + \frac{i \sin[e]}{2 c^2} \right) \sin[4 f x] (a + i a \tan[e + f x])^3 \right. \\
 & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \quad \quad \quad 1 \\
 & \frac{(\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x])}{x \cos[e + f x]^4 \left( -\frac{A \cos[e]}{2 c^2} + \frac{5 i B \cos[e]}{2 c^2} + \frac{A \cos[e]^3}{2 c^2} - \frac{5 i B \cos[e]^3}{2 c^2} + \frac{i A \sin[e]}{c^2} + \frac{5 B \sin[e]}{c^2} - \right. \\
 & \quad \frac{2 i A \cos[e]^2 \sin[e]}{c^2} - \frac{10 B \cos[e]^2 \sin[e]}{c^2} - \frac{3 A \cos[e] \sin[e]^2}{c^2} + \frac{15 i B \cos[e] \sin[e]^2}{c^2} + \\
 & \quad \frac{2 i A \sin[e]^3}{c^2} + \frac{10 B \sin[e]^3}{c^2} + \frac{A \sin[e] \tan[e]}{2 c^2} - \frac{5 i B \sin[e] \tan[e]}{2 c^2} + \\
 & \quad \left. \frac{A \sin[e]^3 \tan[e]}{2 c^2} - \frac{5 i B \sin[e]^3 \tan[e]}{2 c^2} + i (A - 5 i B) \left( \frac{\cos[3 e]}{c^2} - \frac{i \sin[3 e]}{c^2} \right) \tan[e] \right) \\
 & (a + i a \tan[e + f x])^3 (A + B \tan[e + f x])
 \end{aligned}$$

### Problem 702: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan[e + f x])^3 (A + B \tan[e + f x])}{(c - i c \tan[e + f x])^6} dx$$

Optimal (type 3, 127 leaves, 3 steps):

$$\frac{2 a^3 (i A + B)}{3 c^6 f (i + \tan[e + f x])^6} - \frac{4 a^3 (A - 2 i B)}{5 c^6 f (i + \tan[e + f x])^5} - \frac{a^3 (i A + 5 B)}{4 c^6 f (i + \tan[e + f x])^4} - \frac{i a^3 B}{3 c^6 f (i + \tan[e + f x])^3}$$

Result (type 3, 871 leaves):

$$\begin{aligned} & \left( (-i A + B) \cos[6 f x] \cos[e + f x]^4 \left( \frac{\cos[3 e]}{48 c^6} + \frac{i \sin[3 e]}{48 c^6} \right) (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\ & \left( (-3 i A + B) \cos[8 f x] \cos[e + f x]^4 \left( \frac{\cos[5 e]}{64 c^6} + \frac{i \sin[5 e]}{64 c^6} \right) (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\ & \left( (3 A - i B) \cos[10 f x] \cos[e + f x]^4 \left( -\frac{i \cos[7 e]}{80 c^6} + \frac{\sin[7 e]}{80 c^6} \right) (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\ & \left( (A - i B) \cos[12 f x] \cos[e + f x]^4 \left( -\frac{i \cos[9 e]}{96 c^6} + \frac{\sin[9 e]}{96 c^6} \right) (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\ & \left( (A + i B) \cos[e + f x]^4 \left( \frac{\cos[3 e]}{48 c^6} + \frac{i \sin[3 e]}{48 c^6} \right) \sin[6 f x] (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\ & \left( (3 A + i B) \cos[e + f x]^4 \left( \frac{\cos[5 e]}{64 c^6} + \frac{i \sin[5 e]}{64 c^6} \right) \sin[8 f x] (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\ & \left( (3 A - i B) \cos[e + f x]^4 \left( \frac{\cos[7 e]}{80 c^6} + \frac{i \sin[7 e]}{80 c^6} \right) \sin[10 f x] (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\ & \left( (A - i B) \cos[e + f x]^4 \left( \frac{\cos[9 e]}{96 c^6} + \frac{i \sin[9 e]}{96 c^6} \right) \sin[12 f x] (a + i a \tan[e + f x])^3 \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) \end{aligned}$$

### Problem 704: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan[e + f x])^3 (A + B \tan[e + f x])}{(c - i c \tan[e + f x])^8} dx$$

Optimal (type 3, 127 leaves, 3 steps):

$$-\frac{a^3 (i A + B)}{2 c^8 f (i + \tan[e + f x])^8} + \frac{4 a^3 (A - 2 i B)}{7 c^8 f (i + \tan[e + f x])^7} +$$

$$\frac{a^3 (i A + 5 B)}{6 c^8 f (i + \tan[e + f x])^6} + \frac{i a^3 B}{5 c^8 f (i + \tan[e + f x])^5}$$

Result (type 3, 1311 leaves):

$$\left( (-i A + B) \cos[6 f x] \cos[e + f x]^4 \left( \frac{\cos[3 e]}{192 c^8} + \frac{i \sin[3 e]}{192 c^8} \right) (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (-5 i A + 3 B) \cos[8 f x] \cos[e + f x]^4 \left( \frac{\cos[5 e]}{256 c^8} + \frac{i \sin[5 e]}{256 c^8} \right) (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (-5 i A + B) \cos[10 f x] \cos[e + f x]^4 \left( \frac{\cos[7 e]}{160 c^8} + \frac{i \sin[7 e]}{160 c^8} \right) (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (5 A - i B) \cos[12 f x] \cos[e + f x]^4 \left( -\frac{i \cos[9 e]}{192 c^8} + \frac{\sin[9 e]}{192 c^8} \right) (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (5 A - 3 i B) \cos[14 f x] \cos[e + f x]^4 \left( -\frac{i \cos[11 e]}{448 c^8} + \frac{\sin[11 e]}{448 c^8} \right) (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (A - i B) \cos[16 f x] \cos[e + f x]^4 \left( -\frac{i \cos[13 e]}{512 c^8} + \frac{\sin[13 e]}{512 c^8} \right) (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (A + i B) \cos[e + f x]^4 \left( \frac{\cos[3 e]}{192 c^8} + \frac{i \sin[3 e]}{192 c^8} \right) \sin[6 f x] (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (5 A + 3 i B) \cos[e + f x]^4 \left( \frac{\cos[5 e]}{256 c^8} + \frac{i \sin[5 e]}{256 c^8} \right) \sin[8 f x] (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\left( (5 A + i B) \cos[e + f x]^4 \left( \frac{\cos[7 e]}{160 c^8} + \frac{i \sin[7 e]}{160 c^8} \right) \sin[10 f x] (a + i a \tan[e + f x])^3 \right. \\ \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) +$$

$$\begin{aligned}
 & \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (5A - i B) \cos[e + f x]^4 \left( \frac{\cos[9e]}{192 c^8} + \frac{i \sin[9e]}{192 c^8} \right) \sin[12 f x] (a + i a \tan[e + f x])^3 \right. \\
 & \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (5A - 3 i B) \cos[e + f x]^4 \left( \frac{\cos[11e]}{448 c^8} + \frac{i \sin[11e]}{448 c^8} \right) \sin[14 f x] (a + i a \tan[e + f x])^3 \right. \\
 & \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right) + \\
 & \left( (A - i B) \cos[e + f x]^4 \left( \frac{\cos[13e]}{512 c^8} + \frac{i \sin[13e]}{512 c^8} \right) \sin[16 f x] (a + i a \tan[e + f x])^3 \right. \\
 & \left. (A + B \tan[e + f x]) \right) / \left( f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x]) \right)
 \end{aligned}$$

**Problem 707: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^3}{a + i a \tan[e + f x]} dx$$

Optimal (type 3, 121 leaves, 3 steps):

$$\begin{aligned}
 & - \frac{4 (A + 2 i B) c^3 x}{a} - \frac{4 (i A - 2 B) c^3 \log[\cos[e + f x]]}{a f} - \\
 & \frac{4 (A + i B) c^3}{a f (i - \tan[e + f x])} + \frac{(A + 4 i B) c^3 \tan[e + f x]}{a f} + \frac{B c^3 \tan[e + f x]^2}{2 a f}
 \end{aligned}$$

Result (type 3, 972 leaves):

$$\begin{aligned} & \left( \left( -i A c^3 \cos\left[\frac{e}{2}\right] + 2 B c^3 \cos\left[\frac{e}{2}\right] + A c^3 \sin\left[\frac{e}{2}\right] + 2 i B c^3 \sin\left[\frac{e}{2}\right] \right) \right. \\ & \quad \left. \left( -4 i \operatorname{ArcTan}[\tan[f x]] \cos\left[\frac{e}{2}\right] + 4 \operatorname{ArcTan}[\tan[f x]] \sin\left[\frac{e}{2}\right] \right) (\cos[f x] + i \sin[f x]) \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x]) \right) + \\ & \left( \left( -i A c^3 \cos\left[\frac{e}{2}\right] + 2 B c^3 \cos\left[\frac{e}{2}\right] + A c^3 \sin\left[\frac{e}{2}\right] + 2 i B c^3 \sin\left[\frac{e}{2}\right] \right) \right. \\ & \quad \left. \left( 2 \cos\left[\frac{e}{2}\right] \log[\cos[e + f x]^2] + 2 i \log[\cos[e + f x]^2] \sin\left[\frac{e}{2}\right] \right) (\cos[f x] + i \sin[f x]) \right. \\ & \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x]) \right) + \\ & \left( (A + i B) \cos[2 f x] (2 i c^3 \cos[e] + 2 c^3 \sin[e]) (\cos[f x] + i \sin[f x]) (A + B \tan[e + f x]) \right) / \\ & \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x]) \right) + \\ & \left( \sec[e + f x]^2 \left( \frac{1}{2} B c^3 \cos[e] + \frac{1}{2} i B c^3 \sin[e] \right) (\cos[f x] + i \sin[f x]) (A + B \tan[e + f x]) \right) / \\ & \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x]) \right) + \\ & \left( (A + 2 i B) (-4 c^3 f x \cos[e] - 4 i c^3 f x \sin[e]) (\cos[f x] + i \sin[f x]) (A + B \tan[e + f x]) \right) / \\ & \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x]) \right) + \\ & \left( (A + i B) (2 c^3 \cos[e] - 2 i c^3 \sin[e]) (\cos[f x] + i \sin[f x]) \sin[2 f x] (A + B \tan[e + f x]) \right) / \\ & \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x]) \right) + \\ & \left( \sec[e + f x] (\cos[f x] + i \sin[f x]) (i A c^3 \cos[e - f x] - 4 B c^3 \cos[e - f x] - \right. \\ & \quad \left. i A c^3 \cos[e + f x] + 4 B c^3 \cos[e + f x] - A c^3 \sin[e - f x] - 4 i B c^3 \sin[e - f x] + \right. \\ & \quad \left. A c^3 \sin[e + f x] + 4 i B c^3 \sin[e + f x]) (A + B \tan[e + f x]) \right) / \\ & \left( 2 f \left( \cos\left[\frac{e}{2}\right] - \sin\left[\frac{e}{2}\right] \right) \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) (A \cos[e + f x] + B \sin[e + f x]) \right. \\ & \quad \left. (a + i a \tan[e + f x]) \right) + (x (\cos[f x] + i \sin[f x]) \\ & \quad (4 A c^3 \sec[e] + 8 i B c^3 \sec[e] + i (A + 2 i B) (4 c^3 \cos[e] + 4 i c^3 \sin[e]) \tan[e]) \\ & \quad (A + B \tan[e + f x])) / \left( (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x]) \right) \end{aligned}$$

**Problem 709: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])}{a + i a \tan[e + f x]} dx$$

Optimal (type 3, 57 leaves, 3 steps):

$$-\frac{i B c x}{a} + \frac{B c \log[\cos[e + f x]]}{a f} - \frac{(A + i B) c}{a f (i - \tan[e + f x])}$$

Result (type 3, 124 leaves):

$$\begin{aligned} & (c \cos[e + f x] (A + B \tan[e + f x]) (A + i B - i B \log[\cos[e + f x]^2] + \\ & \quad (-i A + B + B \log[\cos[e + f x]^2]) \tan[e + f x] - 2 i B \operatorname{ArcTan}[\tan[f x]] (-i + \tan[e + f x])) / \\ & (2 a f (A \cos[e + f x] + B \sin[e + f x]) (-i + \tan[e + f x])) \end{aligned}$$

### Problem 710: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \tan[e + f x]}{a + i a \tan[e + f x]} dx$$

Optimal (type 3, 47 leaves, 2 steps):

$$\frac{(A - i B) x}{2 a} + \frac{i A - B}{2 f (a + i a \tan[e + f x])}$$

Result (type 3, 102 leaves):

$$\frac{(\cos[e + f x] (A + B \tan[e + f x]) (A - 2 i A f x + B (i - 2 f x) + (B - 2 i B f x + A (-i + 2 f x)) \tan[e + f x]))}{(4 a f (A \cos[e + f x] + B \sin[e + f x]) (-i + \tan[e + f x]))}$$

### Problem 715: Attempted integration timed out after 120 seconds.

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^n}{(a + i a \tan[e + f x])^2} dx$$

Optimal (type 5, 115 leaves, 3 steps):

$$\frac{1}{16 a^2 f n} (i A (2 - n) + B (2 + n)) \text{Hypergeometric2F1}\left[2, n, 1 + n, \frac{1}{2} (1 - i \tan[e + f x])\right] \\ (c - i c \tan[e + f x])^n + \frac{(i A - B) (c - i c \tan[e + f x])^n}{4 a^2 f (1 + i \tan[e + f x])^2}$$

Result (type 1, 1 leaves):

???

### Problem 716: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^5}{(a + i a \tan[e + f x])^2} dx$$

Optimal (type 3, 194 leaves, 3 steps):

$$\frac{8 (3 A + 7 i B) c^5 x}{a^2} + \frac{8 (3 i A - 7 B) c^5 \text{Log}[\cos[e + f x]]}{a^2 f} - \\ \frac{8 (i A - B) c^5}{a^2 f (i - \tan[e + f x])^2} + \frac{16 (2 A + 3 i B) c^5}{a^2 f (i - \tan[e + f x])} - \\ \frac{(7 A + 24 i B) c^5 \tan[e + f x]}{a^2 f} + \frac{(i A - 7 B) c^5 \tan[e + f x]^2}{2 a^2 f} + \frac{i B c^5 \tan[e + f x]^3}{3 a^2 f}$$

Result (type 3, 1357 leaves):

$$\begin{aligned}
& \left( 4 (-3 i A + 5 B) c^5 \cos[2 f x] \sec[e + f x] (\cos[f x] + i \sin[f x])^2 (A + B \tan[e + f x]) \right) / \\
& \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( \sec[e + f x] (3 A c^5 \cos[e] + 7 i B c^5 \cos[e] + 3 i A c^5 \sin[e] - 7 B c^5 \sin[e]) \right. \\
& \quad \left. (8 \operatorname{ArcTan}[\tan[f x]] \cos[e] + 8 i \operatorname{ArcTan}[\tan[f x]] \sin[e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( \sec[e + f x] (3 A c^5 \cos[e] + 7 i B c^5 \cos[e] + 3 i A c^5 \sin[e] - 7 B c^5 \sin[e]) \right. \\
& \quad \left. (4 i \cos[e] \log[\cos[e + f x]^2] - 4 \log[\cos[e + f x]^2] \sin[e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( \sec[e] \sec[e + f x]^3 (3 A \cos[e] + 21 i B \cos[e] + 2 B \sin[e]) \right. \\
& \quad \left. \left( \frac{1}{6} i c^5 \cos[2 e] - \frac{1}{6} c^5 \sin[2 e] \right) (\cos[f x] + i \sin[f x])^2 (A + B \tan[e + f x]) \right) / \\
& \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( (A + i B) \cos[4 f x] \sec[e + f x] (2 i c^5 \cos[2 e] + 2 c^5 \sin[2 e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( (3 A + 7 i B) \sec[e + f x] (8 c^5 f x \cos[2 e] + 8 i c^5 f x \sin[2 e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) - \\
& \left( 4 (3 A + 5 i B) c^5 \sec[e + f x] (\cos[f x] + i \sin[f x])^2 \sin[2 f x] (A + B \tan[e + f x]) \right) / \\
& \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( (A + i B) \sec[e + f x] (2 c^5 \cos[2 e] - 2 i c^5 \sin[2 e]) (\cos[f x] + i \sin[f x])^2 \sin[4 f x] \right. \\
& \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( \sec[e] \sec[e + f x]^4 (\cos[f x] + i \sin[f x])^2 \left( -\frac{1}{2} B c^5 \cos[2 e - f x] + \frac{1}{2} B c^5 \cos[2 e + f x] - \right. \right. \\
& \quad \left. \left. \frac{1}{2} i B c^5 \sin[2 e - f x] + \frac{1}{2} i B c^5 \sin[2 e + f x] \right) (A + B \tan[e + f x]) \right) / \\
& \left( 3 f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( \sec[e] \sec[e + f x]^2 (\cos[f x] + i \sin[f x])^2 \left( -\frac{21}{2} i A c^5 \cos[2 e - f x] + \frac{73}{2} B c^5 \cos[2 e - f x] + \right. \right. \\
& \quad \left. \frac{21}{2} i A c^5 \cos[2 e + f x] - \frac{73}{2} B c^5 \cos[2 e + f x] + \frac{21}{2} A c^5 \sin[2 e - f x] + \frac{73}{2} i B c^5 \right. \\
& \quad \left. \sin[2 e - f x] - \frac{21}{2} A c^5 \sin[2 e + f x] - \frac{73}{2} i B c^5 \sin[2 e + f x] \right) (A + B \tan[e + f x]) \right) / \\
& \left( 3 f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \left( x \sec[e + f x] (\cos[f x] + i \sin[f x])^2 (-24 A c^5 - 56 i B c^5 - 24 i A c^5 \tan[e] + 56 B c^5 \tan[e] + \right. \\
& \quad \left. (-3 i A + 7 B) (8 c^5 \cos[2 e] + 8 i c^5 \sin[2 e]) \tan[e] (A + B \tan[e + f x]) \right) / \\
& \left( (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right)
\end{aligned}$$



Problem 717: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^4}{(a + i a \tan[e + f x])^2} dx$$

Optimal (type 3, 158 leaves, 3 steps):

$$\frac{6 (A + 3 i B) c^4 x}{a^2} + \frac{6 (i A - 3 B) c^4 \text{Log}[\text{Cos}[e + f x]]}{a^2 f} - \frac{4 (i A - B) c^4}{a^2 f (i - \text{Tan}[e + f x])^2} +$$

$$\frac{4 (3 A + 5 i B) c^4}{a^2 f (i - \text{Tan}[e + f x])} - \frac{(A + 6 i B) c^4 \text{Tan}[e + f x]}{a^2 f} - \frac{B c^4 \text{Tan}[e + f x]^2}{2 a^2 f}$$

Result (type 3, 1079 leaves):

$$\begin{aligned}
& c^4 \left( \left( 4 (-i A + 2 B) \cos[2 f x] \sec[e + f x] (\cos[f x] + i \sin[f x])^2 (A + B \tan[e + f x]) \right) / \right. \\
& \quad \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( \sec[e + f x] (A \cos[e] + 3 i B \cos[e] + i A \sin[e] - 3 B \sin[e]) \right. \\
& \quad \quad \left. (6 \operatorname{ArcTan}[\tan[f x]] \cos[e] + 6 i \operatorname{ArcTan}[\tan[f x]] \sin[e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( \sec[e + f x] (A \cos[e] + 3 i B \cos[e] + i A \sin[e] - 3 B \sin[e]) \right. \\
& \quad \quad \left. (3 i \cos[e] \log[\cos[e + f x]^2] - 3 \log[\cos[e + f x]^2] \sin[e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( (A + i B) \cos[4 f x] \sec[e + f x] (i \cos[2 e] + \sin[2 e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( \sec[e + f x]^3 \left( -\frac{1}{2} B \cos[2 e] - \frac{1}{2} i B \sin[2 e] \right) (\cos[f x] + i \sin[f x])^2 (A + B \tan[e + f x]) \right) / \\
& \quad \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( (A + 3 i B) \sec[e + f x] (6 f x \cos[2 e] + 6 i f x \sin[2 e]) (\cos[f x] + i \sin[f x])^2 \right. \\
& \quad \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) - \\
& \quad \left( 4 (A + 2 i B) \sec[e + f x] (\cos[f x] + i \sin[f x])^2 \sin[2 f x] (A + B \tan[e + f x]) \right) / \\
& \quad \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( (A + i B) \sec[e + f x] (\cos[2 e] - i \sin[2 e]) (\cos[f x] + i \sin[f x])^2 \sin[4 f x] \right. \\
& \quad \quad \left. (A + B \tan[e + f x]) \right) / \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( \sec[e] \sec[e + f x]^2 (\cos[f x] + i \sin[f x])^2 \left( -\frac{1}{2} i A \cos[2 e - f x] + 3 B \cos[2 e - f x] + \right. \right. \\
& \quad \quad \left. \frac{1}{2} i A \cos[2 e + f x] - 3 B \cos[2 e + f x] + \frac{1}{2} A \sin[2 e - f x] + 3 i B \sin[2 e - f x] - \right. \\
& \quad \quad \left. \frac{1}{2} A \sin[2 e + f x] - 3 i B \sin[2 e + f x] \right) (A + B \tan[e + f x]) \right) / \\
& \quad \left( f (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) + \\
& \quad \left( x \sec[e + f x] (\cos[f x] + i \sin[f x])^2 (-6 A - 18 i B - 6 i A \tan[e] + 18 B \tan[e] + \right. \\
& \quad \quad \left. (-i A + 3 B) (6 \cos[2 e] + 6 i \sin[2 e]) \tan[e] \right) (A + B \tan[e + f x]) \right) / \\
& \quad \left. \left( (A \cos[e + f x] + B \sin[e + f x]) (a + i a \tan[e + f x])^2 \right) \right)
\end{aligned}$$

**Problem 718: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^3}{(a + i a \tan[e + f x])^2} dx$$

Optimal (type 3, 128 leaves, 3 steps):

$$\frac{(A+5iB)c^3x}{a^2} + \frac{(iA-5B)c^3 \operatorname{Log}[\operatorname{Cos}[e+fx]]}{a^2 f} - \frac{2(iA-B)c^3}{a^2 f (i-\operatorname{Tan}[e+fx])^2} + \frac{4(A+2iB)c^3}{a^2 f (i-\operatorname{Tan}[e+fx])} - \frac{iBc^3 \operatorname{Tan}[e+fx]}{a^2 f}$$

Result (type 3, 1023 leaves):

$$\begin{aligned} & \left( (-iA+3B)c^3 \operatorname{Cos}[2fx] \operatorname{Sec}[e+fx] (\operatorname{Cos}[fx]+i\operatorname{Sin}[fx])^2 (A+B \operatorname{Tan}[e+fx]) \right) / \\ & \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) + \\ & \left( \operatorname{Sec}[e+fx] (A c^3 \operatorname{Cos}[e]+5iB c^3 \operatorname{Cos}[e]+iA c^3 \operatorname{Sin}[e]-5B c^3 \operatorname{Sin}[e]) \right. \\ & \quad \left. (\operatorname{ArcTan}[\operatorname{Tan}[fx]] \operatorname{Cos}[e]+i \operatorname{ArcTan}[\operatorname{Tan}[fx]] \operatorname{Sin}[e]) (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 \right. \\ & \quad \left. (A+B \operatorname{Tan}[e+fx]) \right) / \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) + \\ & \left( \operatorname{Sec}[e+fx] (A c^3 \operatorname{Cos}[e]+5iB c^3 \operatorname{Cos}[e]+iA c^3 \operatorname{Sin}[e]-5B c^3 \operatorname{Sin}[e]) \right. \\ & \quad \left. \left( \frac{1}{2} i \operatorname{Cos}[e] \operatorname{Log}[\operatorname{Cos}[e+fx]^2] - \frac{1}{2} \operatorname{Log}[\operatorname{Cos}[e+fx]^2] \operatorname{Sin}[e] \right) (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 \right. \\ & \quad \left. (A+B \operatorname{Tan}[e+fx]) \right) / \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) + \\ & \left( (A+iB) \operatorname{Cos}[4fx] \operatorname{Sec}[e+fx] \left( \frac{1}{2} i c^3 \operatorname{Cos}[2e] + \frac{1}{2} c^3 \operatorname{Sin}[2e] \right) (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 \right. \\ & \quad \left. (A+B \operatorname{Tan}[e+fx]) \right) / \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) + \\ & \left( (A+5iB) \operatorname{Sec}[e+fx] (c^3 f x \operatorname{Cos}[2e]+i c^3 f x \operatorname{Sin}[2e]) (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 \right. \\ & \quad \left. (A+B \operatorname{Tan}[e+fx]) \right) / \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) - \\ & \left( (A+3iB) c^3 \operatorname{Sec}[e+fx] (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 \operatorname{Sin}[2fx] (A+B \operatorname{Tan}[e+fx]) \right) / \\ & \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) + \\ & \left( (A+iB) \operatorname{Sec}[e+fx] \left( \frac{1}{2} c^3 \operatorname{Cos}[2e] - \frac{1}{2} i c^3 \operatorname{Sin}[2e] \right) (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 \operatorname{Sin}[4fx] \right. \\ & \quad \left. (A+B \operatorname{Tan}[e+fx]) \right) / \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) + \\ & \left( \operatorname{Sec}[e] \operatorname{Sec}[e+fx]^2 (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 \left( \frac{1}{2} B c^3 \operatorname{Cos}[2e-fx] - \frac{1}{2} B c^3 \operatorname{Cos}[2e+fx] + \right. \right. \\ & \quad \left. \left. \frac{1}{2} i B c^3 \operatorname{Sin}[2e-fx] - \frac{1}{2} i B c^3 \operatorname{Sin}[2e+fx] \right) (A+B \operatorname{Tan}[e+fx]) \right) / \\ & \left( f(A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) + \\ & \left( x \operatorname{Sec}[e+fx] (\operatorname{Cos}[fx]+i \operatorname{Sin}[fx])^2 (-A c^3 - 5iB c^3 - iA c^3 \operatorname{Tan}[e] + 5B c^3 \operatorname{Tan}[e] + \right. \\ & \quad \left. (-iA+5B) (c^3 \operatorname{Cos}[2e]+i c^3 \operatorname{Sin}[2e]) \operatorname{Tan}[e] \right) (A+B \operatorname{Tan}[e+fx]) / \\ & \left( (A \operatorname{Cos}[e+fx]+B \operatorname{Sin}[e+fx]) (a+i a \operatorname{Tan}[e+fx])^2 \right) \end{aligned}$$

**Problem 727: Attempted integration timed out after 120 seconds.**

$$\int \frac{(A+B \operatorname{Tan}[e+fx]) (c-i c \operatorname{Tan}[e+fx])^n}{(a+i a \operatorname{Tan}[e+fx])^3} dx$$

Optimal (type 5, 115 leaves, 3 steps):

$$\frac{1}{48 a^3 f n} (\text{i A } (3 - n) + B (3 + n)) \text{Hypergeometric2F1}\left[3, n, 1 + n, \frac{1}{2} (1 - \text{i Tan}[e + f x])\right] \\ (c - \text{i c Tan}[e + f x])^n + \frac{(\text{i A} - B) (c - \text{i c Tan}[e + f x])^n}{6 a^3 f (1 + \text{i Tan}[e + f x])^3}$$

Result (type 1, 1 leaves):

???

**Problem 728: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \text{Tan}[e + f x]) (c - \text{i c Tan}[e + f x])^5}{(a + \text{i a Tan}[e + f x])^3} dx$$

Optimal (type 3, 191 leaves, 3 steps):

$$-\frac{8 (A + 4 \text{i B}) c^5 x}{a^3} - \frac{8 (\text{i A} - 4 B) c^5 \text{Log}[\text{Cos}[e + f x]]}{a^3 f} + \frac{16 (A + \text{i B}) c^5}{3 a^3 f (\text{i} - \text{Tan}[e + f x])^3} + \\ \frac{8 (2 \text{i A} - 3 B) c^5}{a^3 f (\text{i} - \text{Tan}[e + f x])^2} - \frac{8 (3 A + 7 \text{i B}) c^5}{a^3 f (\text{i} - \text{Tan}[e + f x])} + \frac{(A + 8 \text{i B}) c^5 \text{Tan}[e + f x]}{a^3 f} + \frac{B c^5 \text{Tan}[e + f x]^2}{2 a^3 f}$$

Result (type 3, 1496 leaves):

$$\begin{aligned}
 & \left( (A+3iB) \cos[2fx] \sec[e+fx]^2 (6ic^5 \cos[e] - 6c^5 \sin[e]) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( (-iA+2B) \cos[4fx] \sec[e+fx]^2 (2c^5 \cos[e] - 2ic^5 \sin[e]) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( \sec[e+fx]^2 \left( -iAc^5 \cos\left[\frac{3e}{2}\right] + 4Bc^5 \cos\left[\frac{3e}{2}\right] + Ac^5 \sin\left[\frac{3e}{2}\right] + 4iBc^5 \sin\left[\frac{3e}{2}\right] \right) \right. \\
 & \quad \left. \left( 8 \cos\left[\frac{3e}{2}\right] \log[\cos[e+fx]] + 8i \log[\cos[e+fx]] \sin\left[\frac{3e}{2}\right] \right) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( (A+iB) \cos[6fx] \sec[e+fx]^2 \left( \frac{2}{3} ic^5 \cos[3e] + \frac{2}{3} c^5 \sin[3e] \right) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( \sec[e+fx]^4 \left( \frac{1}{2} Bc^5 \cos[3e] + \frac{1}{2} ic^5 \sin[3e] \right) (\cos[fx] + i \sin[fx])^3 (A+B \tan[e+fx]) \right) / \\
 & \quad \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( (A+4iB) \sec[e+fx]^2 (-8c^5 fx \cos[3e] - 8ic^5 fx \sin[3e]) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( (A+3iB) \sec[e+fx]^2 (6c^5 \cos[e] + 6ic^5 \sin[e]) (\cos[fx] + i \sin[fx])^3 \sin[2fx] \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( (A+2iB) \sec[e+fx]^2 (-2c^5 \cos[e] + 2ic^5 \sin[e]) (\cos[fx] + i \sin[fx])^3 \sin[4fx] \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( (A+iB) \sec[e+fx]^2 \left( \frac{2}{3} c^5 \cos[3e] - \frac{2}{3} ic^5 \sin[3e] \right) (\cos[fx] + i \sin[fx])^3 \sin[6fx] \right. \\
 & \quad \left. (A+B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \left( \sec[e+fx]^3 (\cos[fx] + i \sin[fx])^3 \left( \frac{1}{2} ic^5 \cos[3e-fx] - 4Bc^5 \cos[3e-fx] - \right. \right. \\
 & \quad \left. \frac{1}{2} ic^5 \cos[3e+fx] + 4Bc^5 \cos[3e+fx] - \frac{1}{2} Ac^5 \sin[3e-fx] - 4iBc^5 \sin[3e-fx] + \right. \\
 & \quad \left. \frac{1}{2} Ac^5 \sin[3e+fx] + 4iBc^5 \sin[3e+fx] \right) (A+B \tan[e+fx]) \right) / \left( f \left( \cos\left[\frac{e}{2}\right] - \sin\left[\frac{e}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) (A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3 \right) + \\
 & \frac{1}{(A \cos[e+fx] + B \sin[e+fx]) (a+ia \tan[e+fx])^3} \times \sec[e+fx]^2 (\cos[fx] + i \sin[fx])^3 \\
 & \quad (4Ac^5 \cos[e] + 16iBc^5 \cos[e] - 4Ac^5 \cos[e]^3 - 16iBc^5 \cos[e]^3 + 8iAc^5 \sin[e] - \\
 & \quad 32Bc^5 \sin[e] - 16iAc^5 \cos[e]^2 \sin[e] + 64Bc^5 \cos[e]^2 \sin[e] + 24Ac^5 \cos[e] \sin[e]^2 + \\
 & \quad 96iBc^5 \cos[e] \sin[e]^2 + 16iAc^5 \sin[e]^3 - 64Bc^5 \sin[e]^3 - 4Ac^5 \sin[e] \tan[e] - \\
 & \quad 16iBc^5 \sin[e] \tan[e] - 4Ac^5 \sin[e]^3 \tan[e] - 16iBc^5 \sin[e]^3 \tan[e] + \\
 & \quad i(A+4iB) (8c^5 \cos[3e] + 8ic^5 \sin[3e]) \tan[e]) (A+B \tan[e+fx])
 \end{aligned}$$

### Problem 729: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^4}{(a + i a \tan[e + f x])^3} dx$$

Optimal (type 3, 164 leaves, 3 steps):

$$\begin{aligned} & - \frac{(A + 7 i B) c^4 x}{a^3} - \frac{(i A - 7 B) c^4 \operatorname{Log}[\operatorname{Cos}[e + f x]]}{a^3 f} + \frac{8 (A + i B) c^4}{3 a^3 f (i - \tan[e + f x])^3} + \\ & \frac{2 (3 i A - 5 B) c^4}{a^3 f (i - \tan[e + f x])^2} - \frac{6 (A + 3 i B) c^4}{a^3 f (i - \tan[e + f x])} + \frac{i B c^4 \tan[e + f x]}{a^3 f} \end{aligned}$$

Result (type 3, 1239 leaves):

$$\begin{aligned}
 & c^4 \left( \left( (A + 5iB) \cos[2fx] \sec[e+fx]^2 (i \cos[e] - \sin[e]) (\cos[fx] + i \sin[fx])^3 \right. \right. \\
 & \quad \left. \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \right. \\
 & \left( (-iA + 3B) \cos[4fx] \sec[e+fx]^2 \left( \frac{\cos[e]}{2} - \frac{1}{2} i \sin[e] \right) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \left( \sec[e+fx]^2 \left( -iA \cos\left[\frac{3e}{2}\right] + 7B \cos\left[\frac{3e}{2}\right] + A \sin\left[\frac{3e}{2}\right] + 7iB \sin\left[\frac{3e}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{3e}{2}\right] \log[\cos[e+fx]] + i \log[\cos[e+fx]] \sin\left[\frac{3e}{2}\right] \right) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \left( (A + iB) \cos[6fx] \sec[e+fx]^2 \left( \frac{1}{3} i \cos[3e] + \frac{1}{3} \sin[3e] \right) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \left( (A + 7iB) \sec[e+fx]^2 (-fx \cos[3e] - i fx \sin[3e]) (\cos[fx] + i \sin[fx])^3 \right. \\
 & \quad \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \left( (A + 5iB) \sec[e+fx]^2 (\cos[e] + i \sin[e]) (\cos[fx] + i \sin[fx])^3 \sin[2fx] \right. \\
 & \quad \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \left( (A + 3iB) \sec[e+fx]^2 \left( -\frac{\cos[e]}{2} + \frac{1}{2} i \sin[e] \right) (\cos[fx] + i \sin[fx])^3 \sin[4fx] \right. \\
 & \quad \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \left( (A + iB) \sec[e+fx]^2 \left( \frac{1}{3} \cos[3e] - \frac{1}{3} i \sin[3e] \right) (\cos[fx] + i \sin[fx])^3 \sin[6fx] \right. \\
 & \quad \left. (A + B \tan[e+fx]) \right) / \left( f (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \left( \sec[e+fx]^3 (\cos[fx] + i \sin[fx])^3 \left( -\frac{1}{2} B \cos[3e - fx] + \frac{1}{2} B \cos[3e + fx] - \right. \right. \\
 & \quad \left. \left. \frac{1}{2} i B \sin[3e - fx] + \frac{1}{2} i B \sin[3e + fx] \right) (A + B \tan[e+fx]) \right) / \left( f \left( \cos\left[\frac{e}{2}\right] - \sin\left[\frac{e}{2}\right] \right) \right. \\
 & \quad \left. \left( \cos\left[\frac{e}{2}\right] + \sin\left[\frac{e}{2}\right] \right) (A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3 \right) + \\
 & \frac{1}{(A \cos[e+fx] + B \sin[e+fx]) (a + ia \tan[e+fx])^3} \times \sec[e+fx]^2 (\cos[fx] + i \sin[fx])^3 \\
 & \left( \frac{1}{2} A \cos[e] + \frac{7}{2} i B \cos[e] - \frac{1}{2} A \cos[e]^3 - \frac{7}{2} i B \cos[e]^3 + i A \sin[e] - 7 B \sin[e] - \right. \\
 & \quad 2 i A \cos[e]^2 \sin[e] + 14 B \cos[e]^2 \sin[e] + 3 A \cos[e] \sin[e]^2 + 21 i B \cos[e] \sin[e]^2 + 2 i \\
 & \quad A \sin[e]^3 - 14 B \sin[e]^3 - \frac{1}{2} A \sin[e] \tan[e] - \frac{7}{2} i B \sin[e] \tan[e] - \frac{1}{2} A \sin[e]^3 \tan[e] - \\
 & \quad \left. \frac{7}{2} i B \sin[e]^3 \tan[e] + i (A + 7iB) (\cos[3e] + i \sin[3e]) \tan[e] \right) (A + B \tan[e+fx]) \Big)
 \end{aligned}$$

### Problem 756: Result more than twice size of optimal antiderivative.

$$\int (a + i a \tan[e + f x])^3 (A + B \tan[e + f x]) (c - i c \tan[e + f x])^{7/2} dx$$

Optimal (type 3, 144 leaves, 3 steps):

$$\frac{8 a^3 (i A + B) (c - i c \tan[e + f x])^{7/2}}{7 f} - \frac{8 a^3 (i A + 2 B) (c - i c \tan[e + f x])^{9/2}}{9 c f} + \frac{2 a^3 (i A + 5 B) (c - i c \tan[e + f x])^{11/2}}{11 c^2 f} - \frac{2 a^3 B (c - i c \tan[e + f x])^{13/2}}{13 c^3 f}$$

Result (type 3, 441 leaves):

$$\frac{1}{f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x])} \cos[e + f x]^4$$

$$\left( (13 A + i B) \sec[e] \sec[e + f x]^4 (\cos[e] - 9 i \sin[e]) \left( \frac{2 i c^3 \cos[3 e]}{1287} + \frac{2 c^3 \sin[3 e]}{1287} \right) + (13 A + i B) \sec[e] \sec[e + f x]^2 (\cos[e] - 5 i \sin[e]) \left( \frac{32 i c^3 \cos[3 e]}{9009} + \frac{32 c^3 \sin[3 e]}{9009} \right) + \sec[e + f x]^6 \left( \frac{2}{13} B c^3 \cos[3 e] - \frac{2}{13} i B c^3 \sin[3 e] \right) + (13 A + i B) \sec[e] \left( \frac{256 i c^3 \cos[4 e]}{9009} + \frac{256 c^3 \sin[4 e]}{9009} \right) + \sec[e] \sec[e + f x]^5 \left( \frac{2}{143} \cos[3 e] - \frac{2}{143} i \sin[3 e] \right) (13 A c^3 \sin[f x] + i B c^3 \sin[f x]) + \sec[e] \sec[e + f x]^3 \left( \frac{160 \cos[3 e]}{9009} - \frac{160 i \sin[3 e]}{9009} \right) (13 A c^3 \sin[f x] + i B c^3 \sin[f x]) + \sec[e] \sec[e + f x] \left( \frac{256 \cos[3 e]}{9009} - \frac{256 i \sin[3 e]}{9009} \right) (13 A c^3 \sin[f x] + i B c^3 \sin[f x]) \right) \sqrt{\sec[e + f x] (c \cos[e + f x] - i c \sin[e + f x])} (a + i a \tan[e + f x])^3 (A + B \tan[e + f x])$$

### Problem 757: Result more than twice size of optimal antiderivative.

$$\int (a + i a \tan[e + f x])^3 (A + B \tan[e + f x]) (c - i c \tan[e + f x])^{5/2} dx$$

Optimal (type 3, 144 leaves, 3 steps):

$$\frac{8 a^3 (i A + B) (c - i c \tan[e + f x])^{5/2}}{5 f} - \frac{8 a^3 (i A + 2 B) (c - i c \tan[e + f x])^{7/2}}{7 c f} + \frac{2 a^3 (i A + 5 B) (c - i c \tan[e + f x])^{9/2}}{9 c^2 f} - \frac{2 a^3 B (c - i c \tan[e + f x])^{11/2}}{11 c^3 f}$$

Result (type 3, 391 leaves):



$$\begin{aligned}
 & \frac{1}{f (\cos [f x] + i \sin [f x])^3 (A \cos [e + f x] + B \sin [e + f x])} \\
 & \cos [e + f x]^4 \left( (11 i A + B) \sec [e] \sec [e + f x]^2 (\cos [e] - 5 i \sin [e]) \right. \\
 & \quad \left( \frac{16 c^2 \cos [3 e]}{3465} - \frac{16 i c^2 \sin [3 e]}{3465} \right) + \sec [e] \sec [e + f x]^4 \\
 & \quad (11 i A \cos [e] + 10 B \cos [e] + 9 i B \sin [e]) \left( \frac{2}{99} c^2 \cos [3 e] - \frac{2}{99} i c^2 \sin [3 e] \right) + \\
 & \quad (11 i A + B) \sec [e] \left( \frac{128 c^2 \cos [4 e]}{3465} - \frac{128 i c^2 \sin [4 e]}{3465} \right) + \\
 & \quad i B c^2 \sec [e] \sec [e + f x]^5 \left( \frac{2}{11} \cos [3 e] - \frac{2}{11} i \sin [3 e] \right) \sin [f x] + \\
 & \quad \sec [e] \sec [e + f x]^3 \left( \frac{16}{693} \cos [3 e] - \frac{16}{693} i \sin [3 e] \right) (11 A c^2 \sin [f x] - i B c^2 \sin [f x]) + \\
 & \quad \left. \sec [e] \sec [e + f x] \left( \frac{128 \cos [3 e]}{3465} - \frac{128 i \sin [3 e]}{3465} \right) (11 A c^2 \sin [f x] - i B c^2 \sin [f x]) \right) \\
 & \sqrt{\sec [e + f x] (c \cos [e + f x] - i c \sin [e + f x])} (a + i a \tan [e + f x])^3 \\
 & (A + B \tan [e + f x])
 \end{aligned}$$

**Problem 758: Result more than twice size of optimal antiderivative.**

$$\int (a + i a \tan [e + f x])^3 (A + B \tan [e + f x]) (c - i c \tan [e + f x])^{3/2} dx$$

Optimal (type 3, 144 leaves, 3 steps):

$$\begin{aligned}
 & \frac{8 a^3 (i A + B) (c - i c \tan [e + f x])^{3/2}}{3 f} - \frac{8 a^3 (i A + 2 B) (c - i c \tan [e + f x])^{5/2}}{5 c f} + \\
 & \frac{2 a^3 (i A + 5 B) (c - i c \tan [e + f x])^{7/2}}{7 c^2 f} - \frac{2 a^3 B (c - i c \tan [e + f x])^{9/2}}{9 c^3 f}
 \end{aligned}$$

Result (type 3, 319 leaves):

$$\begin{aligned}
 & \frac{1}{f (\cos [f x] + i \sin [f x])^3 (A \cos [e + f x] + B \sin [e + f x])} \\
 & \cos [e + f x]^4 \left( \sec [e] \sec [e + f x]^2 (117 i A \cos [e] + 109 B \cos [e] - 45 A \sin [e] + 85 i B \sin [e]) \right. \\
 & \quad \left( \frac{2}{315} c \cos [3 e] - \frac{2}{315} i c \sin [3 e] \right) + \sec [e + f x]^4 \left( -\frac{2}{9} B c \cos [3 e] + \frac{2}{9} i B c \sin [3 e] \right) + \\
 & \quad (3 i A + B) \sec [e] \left( \frac{64}{315} c \cos [4 e] - \frac{64}{315} i c \sin [4 e] \right) + \\
 & \quad \sec [e] \sec [e + f x] \left( \frac{64}{315} \cos [3 e] - \frac{64}{315} i \sin [3 e] \right) (3 A c \sin [f x] - i B c \sin [f x]) + \\
 & \quad \left. \sec [e] \sec [e + f x]^3 \left( -\frac{2}{63} \cos [3 e] + \frac{2}{63} i \sin [3 e] \right) (9 A c \sin [f x] - 17 i B c \sin [f x]) \right) \\
 & \sqrt{\sec [e + f x] (c \cos [e + f x] - i c \sin [e + f x])} (a + i a \tan [e + f x])^3 (A + B \tan [e + f x])
 \end{aligned}$$

### Problem 762: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan[e + f x])^3 (A + B \tan[e + f x])}{(c - i c \tan[e + f x])^{5/2}} dx$$

Optimal (type 3, 140 leaves, 3 steps):

$$-\frac{8 a^3 (i A + B)}{5 f (c - i c \tan[e + f x])^{5/2}} + \frac{8 a^3 (i A + 2 B)}{3 c f (c - i c \tan[e + f x])^{3/2}} - \frac{2 a^3 (i A + 5 B)}{c^2 f \sqrt{c - i c \tan[e + f x]}} - \frac{2 a^3 B \sqrt{c - i c \tan[e + f x]}}{c^3 f}$$

Result (type 3, 354 leaves):

$$\frac{1}{f (\cos[f x] + i \sin[f x])^3 (A \cos[e + f x] + B \sin[e + f x])} \cos[e + f x]^4 \left( (i A + 11 B) \cos[4 f x] \left( \frac{\cos[e]}{15 c^3} + \frac{i \sin[e]}{15 c^3} \right) + (i A + 11 B) \cos[2 f x] \left( -\frac{4 \cos[e]}{15 c^3} + \frac{4 i \sin[e]}{15 c^3} \right) + (i A + 11 B) \left( -\frac{8 \cos[3 e]}{15 c^3} + \frac{8 i \sin[3 e]}{15 c^3} \right) + (A - i B) \cos[6 f x] \left( -\frac{i \cos[3 e]}{5 c^3} + \frac{\sin[3 e]}{5 c^3} \right) + (A - 11 i B) \left( \frac{4 \cos[e]}{15 c^3} - \frac{4 i \sin[e]}{15 c^3} \right) \sin[2 f x] + (A - 11 i B) \left( -\frac{\cos[e]}{15 c^3} - \frac{i \sin[e]}{15 c^3} \right) \sin[4 f x] + (A - i B) \left( \frac{\cos[3 e]}{5 c^3} + \frac{i \sin[3 e]}{5 c^3} \right) \sin[6 f x] \right) \sqrt{\sec[e + f x] (c \cos[e + f x] - i c \sin[e + f x])} (a + i a \tan[e + f x])^3 (A + B \tan[e + f x])$$

### Problem 763: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + i a \tan[e + f x])^3 (A + B \tan[e + f x])}{(c - i c \tan[e + f x])^{7/2}} dx$$

Optimal (type 3, 142 leaves, 3 steps):

$$-\frac{8 a^3 (i A + B)}{7 f (c - i c \tan[e + f x])^{7/2}} + \frac{8 a^3 (i A + 2 B)}{5 c f (c - i c \tan[e + f x])^{5/2}} - \frac{2 a^3 (i A + 5 B)}{3 c^2 f (c - i c \tan[e + f x])^{3/2}} + \frac{2 a^3 B}{c^3 f \sqrt{c - i c \tan[e + f x]}}$$

Result (type 3, 432 leaves):

$$\frac{1}{f (\cos [f x] + i \sin [f x])^3 (A \cos [e + f x] + B \sin [e + f x])} \cos [e + f x]^4$$

$$\left( (A + 13 i B) \cos [4 f x] \left( \frac{i \cos [e]}{210 c^4} - \frac{\sin [e]}{210 c^4} \right) + (-i A + 13 B) \cos [2 f x] \left( \frac{2 \cos [e]}{105 c^4} - \frac{2 i \sin [e]}{105 c^4} \right) + \right.$$

$$\left. (-3 i A + 4 B) \cos [6 f x] \left( \frac{\cos [3 e]}{35 c^4} + \frac{i \sin [3 e]}{35 c^4} \right) + (-i A + 13 B) \left( \frac{4 \cos [3 e]}{105 c^4} - \frac{4 i \sin [3 e]}{105 c^4} \right) + \right.$$

$$\left. (A - i B) \cos [8 f x] \left( -\frac{i \cos [5 e]}{14 c^4} + \frac{\sin [5 e]}{14 c^4} \right) + (A + 13 i B) \right.$$

$$\left. \left( \frac{2 \cos [e]}{105 c^4} - \frac{2 i \sin [e]}{105 c^4} \right) \sin [2 f x] + (A + 13 i B) \left( -\frac{\cos [e]}{210 c^4} - \frac{i \sin [e]}{210 c^4} \right) \sin [4 f x] + \right.$$

$$\left. (3 A + 4 i B) \left( \frac{\cos [3 e]}{35 c^4} + \frac{i \sin [3 e]}{35 c^4} \right) \sin [6 f x] + (A - i B) \left( \frac{\cos [5 e]}{14 c^4} + \frac{i \sin [5 e]}{14 c^4} \right) \sin [8 f x] \right)$$

$$\sqrt{\sec [e + f x] (c \cos [e + f x] - i c \sin [e + f x])} (a + i a \tan [e + f x])^3 (A + B \tan [e + f x])$$

Problem 764: Attempted integration timed out after 120 seconds.

$$\int \frac{(A + B \tan [e + f x]) (c - i c \tan [e + f x])^{7/2}}{a + i a \tan [e + f x]} dx$$

Optimal (type 3, 220 leaves, 7 steps):

$$-\frac{2 \sqrt{2} (5 i A - 9 B) c^{7/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{c - i c \tan [e + f x]}}{\sqrt{2} \sqrt{c}} \right]}{a f} +$$

$$\frac{2 (5 i A - 9 B) c^3 \sqrt{c - i c \tan [e + f x]}}{a f} + \frac{(5 i A - 9 B) c^2 (c - i c \tan [e + f x])^{3/2}}{3 a f} +$$

$$\frac{(5 i A - 9 B) c (c - i c \tan [e + f x])^{5/2}}{10 a f} + \frac{(i A - B) (c - i c \tan [e + f x])^{7/2}}{2 a f (1 + i \tan [e + f x])}$$

Result (type 1, 1 leaves):

???

Problem 765: Attempted integration timed out after 120 seconds.

$$\int \frac{(A + B \tan [e + f x]) (c - i c \tan [e + f x])^{5/2}}{a + i a \tan [e + f x]} dx$$

Optimal (type 3, 180 leaves, 6 steps):

$$-\frac{\sqrt{2} (3 i A - 7 B) c^{5/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{c - i c \tan [e + f x]}}{\sqrt{2} \sqrt{c}} \right]}{a f} + \frac{(3 i A - 7 B) c^2 \sqrt{c - i c \tan [e + f x]}}{a f} +$$

$$\frac{(3 i A - 7 B) c (c - i c \tan [e + f x])^{3/2}}{6 a f} + \frac{(i A - B) (c - i c \tan [e + f x])^{5/2}}{2 a f (1 + i \tan [e + f x])}$$

Result (type 1, 1 leaves):

???

**Problem 766:** Attempted integration timed out after 120 seconds.

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^{3/2}}{a + i a \tan[e + f x]} dx$$

Optimal (type 3, 144 leaves, 5 steps):

$$\frac{(i A - 5 B) c^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{c - i c \tan[e + f x]}}{\sqrt{2} \sqrt{c}}\right]}{\sqrt{2} a f} + \frac{(i A - 5 B) c \sqrt{c - i c \tan[e + f x]}}{2 a f} + \frac{(i A - B) (c - i c \tan[e + f x])^{3/2}}{2 a f (1 + i \tan[e + f x])}$$

Result (type 1, 1 leaves):

???

**Problem 771:** Attempted integration timed out after 120 seconds.

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^{9/2}}{(a + i a \tan[e + f x])^2} dx$$

Optimal (type 3, 275 leaves, 8 steps):

$$\frac{7 (5 i A - 13 B) c^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{c - i c \tan[e + f x]}}{\sqrt{2} \sqrt{c}}\right]}{\sqrt{2} a^2 f} - \frac{7 (5 i A - 13 B) c^4 \sqrt{c - i c \tan[e + f x]}}{2 a^2 f} - \frac{7 (5 i A - 13 B) c^3 (c - i c \tan[e + f x])^{3/2}}{12 a^2 f} - \frac{7 (5 i A - 13 B) c^2 (c - i c \tan[e + f x])^{5/2}}{40 a^2 f} + \frac{(5 i A - 13 B) c (c - i c \tan[e + f x])^{7/2}}{8 a^2 f (1 + i \tan[e + f x])} + \frac{(i A - B) (c - i c \tan[e + f x])^{9/2}}{4 a^2 f (1 + i \tan[e + f x])^2}$$

Result (type 1, 1 leaves):

???

**Problem 772:** Attempted integration timed out after 120 seconds.

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^{7/2}}{(a + i a \tan[e + f x])^2} dx$$

Optimal (type 3, 238 leaves, 7 steps):

$$\frac{5 (3 i A - 11 B) c^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{c-i c \operatorname{Tan}[e+f x]}}{\sqrt{2} \sqrt{c}}\right]}{2 \sqrt{2} a^2 f} - \frac{5 (3 i A - 11 B) c^3 \sqrt{c-i c \operatorname{Tan}[e+f x]}}{4 a^2 f} - \frac{5 (3 i A - 11 B) c^2 (c-i c \operatorname{Tan}[e+f x])^{3/2}}{24 a^2 f} - \frac{(3 i A - 11 B) c (c-i c \operatorname{Tan}[e+f x])^{5/2}}{8 a^2 f (1+i \operatorname{Tan}[e+f x])} + \frac{(i A - B) (c-i c \operatorname{Tan}[e+f x])^{7/2}}{4 a^2 f (1+i \operatorname{Tan}[e+f x])^2}$$

Result (type 1, 1 leaves):

???

**Problem 773: Attempted integration timed out after 120 seconds.**

$$\int \frac{(A+B \operatorname{Tan}[e+f x]) (c-i c \operatorname{Tan}[e+f x])^{5/2}}{(a+i a \operatorname{Tan}[e+f x])^2} dx$$

Optimal (type 3, 199 leaves, 6 steps):

$$\frac{3 (i A - 9 B) c^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{c-i c \operatorname{Tan}[e+f x]}}{\sqrt{2} \sqrt{c}}\right]}{4 \sqrt{2} a^2 f} - \frac{3 (i A - 9 B) c^2 \sqrt{c-i c \operatorname{Tan}[e+f x]}}{8 a^2 f} - \frac{(i A - 9 B) c (c-i c \operatorname{Tan}[e+f x])^{3/2}}{8 a^2 f (1+i \operatorname{Tan}[e+f x])} + \frac{(i A - B) (c-i c \operatorname{Tan}[e+f x])^{5/2}}{4 a^2 f (1+i \operatorname{Tan}[e+f x])^2}$$

Result (type 1, 1 leaves):

???

**Problem 779: Attempted integration timed out after 120 seconds.**

$$\int \frac{(A+B \operatorname{Tan}[e+f x]) (c-i c \operatorname{Tan}[e+f x])^{9/2}}{(a+i a \operatorname{Tan}[e+f x])^3} dx$$

Optimal (type 3, 291 leaves, 8 steps):

$$-\frac{35 (i A - 5 B) c^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{c-i c \operatorname{Tan}[e+f x]}}{\sqrt{2} \sqrt{c}}\right]}{4 \sqrt{2} a^3 f} + \frac{35 (i A - 5 B) c^4 \sqrt{c-i c \operatorname{Tan}[e+f x]}}{8 a^3 f} + \frac{35 (i A - 5 B) c^3 (c-i c \operatorname{Tan}[e+f x])^{3/2}}{48 a^3 f} + \frac{7 (i A - 5 B) c^2 (c-i c \operatorname{Tan}[e+f x])^{5/2}}{16 a^3 f (1+i \operatorname{Tan}[e+f x])} - \frac{(i A - 5 B) c (c-i c \operatorname{Tan}[e+f x])^{7/2}}{8 a^3 f (1+i \operatorname{Tan}[e+f x])^2} + \frac{(i A - B) (c-i c \operatorname{Tan}[e+f x])^{9/2}}{6 a^3 f (1+i \operatorname{Tan}[e+f x])^3}$$

Result (type 1, 1 leaves):

???

**Problem 780: Attempted integration timed out after 120 seconds.**

$$\int \frac{(A + B \tan[e + f x]) (c - i c \tan[e + f x])^{7/2}}{(a + i a \tan[e + f x])^3} dx$$

Optimal (type 3, 252 leaves, 7 steps):

$$\begin{aligned} & - \frac{5 (i A - 13 B) c^{7/2} \text{ArcTanH}\left[\frac{\sqrt{c - i c \tan[e + f x]}}{\sqrt{2} \sqrt{c}}\right]}{8 \sqrt{2} a^3 f} + \\ & \frac{5 (i A - 13 B) c^3 \sqrt{c - i c \tan[e + f x]}}{16 a^3 f} + \frac{5 (i A - 13 B) c^2 (c - i c \tan[e + f x])^{3/2}}{48 a^3 f (1 + i \tan[e + f x])} - \\ & \frac{(i A - 13 B) c (c - i c \tan[e + f x])^{5/2}}{24 a^3 f (1 + i \tan[e + f x])^2} + \frac{(i A - B) (c - i c \tan[e + f x])^{7/2}}{6 a^3 f (1 + i \tan[e + f x])^3} \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 796: Result more than twice size of optimal antiderivative.**

$$\int (a + i a \tan[e + f x])^{3/2} (A + B \tan[e + f x]) (c - i c \tan[e + f x])^{5/2} dx$$

Optimal (type 3, 226 leaves, 7 steps):

$$\begin{aligned} & - \frac{a^{3/2} (4 i A - B) c^{5/2} \text{ArcTan}\left[\frac{\sqrt{c} \sqrt{a + i a \tan[e + f x]}}{\sqrt{a} \sqrt{c - i c \tan[e + f x]}}\right]}{4 f} + \frac{1}{8 f} \\ & \frac{a (4 A + i B) c^2 \tan[e + f x] \sqrt{a + i a \tan[e + f x]} \sqrt{c - i c \tan[e + f x]} - (4 i A - B) c (a + i a \tan[e + f x])^{3/2} (c - i c \tan[e + f x])^{3/2}}{12 f} + \\ & \frac{B (a + i a \tan[e + f x])^{3/2} (c - i c \tan[e + f x])^{5/2}}{4 f} \end{aligned}$$

Result (type 3, 454 leaves):

$$\left( (-4 \, i \, A + B) \, c^3 \, e^{-i \, (2e+fx)} \, \sqrt{e^{i \, fx}} \, \sqrt{\frac{e^{i \, (e+fx)}}{1 + e^{2 \, i \, (e+fx)}}} \right. \\ \left. \operatorname{ArcTan}\left[e^{i \, (e+fx)}\right] \left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2} \left(A + B \, \operatorname{Tan}[e + fx]\right) \right) / \\ \left( 4 \sqrt{\frac{c}{1 + e^{2 \, i \, (e+fx)}}} \, f \, \operatorname{Sec}[e + fx]^{5/2} \left(\operatorname{Cos}[fx] + i \, \operatorname{Sin}[fx]\right)^{3/2} \left(A \, \operatorname{Cos}[e + fx] + B \, \operatorname{Sin}[e + fx]\right) \right) + \\ \frac{1}{f \left(\operatorname{Cos}[fx] + i \, \operatorname{Sin}[fx]\right) \left(A \, \operatorname{Cos}[e + fx] + B \, \operatorname{Sin}[e + fx]\right)} \\ \frac{\operatorname{Cos}[e + fx]^2 \sqrt{\operatorname{Sec}[e + fx] \left(c \, \operatorname{Cos}[e + fx] - i \, c \, \operatorname{Sin}[e + fx]\right)}}{\left(\operatorname{Sec}[e] \operatorname{Sec}[e + fx]^2 \left(-4 \, i \, A \, \operatorname{Cos}[e] + 4 \, B \, \operatorname{Cos}[e] - 3 \, i \, B \, \operatorname{Sin}[e]\right) \right.} \\ \left. \left(\frac{1}{12} \, c^2 \, \operatorname{Cos}[e] - \frac{1}{12} \, i \, c^2 \, \operatorname{Sin}[e]\right) - i \, B \, c^2 \, \operatorname{Sec}[e] \operatorname{Sec}[e + fx]^3 \left(\frac{\operatorname{Cos}[e]}{4} - \frac{1}{4} \, i \, \operatorname{Sin}[e]\right) \right.} \\ \left. \operatorname{Sin}[fx] + \operatorname{Sec}[e] \operatorname{Sec}[e + fx] \left(\frac{\operatorname{Cos}[e]}{8} - \frac{1}{8} \, i \, \operatorname{Sin}[e]\right) \right) \left(4 \, A \, c^2 \, \operatorname{Sin}[fx] + i \, B \, c^2 \, \operatorname{Sin}[fx]\right) + \\ \left(4 \, A + i \, B\right) \left(\frac{1}{8} \, c^2 \, \operatorname{Cos}[e] - \frac{1}{8} \, i \, c^2 \, \operatorname{Sin}[e]\right) \operatorname{Tan}[e] \left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2} \left(A + B \, \operatorname{Tan}[e + fx]\right)$$

### Problem 804: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2} \left(A + B \, \operatorname{Tan}[e + fx]\right)}{\left(c - i \, c \, \operatorname{Tan}[e + fx]\right)^{11/2}} \, dx$$

Optimal (type 3, 261 leaves, 6 steps):

$$\frac{(i \, A + B) \left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2}}{11 \, f \left(c - i \, c \, \operatorname{Tan}[e + fx]\right)^{11/2}} - \\ \frac{(4 \, i \, A - 7 \, B) \left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2}}{99 \, c \, f \left(c - i \, c \, \operatorname{Tan}[e + fx]\right)^{9/2}} - \frac{(4 \, i \, A - 7 \, B) \left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2}}{231 \, c^2 \, f \left(c - i \, c \, \operatorname{Tan}[e + fx]\right)^{7/2}} - \\ \frac{2 \left(4 \, i \, A - 7 \, B\right) \left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2}}{1155 \, c^3 \, f \left(c - i \, c \, \operatorname{Tan}[e + fx]\right)^{5/2}} - \frac{2 \left(4 \, i \, A - 7 \, B\right) \left(a + i \, a \, \operatorname{Tan}[e + fx]\right)^{3/2}}{3465 \, c^4 \, f \left(c - i \, c \, \operatorname{Tan}[e + fx]\right)^{3/2}}$$

Result (type 3, 569 leaves):

$$\begin{aligned}
 & \frac{1}{f (\cos [f x] + i \sin [f x]) (A \cos [e + f x] + B \sin [e + f x])} \\
 & \cos [e + f x]^2 \left( (-i A + B) \cos [2 f x] \left( \frac{\cos [e]}{96 c^6} + \frac{i \sin [e]}{96 c^6} \right) + (-17 i A + 11 B) \cos [4 f x] \right. \\
 & \quad \left( \frac{\cos [3 e]}{480 c^6} + \frac{i \sin [3 e]}{480 c^6} \right) + (-29 i A + 7 B) \cos [6 f x] \left( \frac{\cos [5 e]}{560 c^6} + \frac{i \sin [5 e]}{560 c^6} \right) + \\
 & \quad (41 A - 7 i B) \cos [8 f x] \left( -\frac{i \cos [7 e]}{1008 c^6} + \frac{\sin [7 e]}{1008 c^6} \right) + (53 A - 31 i B) \cos [10 f x] \\
 & \quad \left( -\frac{i \cos [9 e]}{3168 c^6} + \frac{\sin [9 e]}{3168 c^6} \right) + (A - i B) \cos [12 f x] \left( -\frac{i \cos [11 e]}{352 c^6} + \frac{\sin [11 e]}{352 c^6} \right) + \\
 & \quad (A + i B) \left( \frac{\cos [e]}{96 c^6} + \frac{i \sin [e]}{96 c^6} \right) \sin [2 f x] + (17 A + 11 i B) \left( \frac{\cos [3 e]}{480 c^6} + \frac{i \sin [3 e]}{480 c^6} \right) \sin [4 f x] + \\
 & \quad (29 A + 7 i B) \left( \frac{\cos [5 e]}{560 c^6} + \frac{i \sin [5 e]}{560 c^6} \right) \sin [6 f x] + \\
 & \quad (41 A - 7 i B) \left( \frac{\cos [7 e]}{1008 c^6} + \frac{i \sin [7 e]}{1008 c^6} \right) \sin [8 f x] + (53 A - 31 i B) \\
 & \quad \left( \frac{\cos [9 e]}{3168 c^6} + \frac{i \sin [9 e]}{3168 c^6} \right) \sin [10 f x] + (A - i B) \left( \frac{\cos [11 e]}{352 c^6} + \frac{i \sin [11 e]}{352 c^6} \right) \sin [12 f x] \Big) \\
 & \sqrt{\sec [e + f x] (c \cos [e + f x] - i c \sin [e + f x])} (a + i a \tan [e + f x])^{3/2} \\
 & (A + B \tan [e + f x])
 \end{aligned}$$

**Problem 806: Result more than twice size of optimal antiderivative.**

$$\int (a + i a \tan [e + f x])^{5/2} (A + B \tan [e + f x]) (c - i c \tan [e + f x])^{5/2} dx$$

Optimal (type 3, 213 leaves, 7 steps):

$$\begin{aligned}
 & \frac{3 i a^{5/2} A c^{5/2} \operatorname{ArcTan} \left[ \frac{\sqrt{c} \sqrt{a + i a \tan [e + f x]}}{\sqrt{a} \sqrt{c - i c \tan [e + f x]}} \right]}{4 f} + \\
 & \frac{3 a^2 A c^2 \tan [e + f x] \sqrt{a + i a \tan [e + f x]} \sqrt{c - i c \tan [e + f x]}}{8 f} + \\
 & \frac{a A c \tan [e + f x] (a + i a \tan [e + f x])^{3/2} (c - i c \tan [e + f x])^{3/2}}{4 f} + \\
 & \frac{B (a + i a \tan [e + f x])^{5/2} (c - i c \tan [e + f x])^{5/2}}{5 f}
 \end{aligned}$$

Result (type 3, 459 leaves):



$$\begin{aligned}
 & - \left( \left( 3 \, i \, A \, c^3 \, e^{-i (3 e+f x)} \sqrt{e^{i f x}} \sqrt{\frac{e^{i (e+f x)}}{1+e^{2 i (e+f x)}}} \operatorname{ArcTan}\left[e^{i (e+f x)}\right] \right. \right. \\
 & \quad \left. \left. (a+i a \operatorname{Tan}[e+f x])^{5/2} (A+B \operatorname{Tan}[e+f x]) \right) / \left( 4 \sqrt{\frac{c}{1+e^{2 i (e+f x)}}} f \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^{7/2} (\operatorname{Cos}[f x]+i \operatorname{Sin}[f x])^{5/2} (A \operatorname{Cos}[e+f x]+B \operatorname{Sin}[e+f x]) \right) \right) + \\
 & \quad \frac{1}{f (\operatorname{Cos}[f x]+i \operatorname{Sin}[f x])^2 (A \operatorname{Cos}[e+f x]+B \operatorname{Sin}[e+f x])} \\
 & \quad \operatorname{Cos}[e+f x]^3 \sqrt{\operatorname{Sec}[e+f x] (c \operatorname{Cos}[e+f x]-i c \operatorname{Sin}[e+f x])} \\
 & \quad \left( \operatorname{Sec}[e+f x]^4 \left( \frac{1}{5} B c^2 \operatorname{Cos}[2 e]-\frac{1}{5} i B c^2 \operatorname{Sin}[2 e] \right) + \right. \\
 & \quad A c^2 \operatorname{Sec}[e] \operatorname{Sec}[e+f x]^3 \left( \frac{1}{4} \operatorname{Cos}[2 e]-\frac{1}{4} i \operatorname{Sin}[2 e] \right) \operatorname{Sin}[f x]+ \\
 & \quad A c^2 \operatorname{Sec}[e] \operatorname{Sec}[e+f x] \left( \frac{3}{8} \operatorname{Cos}[2 e]-\frac{3}{8} i \operatorname{Sin}[2 e] \right) \operatorname{Sin}[f x]+ \\
 & \quad \operatorname{Sec}[e+f x]^2 \left( \frac{1}{4} A c^2 \operatorname{Cos}[2 e]-\frac{1}{4} i A c^2 \operatorname{Sin}[2 e] \right) \operatorname{Tan}[e]+ \\
 & \quad \left. \left( \frac{3}{8} A c^2 \operatorname{Cos}[2 e]-\frac{3}{8} i A c^2 \operatorname{Sin}[2 e] \right) \operatorname{Tan}[e] \right) (a+i a \operatorname{Tan}[e+f x])^{5/2} (A+B \operatorname{Tan}[e+f x])
 \end{aligned}$$

**Problem 807: Result more than twice size of optimal antiderivative.**

$$\int (a+i a \operatorname{Tan}[e+f x])^{5/2} (A+B \operatorname{Tan}[e+f x]) (c-i c \operatorname{Tan}[e+f x])^{3/2} dx$$

Optimal (type 3, 222 leaves, 7 steps):

$$\begin{aligned}
 & \frac{a^{5/2} (4 i A+B) c^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{c} \sqrt{a+i a \operatorname{Tan}[e+f x]}}{\sqrt{a} \sqrt{c-i c \operatorname{Tan}[e+f x]}}\right]}{4 f} + \frac{1}{8 f} \\
 & \frac{a^2 (4 A-i B) c \operatorname{Tan}[e+f x] \sqrt{a+i a \operatorname{Tan}[e+f x]} \sqrt{c-i c \operatorname{Tan}[e+f x]} +}{12 f} \\
 & \frac{a (4 i A+B) (a+i a \operatorname{Tan}[e+f x])^{3/2} (c-i c \operatorname{Tan}[e+f x])^{3/2}}{12 f} + \\
 & \frac{B (a+i a \operatorname{Tan}[e+f x])^{5/2} (c-i c \operatorname{Tan}[e+f x])^{3/2}}{4 f}
 \end{aligned}$$

Result (type 3, 460 leaves):

$$\begin{aligned}
 & - \left( \left( i (4A - iB) c^2 e^{-i(3e+fx)} \sqrt{e^{ifx}} \sqrt{\frac{e^{i(e+fx)}}{1+e^{2i(e+fx)}}} \operatorname{ArcTan}[e^{i(e+fx)}] \right. \right. \\
 & \quad \left. \left. (a + ia \operatorname{Tan}[e+fx])^{5/2} (A + B \operatorname{Tan}[e+fx]) \right) / \left( 4 \sqrt{\frac{c}{1+e^{2i(e+fx)}}} f \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+fx]^{7/2} (\operatorname{Cos}[fx] + i \operatorname{Sin}[fx])^{5/2} (A \operatorname{Cos}[e+fx] + B \operatorname{Sin}[e+fx]) \right) \right) + \\
 & \quad \frac{1}{f (\operatorname{Cos}[fx] + i \operatorname{Sin}[fx])^2 (A \operatorname{Cos}[e+fx] + B \operatorname{Sin}[e+fx])} \\
 & \quad \frac{\operatorname{Cos}[e+fx]^3 \sqrt{\operatorname{Sec}[e+fx] (c \operatorname{Cos}[e+fx] - i c \operatorname{Sin}[e+fx])}}{\left( \operatorname{Sec}[e] \operatorname{Sec}[e+fx]^2 (4iA \operatorname{Cos}[e] + 4B \operatorname{Cos}[e] + 3iB \operatorname{Sin}[e]) \right.} \\
 & \quad \left. \left( \frac{1}{12} c \operatorname{Cos}[2e] - \frac{1}{12} i c \operatorname{Sin}[2e] \right) + iBc \operatorname{Sec}[e] \operatorname{Sec}[e+fx]^3 \left( \frac{1}{4} \operatorname{Cos}[2e] - \frac{1}{4} i \operatorname{Sin}[2e] \right) \right) \\
 & \quad \operatorname{Sin}[fx] + \operatorname{Sec}[e] \operatorname{Sec}[e+fx] \left( \frac{1}{8} \operatorname{Cos}[2e] - \frac{1}{8} i \operatorname{Sin}[2e] \right) (4Ac \operatorname{Sin}[fx] - iBc \operatorname{Sin}[fx]) + \\
 & \quad (4A - iB) \left( \frac{1}{8} c \operatorname{Cos}[2e] - \frac{1}{8} i c \operatorname{Sin}[2e] \right) \operatorname{Tan}[e] \left) (a + ia \operatorname{Tan}[e+fx])^{5/2} (A + B \operatorname{Tan}[e+fx]) \right)
 \end{aligned}$$

**Problem 813: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + ia \operatorname{Tan}[e+fx])^{5/2} (A + B \operatorname{Tan}[e+fx])}{(c - ic \operatorname{Tan}[e+fx])^{9/2}} dx$$

Optimal (type 3, 155 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{(iA + B) (a + ia \operatorname{Tan}[e+fx])^{5/2}}{9f (c - ic \operatorname{Tan}[e+fx])^{9/2}} - \\
 & \frac{(2iA - 7B) (a + ia \operatorname{Tan}[e+fx])^{5/2}}{63cf (c - ic \operatorname{Tan}[e+fx])^{7/2}} - \frac{(2iA - 7B) (a + ia \operatorname{Tan}[e+fx])^{5/2}}{315c^2f (c - ic \operatorname{Tan}[e+fx])^{5/2}}
 \end{aligned}$$

Result (type 3, 417 leaves):

$$\begin{aligned}
 & \frac{1}{f (\cos [f x] + i \sin [f x])^2 (A \cos [e + f x] + B \sin [e + f x])} \\
 & \cos [e + f x]^3 \left( (-i A + B) \cos [4 f x] \left( \frac{\cos [2 e]}{40 c^5} + \frac{i \sin [2 e]}{40 c^5} \right) + (-17 i A + 7 B) \cos [6 f x] \right. \\
 & \quad \left. \left( \frac{\cos [4 e]}{280 c^5} + \frac{i \sin [4 e]}{280 c^5} \right) + (25 A - 7 i B) \cos [8 f x] \left( -\frac{i \cos [6 e]}{504 c^5} + \frac{\sin [6 e]}{504 c^5} \right) + \right. \\
 & \quad (A - i B) \cos [10 f x] \left( -\frac{i \cos [8 e]}{72 c^5} + \frac{\sin [8 e]}{72 c^5} \right) + (A + i B) \left( \frac{\cos [2 e]}{40 c^5} + \frac{i \sin [2 e]}{40 c^5} \right) \sin [4 f x] + \\
 & \quad (17 A + 7 i B) \left( \frac{\cos [4 e]}{280 c^5} + \frac{i \sin [4 e]}{280 c^5} \right) \sin [6 f x] + (25 A - 7 i B) \\
 & \quad \left. \left( \frac{\cos [6 e]}{504 c^5} + \frac{i \sin [6 e]}{504 c^5} \right) \sin [8 f x] + (A - i B) \left( \frac{\cos [8 e]}{72 c^5} + \frac{i \sin [8 e]}{72 c^5} \right) \sin [10 f x] \right) \\
 & \sqrt{\sec [e + f x] (c \cos [e + f x] - i c \sin [e + f x])} (a + i a \tan [e + f x])^{5/2} (A + B \tan [e + f x])
 \end{aligned}$$

**Problem 814: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [e + f x])^{5/2} (A + B \tan [e + f x])}{(c - i c \tan [e + f x])^{11/2}} dx$$

Optimal (type 3, 208 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{(i A + B) (a + i a \tan [e + f x])^{5/2}}{11 f (c - i c \tan [e + f x])^{11/2}} - \frac{(3 i A - 8 B) (a + i a \tan [e + f x])^{5/2}}{99 c f (c - i c \tan [e + f x])^{9/2}} \\
 & -\frac{2 (3 i A - 8 B) (a + i a \tan [e + f x])^{5/2}}{693 c^2 f (c - i c \tan [e + f x])^{7/2}} - \frac{2 (3 i A - 8 B) (a + i a \tan [e + f x])^{5/2}}{3465 c^3 f (c - i c \tan [e + f x])^{5/2}}
 \end{aligned}$$

Result (type 3, 495 leaves):

$$\begin{aligned}
& \frac{1}{f \left( \cos [f x] + i \sin [f x] \right)^2 \left( A \cos [e + f x] + B \sin [e + f x] \right)} \\
& \cos [e + f x]^3 \left( (-i A + B) \cos [4 f x] \left( \frac{\cos [2 e]}{80 c^6} + \frac{i \sin [2 e]}{80 c^6} \right) + \right. \\
& \quad \left. (-11 i A + 6 B) \cos [6 f x] \left( \frac{\cos [4 e]}{280 c^6} + \frac{i \sin [4 e]}{280 c^6} \right) + (-24 i A + B) \cos [8 f x] \right. \\
& \quad \left. \left( \frac{\cos [6 e]}{504 c^6} + \frac{i \sin [6 e]}{504 c^6} \right) + (21 A - 10 i B) \cos [10 f x] \left( -\frac{i \cos [8 e]}{792 c^6} + \frac{\sin [8 e]}{792 c^6} \right) + \right. \\
& \quad \left. (A - i B) \cos [12 f x] \left( -\frac{i \cos [10 e]}{176 c^6} + \frac{\sin [10 e]}{176 c^6} \right) + (A + i B) \left( \frac{\cos [2 e]}{80 c^6} + \frac{i \sin [2 e]}{80 c^6} \right) \right) \\
& \sin [4 f x] + (11 A + 6 i B) \left( \frac{\cos [4 e]}{280 c^6} + \frac{i \sin [4 e]}{280 c^6} \right) \sin [6 f x] + \\
& \quad (24 A + i B) \left( \frac{\cos [6 e]}{504 c^6} + \frac{i \sin [6 e]}{504 c^6} \right) \sin [8 f x] + (21 A - 10 i B) \left( \frac{\cos [8 e]}{792 c^6} + \frac{i \sin [8 e]}{792 c^6} \right) \\
& \quad \sin [10 f x] + (A - i B) \left( \frac{\cos [10 e]}{176 c^6} + \frac{i \sin [10 e]}{176 c^6} \right) \sin [12 f x] \Big) \\
& \sqrt{\sec [e + f x] \left( c \cos [e + f x] - i c \sin [e + f x] \right) \left( a + i a \tan [e + f x] \right)^{5/2}} \\
& (A + B \tan [e + f x])
\end{aligned}$$

**Problem 815: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [e + f x])^{5/2} (A + B \tan [e + f x])}{(c - i c \tan [e + f x])^{13/2}} dx$$

Optimal (type 3, 261 leaves, 6 steps):

$$\begin{aligned}
& -\frac{(i A + B) (a + i a \tan [e + f x])^{5/2}}{13 f (c - i c \tan [e + f x])^{13/2}} - \\
& \frac{(4 i A - 9 B) (a + i a \tan [e + f x])^{5/2}}{143 c f (c - i c \tan [e + f x])^{11/2}} - \frac{(4 i A - 9 B) (a + i a \tan [e + f x])^{5/2}}{429 c^2 f (c - i c \tan [e + f x])^{9/2}} - \\
& \frac{2 (4 i A - 9 B) (a + i a \tan [e + f x])^{5/2}}{3003 c^3 f (c - i c \tan [e + f x])^{7/2}} - \frac{2 (4 i A - 9 B) (a + i a \tan [e + f x])^{5/2}}{15015 c^4 f (c - i c \tan [e + f x])^{5/2}}
\end{aligned}$$

Result (type 3, 577 leaves):

$$\begin{aligned}
 & \frac{1}{f \left( \cos [f x] + i \sin [f x] \right)^2 \left( A \cos [e + f x] + B \sin [e + f x] \right)} \\
 & \cos [e + f x]^3 \left( (-i A + B) \cos [4 f x] \left( \frac{\cos [2 e]}{160 c^7} + \frac{i \sin [2 e]}{160 c^7} \right) + \right. \\
 & \quad \left. (-27 i A + 17 B) \cos [6 f x] \left( \frac{\cos [4 e]}{1120 c^7} + \frac{i \sin [4 e]}{1120 c^7} \right) + (-13 i A + 3 B) \cos [8 f x] \right. \\
 & \quad \left. \left( \frac{\cos [6 e]}{336 c^7} + \frac{i \sin [6 e]}{336 c^7} \right) + (17 A - 3 i B) \cos [10 f x] \left( -\frac{i \cos [8 e]}{528 c^7} + \frac{\sin [8 e]}{528 c^7} \right) + \right. \\
 & \quad \left. (63 A - 37 i B) \cos [12 f x] \left( -\frac{i \cos [10 e]}{4576 c^7} + \frac{\sin [10 e]}{4576 c^7} \right) + (A - i B) \cos [14 f x] \right. \\
 & \quad \left. \left( -\frac{i \cos [12 e]}{416 c^7} + \frac{\sin [12 e]}{416 c^7} \right) + (A + i B) \left( \frac{\cos [2 e]}{160 c^7} + \frac{i \sin [2 e]}{160 c^7} \right) \sin [4 f x] + \right. \\
 & \quad \left. (27 A + 17 i B) \left( \frac{\cos [4 e]}{1120 c^7} + \frac{i \sin [4 e]}{1120 c^7} \right) \sin [6 f x] + (13 A + 3 i B) \left( \frac{\cos [6 e]}{336 c^7} + \frac{i \sin [6 e]}{336 c^7} \right) \right. \\
 & \quad \left. \sin [8 f x] + (17 A - 3 i B) \left( \frac{\cos [8 e]}{528 c^7} + \frac{i \sin [8 e]}{528 c^7} \right) \sin [10 f x] + (63 A - 37 i B) \right. \\
 & \quad \left. \left( \frac{\cos [10 e]}{4576 c^7} + \frac{i \sin [10 e]}{4576 c^7} \right) \sin [12 f x] + (A - i B) \left( \frac{\cos [12 e]}{416 c^7} + \frac{i \sin [12 e]}{416 c^7} \right) \sin [14 f x] \right) \\
 & \sqrt{\sec [e + f x] \left( c \cos [e + f x] - i c \sin [e + f x] \right) \left( a + i a \tan [e + f x] \right)^{5/2}} \\
 & (A + B \tan [e + f x])
 \end{aligned}$$

### Problem 817: Result more than twice size of optimal antiderivative.

$$\int (a + i a \tan [e + f x])^{7/2} (A + B \tan [e + f x]) (c - i c \tan [e + f x])^{7/2} dx$$

Optimal (type 3, 267 leaves, 8 steps):

$$\begin{aligned}
 & \frac{5 i a^{7/2} A c^{7/2} \operatorname{ArcTan} \left[ \frac{\sqrt{c} \sqrt{a + i a \tan [e + f x]}}{\sqrt{a} \sqrt{c - i c \tan [e + f x]}} \right]}{8 f} + \\
 & \frac{5 a^3 A c^3 \tan [e + f x] \sqrt{a + i a \tan [e + f x]} \sqrt{c - i c \tan [e + f x]}}{16 f} + \\
 & \frac{5 a^2 A c^2 \tan [e + f x] (a + i a \tan [e + f x])^{3/2} (c - i c \tan [e + f x])^{3/2}}{24 f} + \\
 & \frac{a A c \tan [e + f x] (a + i a \tan [e + f x])^{5/2} (c - i c \tan [e + f x])^{5/2}}{6 f} + \\
 & \frac{B (a + i a \tan [e + f x])^{7/2} (c - i c \tan [e + f x])^{7/2}}{7 f}
 \end{aligned}$$

Result (type 3, 535 leaves):

$$\begin{aligned}
 & - \left( \left( 5 i A c^4 e^{-i (4 e+f x)} \sqrt{e^{i f x}} \sqrt{\frac{e^{i (e+f x)}}{1+e^{2 i (e+f x)}}} \operatorname{ArcTan}\left[e^{i (e+f x)}\right] \right. \right. \\
 & \quad \left. \left. (a+i a \operatorname{Tan}[e+f x])^{7/2} (A+B \operatorname{Tan}[e+f x]) \right) / \left( 8 \sqrt{\frac{c}{1+e^{2 i (e+f x)}}} f \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^{9/2} (\operatorname{Cos}[f x]+i \operatorname{Sin}[f x])^{7/2} (A \operatorname{Cos}[e+f x]+B \operatorname{Sin}[e+f x]) \right) \right) + \\
 & \quad \frac{1}{f (\operatorname{Cos}[f x]+i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e+f x]+B \operatorname{Sin}[e+f x])} \\
 & \quad \operatorname{Cos}[e+f x]^4 \sqrt{\operatorname{Sec}[e+f x] (c \operatorname{Cos}[e+f x]-i c \operatorname{Sin}[e+f x])} \\
 & \quad \left( \operatorname{Sec}[e+f x]^6 \left( \frac{1}{7} B c^3 \operatorname{Cos}[3 e]-\frac{1}{7} i B c^3 \operatorname{Sin}[3 e] \right) + \right. \\
 & \quad A c^3 \operatorname{Sec}[e] \operatorname{Sec}[e+f x]^5 \left( \frac{1}{6} \operatorname{Cos}[3 e]-\frac{1}{6} i \operatorname{Sin}[3 e] \right) \operatorname{Sin}[f x]+ \\
 & \quad A c^3 \operatorname{Sec}[e] \operatorname{Sec}[e+f x]^3 \left( \frac{5}{24} \operatorname{Cos}[3 e]-\frac{5}{24} i \operatorname{Sin}[3 e] \right) \operatorname{Sin}[f x]+ \\
 & \quad A c^3 \operatorname{Sec}[e] \operatorname{Sec}[e+f x] \left( \frac{5}{16} \operatorname{Cos}[3 e]-\frac{5}{16} i \operatorname{Sin}[3 e] \right) \operatorname{Sin}[f x]+ \\
 & \quad \operatorname{Sec}[e+f x]^4 \left( \frac{1}{6} A c^3 \operatorname{Cos}[3 e]-\frac{1}{6} i A c^3 \operatorname{Sin}[3 e] \right) \operatorname{Tan}[e]+ \\
 & \quad \operatorname{Sec}[e+f x]^2 \left( \frac{5}{24} A c^3 \operatorname{Cos}[3 e]-\frac{5}{24} i A c^3 \operatorname{Sin}[3 e] \right) \operatorname{Tan}[e]+ \\
 & \quad \left. \left( \frac{5}{16} A c^3 \operatorname{Cos}[3 e]-\frac{5}{16} i A c^3 \operatorname{Sin}[3 e] \right) \operatorname{Tan}[e] \right) (a+i a \operatorname{Tan}[e+f x])^{7/2} (A+B \operatorname{Tan}[e+f x])
 \end{aligned}$$

**Problem 818: Result more than twice size of optimal antiderivative.**

$$\int (a+i a \operatorname{Tan}[e+f x])^{7/2} (A+B \operatorname{Tan}[e+f x]) (c-i c \operatorname{Tan}[e+f x])^{5/2} dx$$

Optimal (type 3, 284 leaves, 8 steps):

$$\begin{aligned}
 & \frac{a^{7/2} (6 i A+B) c^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{c} \sqrt{a+i a \operatorname{Tan}[e+f x]}}{\sqrt{a} \sqrt{c-i c \operatorname{Tan}[e+f x]}}\right]}{8 f} + \frac{1}{16 f} \\
 & \frac{a^3 (6 A-i B) c^2 \operatorname{Tan}[e+f x] \sqrt{a+i a \operatorname{Tan}[e+f x]} \sqrt{c-i c \operatorname{Tan}[e+f x]}}{24 f} + \\
 & \frac{a^2 (6 A-i B) c \operatorname{Tan}[e+f x] (a+i a \operatorname{Tan}[e+f x])^{3/2} (c-i c \operatorname{Tan}[e+f x])^{3/2}}{30 f} + \\
 & \frac{B (a+i a \operatorname{Tan}[e+f x])^{7/2} (c-i c \operatorname{Tan}[e+f x])^{5/2}}{6 f}
 \end{aligned}$$



$$\begin{aligned}
 & - \left( \left( 2 B e^{-i (4 e+f x)} \sqrt{e^{i f x}} \sqrt{\frac{e^{i (e+f x)}}{1+e^{2 i (e+f x)}}} \operatorname{ArcTan}\left[e^{i (e+f x)}\right] \right. \right. \\
 & \quad \left. \left. (a+i a \operatorname{Tan}[e+f x])^{7/2} (A+B \operatorname{Tan}[e+f x]) \right) / \left( c^3 \sqrt{\frac{c}{1+e^{2 i (e+f x)}}} f \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}[e+f x]^{9/2} (\operatorname{Cos}[f x]+i \operatorname{Sin}[f x])^{7/2} (A \operatorname{Cos}[e+f x]+B \operatorname{Sin}[e+f x]) \right) \right) + \\
 & \frac{1}{f (\operatorname{Cos}[f x]+i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e+f x]+B \operatorname{Sin}[e+f x])} \operatorname{Cos}[e+f x]^4 \\
 & \left( \frac{B \operatorname{Cos}[3 e]}{c^4} + \operatorname{Cos}[4 f x] \left( -\frac{2 B \operatorname{Cos}[e]}{15 c^4} - \frac{2 i B \operatorname{Sin}[e]}{15 c^4} \right) + \operatorname{Cos}[2 f x] \left( \frac{2 B \operatorname{Cos}[e]}{3 c^4} - \frac{2 i B \operatorname{Sin}[e]}{3 c^4} \right) - \right. \\
 & \quad \left. \frac{i B \operatorname{Sin}[3 e]}{c^4} + (-5 i A+9 B) \operatorname{Cos}[6 f x] \left( \frac{\operatorname{Cos}[3 e]}{70 c^4} + \frac{i \operatorname{Sin}[3 e]}{70 c^4} \right) + \right. \\
 & \quad (A-i B) \operatorname{Cos}[8 f x] \left( -\frac{i \operatorname{Cos}[5 e]}{14 c^4} + \frac{\operatorname{Sin}[5 e]}{14 c^4} \right) + \left( \frac{2 i B \operatorname{Cos}[e]}{3 c^4} + \frac{2 B \operatorname{Sin}[e]}{3 c^4} \right) \operatorname{Sin}[2 f x] + \\
 & \quad \left( -\frac{2 i B \operatorname{Cos}[e]}{15 c^4} + \frac{2 B \operatorname{Sin}[e]}{15 c^4} \right) \operatorname{Sin}[4 f x] + (5 A+9 i B) \left( \frac{\operatorname{Cos}[3 e]}{70 c^4} + \frac{i \operatorname{Sin}[3 e]}{70 c^4} \right) \operatorname{Sin}[6 f x] + \\
 & \quad \left. (A-i B) \left( \frac{\operatorname{Cos}[5 e]}{14 c^4} + \frac{i \operatorname{Sin}[5 e]}{14 c^4} \right) \operatorname{Sin}[8 f x] \right) \\
 & \sqrt{\operatorname{Sec}[e+f x] (c \operatorname{Cos}[e+f x]-i c \operatorname{Sin}[e+f x])} (a+i a \operatorname{Tan}[e+f x])^{7/2} (A+B \operatorname{Tan}[e+f x])
 \end{aligned}$$

**Problem 825: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a+i a \operatorname{Tan}[e+f x])^{7/2} (A+B \operatorname{Tan}[e+f x])}{(c-i c \operatorname{Tan}[e+f x])^{9/2}} dx$$

Optimal (type 3, 102 leaves, 3 steps):

$$-\frac{(i A+B)(a+i a \operatorname{Tan}[e+f x])^{7/2}}{9 f (c-i c \operatorname{Tan}[e+f x])^{9/2}} - \frac{(i A-8 B)(a+i a \operatorname{Tan}[e+f x])^{7/2}}{63 c f (c-i c \operatorname{Tan}[e+f x])^{7/2}}$$

Result (type 3, 335 leaves):

$$\begin{aligned}
 & \frac{1}{f (\operatorname{Cos}[f x]+i \operatorname{Sin}[f x])^3 (A \operatorname{Cos}[e+f x]+B \operatorname{Sin}[e+f x])} \operatorname{Cos}[e+f x]^4 \\
 & \left( (-i A+B) \operatorname{Cos}[6 f x] \left( \frac{\operatorname{Cos}[3 e]}{28 c^5} + \frac{i \operatorname{Sin}[3 e]}{28 c^5} \right) + (-8 i A+B) \operatorname{Cos}[8 f x] \left( \frac{\operatorname{Cos}[5 e]}{126 c^5} + \frac{i \operatorname{Sin}[5 e]}{126 c^5} \right) + \right. \\
 & \quad (A-i B) \operatorname{Cos}[10 f x] \left( -\frac{i \operatorname{Cos}[7 e]}{36 c^5} + \frac{\operatorname{Sin}[7 e]}{36 c^5} \right) + (A+i B) \left( \frac{\operatorname{Cos}[3 e]}{28 c^5} + \frac{i \operatorname{Sin}[3 e]}{28 c^5} \right) \operatorname{Sin}[6 f x] + \\
 & \quad \left. (8 A+i B) \left( \frac{\operatorname{Cos}[5 e]}{126 c^5} + \frac{i \operatorname{Sin}[5 e]}{126 c^5} \right) \operatorname{Sin}[8 f x] + (A-i B) \left( \frac{\operatorname{Cos}[7 e]}{36 c^5} + \frac{i \operatorname{Sin}[7 e]}{36 c^5} \right) \operatorname{Sin}[10 f x] \right) \\
 & \sqrt{\operatorname{Sec}[e+f x] (c \operatorname{Cos}[e+f x]-i c \operatorname{Sin}[e+f x])} (a+i a \operatorname{Tan}[e+f x])^{7/2} (A+B \operatorname{Tan}[e+f x])
 \end{aligned}$$



**Problem 826: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan[e + f x])^{7/2} (A + B \tan[e + f x])}{(c - i c \tan[e + f x])^{11/2}} dx$$

Optimal (type 3, 155 leaves, 4 steps):

$$\begin{aligned} & - \frac{(i A + B) (a + i a \tan[e + f x])^{7/2}}{11 f (c - i c \tan[e + f x])^{11/2}} - \\ & \frac{(2 i A - 9 B) (a + i a \tan[e + f x])^{7/2}}{99 c f (c - i c \tan[e + f x])^{9/2}} - \frac{(2 i A - 9 B) (a + i a \tan[e + f x])^{7/2}}{693 c^2 f (c - i c \tan[e + f x])^{7/2}} \end{aligned}$$

Result (type 3, 417 leaves):

$$\begin{aligned} & \frac{1}{f (\cos[fx] + i \sin[fx])^3 (A \cos[e + fx] + B \sin[e + fx])} \\ & \cos[e + fx]^4 \left( (-i A + B) \cos[6fx] \left( \frac{\cos[3e]}{56 c^6} + \frac{i \sin[3e]}{56 c^6} \right) + (-23 i A + 9 B) \cos[8fx] \right. \\ & \quad \left( \frac{\cos[5e]}{504 c^6} + \frac{i \sin[5e]}{504 c^6} \right) + (31 A - 9 i B) \cos[10fx] \left( -\frac{i \cos[7e]}{792 c^6} + \frac{\sin[7e]}{792 c^6} \right) + \\ & \quad (A - i B) \cos[12fx] \left( -\frac{i \cos[9e]}{88 c^6} + \frac{\sin[9e]}{88 c^6} \right) + (A + i B) \left( \frac{\cos[3e]}{56 c^6} + \frac{i \sin[3e]}{56 c^6} \right) \sin[6fx] + \\ & \quad (23 A + 9 i B) \left( \frac{\cos[5e]}{504 c^6} + \frac{i \sin[5e]}{504 c^6} \right) \sin[8fx] + (31 A - 9 i B) \\ & \quad \left. \left( \frac{\cos[7e]}{792 c^6} + \frac{i \sin[7e]}{792 c^6} \right) \sin[10fx] + (A - i B) \left( \frac{\cos[9e]}{88 c^6} + \frac{i \sin[9e]}{88 c^6} \right) \sin[12fx] \right) \\ & \sqrt{\sec[e + fx] (c \cos[e + fx] - i c \sin[e + fx])} (a + i a \tan[e + fx])^{7/2} (A + B \tan[e + fx]) \end{aligned}$$

**Problem 827: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan[e + f x])^{7/2} (A + B \tan[e + f x])}{(c - i c \tan[e + f x])^{13/2}} dx$$

Optimal (type 3, 208 leaves, 5 steps):

$$\begin{aligned} & - \frac{(i A + B) (a + i a \tan[e + f x])^{7/2}}{13 f (c - i c \tan[e + f x])^{13/2}} - \frac{(3 i A - 10 B) (a + i a \tan[e + f x])^{7/2}}{143 c f (c - i c \tan[e + f x])^{11/2}} - \\ & \frac{2 (3 i A - 10 B) (a + i a \tan[e + f x])^{7/2}}{1287 c^2 f (c - i c \tan[e + f x])^{9/2}} - \frac{2 (3 i A - 10 B) (a + i a \tan[e + f x])^{7/2}}{9009 c^3 f (c - i c \tan[e + f x])^{7/2}} \end{aligned}$$

Result (type 3, 495 leaves):

$$\frac{1}{f \left( \cos [f x] + i \sin [f x] \right)^3 \left( A \cos [e + f x] + B \sin [e + f x] \right)}$$

$$\cos [e + f x]^4 \left( (-i A + B) \cos [6 f x] \left( \frac{\cos [3 e]}{112 c^7} + \frac{i \sin [3 e]}{112 c^7} \right) + \right.$$

$$\left. (-15 i A + 8 B) \cos [8 f x] \left( \frac{\cos [5 e]}{504 c^7} + \frac{i \sin [5 e]}{504 c^7} \right) + (-30 i A + B) \cos [10 f x] \right.$$

$$\left. \left( \frac{\cos [7 e]}{792 c^7} + \frac{i \sin [7 e]}{792 c^7} \right) + (25 A - 12 i B) \cos [12 f x] \left( -\frac{i \cos [9 e]}{1144 c^7} + \frac{\sin [9 e]}{1144 c^7} \right) + \right.$$

$$\left. (A - i B) \cos [14 f x] \left( -\frac{i \cos [11 e]}{208 c^7} + \frac{\sin [11 e]}{208 c^7} \right) + (A + i B) \left( \frac{\cos [3 e]}{112 c^7} + \frac{i \sin [3 e]}{112 c^7} \right) \right.$$

$$\sin [6 f x] + (15 A + 8 i B) \left( \frac{\cos [5 e]}{504 c^7} + \frac{i \sin [5 e]}{504 c^7} \right) \sin [8 f x] +$$

$$(30 A + i B) \left( \frac{\cos [7 e]}{792 c^7} + \frac{i \sin [7 e]}{792 c^7} \right) \sin [10 f x] + (25 A - 12 i B) \left( \frac{\cos [9 e]}{1144 c^7} + \frac{i \sin [9 e]}{1144 c^7} \right)$$

$$\sin [12 f x] + (A - i B) \left( \frac{\cos [11 e]}{208 c^7} + \frac{i \sin [11 e]}{208 c^7} \right) \sin [14 f x] \Bigg)$$

$$\sqrt{\sec [e + f x] \left( c \cos [e + f x] - i c \sin [e + f x] \right) \left( a + i a \tan [e + f x] \right)^{7/2}}$$

$$(A + B \tan [e + f x])$$

**Problem 828: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [e + f x])^{7/2} (A + B \tan [e + f x])}{(c - i c \tan [e + f x])^{15/2}} dx$$

Optimal (type 3, 261 leaves, 6 steps):

$$\frac{(i A + B) (a + i a \tan [e + f x])^{7/2}}{15 f (c - i c \tan [e + f x])^{15/2}} -$$

$$\frac{(4 i A - 11 B) (a + i a \tan [e + f x])^{7/2}}{195 c f (c - i c \tan [e + f x])^{13/2}} - \frac{(4 i A - 11 B) (a + i a \tan [e + f x])^{7/2}}{715 c^2 f (c - i c \tan [e + f x])^{11/2}} -$$

$$\frac{2 (4 i A - 11 B) (a + i a \tan [e + f x])^{7/2}}{6435 c^3 f (c - i c \tan [e + f x])^{9/2}} - \frac{2 (4 i A - 11 B) (a + i a \tan [e + f x])^{7/2}}{45045 c^4 f (c - i c \tan [e + f x])^{7/2}}$$

Result (type 3, 577 leaves):

$$\begin{aligned}
 & \frac{1}{f (\cos [f x] + i \sin [f x])^3 (A \cos [e + f x] + B \sin [e + f x])} \\
 & \cos [e + f x]^4 \left( (-i A + B) \cos [6 f x] \left( \frac{\cos [3 e]}{224 c^8} + \frac{i \sin [3 e]}{224 c^8} \right) + \right. \\
 & \quad (-37 i A + 23 B) \cos [8 f x] \left( \frac{\cos [5 e]}{2016 c^8} + \frac{i \sin [5 e]}{2016 c^8} \right) + (-49 i A + 11 B) \cos [10 f x] \\
 & \quad \left( \frac{\cos [7 e]}{1584 c^8} + \frac{i \sin [7 e]}{1584 c^8} \right) + (61 A - 11 i B) \cos [12 f x] \left( -\frac{i \cos [9 e]}{2288 c^8} + \frac{\sin [9 e]}{2288 c^8} \right) + \\
 & \quad (73 A - 43 i B) \cos [14 f x] \left( -\frac{i \cos [11 e]}{6240 c^8} + \frac{\sin [11 e]}{6240 c^8} \right) + (A - i B) \cos [16 f x] \\
 & \quad \left( -\frac{i \cos [13 e]}{480 c^8} + \frac{\sin [13 e]}{480 c^8} \right) + (A + i B) \left( \frac{\cos [3 e]}{224 c^8} + \frac{i \sin [3 e]}{224 c^8} \right) \sin [6 f x] + \\
 & \quad (37 A + 23 i B) \left( \frac{\cos [5 e]}{2016 c^8} + \frac{i \sin [5 e]}{2016 c^8} \right) \sin [8 f x] + (49 A + 11 i B) \left( \frac{\cos [7 e]}{1584 c^8} + \frac{i \sin [7 e]}{1584 c^8} \right) \\
 & \quad \sin [10 f x] + (61 A - 11 i B) \left( \frac{\cos [9 e]}{2288 c^8} + \frac{i \sin [9 e]}{2288 c^8} \right) \sin [12 f x] + (73 A - 43 i B) \\
 & \quad \left( \frac{\cos [11 e]}{6240 c^8} + \frac{i \sin [11 e]}{6240 c^8} \right) \sin [14 f x] + (A - i B) \left( \frac{\cos [13 e]}{480 c^8} + \frac{i \sin [13 e]}{480 c^8} \right) \sin [16 f x] \Big) \\
 & \sqrt{\sec [e + f x] (c \cos [e + f x] - i c \sin [e + f x])} (a + i a \tan [e + f x])^{7/2} \\
 & (A + B \tan [e + f x])
 \end{aligned}$$

**Problem 829: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + i a \tan [e + f x])^{7/2} (A + B \tan [e + f x])}{(c - i c \tan [e + f x])^{17/2}} dx$$

Optimal (type 3, 314 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{(i A + B) (a + i a \tan [e + f x])^{7/2}}{17 f (c - i c \tan [e + f x])^{17/2}} - \frac{(5 i A - 12 B) (a + i a \tan [e + f x])^{7/2}}{255 c f (c - i c \tan [e + f x])^{15/2}} - \\
 & \frac{4 (5 i A - 12 B) (a + i a \tan [e + f x])^{7/2}}{3315 c^2 f (c - i c \tan [e + f x])^{13/2}} - \frac{4 (5 i A - 12 B) (a + i a \tan [e + f x])^{7/2}}{12155 c^3 f (c - i c \tan [e + f x])^{11/2}} - \\
 & \frac{8 (5 i A - 12 B) (a + i a \tan [e + f x])^{7/2}}{109395 c^4 f (c - i c \tan [e + f x])^{9/2}} - \frac{8 (5 i A - 12 B) (a + i a \tan [e + f x])^{7/2}}{765765 c^5 f (c - i c \tan [e + f x])^{7/2}}
 \end{aligned}$$

Result (type 3, 655 leaves):

$$\begin{aligned}
 & \frac{1}{f \left( \cos [f x] + i \sin [f x] \right)^3 \left( A \cos [e + f x] + B \sin [e + f x] \right)} \\
 & \cos [e + f x]^4 \left( (-i A + B) \cos [6 f x] \left( \frac{\cos [3 e]}{448 c^9} + \frac{i \sin [3 e]}{448 c^9} \right) + \right. \\
 & \quad (-22 i A + 15 B) \cos [8 f x] \left( \frac{\cos [5 e]}{2016 c^9} + \frac{i \sin [5 e]}{2016 c^9} \right) + \\
 & \quad (-145 i A + 51 B) \cos [10 f x] \left( \frac{\cos [7 e]}{6336 c^9} + \frac{i \sin [7 e]}{6336 c^9} \right) + (-60 i A + B) \cos [12 f x] \\
 & \quad \left( \frac{\cos [9 e]}{2288 c^9} + \frac{i \sin [9 e]}{2288 c^9} \right) + (215 A - 69 i B) \cos [14 f x] \left( -\frac{i \cos [11 e]}{12480 c^9} + \frac{\sin [11 e]}{12480 c^9} \right) + \\
 & \quad (50 A - 33 i B) \cos [16 f x] \left( -\frac{i \cos [13 e]}{8160 c^9} + \frac{\sin [13 e]}{8160 c^9} \right) + (A - i B) \cos [18 f x] \\
 & \quad \left( -\frac{i \cos [15 e]}{1088 c^9} + \frac{\sin [15 e]}{1088 c^9} \right) + (A + i B) \left( \frac{\cos [3 e]}{448 c^9} + \frac{i \sin [3 e]}{448 c^9} \right) \sin [6 f x] + \\
 & \quad (22 A + 15 i B) \left( \frac{\cos [5 e]}{2016 c^9} + \frac{i \sin [5 e]}{2016 c^9} \right) \sin [8 f x] + (145 A + 51 i B) \\
 & \quad \left( \frac{\cos [7 e]}{6336 c^9} + \frac{i \sin [7 e]}{6336 c^9} \right) \sin [10 f x] + (60 A + i B) \left( \frac{\cos [9 e]}{2288 c^9} + \frac{i \sin [9 e]}{2288 c^9} \right) \sin [12 f x] + \\
 & \quad (215 A - 69 i B) \left( \frac{\cos [11 e]}{12480 c^9} + \frac{i \sin [11 e]}{12480 c^9} \right) \sin [14 f x] + (50 A - 33 i B) \\
 & \quad \left( \frac{\cos [13 e]}{8160 c^9} + \frac{i \sin [13 e]}{8160 c^9} \right) \sin [16 f x] + (A - i B) \left( \frac{\cos [15 e]}{1088 c^9} + \frac{i \sin [15 e]}{1088 c^9} \right) \sin [18 f x] \Big) \\
 & \sqrt{\sec [e + f x] \left( c \cos [e + f x] - i c \sin [e + f x] \right) \left( a + i a \tan [e + f x] \right)^{7/2}} \\
 & (A + B \tan [e + f x])
 \end{aligned}$$

**Problem 855: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \tan [e + f x]) (c + d \tan [e + f x])}{(a + i a \tan [e + f x])^{3/2}} dx$$

Optimal (type 3, 147 leaves, 4 steps):

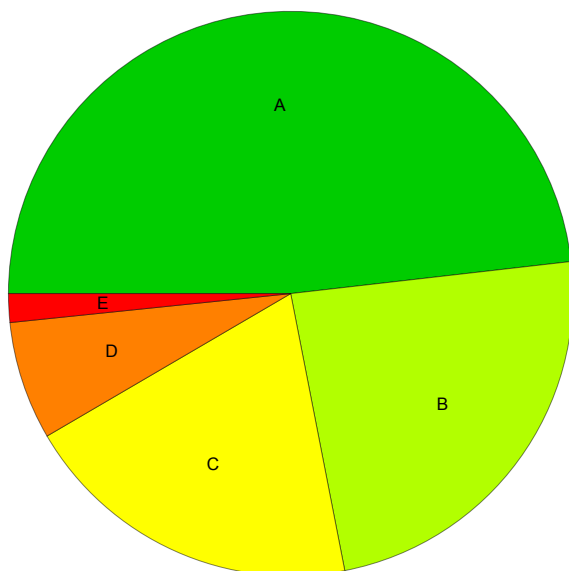
$$\begin{aligned}
 & -\frac{(i A + B) (c - i d) \operatorname{ArcTanh} \left[ \frac{\sqrt{a + i a \tan [e + f x]}}{\sqrt{2} \sqrt{a}} \right]}{2 \sqrt{2} a^{3/2} f} + \\
 & \frac{(i A - B) (c + i d)}{3 f (a + i a \tan [e + f x])^{3/2}} + \frac{B (c + 3 i d) + A (i c + d)}{2 a f \sqrt{a + i a \tan [e + f x]}}
 \end{aligned}$$

Result (type 3, 480 leaves):

$$\begin{aligned}
 & - \left( \left( i (A - i B) (c - i d) e^{2 i e} \sqrt{e^{i f x}} \operatorname{ArcSinh}\left[e^{i (e+f x)}\right] \right. \right. \\
 & \quad \left. \left. (\cos [f x] + i \sin [f x])^{3/2} (A + B \tan [e + f x]) (c + d \tan [e + f x]) \right) \right) / \\
 & \left( 2 \sqrt{2} \sqrt{\frac{e^{i (e+f x)}}{1 + e^{2 i (e+f x)}}} \sqrt{1 + e^{2 i (e+f x)}} f \sqrt{\sec [e + f x]} (A \cos [e + f x] + B \sin [e + f x]) \right. \\
 & \quad \left. (c \cos [e + f x] + d \sin [e + f x]) (a + i a \tan [e + f x])^{3/2} \right) + \\
 & \left( (\cos [f x] + i \sin [f x])^2 \left( \frac{1}{12} (5 i A c + B c + A d + 7 i B d) \cos [2 f x] + (2 i A c + B c + A d + 4 i B d) \right. \right. \\
 & \quad \left. \left( \frac{1}{6} \cos [2 e] + \frac{1}{6} i \sin [2 e] \right) + (A + i B) (c + i d) \cos [4 f x] \left( \frac{1}{12} i \cos [2 e] + \frac{1}{12} \sin [2 e] \right) + \right. \\
 & \quad \left. \frac{1}{12} (5 A c - i B c - i A d + 7 B d) \sin [2 f x] + (A + i B) (c + i d) \right. \\
 & \quad \left. \left( \frac{1}{12} \cos [2 e] - \frac{1}{12} i \sin [2 e] \right) \sin [4 f x] \right) (A + B \tan [e + f x]) (c + d \tan [e + f x]) \Big/ \\
 & \left( f (A \cos [e + f x] + B \sin [e + f x]) (c \cos [e + f x] + d \sin [e + f x]) (a + i a \tan [e + f x])^{3/2} \right)
 \end{aligned}$$

## Summary of Integration Test Results

855 integration problems



A - 412 optimal antiderivatives

B - 203 more than twice size of optimal antiderivatives

C - 168 unnecessarily complex antiderivatives

D - 58 unable to integrate problems

E - 14 integration timeouts